

# Mathematica 11.3 Integration Test Results

Test results for the 879 problems in "4.5.1.2 (d sec)^n (a+b sec)^m.m"

Problem 1: Result more than twice size of optimal antiderivative.

$$\int \text{Sec}[c + d x]^4 (a + a \text{Sec}[c + d x]) dx$$

Optimal (type 3, 85 leaves, 6 steps):

$$\frac{3 a \text{ArcTanh}[\text{Sin}[c + d x]]}{8 d} + \frac{a \text{Tan}[c + d x]}{d} + \frac{3 a \text{Sec}[c + d x] \text{Tan}[c + d x]}{8 d} + \frac{a \text{Sec}[c + d x]^3 \text{Tan}[c + d x]}{4 d} + \frac{a \text{Tan}[c + d x]^3}{3 d}$$

Result (type 3, 227 leaves):

$$\begin{aligned} & - \frac{3 a \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c + d x)\right] - \text{Sin}\left[\frac{1}{2}(c + d x)\right]\right]}{8 d} + \\ & \frac{3 a \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c + d x)\right] + \text{Sin}\left[\frac{1}{2}(c + d x)\right]\right]}{8 d} + \frac{a}{16 d \left(\text{Cos}\left[\frac{1}{2}(c + d x)\right] - \text{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^4} + \\ & \frac{3 a}{16 d \left(\text{Cos}\left[\frac{1}{2}(c + d x)\right] - \text{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^2} - \frac{a}{16 d \left(\text{Cos}\left[\frac{1}{2}(c + d x)\right] + \text{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^4} - \\ & \frac{3 a}{16 d \left(\text{Cos}\left[\frac{1}{2}(c + d x)\right] + \text{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^2} + \frac{2 a \text{Tan}[c + d x]}{3 d} + \frac{a \text{Sec}[c + d x]^2 \text{Tan}[c + d x]}{3 d} \end{aligned}$$

Problem 2: Result more than twice size of optimal antiderivative.

$$\int \text{Sec}[c + d x]^3 (a + a \text{Sec}[c + d x]) dx$$

Optimal (type 3, 63 leaves, 5 steps):

$$\frac{a \text{ArcTanh}[\text{Sin}[c + d x]]}{2 d} + \frac{a \text{Tan}[c + d x]}{d} + \frac{a \text{Sec}[c + d x] \text{Tan}[c + d x]}{2 d} + \frac{a \text{Tan}[c + d x]^3}{3 d}$$

Result (type 3, 163 leaves):

$$\begin{aligned}
 & - \frac{a \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right]}{2d} + \\
 & \frac{a \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right]}{2d} + \frac{a}{4d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^2} - \\
 & \frac{a}{4d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^2} + \frac{2a \operatorname{Tan}[c+dx]}{3d} + \frac{a \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx]}{3d}
 \end{aligned}$$

**Problem 3: Result more than twice size of optimal antiderivative.**

$$\int \operatorname{Sec}[c+dx]^2 (a + a \operatorname{Sec}[c+dx]) dx$$

Optimal (type 3, 47 leaves, 5 steps):

$$\frac{a \operatorname{ArcTanh}[\operatorname{Sin}[c+dx]]}{2d} + \frac{a \operatorname{Tan}[c+dx]}{d} + \frac{a \operatorname{Sec}[c+dx] \operatorname{Tan}[c+dx]}{2d}$$

Result (type 3, 138 leaves):

$$\begin{aligned}
 & - \frac{a \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right]}{2d} + \\
 & \frac{a \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right]}{2d} + \frac{a}{4d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^2} - \\
 & \frac{a}{4d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^2} + \frac{a \operatorname{Tan}[c+dx]}{d}
 \end{aligned}$$

**Problem 4: Result more than twice size of optimal antiderivative.**

$$\int \operatorname{Sec}[c+dx] (a + a \operatorname{Sec}[c+dx]) dx$$

Optimal (type 3, 24 leaves, 4 steps):

$$\frac{a \operatorname{ArcTanh}[\operatorname{Sin}[c+dx]]}{d} + \frac{a \operatorname{Tan}[c+dx]}{d}$$

Result (type 3, 81 leaves):

$$- \frac{a \operatorname{Log}\left[\operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] - \operatorname{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right]}{d} + \frac{a \operatorname{Log}\left[\operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] + \operatorname{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right]}{d} + \frac{a \operatorname{Tan}[c+dx]}{d}$$

**Problem 5: Result more than twice size of optimal antiderivative.**

$$\int (a + a \operatorname{Sec}[c+dx]) dx$$

Optimal (type 3, 16 leaves, 2 steps):

$$a x + \frac{a \operatorname{ArcTanh}[\operatorname{Sin}[c + d x]]}{d}$$

Result (type 3, 73 leaves):

$$a x - \frac{a \operatorname{Log}\left[\operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right] - \operatorname{Sin}\left[\frac{c}{2} + \frac{d x}{2}\right]\right]}{d} + \frac{a \operatorname{Log}\left[\operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right] + \operatorname{Sin}\left[\frac{c}{2} + \frac{d x}{2}\right]\right]}{d}$$

**Problem 10: Result more than twice size of optimal antiderivative.**

$$\int \operatorname{Sec}[c + d x]^4 (a + a \operatorname{Sec}[c + d x])^2 dx$$

Optimal (type 3, 122 leaves, 7 steps):

$$\frac{3 a^2 \operatorname{ArcTanh}[\operatorname{Sin}[c + d x]]}{4 d} + \frac{9 a^2 \operatorname{Tan}[c + d x]}{5 d} + \frac{3 a^2 \operatorname{Sec}[c + d x] \operatorname{Tan}[c + d x]}{4 d} + \frac{a^2 \operatorname{Sec}[c + d x]^3 \operatorname{Tan}[c + d x]}{2 d} + \frac{a^2 \operatorname{Sec}[c + d x]^4 \operatorname{Tan}[c + d x]}{5 d} + \frac{3 a^2 \operatorname{Tan}[c + d x]^3}{5 d}$$

Result (type 3, 487 leaves):

$$\begin{aligned} & -\frac{1}{640 d} a^2 \operatorname{Sec}[c] \operatorname{Sec}[c + d x]^5 \left( 75 \operatorname{Cos}[2 c + 3 d x] \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] + \right. \\ & \quad 75 \operatorname{Cos}[4 c + 3 d x] \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] + \\ & \quad 15 \operatorname{Cos}[4 c + 5 d x] \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] + \\ & \quad 15 \operatorname{Cos}[6 c + 5 d x] \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] + \\ & \quad 150 \operatorname{Cos}[d x] \left( \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] - \right. \\ & \quad \quad \left. \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] \right) + 150 \operatorname{Cos}[2 c + d x] \\ & \quad \left. \left( \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] - \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] \right) - \right. \\ & \quad 75 \operatorname{Cos}[2 c + 3 d x] \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] - \\ & \quad 75 \operatorname{Cos}[4 c + 3 d x] \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] - \\ & \quad 15 \operatorname{Cos}[4 c + 5 d x] \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] - \\ & \quad 15 \operatorname{Cos}[6 c + 5 d x] \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] - \\ & \quad 400 \operatorname{Sin}[d x] + 80 \operatorname{Sin}[2 c + d x] - 140 \operatorname{Sin}[c + 2 d x] - 140 \operatorname{Sin}[3 c + 2 d x] - \\ & \quad \left. 240 \operatorname{Sin}[2 c + 3 d x] - 30 \operatorname{Sin}[3 c + 4 d x] - 30 \operatorname{Sin}[5 c + 4 d x] - 48 \operatorname{Sin}[4 c + 5 d x] \right) \end{aligned}$$

### Problem 11: Result more than twice size of optimal antiderivative.

$$\int \text{Sec}[c + dx]^3 (a + a \text{Sec}[c + dx])^2 dx$$

Optimal (type 3, 96 leaves, 6 steps):

$$\frac{7 a^2 \text{ArcTanh}\left[\frac{\text{Sin}[c + dx]}{2}\right]}{8 d} + \frac{2 a^2 \text{Tan}[c + dx]}{d} + \frac{7 a^2 \text{Sec}[c + dx] \text{Tan}[c + dx]}{8 d} + \frac{a^2 \text{Sec}[c + dx]^3 \text{Tan}[c + dx]}{4 d} + \frac{2 a^2 \text{Tan}[c + dx]^3}{3 d}$$

Result (type 3, 877 leaves):

$$\begin{aligned} & -\frac{1}{32 d} 7 \text{Cos}[c + dx]^2 \text{Log}\left[\text{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] - \text{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right] \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a + a \text{Sec}[c + dx])^2 + \\ & \frac{1}{32 d} 7 \text{Cos}[c + dx]^2 \text{Log}\left[\text{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] + \text{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right] \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a + a \text{Sec}[c + dx])^2 + \\ & \frac{\text{Cos}[c + dx]^2 \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a + a \text{Sec}[c + dx])^2}{64 d \left(\text{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] - \text{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right)^4} + \\ & \frac{\text{Cos}[c + dx]^2 \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a + a \text{Sec}[c + dx])^2 \text{Sin}\left[\frac{dx}{2}\right]}{12 d \left(\text{Cos}\left[\frac{c}{2}\right] - \text{Sin}\left[\frac{c}{2}\right]\right) \left(\text{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] - \text{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right)^3} + \\ & \left(\text{Cos}[c + dx]^2 \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a + a \text{Sec}[c + dx])^2 \left(29 \text{Cos}\left[\frac{c}{2}\right] - 13 \text{Sin}\left[\frac{c}{2}\right]\right)\right) / \\ & \left(192 d \left(\text{Cos}\left[\frac{c}{2}\right] - \text{Sin}\left[\frac{c}{2}\right]\right) \left(\text{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] - \text{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right)^2\right) + \\ & \frac{\text{Cos}[c + dx]^2 \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a + a \text{Sec}[c + dx])^2 \text{Sin}\left[\frac{dx}{2}\right]}{3 d \left(\text{Cos}\left[\frac{c}{2}\right] - \text{Sin}\left[\frac{c}{2}\right]\right) \left(\text{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] - \text{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right)} - \\ & \frac{\text{Cos}[c + dx]^2 \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a + a \text{Sec}[c + dx])^2}{64 d \left(\text{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] + \text{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right)^4} + \\ & \frac{\text{Cos}[c + dx]^2 \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a + a \text{Sec}[c + dx])^2 \text{Sin}\left[\frac{dx}{2}\right]}{12 d \left(\text{Cos}\left[\frac{c}{2}\right] + \text{Sin}\left[\frac{c}{2}\right]\right) \left(\text{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] + \text{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right)^3} + \\ & \left(\text{Cos}[c + dx]^2 \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a + a \text{Sec}[c + dx])^2 \left(-29 \text{Cos}\left[\frac{c}{2}\right] - 13 \text{Sin}\left[\frac{c}{2}\right]\right)\right) / \\ & \left(192 d \left(\text{Cos}\left[\frac{c}{2}\right] + \text{Sin}\left[\frac{c}{2}\right]\right) \left(\text{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] + \text{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right)^2\right) + \\ & \frac{\text{Cos}[c + dx]^2 \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a + a \text{Sec}[c + dx])^2 \text{Sin}\left[\frac{dx}{2}\right]}{3 d \left(\text{Cos}\left[\frac{c}{2}\right] + \text{Sin}\left[\frac{c}{2}\right]\right) \left(\text{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] + \text{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right)} \end{aligned}$$

### Problem 12: Result more than twice size of optimal antiderivative.

$$\int \sec [c + d x]^2 (a + a \sec [c + d x])^2 dx$$

Optimal (type 3, 74 leaves, 6 steps):

$$\frac{a^2 \operatorname{ArcTanh}[\sin [c + d x]]}{d} + \frac{5 a^2 \tan [c + d x]}{3 d} + \frac{a^2 \sec [c + d x] \tan [c + d x]}{d} + \frac{a^2 \sec [c + d x]^2 \tan [c + d x]}{3 d}$$

Result (type 3, 318 leaves):

$$\begin{aligned} & -\frac{1}{24 d} a^2 \sec [c] \sec [c + d x]^3 \left( 3 \cos [2 c + 3 d x] \operatorname{Log} \left[ \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right] + \right. \\ & \quad 3 \cos [4 c + 3 d x] \operatorname{Log} \left[ \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right] + \\ & \quad 9 \cos [d x] \left( \operatorname{Log} \left[ \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right] - \right. \\ & \quad \quad \left. \operatorname{Log} \left[ \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right] \right) + 9 \cos [2 c + d x] \\ & \quad \left( \operatorname{Log} \left[ \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right] - \operatorname{Log} \left[ \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right] \right) - \\ & \quad 3 \cos [2 c + 3 d x] \operatorname{Log} \left[ \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right] - \\ & \quad 3 \cos [4 c + 3 d x] \operatorname{Log} \left[ \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right] - 24 \sin [d x] + \\ & \quad \left. 6 \sin [2 c + d x] - 6 \sin [c + 2 d x] - 6 \sin [3 c + 2 d x] - 10 \sin [2 c + 3 d x] \right) \end{aligned}$$

### Problem 13: Result more than twice size of optimal antiderivative.

$$\int \sec [c + d x] (a + a \sec [c + d x])^2 dx$$

Optimal (type 3, 54 leaves, 5 steps):

$$\frac{3 a^2 \operatorname{ArcTanh}[\sin [c + d x]]}{2 d} + \frac{2 a^2 \tan [c + d x]}{d} + \frac{a^2 \sec [c + d x] \tan [c + d x]}{2 d}$$

Result (type 3, 219 leaves):

$$\frac{1}{16d} a^2 (1 + \cos [c + dx])^2 \operatorname{Sec} \left[ \frac{1}{2} (c + dx) \right]^4$$

$$\left( -6 \operatorname{Log} \left[ \cos \left[ \frac{1}{2} (c + dx) \right] - \sin \left[ \frac{1}{2} (c + dx) \right] \right] + 6 \operatorname{Log} \left[ \cos \left[ \frac{1}{2} (c + dx) \right] + \sin \left[ \frac{1}{2} (c + dx) \right] \right] + \right.$$

$$\frac{1}{\left( \cos \left[ \frac{1}{2} (c + dx) \right] - \sin \left[ \frac{1}{2} (c + dx) \right] \right)^2} - \frac{1}{\left( \cos \left[ \frac{1}{2} (c + dx) \right] + \sin \left[ \frac{1}{2} (c + dx) \right] \right)^2} +$$

$$\left. \frac{8 \sin [dx]}{\left( \left( \cos \left[ \frac{c}{2} \right] - \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{c}{2} \right] + \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{1}{2} (c + dx) \right] - \sin \left[ \frac{1}{2} (c + dx) \right] \right) \left( \cos \left[ \frac{1}{2} (c + dx) \right] + \sin \left[ \frac{1}{2} (c + dx) \right] \right)} \right)$$

**Problem 14: Result more than twice size of optimal antiderivative.**

$$\int (a + a \operatorname{Sec} [c + dx])^2 dx$$

Optimal (type 3, 34 leaves, 4 steps):

$$a^2 x + \frac{2 a^2 \operatorname{ArcTanh} [\sin [c + dx]]}{d} + \frac{a^2 \tan [c + dx]}{d}$$

Result (type 3, 171 leaves):

$$\frac{1}{4d} a^2 (1 + \cos [c + dx])^2 \operatorname{Sec} \left[ \frac{1}{2} (c + dx) \right]^4$$

$$\left( dx - 2 \operatorname{Log} \left[ \cos \left[ \frac{1}{2} (c + dx) \right] - \sin \left[ \frac{1}{2} (c + dx) \right] \right] + 2 \operatorname{Log} \left[ \cos \left[ \frac{1}{2} (c + dx) \right] + \sin \left[ \frac{1}{2} (c + dx) \right] \right] + \right.$$

$$\left. \frac{\sin [dx]}{\left( \left( \cos \left[ \frac{c}{2} \right] - \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{c}{2} \right] + \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{1}{2} (c + dx) \right] - \sin \left[ \frac{1}{2} (c + dx) \right] \right) \left( \cos \left[ \frac{1}{2} (c + dx) \right] + \sin \left[ \frac{1}{2} (c + dx) \right] \right)} \right)$$

**Problem 15: Result more than twice size of optimal antiderivative.**

$$\int \cos [c + dx] (a + a \operatorname{Sec} [c + dx])^2 dx$$

Optimal (type 3, 34 leaves, 4 steps):

$$2 a^2 x + \frac{a^2 \operatorname{ArcTanh} [\sin [c + dx]]}{d} + \frac{a^2 \sin [c + dx]}{d}$$

Result (type 3, 106 leaves):

$$2 a^2 x - \frac{a^2 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] - \operatorname{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right]}{d} +$$

$$\frac{a^2 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] + \operatorname{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right]}{d} + \frac{a^2 \operatorname{Cos}[dx] \operatorname{Sin}[c]}{d} + \frac{a^2 \operatorname{Cos}[c] \operatorname{Sin}[dx]}{d}$$

**Problem 20: Result more than twice size of optimal antiderivative.**

$$\int \operatorname{Sec}[c + dx]^3 (a + a \operatorname{Sec}[c + dx])^3 dx$$

Optimal (type 3, 114 leaves, 11 steps):

$$\frac{13 a^3 \operatorname{ArcTanh}\left[\operatorname{Sin}[c + dx]\right]}{8 d} + \frac{4 a^3 \operatorname{Tan}[c + dx]}{d} + \frac{13 a^3 \operatorname{Sec}[c + dx] \operatorname{Tan}[c + dx]}{8 d} +$$

$$\frac{3 a^3 \operatorname{Sec}[c + dx]^3 \operatorname{Tan}[c + dx]}{4 d} + \frac{5 a^3 \operatorname{Tan}[c + dx]^3}{3 d} + \frac{a^3 \operatorname{Tan}[c + dx]^5}{5 d}$$

Result (type 3, 487 leaves):

$$-\frac{1}{3840 d} a^3 \operatorname{Sec}[c] \operatorname{Sec}[c + dx]^5 \left( 975 \operatorname{Cos}[2c + 3dx] \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right]\right] + \right.$$

$$975 \operatorname{Cos}[4c + 3dx] \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right]\right] +$$

$$195 \operatorname{Cos}[4c + 5dx] \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right]\right] +$$

$$195 \operatorname{Cos}[6c + 5dx] \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right]\right] +$$

$$1950 \operatorname{Cos}[dx] \left( \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right]\right] - \right.$$

$$\left. \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right]\right] \right) + 1950 \operatorname{Cos}[2c + dx]$$

$$\left( \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right]\right] - \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right]\right] \right) -$$

$$975 \operatorname{Cos}[2c + 3dx] \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right]\right] -$$

$$975 \operatorname{Cos}[4c + 3dx] \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right]\right] -$$

$$195 \operatorname{Cos}[4c + 5dx] \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right]\right] -$$

$$195 \operatorname{Cos}[6c + 5dx] \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right]\right] - 4640 \operatorname{Sin}[dx] +$$

$$1440 \operatorname{Sin}[2c + dx] - 1500 \operatorname{Sin}[c + 2dx] - 1500 \operatorname{Sin}[3c + 2dx] -$$

$$3040 \operatorname{Sin}[2c + 3dx] - 390 \operatorname{Sin}[3c + 4dx] - 390 \operatorname{Sin}[5c + 4dx] - 608 \operatorname{Sin}[4c + 5dx] \left. \right)$$

### Problem 21: Result more than twice size of optimal antiderivative.

$$\int \text{Sec}[c + dx]^2 (a + a \text{Sec}[c + dx])^3 dx$$

Optimal (type 3, 93 leaves, 11 steps):

$$\frac{15 a^3 \text{ArcTanh}[\text{Sin}[c + dx]]}{8 d} + \frac{4 a^3 \text{Tan}[c + dx]}{d} + \frac{15 a^3 \text{Sec}[c + dx] \text{Tan}[c + dx]}{8 d} + \frac{a^3 \text{Sec}[c + dx]^3 \text{Tan}[c + dx]}{4 d} + \frac{a^3 \text{Tan}[c + dx]^3}{d}$$

Result (type 3, 877 leaves):

$$\begin{aligned} & -\frac{1}{64 d} 15 \text{Cos}[c + dx]^3 \text{Log}\left[\text{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] - \text{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right] \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \text{Sec}[c + dx])^3 + \\ & \frac{1}{64 d} 15 \text{Cos}[c + dx]^3 \text{Log}\left[\text{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] + \text{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right] \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \text{Sec}[c + dx])^3 + \\ & \frac{\text{Cos}[c + dx]^3 \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \text{Sec}[c + dx])^3}{128 d \left(\text{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] - \text{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right)^4} + \\ & \frac{\text{Cos}[c + dx]^3 \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \text{Sec}[c + dx])^3 \text{Sin}\left[\frac{dx}{2}\right]}{16 d \left(\text{Cos}\left[\frac{c}{2}\right] - \text{Sin}\left[\frac{c}{2}\right]\right) \left(\text{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] - \text{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right)^3} + \\ & \left(\text{Cos}[c + dx]^3 \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \text{Sec}[c + dx])^3 \left(19 \text{Cos}\left[\frac{c}{2}\right] - 11 \text{Sin}\left[\frac{c}{2}\right]\right)\right) / \\ & \left(128 d \left(\text{Cos}\left[\frac{c}{2}\right] - \text{Sin}\left[\frac{c}{2}\right]\right) \left(\text{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] - \text{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right)^2\right) + \\ & \frac{3 \text{Cos}[c + dx]^3 \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \text{Sec}[c + dx])^3 \text{Sin}\left[\frac{dx}{2}\right]}{8 d \left(\text{Cos}\left[\frac{c}{2}\right] - \text{Sin}\left[\frac{c}{2}\right]\right) \left(\text{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] - \text{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right)} - \\ & \frac{\text{Cos}[c + dx]^3 \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \text{Sec}[c + dx])^3}{128 d \left(\text{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] + \text{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right)^4} + \\ & \frac{\text{Cos}[c + dx]^3 \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \text{Sec}[c + dx])^3 \text{Sin}\left[\frac{dx}{2}\right]}{16 d \left(\text{Cos}\left[\frac{c}{2}\right] + \text{Sin}\left[\frac{c}{2}\right]\right) \left(\text{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] + \text{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right)^3} + \\ & \left(\text{Cos}[c + dx]^3 \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \text{Sec}[c + dx])^3 \left(-19 \text{Cos}\left[\frac{c}{2}\right] - 11 \text{Sin}\left[\frac{c}{2}\right]\right)\right) / \\ & \left(128 d \left(\text{Cos}\left[\frac{c}{2}\right] + \text{Sin}\left[\frac{c}{2}\right]\right) \left(\text{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] + \text{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right)^2\right) + \\ & \frac{3 \text{Cos}[c + dx]^3 \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \text{Sec}[c + dx])^3 \text{Sin}\left[\frac{dx}{2}\right]}{8 d \left(\text{Cos}\left[\frac{c}{2}\right] + \text{Sin}\left[\frac{c}{2}\right]\right) \left(\text{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] + \text{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right)} \end{aligned}$$



### Problem 22: Result more than twice size of optimal antiderivative.

$$\int \sec [c + d x] (a + a \sec [c + d x])^3 dx$$

Optimal (type 3, 72 leaves, 9 steps):

$$\frac{5 a^3 \operatorname{ArcTanh}[\sin [c + d x]]}{2 d} + \frac{4 a^3 \tan [c + d x]}{d} + \frac{3 a^3 \sec [c + d x] \tan [c + d x]}{2 d} + \frac{a^3 \tan [c + d x]^3}{3 d}$$

Result (type 3, 733 leaves):

$$\begin{aligned} & -\frac{1}{16 d} 5 \cos [c + d x]^3 \operatorname{Log}\left[\cos \left[\frac{c}{2} + \frac{d x}{2}\right] - \sin \left[\frac{c}{2} + \frac{d x}{2}\right]\right] \sec \left[\frac{c}{2} + \frac{d x}{2}\right]^6 (a + a \sec [c + d x])^3 + \\ & \frac{1}{16 d} 5 \cos [c + d x]^3 \operatorname{Log}\left[\cos \left[\frac{c}{2} + \frac{d x}{2}\right] + \sin \left[\frac{c}{2} + \frac{d x}{2}\right]\right] \sec \left[\frac{c}{2} + \frac{d x}{2}\right]^6 (a + a \sec [c + d x])^3 + \\ & \frac{\cos [c + d x]^3 \sec \left[\frac{c}{2} + \frac{d x}{2}\right]^6 (a + a \sec [c + d x])^3 \sin \left[\frac{d x}{2}\right]}{48 d \left(\cos \left[\frac{c}{2}\right] - \sin \left[\frac{c}{2}\right]\right) \left(\cos \left[\frac{c}{2} + \frac{d x}{2}\right] - \sin \left[\frac{c}{2} + \frac{d x}{2}\right]\right)^3} + \\ & \left(\cos [c + d x]^3 \sec \left[\frac{c}{2} + \frac{d x}{2}\right]^6 (a + a \sec [c + d x])^3 \left(5 \cos \left[\frac{c}{2}\right] - 4 \sin \left[\frac{c}{2}\right]\right)\right) / \\ & \left(48 d \left(\cos \left[\frac{c}{2}\right] - \sin \left[\frac{c}{2}\right]\right) \left(\cos \left[\frac{c}{2} + \frac{d x}{2}\right] - \sin \left[\frac{c}{2} + \frac{d x}{2}\right]\right)^2\right) + \\ & \frac{11 \cos [c + d x]^3 \sec \left[\frac{c}{2} + \frac{d x}{2}\right]^6 (a + a \sec [c + d x])^3 \sin \left[\frac{d x}{2}\right]}{24 d \left(\cos \left[\frac{c}{2}\right] - \sin \left[\frac{c}{2}\right]\right) \left(\cos \left[\frac{c}{2} + \frac{d x}{2}\right] - \sin \left[\frac{c}{2} + \frac{d x}{2}\right]\right)} + \\ & \frac{\cos [c + d x]^3 \sec \left[\frac{c}{2} + \frac{d x}{2}\right]^6 (a + a \sec [c + d x])^3 \sin \left[\frac{d x}{2}\right]}{48 d \left(\cos \left[\frac{c}{2}\right] + \sin \left[\frac{c}{2}\right]\right) \left(\cos \left[\frac{c}{2} + \frac{d x}{2}\right] + \sin \left[\frac{c}{2} + \frac{d x}{2}\right]\right)^3} + \\ & \left(\cos [c + d x]^3 \sec \left[\frac{c}{2} + \frac{d x}{2}\right]^6 (a + a \sec [c + d x])^3 \left(-5 \cos \left[\frac{c}{2}\right] - 4 \sin \left[\frac{c}{2}\right]\right)\right) / \\ & \left(48 d \left(\cos \left[\frac{c}{2}\right] + \sin \left[\frac{c}{2}\right]\right) \left(\cos \left[\frac{c}{2} + \frac{d x}{2}\right] + \sin \left[\frac{c}{2} + \frac{d x}{2}\right]\right)^2\right) + \\ & \frac{11 \cos [c + d x]^3 \sec \left[\frac{c}{2} + \frac{d x}{2}\right]^6 (a + a \sec [c + d x])^3 \sin \left[\frac{d x}{2}\right]}{24 d \left(\cos \left[\frac{c}{2}\right] + \sin \left[\frac{c}{2}\right]\right) \left(\cos \left[\frac{c}{2} + \frac{d x}{2}\right] + \sin \left[\frac{c}{2} + \frac{d x}{2}\right]\right)} \end{aligned}$$

### Problem 23: Result more than twice size of optimal antiderivative.

$$\int (a + a \sec [c + d x])^3 dx$$

Optimal (type 3, 66 leaves, 5 steps):

$$a^3 x + \frac{7 a^3 \operatorname{ArcTanh}[\sin [c + d x]]}{2 d} + \frac{5 a^3 \tan [c + d x]}{2 d} + \frac{(a^3 + a^3 \sec [c + d x]) \tan [c + d x]}{2 d}$$

Result (type 3, 235 leaves):

$$\frac{1}{32} a^3 (1 + \cos [c + d x])^3 \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^6$$

$$\left(4 x - \frac{14 \operatorname{Log}\left[\cos\left[\frac{1}{2}(c + d x)\right] - \sin\left[\frac{1}{2}(c + d x)\right]\right]}{d} + \frac{14 \operatorname{Log}\left[\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right]\right]}{d} + \frac{1}{d\left(\cos\left[\frac{1}{2}(c + d x)\right] - \sin\left[\frac{1}{2}(c + d x)\right]\right)^2} - \frac{1}{d\left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right]\right)^2} + \frac{(12 \sin [d x]) / \left(d\left(\cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right]\right)\left(\cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right]\right)\left(\cos\left[\frac{1}{2}(c + d x)\right] - \sin\left[\frac{1}{2}(c + d x)\right]\right)\left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right]\right)}{\right)$$

**Problem 24: Result more than twice size of optimal antiderivative.**

$$\int \cos [c + d x] (a + a \operatorname{Sec}[c + d x])^3 dx$$

Optimal (type 3, 48 leaves, 6 steps):

$$3 a^3 x + \frac{3 a^3 \operatorname{ArcTanh}[\sin [c + d x]]}{d} + \frac{a^3 \sin [c + d x]}{d} + \frac{a^3 \tan [c + d x]}{d}$$

Result (type 3, 211 leaves):

$$\frac{1}{8} a^3 (1 + \cos [c + d x])^3 \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^6 \left(3 x - \frac{3 \operatorname{Log}\left[\cos\left[\frac{1}{2}(c + d x)\right] - \sin\left[\frac{1}{2}(c + d x)\right]\right]}{d} + \frac{3 \operatorname{Log}\left[\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right]\right]}{d} + \frac{\cos [d x] \sin [c]}{d} + \frac{\cos [c] \sin [d x]}{d} + \frac{\sin\left[\frac{d x}{2}\right]}{d\left(\cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right]\right)\left(\cos\left[\frac{1}{2}(c + d x)\right] - \sin\left[\frac{1}{2}(c + d x)\right]\right)} + \frac{\sin\left[\frac{d x}{2}\right]}{d\left(\cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right]\right)\left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right]\right)}\right)$$

**Problem 31: Result more than twice size of optimal antiderivative.**

$$\int \sec [c + d x]^2 (a + a \operatorname{Sec}[c + d x])^4 dx$$

Optimal (type 3, 111 leaves, 13 steps):

$$\frac{7 a^4 \operatorname{ArcTanh}[\sin [c + d x]]}{2 d} + \frac{8 a^4 \tan [c + d x]}{d} + \frac{7 a^4 \sec [c + d x] \tan [c + d x]}{2 d} + \frac{a^4 \sec [c + d x]^3 \tan [c + d x]}{d} + \frac{8 a^4 \tan [c + d x]^3}{3 d} + \frac{a^4 \tan [c + d x]^5}{5 d}$$

Result (type 3, 498 leaves):

$$\begin{aligned}
 & -\frac{1}{960d} a^4 \sec[c] \sec[c+dx]^5 \left( 525 \cos[2c+3dx] \log\left[\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right] + \right. \\
 & \quad 525 \cos[4c+3dx] \log\left[\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right] + \\
 & \quad 105 \cos[4c+5dx] \log\left[\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right] + \\
 & \quad 105 \cos[6c+5dx] \log\left[\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right] + \\
 & \quad 1050 \cos[dx] \left( \log\left[\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right] - \right. \\
 & \quad \quad \left. \log\left[\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right] \right) + 1050 \cos[2c+dx] \\
 & \quad \left( \log\left[\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right] - \log\left[\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right] \right) - \\
 & \quad 525 \cos[2c+3dx] \log\left[\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right] - \\
 & \quad 525 \cos[4c+3dx] \log\left[\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right] - \\
 & \quad 105 \cos[4c+5dx] \log\left[\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right] - \\
 & \quad 105 \cos[6c+5dx] \log\left[\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right] - 2360 \sin[dx] + \\
 & \quad 960 \sin[2c+dx] - 660 \sin[c+2dx] - 660 \sin[3c+2dx] - 1600 \sin[2c+3dx] + \\
 & \quad \left. 60 \sin[4c+3dx] - 210 \sin[3c+4dx] - 210 \sin[5c+4dx] - 332 \sin[4c+5dx] \right)
 \end{aligned}$$

**Problem 32: Result more than twice size of optimal antiderivative.**

$$\int \sec[c+dx] (a + a \sec[c+dx])^4 dx$$

Optimal (type 3, 96 leaves, 12 steps):

$$\begin{aligned}
 & \frac{35 a^4 \operatorname{ArcTanh}[\sin[c+dx]]}{8 d} + \frac{8 a^4 \tan[c+dx]}{d} + \\
 & \frac{27 a^4 \sec[c+dx] \tan[c+dx]}{8 d} + \frac{a^4 \sec[c+dx]^3 \tan[c+dx]}{4 d} + \frac{4 a^4 \tan[c+dx]^3}{3 d}
 \end{aligned}$$

Result (type 3, 877 leaves):

$$\begin{aligned}
 & -\frac{1}{128 d} 35 \cos [c+d x]^4 \operatorname{Log}\left[\cos \left[\frac{c}{2}+\frac{d x}{2}\right]-\sin \left[\frac{c}{2}+\frac{d x}{2}\right]\right] \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^8 (a+a \sec [c+d x])^4 + \\
 & \frac{1}{128 d} 35 \cos [c+d x]^4 \operatorname{Log}\left[\cos \left[\frac{c}{2}+\frac{d x}{2}\right]+\sin \left[\frac{c}{2}+\frac{d x}{2}\right]\right] \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^8 (a+a \sec [c+d x])^4 + \\
 & \frac{\cos [c+d x]^4 \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^8 (a+a \sec [c+d x])^4}{256 d\left(\cos \left[\frac{c}{2}+\frac{d x}{2}\right]-\sin \left[\frac{c}{2}+\frac{d x}{2}\right]\right)^4} + \\
 & \frac{\cos [c+d x]^4 \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^8 (a+a \sec [c+d x])^4 \sin \left[\frac{d x}{2}\right]}{24 d\left(\cos \left[\frac{c}{2}\right]-\sin \left[\frac{c}{2}\right]\right)\left(\cos \left[\frac{c}{2}+\frac{d x}{2}\right]-\sin \left[\frac{c}{2}+\frac{d x}{2}\right]\right)^3} + \\
 & \left(\cos [c+d x]^4 \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^8 (a+a \sec [c+d x])^4\left(97 \cos \left[\frac{c}{2}\right]-65 \sin \left[\frac{c}{2}\right]\right)\right) / \\
 & \left(768 d\left(\cos \left[\frac{c}{2}\right]-\sin \left[\frac{c}{2}\right]\right)\left(\cos \left[\frac{c}{2}+\frac{d x}{2}\right]-\sin \left[\frac{c}{2}+\frac{d x}{2}\right]\right)^2\right) + \\
 & \frac{5 \cos [c+d x]^4 \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^8 (a+a \sec [c+d x])^4 \sin \left[\frac{d x}{2}\right]}{12 d\left(\cos \left[\frac{c}{2}\right]-\sin \left[\frac{c}{2}\right]\right)\left(\cos \left[\frac{c}{2}+\frac{d x}{2}\right]-\sin \left[\frac{c}{2}+\frac{d x}{2}\right]\right)} - \\
 & \frac{\cos [c+d x]^4 \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^8 (a+a \sec [c+d x])^4}{256 d\left(\cos \left[\frac{c}{2}+\frac{d x}{2}\right]+\sin \left[\frac{c}{2}+\frac{d x}{2}\right]\right)^4} + \\
 & \frac{\cos [c+d x]^4 \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^8 (a+a \sec [c+d x])^4 \sin \left[\frac{d x}{2}\right]}{24 d\left(\cos \left[\frac{c}{2}\right]+\sin \left[\frac{c}{2}\right]\right)\left(\cos \left[\frac{c}{2}+\frac{d x}{2}\right]+\sin \left[\frac{c}{2}+\frac{d x}{2}\right]\right)^3} + \\
 & \left(\cos [c+d x]^4 \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^8 (a+a \sec [c+d x])^4\left(-97 \cos \left[\frac{c}{2}\right]-65 \sin \left[\frac{c}{2}\right]\right)\right) / \\
 & \left(768 d\left(\cos \left[\frac{c}{2}\right]+\sin \left[\frac{c}{2}\right]\right)\left(\cos \left[\frac{c}{2}+\frac{d x}{2}\right]+\sin \left[\frac{c}{2}+\frac{d x}{2}\right]\right)^2\right) + \\
 & \frac{5 \cos [c+d x]^4 \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^8 (a+a \sec [c+d x])^4 \sin \left[\frac{d x}{2}\right]}{12 d\left(\cos \left[\frac{c}{2}\right]+\sin \left[\frac{c}{2}\right]\right)\left(\cos \left[\frac{c}{2}+\frac{d x}{2}\right]+\sin \left[\frac{c}{2}+\frac{d x}{2}\right]\right)}
 \end{aligned}$$

**Problem 33: Result more than twice size of optimal antiderivative.**

$$\int (a+a \sec [c+d x])^4 dx$$

Optimal (type 3, 91 leaves, 6 steps):

$$\begin{aligned}
 & a^4 x + \frac{6 a^4 \operatorname{ArcTanh}[\sin [c+d x]]}{d} + \frac{5 a^4 \tan [c+d x]}{d} + \\
 & \frac{\left(a^2+a^2 \sec [c+d x]\right)^2 \tan [c+d x]}{3 d} + \frac{4\left(a^4+a^4 \sec [c+d x]\right) \tan [c+d x]}{3 d}
 \end{aligned}$$

Result (type 3, 773 leaves):

$$\begin{aligned}
 & \frac{1}{16} x \cos [c+d x]^4 \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^8 (a+a \sec [c+d x])^4 - \frac{1}{8 d} \\
 & 3 \cos [c+d x]^4 \log \left[\cos \left[\frac{c}{2}+\frac{d x}{2}\right]-\sin \left[\frac{c}{2}+\frac{d x}{2}\right]\right] \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^8 (a+a \sec [c+d x])^4 + \\
 & \frac{1}{8 d} 3 \cos [c+d x]^4 \log \left[\cos \left[\frac{c}{2}+\frac{d x}{2}\right]+\sin \left[\frac{c}{2}+\frac{d x}{2}\right]\right] \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^8 (a+a \sec [c+d x])^4 + \\
 & \frac{\cos [c+d x]^4 \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^8 (a+a \sec [c+d x])^4 \sin \left[\frac{d x}{2}\right]}{96 d\left(\cos \left[\frac{c}{2}\right]-\sin \left[\frac{c}{2}\right]\right)\left(\cos \left[\frac{c}{2}+\frac{d x}{2}\right]-\sin \left[\frac{c}{2}+\frac{d x}{2}\right]\right)^3} + \\
 & \left(\cos [c+d x]^4 \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^8 (a+a \sec [c+d x])^4\left(13 \cos \left[\frac{c}{2}\right]-11 \sin \left[\frac{c}{2}\right]\right)\right) / \\
 & \left(192 d\left(\cos \left[\frac{c}{2}\right]-\sin \left[\frac{c}{2}\right]\right)\left(\cos \left[\frac{c}{2}+\frac{d x}{2}\right]-\sin \left[\frac{c}{2}+\frac{d x}{2}\right]\right)^2\right) + \\
 & \frac{5 \cos [c+d x]^4 \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^8 (a+a \sec [c+d x])^4 \sin \left[\frac{d x}{2}\right]}{12 d\left(\cos \left[\frac{c}{2}\right]-\sin \left[\frac{c}{2}\right]\right)\left(\cos \left[\frac{c}{2}+\frac{d x}{2}\right]-\sin \left[\frac{c}{2}+\frac{d x}{2}\right]\right)} + \\
 & \frac{\cos [c+d x]^4 \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^8 (a+a \sec [c+d x])^4 \sin \left[\frac{d x}{2}\right]}{96 d\left(\cos \left[\frac{c}{2}\right]+\sin \left[\frac{c}{2}\right]\right)\left(\cos \left[\frac{c}{2}+\frac{d x}{2}\right]+\sin \left[\frac{c}{2}+\frac{d x}{2}\right]\right)^3} + \\
 & \left(\cos [c+d x]^4 \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^8 (a+a \sec [c+d x])^4\left(-13 \cos \left[\frac{c}{2}\right]-11 \sin \left[\frac{c}{2}\right]\right)\right) / \\
 & \left(192 d\left(\cos \left[\frac{c}{2}\right]+\sin \left[\frac{c}{2}\right]\right)\left(\cos \left[\frac{c}{2}+\frac{d x}{2}\right]+\sin \left[\frac{c}{2}+\frac{d x}{2}\right]\right)^2\right) + \\
 & \frac{5 \cos [c+d x]^4 \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^8 (a+a \sec [c+d x])^4 \sin \left[\frac{d x}{2}\right]}{12 d\left(\cos \left[\frac{c}{2}\right]+\sin \left[\frac{c}{2}\right]\right)\left(\cos \left[\frac{c}{2}+\frac{d x}{2}\right]+\sin \left[\frac{c}{2}+\frac{d x}{2}\right]\right)}
 \end{aligned}$$

**Problem 34: Result more than twice size of optimal antiderivative.**

$$\int \cos [c+d x] (a+a \sec [c+d x])^4 dx$$

Optimal (type 3, 73 leaves, 8 steps):

$$4 a^4 x + \frac{13 a^4 \operatorname{ArcTanh}[\sin [c+d x]]}{2 d} + \frac{a^4 \sin [c+d x]}{d} + \frac{4 a^4 \tan [c+d x]}{d} + \frac{a^4 \sec [c+d x] \tan [c+d x]}{2 d}$$

Result (type 3, 272 leaves):

$$\frac{1}{64} a^4 (1 + \cos [c + d x])^4 \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^8$$

$$\left( \frac{26 \operatorname{Log}\left[\cos\left[\frac{1}{2}(c + d x)\right] - \sin\left[\frac{1}{2}(c + d x)\right]\right]}{d} + \frac{26 \operatorname{Log}\left[\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right]\right]}{d} + \right.$$

$$\frac{4 \cos [d x] \sin [c]}{d} + \frac{4 \cos [c] \sin [d x]}{d} + \frac{1}{d \left(\cos\left[\frac{1}{2}(c + d x)\right] - \sin\left[\frac{1}{2}(c + d x)\right]\right)^2} +$$

$$\frac{16 \sin\left[\frac{d x}{2}\right]}{d \left(\cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right]\right) \left(\cos\left[\frac{1}{2}(c + d x)\right] - \sin\left[\frac{1}{2}(c + d x)\right]\right)} -$$

$$\frac{1}{d \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right]\right)^2} +$$

$$\left. \frac{16 \sin\left[\frac{d x}{2}\right]}{d \left(\cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right]\right) \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right]\right)} \right)$$

**Problem 35: Result more than twice size of optimal antiderivative.**

$$\int \cos [c + d x]^2 (a + a \operatorname{Sec} [c + d x])^4 dx$$

Optimal (type 3, 73 leaves, 8 steps):

$$\frac{13 a^4 x}{2} + \frac{4 a^4 \operatorname{ArcTanh}[\sin [c + d x]]}{d} +$$

$$\frac{4 a^4 \sin [c + d x]}{d} + \frac{a^4 \cos [c + d x] \sin [c + d x]}{2 d} + \frac{a^4 \tan [c + d x]}{d}$$

Result (type 3, 241 leaves):

$$\frac{1}{64} a^4 (1 + \cos [c + d x])^4 \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^8$$

$$\left( \frac{16 \operatorname{Log}\left[\cos\left[\frac{1}{2}(c + d x)\right] - \sin\left[\frac{1}{2}(c + d x)\right]\right]}{d} + \frac{16 \operatorname{Log}\left[\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right]\right]}{d} + \right.$$

$$\frac{16 \cos [d x] \sin [c]}{d} + \frac{\cos [2 d x] \sin [2 c]}{d} + \frac{16 \cos [c] \sin [d x]}{d} +$$

$$\frac{\cos [2 c] \sin [2 d x]}{d} + \frac{4 \sin\left[\frac{d x}{2}\right]}{d \left(\cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right]\right) \left(\cos\left[\frac{1}{2}(c + d x)\right] - \sin\left[\frac{1}{2}(c + d x)\right]\right)} +$$

$$\left. \frac{4 \sin\left[\frac{d x}{2}\right]}{d \left(\cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right]\right) \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right]\right)} \right)$$

**Problem 42: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sec [c+d x]^5}{a+a \sec [c+d x]} d x$$

Optimal (type 3, 103 leaves, 6 steps):

$$\frac{3 \operatorname{ArcTanh}[\sin [c+d x]]}{2 a d} + \frac{4 \tan [c+d x]}{a d} - \frac{3 \sec [c+d x] \tan [c+d x]}{2 a d} - \frac{\sec [c+d x]^3 \tan [c+d x]}{d (a+a \sec [c+d x])} + \frac{4 \tan [c+d x]^3}{3 a d}$$

Result (type 3, 374 leaves):

$$\frac{1}{3 a d (1+\sec [c+d x])} \cos \left[ \frac{1}{2} (c+d x) \right] \sec [c+d x] \left( 6 \sec \left[ \frac{c}{2} \right] \sin \left[ \frac{d x}{2} \right] + \frac{1}{8} \cos \left[ \frac{1}{2} (c+d x) \right] \sec [c] \right. \\ \left. \sec [c+d x]^3 \left( 9 \cos [2 c+3 d x] \log \left[ \cos \left[ \frac{1}{2} (c+d x) \right] - \sin \left[ \frac{1}{2} (c+d x) \right] \right] + 9 \cos [4 c+3 d x] \log \left[ \cos \left[ \frac{1}{2} (c+d x) \right] - \sin \left[ \frac{1}{2} (c+d x) \right] \right] + 27 \cos [d x] \right. \right. \\ \left. \left. \left( \log \left[ \cos \left[ \frac{1}{2} (c+d x) \right] - \sin \left[ \frac{1}{2} (c+d x) \right] \right] - \log \left[ \cos \left[ \frac{1}{2} (c+d x) \right] + \sin \left[ \frac{1}{2} (c+d x) \right] \right] \right) + 27 \cos [2 c+d x] \left( \log \left[ \cos \left[ \frac{1}{2} (c+d x) \right] - \sin \left[ \frac{1}{2} (c+d x) \right] \right] - \log \left[ \cos \left[ \frac{1}{2} (c+d x) \right] + \sin \left[ \frac{1}{2} (c+d x) \right] \right] \right. \right. \\ \left. \left. \sin \left[ \frac{1}{2} (c+d x) \right] \right) - 9 \cos [2 c+3 d x] \log \left[ \cos \left[ \frac{1}{2} (c+d x) \right] + \sin \left[ \frac{1}{2} (c+d x) \right] \right] - 9 \cos [4 c+3 d x] \log \left[ \cos \left[ \frac{1}{2} (c+d x) \right] + \sin \left[ \frac{1}{2} (c+d x) \right] \right] + 48 \sin [d x] - \right. \\ \left. \left. 12 \sin [2 c+d x] - 6 \sin [c+2 d x] - 6 \sin [3 c+2 d x] + 2 \theta \sin [2 c+3 d x] \right) \right)$$

**Problem 43: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sec [c+d x]^4}{a+a \sec [c+d x]} d x$$

Optimal (type 3, 85 leaves, 6 steps):

$$\frac{3 \operatorname{ArcTanh}[\sin [c+d x]]}{2 a d} - \frac{2 \tan [c+d x]}{a d} + \frac{3 \sec [c+d x] \tan [c+d x]}{2 a d} - \frac{\sec [c+d x]^2 \tan [c+d x]}{d (a+a \sec [c+d x])}$$

Result (type 3, 250 leaves):

$$\frac{1}{2 a d (1 + \operatorname{Sec}[c + d x])} \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] \operatorname{Sec}[c + d x] \left( -4 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sin}\left[\frac{d x}{2}\right] + \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] \right. \\ \left. -6 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] + 6 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] \right) + \\ \frac{1}{\left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^2} - \frac{1}{\left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^2} - \\ \frac{4 \operatorname{Sin}[d x]}{\left(\left(\operatorname{Cos}\left[\frac{c}{2}\right] - \operatorname{Sin}\left[\frac{c}{2}\right]\right)\left(\operatorname{Cos}\left[\frac{c}{2}\right] + \operatorname{Sin}\left[\frac{c}{2}\right]\right)\right.} \\ \left.\left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)\left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)\right) \right)$$

**Problem 44: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec}[c + d x]^3}{a + a \operatorname{Sec}[c + d x]} dx$$

Optimal (type 3, 51 leaves, 4 steps):

$$-\frac{\operatorname{ArcTanh}[\operatorname{Sin}[c + d x]]}{a d} + \frac{\operatorname{Tan}[c + d x]}{a d} + \frac{\operatorname{Tan}[c + d x]}{d (a + a \operatorname{Sec}[c + d x])}$$

Result (type 3, 194 leaves):

$$\left( 2 \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] \operatorname{Sec}[c + d x] \left( \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sin}\left[\frac{d x}{2}\right] + \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] \right) \right. \\ \left. \left( \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] - \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] \right) + \right. \\ \left. \operatorname{Sin}[d x] \left/ \left( \left( \operatorname{Cos}\left[\frac{c}{2}\right] - \operatorname{Sin}\left[\frac{c}{2}\right] \right) \left( \operatorname{Cos}\left[\frac{c}{2}\right] + \operatorname{Sin}\left[\frac{c}{2}\right] \right) \left( \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right) \right. \right. \right. \\ \left. \left. \left( \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right) \right) \right) \right) \left/ (a d (1 + \operatorname{Sec}[c + d x])) \right)$$

**Problem 45: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec}[c + d x]^2}{a + a \operatorname{Sec}[c + d x]} dx$$

Optimal (type 3, 38 leaves, 3 steps):

$$\frac{\operatorname{ArcTanh}[\operatorname{Sin}[c + d x]]}{a d} - \frac{\operatorname{Tan}[c + d x]}{d (a + a \operatorname{Sec}[c + d x])}$$

Result (type 3, 109 leaves):



$$\begin{aligned}
 & - \left( \left( 2 \cos \left[ \frac{1}{2} (c + d x) \right] \sec [c + d x] \left( \cos \left[ \frac{1}{2} (c + d x) \right] \right. \right. \right. \\
 & \quad \left. \left. \left( \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right] - \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right] \right) \right) + \right. \\
 & \quad \left. \sec \left[ \frac{c}{2} \right] \sin \left[ \frac{d x}{2} \right] \right) / (a d (1 + \sec [c + d x]))
 \end{aligned}$$

**Problem 48: Result more than twice size of optimal antiderivative.**

$$\int \frac{\cos [c + d x]}{a + a \sec [c + d x]} dx$$

Optimal (type 3, 44 leaves, 4 steps):

$$-\frac{x}{a} + \frac{2 \sin [c + d x]}{a d} - \frac{\sin [c + d x]}{d (a + a \sec [c + d x])}$$

Result (type 3, 89 leaves):

$$\begin{aligned}
 & \frac{1}{4 a d} \sec \left[ \frac{c}{2} \right] \sec \left[ \frac{1}{2} (c + d x) \right] \\
 & \left( -2 d x \cos \left[ \frac{d x}{2} \right] - 2 d x \cos \left[ c + \frac{d x}{2} \right] + 5 \sin \left[ \frac{d x}{2} \right] + \sin \left[ c + \frac{d x}{2} \right] + \sin \left[ c + \frac{3 d x}{2} \right] + \sin \left[ 2 c + \frac{3 d x}{2} \right] \right)
 \end{aligned}$$

**Problem 52: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sec [c + d x]^5}{(a + a \sec [c + d x])^2} dx$$

Optimal (type 3, 123 leaves, 7 steps):

$$\begin{aligned}
 & \frac{7 \operatorname{ArcTanh} [\sin [c + d x]]}{2 a^2 d} - \frac{16 \tan [c + d x]}{3 a^2 d} + \frac{7 \sec [c + d x] \tan [c + d x]}{2 a^2 d} - \\
 & \frac{8 \sec [c + d x]^2 \tan [c + d x]}{3 a^2 d (1 + \sec [c + d x])} - \frac{\sec [c + d x]^3 \tan [c + d x]}{3 d (a + a \sec [c + d x])^2}
 \end{aligned}$$

Result (type 3, 300 leaves):

$$\frac{1}{3 a^2 d (1 + \operatorname{Sec}[c + d x])^2} \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] \operatorname{Sec}[c + d x]^2 \left( -2 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sin}\left[\frac{d x}{2}\right] - 40 \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right]^2 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sin}\left[\frac{d x}{2}\right] + \right. \\ \left. 3 \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right]^3 \left( -14 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] + \right. \right. \\ \left. \left. 14 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] + \frac{1}{\left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^2} - \right. \right. \\ \left. \left. \frac{1}{\left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^2} - (8 \operatorname{Sin}[d x]) \right) / \right. \\ \left. \left( \left( \operatorname{Cos}\left[\frac{c}{2}\right] - \operatorname{Sin}\left[\frac{c}{2}\right] \right) \left( \operatorname{Cos}\left[\frac{c}{2}\right] + \operatorname{Sin}\left[\frac{c}{2}\right] \right) \left( \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right) \right. \right. \\ \left. \left. \left( \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right) \right) \right) - 2 \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] \operatorname{Tan}\left[\frac{c}{2}\right] \right)$$

**Problem 53: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec}[c + d x]^4}{(a + a \operatorname{Sec}[c + d x])^2} dx$$

Optimal (type 3, 89 leaves, 6 steps):

$$-\frac{2 \operatorname{ArcTanH}\left[\operatorname{Sin}[c + d x]\right]}{a^2 d} + \frac{4 \operatorname{Tan}[c + d x]}{3 a^2 d} + \frac{2 \operatorname{Tan}[c + d x]}{a^2 d (1 + \operatorname{Sec}[c + d x])} - \frac{\operatorname{Sec}[c + d x]^2 \operatorname{Tan}[c + d x]}{3 d (a + a \operatorname{Sec}[c + d x])^2}$$

Result (type 3, 247 leaves):

$$\frac{1}{3 a^2 d (1 + \operatorname{Sec}[c + d x])^2} 2 \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] \operatorname{Sec}[c + d x]^2 \\ \left( \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sin}\left[\frac{d x}{2}\right] + 14 \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right]^2 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sin}\left[\frac{d x}{2}\right] + 6 \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right]^3 \right. \\ \left. \left( 2 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] - 2 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] + \right. \right. \\ \left. \left. \operatorname{Sin}[d x] \right) / \left( \left( \operatorname{Cos}\left[\frac{c}{2}\right] - \operatorname{Sin}\left[\frac{c}{2}\right] \right) \left( \operatorname{Cos}\left[\frac{c}{2}\right] + \operatorname{Sin}\left[\frac{c}{2}\right] \right) \left( \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right) \right. \right. \\ \left. \left. \left( \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right) \right) \right) + \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] \operatorname{Tan}\left[\frac{c}{2}\right]$$

**Problem 54: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec}[c + d x]^3}{(a + a \operatorname{Sec}[c + d x])^2} dx$$

Optimal (type 3, 66 leaves, 4 steps):

$$\frac{\text{ArcTanh}[\text{Sin}[c + d x]]}{a^2 d} - \frac{5 \text{Tan}[c + d x]}{3 a^2 d (1 + \text{Sec}[c + d x])} + \frac{\text{Tan}[c + d x]}{3 d (a + a \text{Sec}[c + d x])^2}$$

Result (type 3, 160 leaves):

$$\begin{aligned} & - \left( \left( 2 \text{Cos}\left[\frac{1}{2}(c + d x)\right] \text{Sec}[c + d x]^2 \left( 6 \text{Cos}\left[\frac{1}{2}(c + d x)\right]^3 \right. \right. \right. \\ & \quad \left. \left. \left( \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c + d x)\right] - \text{Sin}\left[\frac{1}{2}(c + d x)\right]\right] - \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c + d x)\right] + \text{Sin}\left[\frac{1}{2}(c + d x)\right]\right] \right) \right) + \right. \\ & \quad \left. \text{Sec}\left[\frac{c}{2}\right] \text{Sin}\left[\frac{d x}{2}\right] + 8 \text{Cos}\left[\frac{1}{2}(c + d x)\right]^2 \text{Sec}\left[\frac{c}{2}\right] \text{Sin}\left[\frac{d x}{2}\right] + \right. \\ & \quad \left. \left. \text{Cos}\left[\frac{1}{2}(c + d x)\right] \text{Tan}\left[\frac{c}{2}\right] \right) \right) / \left( 3 a^2 d (1 + \text{Sec}[c + d x])^2 \right) \end{aligned}$$

**Problem 58: Result more than twice size of optimal antiderivative.**

$$\int \frac{\text{Cos}[c + d x]}{(a + a \text{Sec}[c + d x])^2} dx$$

Optimal (type 3, 72 leaves, 5 steps):

$$-\frac{2 x}{a^2} + \frac{10 \text{Sin}[c + d x]}{3 a^2 d} - \frac{2 \text{Sin}[c + d x]}{a^2 d (1 + \text{Sec}[c + d x])} - \frac{\text{Sin}[c + d x]}{3 d (a + a \text{Sec}[c + d x])^2}$$

Result (type 3, 151 leaves):

$$\begin{aligned} & \frac{1}{48 a^2 d} \text{Sec}\left[\frac{c}{2}\right] \text{Sec}\left[\frac{1}{2}(c + d x)\right]^3 \\ & \left( -36 d x \text{Cos}\left[\frac{d x}{2}\right] - 36 d x \text{Cos}\left[c + \frac{d x}{2}\right] - 12 d x \text{Cos}\left[c + \frac{3 d x}{2}\right] - 12 d x \text{Cos}\left[2 c + \frac{3 d x}{2}\right] + \right. \\ & \quad 66 \text{Sin}\left[\frac{d x}{2}\right] - 30 \text{Sin}\left[c + \frac{d x}{2}\right] + 41 \text{Sin}\left[c + \frac{3 d x}{2}\right] + \\ & \quad \left. 9 \text{Sin}\left[2 c + \frac{3 d x}{2}\right] + 3 \text{Sin}\left[2 c + \frac{5 d x}{2}\right] + 3 \text{Sin}\left[3 c + \frac{5 d x}{2}\right] \right) \end{aligned}$$

**Problem 61: Result more than twice size of optimal antiderivative.**

$$\int \frac{\text{Sec}[c + d x]^6}{(a + a \text{Sec}[c + d x])^3} dx$$

Optimal (type 3, 162 leaves, 8 steps):

$$\begin{aligned} & \frac{13 \text{ArcTanh}[\text{Sin}[c + d x]]}{2 a^3 d} - \frac{152 \text{Tan}[c + d x]}{15 a^3 d} + \frac{13 \text{Sec}[c + d x] \text{Tan}[c + d x]}{2 a^3 d} - \\ & \frac{\text{Sec}[c + d x]^4 \text{Tan}[c + d x]}{5 d (a + a \text{Sec}[c + d x])^3} - \frac{11 \text{Sec}[c + d x]^3 \text{Tan}[c + d x]}{15 a d (a + a \text{Sec}[c + d x])^2} - \frac{76 \text{Sec}[c + d x]^2 \text{Tan}[c + d x]}{15 d (a^3 + a^3 \text{Sec}[c + d x])} \end{aligned}$$

Result (type 3, 351 leaves):

$$\begin{aligned}
 & - \frac{1}{480 a^3 d (1 + \text{Sec}[c + d x])^3} \text{Cos}\left[\frac{1}{2}(c + d x)\right] \text{Sec}[c + d x]^3 \\
 & \left( 24960 \text{Cos}\left[\frac{1}{2}(c + d x)\right]^5 \left( \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c + d x)\right] - \text{Sin}\left[\frac{1}{2}(c + d x)\right]\right] - \right. \right. \\
 & \quad \left. \left. \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c + d x)\right] + \text{Sin}\left[\frac{1}{2}(c + d x)\right]\right]\right) + \text{Sec}\left[\frac{c}{2}\right] \text{Sec}[c] \text{Sec}[c + d x]^2 \right. \\
 & \quad \left. \left( -1235 \text{Sin}\left[\frac{d x}{2}\right] + 3805 \text{Sin}\left[\frac{3 d x}{2}\right] - 4329 \text{Sin}\left[c - \frac{d x}{2}\right] + 1989 \text{Sin}\left[c + \frac{d x}{2}\right] - \right. \right. \\
 & \quad 3575 \text{Sin}\left[2 c + \frac{d x}{2}\right] - 475 \text{Sin}\left[c + \frac{3 d x}{2}\right] + 2005 \text{Sin}\left[2 c + \frac{3 d x}{2}\right] - 2275 \text{Sin}\left[3 c + \frac{3 d x}{2}\right] + \\
 & \quad 2673 \text{Sin}\left[c + \frac{5 d x}{2}\right] + 105 \text{Sin}\left[2 c + \frac{5 d x}{2}\right] + 1593 \text{Sin}\left[3 c + \frac{5 d x}{2}\right] - 975 \text{Sin}\left[4 c + \frac{5 d x}{2}\right] + \\
 & \quad 1325 \text{Sin}\left[2 c + \frac{7 d x}{2}\right] + 255 \text{Sin}\left[3 c + \frac{7 d x}{2}\right] + 875 \text{Sin}\left[4 c + \frac{7 d x}{2}\right] - 195 \text{Sin}\left[5 c + \frac{7 d x}{2}\right] + \\
 & \quad \left. \left. 304 \text{Sin}\left[3 c + \frac{9 d x}{2}\right] + 90 \text{Sin}\left[4 c + \frac{9 d x}{2}\right] + 214 \text{Sin}\left[5 c + \frac{9 d x}{2}\right] \right) \right)
 \end{aligned}$$

**Problem 62: Result more than twice size of optimal antiderivative.**

$$\int \frac{\text{Sec}[c + d x]^5}{(a + a \text{Sec}[c + d x])^3} dx$$

Optimal (type 3, 128 leaves, 7 steps):

$$\begin{aligned}
 & - \frac{3 \text{ArcTan}[\text{Sin}[c + d x]]}{a^3 d} + \frac{9 \text{Tan}[c + d x]}{5 a^3 d} - \\
 & \frac{\text{Sec}[c + d x]^3 \text{Tan}[c + d x]}{5 d (a + a \text{Sec}[c + d x])^3} - \frac{3 \text{Sec}[c + d x]^2 \text{Tan}[c + d x]}{5 a d (a + a \text{Sec}[c + d x])^2} + \frac{3 \text{Tan}[c + d x]}{d (a^3 + a^3 \text{Sec}[c + d x])}
 \end{aligned}$$

Result (type 3, 294 leaves):

$$\begin{aligned}
 & \frac{1}{5 a^3 d (1 + \text{Sec}[c + d x])^3} \\
 & 2 \text{Cos}\left[\frac{1}{2}(c + d x)\right] \text{Sec}[c + d x]^3 \left( \text{Sec}\left[\frac{c}{2}\right] \text{Sin}\left[\frac{d x}{2}\right] + 8 \text{Cos}\left[\frac{1}{2}(c + d x)\right]^2 \text{Sec}\left[\frac{c}{2}\right] \text{Sin}\left[\frac{d x}{2}\right] + \right. \\
 & \quad 76 \text{Cos}\left[\frac{1}{2}(c + d x)\right]^4 \text{Sec}\left[\frac{c}{2}\right] \text{Sin}\left[\frac{d x}{2}\right] + 20 \text{Cos}\left[\frac{1}{2}(c + d x)\right]^5 \\
 & \quad \left( 3 \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c + d x)\right] - \text{Sin}\left[\frac{1}{2}(c + d x)\right]\right] - 3 \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c + d x)\right] + \text{Sin}\left[\frac{1}{2}(c + d x)\right]\right] + \right. \\
 & \quad \left. \text{Sin}[d x] / \left( \left( \text{Cos}\left[\frac{c}{2}\right] - \text{Sin}\left[\frac{c}{2}\right] \right) \left( \text{Cos}\left[\frac{c}{2}\right] + \text{Sin}\left[\frac{c}{2}\right] \right) \right. \right. \\
 & \quad \left. \left. \left( \text{Cos}\left[\frac{1}{2}(c + d x)\right] - \text{Sin}\left[\frac{1}{2}(c + d x)\right] \right) \left( \text{Cos}\left[\frac{1}{2}(c + d x)\right] + \text{Sin}\left[\frac{1}{2}(c + d x)\right] \right) \right) \right) + \\
 & \quad \left. \text{Cos}\left[\frac{1}{2}(c + d x)\right] \text{Tan}\left[\frac{c}{2}\right] + 8 \text{Cos}\left[\frac{1}{2}(c + d x)\right]^3 \text{Tan}\left[\frac{c}{2}\right] \right)
 \end{aligned}$$

**Problem 70: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sec [c+d x]^7}{(a+a \sec [c+d x])^4} d x$$

Optimal (type 3, 193 leaves, 9 steps):

$$\frac{21 \operatorname{ArcTanh}[\operatorname{Sin}[c+d x]]}{2 a^4 d} - \frac{576 \operatorname{Tan}[c+d x]}{35 a^4 d} + \frac{21 \sec [c+d x] \operatorname{Tan}[c+d x]}{2 a^4 d} - \frac{43 \sec [c+d x]^3 \operatorname{Tan}[c+d x]}{35 a^4 d (1+\sec [c+d x])^2} - \frac{288 \sec [c+d x]^2 \operatorname{Tan}[c+d x]}{35 a^4 d (1+\sec [c+d x])} - \frac{\sec [c+d x]^5 \operatorname{Tan}[c+d x]}{7 d (a+a \sec [c+d x])^4} - \frac{2 \sec [c+d x]^4 \operatorname{Tan}[c+d x]}{5 a d (a+a \sec [c+d x])^3}$$

Result (type 3, 403 leaves):

$$-\frac{1}{2240 a^4 d (1+\sec [c+d x])^4} \cos \left[ \frac{1}{2} (c+d x) \right] \sec [c+d x]^4 \left( 376320 \cos \left[ \frac{1}{2} (c+d x) \right]^7 \right. \\ \left. \left( \log \left[ \cos \left[ \frac{1}{2} (c+d x) \right] - \sin \left[ \frac{1}{2} (c+d x) \right] \right] - \log \left[ \cos \left[ \frac{1}{2} (c+d x) \right] + \sin \left[ \frac{1}{2} (c+d x) \right] \right] \right) + \right. \\ \left. \sec \left[ \frac{c}{2} \right] \sec [c] \sec [c+d x]^2 \left( -24402 \sin \left[ \frac{d x}{2} \right] + 55556 \sin \left[ \frac{3 d x}{2} \right] - 61054 \sin \left[ c - \frac{d x}{2} \right] + \right. \right. \\ \left. \left. 33614 \sin \left[ c + \frac{d x}{2} \right] - 51842 \sin \left[ 2 c + \frac{d x}{2} \right] - 12460 \sin \left[ c + \frac{3 d x}{2} \right] + 33716 \sin \left[ 2 c + \frac{3 d x}{2} \right] - \right. \right. \\ \left. \left. 34300 \sin \left[ 3 c + \frac{3 d x}{2} \right] + 39788 \sin \left[ c + \frac{5 d x}{2} \right] - 2940 \sin \left[ 2 c + \frac{5 d x}{2} \right] + \right. \right. \\ \left. \left. 26068 \sin \left[ 3 c + \frac{5 d x}{2} \right] - 16660 \sin \left[ 4 c + \frac{5 d x}{2} \right] + 21351 \sin \left[ 2 c + \frac{7 d x}{2} \right] + \right. \right. \\ \left. \left. 1295 \sin \left[ 3 c + \frac{7 d x}{2} \right] + 14911 \sin \left[ 4 c + \frac{7 d x}{2} \right] - 5145 \sin \left[ 5 c + \frac{7 d x}{2} \right] + \right. \right. \\ \left. \left. 7329 \sin \left[ 3 c + \frac{9 d x}{2} \right] + 1225 \sin \left[ 4 c + \frac{9 d x}{2} \right] + 5369 \sin \left[ 5 c + \frac{9 d x}{2} \right] - 735 \sin \left[ 6 c + \frac{9 d x}{2} \right] + \right. \right. \\ \left. \left. 1152 \sin \left[ 4 c + \frac{11 d x}{2} \right] + 280 \sin \left[ 5 c + \frac{11 d x}{2} \right] + 872 \sin \left[ 6 c + \frac{11 d x}{2} \right] \right) \right)$$

**Problem 71: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sec [c+d x]^6}{(a+a \sec [c+d x])^4} d x$$

Optimal (type 3, 159 leaves, 8 steps):

$$-\frac{4 \operatorname{ArcTanh}[\operatorname{Sin}[c+d x]]}{a^4 d} + \frac{244 \operatorname{Tan}[c+d x]}{105 a^4 d} - \frac{88 \sec [c+d x]^2 \operatorname{Tan}[c+d x]}{105 a^4 d (1+\sec [c+d x])^2} + \frac{4 \operatorname{Tan}[c+d x]}{a^4 d (1+\sec [c+d x])} - \frac{\sec [c+d x]^4 \operatorname{Tan}[c+d x]}{7 d (a+a \sec [c+d x])^4} - \frac{12 \sec [c+d x]^3 \operatorname{Tan}[c+d x]}{35 a d (a+a \sec [c+d x])^3}$$

Result (type 3, 349 leaves):

$$\frac{1}{1680 a^4 d (1 + \operatorname{Sec}[c + d x])^4} \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] \operatorname{Sec}[c + d x]^4$$

$$\left(107520 \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right]^7 \left(\operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] - \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right]\right) + \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c] \operatorname{Sec}[c + d x]$$

$$\left(-10780 \operatorname{Sin}\left[\frac{d x}{2}\right] + 18788 \operatorname{Sin}\left[\frac{3 d x}{2}\right] - 20524 \operatorname{Sin}\left[c - \frac{d x}{2}\right] + 14644 \operatorname{Sin}\left[c + \frac{d x}{2}\right] - 16660 \operatorname{Sin}\left[2 c + \frac{d x}{2}\right] - 4690 \operatorname{Sin}\left[c + \frac{3 d x}{2}\right] + 14378 \operatorname{Sin}\left[2 c + \frac{3 d x}{2}\right] - 9100 \operatorname{Sin}\left[3 c + \frac{3 d x}{2}\right] + 11668 \operatorname{Sin}\left[c + \frac{5 d x}{2}\right] - 630 \operatorname{Sin}\left[2 c + \frac{5 d x}{2}\right] + 9358 \operatorname{Sin}\left[3 c + \frac{5 d x}{2}\right] - 2940 \operatorname{Sin}\left[4 c + \frac{5 d x}{2}\right] + 4228 \operatorname{Sin}\left[2 c + \frac{7 d x}{2}\right] + 315 \operatorname{Sin}\left[3 c + \frac{7 d x}{2}\right] + 3493 \operatorname{Sin}\left[4 c + \frac{7 d x}{2}\right] - 420 \operatorname{Sin}\left[5 c + \frac{7 d x}{2}\right] + 664 \operatorname{Sin}\left[3 c + \frac{9 d x}{2}\right] + 105 \operatorname{Sin}\left[4 c + \frac{9 d x}{2}\right] + 559 \operatorname{Sin}\left[5 c + \frac{9 d x}{2}\right]\right)$$

Problem 77: Result more than twice size of optimal antiderivative.

$$\int \frac{1}{(a + a \operatorname{Sec}[c + d x])^4} dx$$

Optimal (type 3, 111 leaves, 5 steps):

$$\frac{x}{a^4} - \frac{11 \operatorname{Tan}[c + d x]}{21 a^4 d (1 + \operatorname{Sec}[c + d x])^2} - \frac{32 \operatorname{Tan}[c + d x]}{21 a^4 d (1 + \operatorname{Sec}[c + d x])} - \frac{\operatorname{Tan}[c + d x]}{7 d (a + a \operatorname{Sec}[c + d x])^4} - \frac{2 \operatorname{Tan}[c + d x]}{7 a d (a + a \operatorname{Sec}[c + d x])^3}$$

Result (type 3, 224 leaves):

$$\frac{1}{2688 a^4 d} \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^7$$

$$\left(735 d x \operatorname{Cos}\left[\frac{d x}{2}\right] + 735 d x \operatorname{Cos}\left[c + \frac{d x}{2}\right] + 441 d x \operatorname{Cos}\left[c + \frac{3 d x}{2}\right] + 441 d x \operatorname{Cos}\left[2 c + \frac{3 d x}{2}\right] + 147 d x \operatorname{Cos}\left[2 c + \frac{5 d x}{2}\right] + 147 d x \operatorname{Cos}\left[3 c + \frac{5 d x}{2}\right] + 21 d x \operatorname{Cos}\left[3 c + \frac{7 d x}{2}\right] + 21 d x \operatorname{Cos}\left[4 c + \frac{7 d x}{2}\right] - 1988 \operatorname{Sin}\left[\frac{d x}{2}\right] + 1652 \operatorname{Sin}\left[c + \frac{d x}{2}\right] - 1428 \operatorname{Sin}\left[c + \frac{3 d x}{2}\right] + 756 \operatorname{Sin}\left[2 c + \frac{3 d x}{2}\right] - 560 \operatorname{Sin}\left[2 c + \frac{5 d x}{2}\right] + 168 \operatorname{Sin}\left[3 c + \frac{5 d x}{2}\right] - 104 \operatorname{Sin}\left[3 c + \frac{7 d x}{2}\right]\right)$$

Problem 78: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Cos}[c + d x]}{(a + a \operatorname{Sec}[c + d x])^4} dx$$

Optimal (type 3, 126 leaves, 7 steps):

$$-\frac{4x}{a^4} + \frac{664 \operatorname{Sin}[c+dx]}{105 a^4 d} - \frac{88 \operatorname{Sin}[c+dx]}{105 a^4 d (1 + \operatorname{Sec}[c+dx])^2} - \frac{4 \operatorname{Sin}[c+dx]}{a^4 d (1 + \operatorname{Sec}[c+dx])} - \frac{\operatorname{Sin}[c+dx]}{7 d (a + a \operatorname{Sec}[c+dx])^4} - \frac{12 \operatorname{Sin}[c+dx]}{35 a d (a + a \operatorname{Sec}[c+dx])^3}$$

Result (type 3, 263 leaves):

$$-\frac{1}{26880 a^4 d} \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^7 \left( 29400 dx \operatorname{Cos}\left[\frac{dx}{2}\right] + 29400 dx \operatorname{Cos}\left[c + \frac{dx}{2}\right] + 17640 dx \operatorname{Cos}\left[c + \frac{3dx}{2}\right] + 17640 dx \operatorname{Cos}\left[2c + \frac{3dx}{2}\right] + 5880 dx \operatorname{Cos}\left[2c + \frac{5dx}{2}\right] + 5880 dx \operatorname{Cos}\left[3c + \frac{5dx}{2}\right] + 840 dx \operatorname{Cos}\left[3c + \frac{7dx}{2}\right] + 840 dx \operatorname{Cos}\left[4c + \frac{7dx}{2}\right] - 60830 \operatorname{Sin}\left[\frac{dx}{2}\right] + 46130 \operatorname{Sin}\left[c + \frac{dx}{2}\right] - 46116 \operatorname{Sin}\left[c + \frac{3dx}{2}\right] + 18060 \operatorname{Sin}\left[2c + \frac{3dx}{2}\right] - 19292 \operatorname{Sin}\left[2c + \frac{5dx}{2}\right] + 2100 \operatorname{Sin}\left[3c + \frac{5dx}{2}\right] - 3791 \operatorname{Sin}\left[3c + \frac{7dx}{2}\right] - 735 \operatorname{Sin}\left[4c + \frac{7dx}{2}\right] - 105 \operatorname{Sin}\left[4c + \frac{9dx}{2}\right] - 105 \operatorname{Sin}\left[5c + \frac{9dx}{2}\right] \right)$$

**Problem 80: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec}[c+dx]^7}{(a+a \operatorname{Sec}[c+dx])^5} dx$$

Optimal (type 3, 200 leaves, 9 steps):

$$-\frac{5 \operatorname{ArcTanh}[\operatorname{Sin}[c+dx]]}{a^5 d} + \frac{181 \operatorname{Tan}[c+dx]}{63 a^5 d} - \frac{\operatorname{Sec}[c+dx]^5 \operatorname{Tan}[c+dx]}{9 d (a + a \operatorname{Sec}[c+dx])^5} - \frac{5 \operatorname{Sec}[c+dx]^4 \operatorname{Tan}[c+dx]}{21 a d (a + a \operatorname{Sec}[c+dx])^4} - \frac{29 \operatorname{Sec}[c+dx]^3 \operatorname{Tan}[c+dx]}{63 a^2 d (a + a \operatorname{Sec}[c+dx])^3} - \frac{67 \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx]}{63 a^3 d (a + a \operatorname{Sec}[c+dx])^2} + \frac{5 \operatorname{Tan}[c+dx]}{d (a^5 + a^5 \operatorname{Sec}[c+dx])}$$

Result (type 3, 401 leaves):

$$\frac{1}{2016 a^5 d (1 + \text{Sec}[c + d x])^5} \text{Cos}\left[\frac{1}{2}(c + d x)\right] \text{Sec}[c + d x]^5 \left( 322560 \text{Cos}\left[\frac{1}{2}(c + d x)\right]^9 \right. \\ \left. \left( \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c + d x)\right] - \text{Sin}\left[\frac{1}{2}(c + d x)\right]\right] - \text{Log}\left[\text{Cos}\left[\frac{1}{2}(c + d x)\right] + \text{Sin}\left[\frac{1}{2}(c + d x)\right]\right] \right) + \right. \\ \left. \text{Sec}\left[\frac{c}{2}\right] \text{Sec}[c] \text{Sec}[c + d x] \left( -33978 \text{Sin}\left[\frac{d x}{2}\right] + 52002 \text{Sin}\left[\frac{3 d x}{2}\right] - 56952 \text{Sin}\left[c - \frac{d x}{2}\right] + \right. \right. \\ \left. \left. 43722 \text{Sin}\left[c + \frac{d x}{2}\right] - 47208 \text{Sin}\left[2 c + \frac{d x}{2}\right] - 18144 \text{Sin}\left[c + \frac{3 d x}{2}\right] + 41796 \text{Sin}\left[2 c + \frac{3 d x}{2}\right] - \right. \right. \\ \left. \left. 28350 \text{Sin}\left[3 c + \frac{3 d x}{2}\right] + 34578 \text{Sin}\left[c + \frac{5 d x}{2}\right] - 5691 \text{Sin}\left[2 c + \frac{5 d x}{2}\right] + \right. \right. \\ \left. \left. 28719 \text{Sin}\left[3 c + \frac{5 d x}{2}\right] - 11550 \text{Sin}\left[4 c + \frac{5 d x}{2}\right] + 15517 \text{Sin}\left[2 c + \frac{7 d x}{2}\right] - \right. \right. \\ \left. \left. 504 \text{Sin}\left[3 c + \frac{7 d x}{2}\right] + 13186 \text{Sin}\left[4 c + \frac{7 d x}{2}\right] - 2835 \text{Sin}\left[5 c + \frac{7 d x}{2}\right] + \right. \right. \\ \left. \left. 4149 \text{Sin}\left[3 c + \frac{9 d x}{2}\right] + 252 \text{Sin}\left[4 c + \frac{9 d x}{2}\right] + 3582 \text{Sin}\left[5 c + \frac{9 d x}{2}\right] - 315 \text{Sin}\left[6 c + \frac{9 d x}{2}\right] + \right. \right. \\ \left. \left. 496 \text{Sin}\left[4 c + \frac{11 d x}{2}\right] + 63 \text{Sin}\left[5 c + \frac{11 d x}{2}\right] + 433 \text{Sin}\left[6 c + \frac{11 d x}{2}\right] \right) \right)$$

**Problem 88: Result more than twice size of optimal antiderivative.**

$$\int \frac{\text{Cos}[c + d x]}{(a + a \text{Sec}[c + d x])^5} dx$$

Optimal (type 3, 159 leaves, 8 steps):

$$-\frac{5 x}{a^5} + \frac{496 \text{Sin}[c + d x]}{63 a^5 d} - \frac{\text{Sin}[c + d x]}{9 d (a + a \text{Sec}[c + d x])^5} - \frac{5 \text{Sin}[c + d x]}{21 a d (a + a \text{Sec}[c + d x])^4} - \\ \frac{29 \text{Sin}[c + d x]}{63 a^2 d (a + a \text{Sec}[c + d x])^3} - \frac{67 \text{Sin}[c + d x]}{63 a^3 d (a + a \text{Sec}[c + d x])^2} - \frac{5 \text{Sin}[c + d x]}{d (a^5 + a^5 \text{Sec}[c + d x])}$$

Result (type 3, 319 leaves):



$$\begin{aligned}
 & - \frac{1}{64512 a^5 d} \\
 & \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^9 \left( 79380 d x \operatorname{Cos}\left[\frac{d x}{2}\right] + 79380 d x \operatorname{Cos}\left[c + \frac{d x}{2}\right] + 52920 d x \operatorname{Cos}\left[c + \frac{3 d x}{2}\right] + \right. \\
 & 52920 d x \operatorname{Cos}\left[2 c + \frac{3 d x}{2}\right] + 22680 d x \operatorname{Cos}\left[2 c + \frac{5 d x}{2}\right] + 22680 d x \operatorname{Cos}\left[3 c + \frac{5 d x}{2}\right] + \\
 & 5670 d x \operatorname{Cos}\left[3 c + \frac{7 d x}{2}\right] + 5670 d x \operatorname{Cos}\left[4 c + \frac{7 d x}{2}\right] + 630 d x \operatorname{Cos}\left[4 c + \frac{9 d x}{2}\right] + \\
 & 630 d x \operatorname{Cos}\left[5 c + \frac{9 d x}{2}\right] - 175014 \operatorname{Sin}\left[\frac{d x}{2}\right] + 143010 \operatorname{Sin}\left[c + \frac{d x}{2}\right] - \\
 & 138726 \operatorname{Sin}\left[c + \frac{3 d x}{2}\right] + 73290 \operatorname{Sin}\left[2 c + \frac{3 d x}{2}\right] - 70389 \operatorname{Sin}\left[2 c + \frac{5 d x}{2}\right] + \\
 & 20475 \operatorname{Sin}\left[3 c + \frac{5 d x}{2}\right] - 21141 \operatorname{Sin}\left[3 c + \frac{7 d x}{2}\right] + 1575 \operatorname{Sin}\left[4 c + \frac{7 d x}{2}\right] - \\
 & \left. 3091 \operatorname{Sin}\left[4 c + \frac{9 d x}{2}\right] - 567 \operatorname{Sin}\left[5 c + \frac{9 d x}{2}\right] - 63 \operatorname{Sin}\left[5 c + \frac{11 d x}{2}\right] - 63 \operatorname{Sin}\left[6 c + \frac{11 d x}{2}\right] \right)
 \end{aligned}$$

**Problem 94: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \sqrt{a + a \operatorname{Sec}[c + d x]} dx$$

Optimal (type 3, 37 leaves, 2 steps):

$$\frac{2 \sqrt{a} \operatorname{ArcTan}\left[\frac{\sqrt{a} \operatorname{Tan}[c+d x]}{\sqrt{a+a \operatorname{Sec}[c+d x]}}\right]}{d}$$

Result (type 4, 331 leaves):

$$\begin{aligned}
& -\frac{1}{d} 8 (-3 - 2\sqrt{2}) \cos\left[\frac{1}{4}(c + dx)\right]^4 \sqrt{\frac{7 - 5\sqrt{2} + (10 - 7\sqrt{2}) \cos\left[\frac{1}{2}(c + dx)\right]}{1 + \cos\left[\frac{1}{2}(c + dx)\right]}} \\
& \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2}(c + dx)\right]}{1 + \cos\left[\frac{1}{2}(c + dx)\right]}} \left(1 - \sqrt{2} + (-2 + \sqrt{2}) \cos\left[\frac{1}{2}(c + dx)\right]\right) \\
& \left( \text{EllipticF}\left[\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c + dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] + \right. \\
& \quad \left. 2 \text{EllipticPi}\left[-3 + 2\sqrt{2}, -\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c + dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] \right) \\
& \sqrt{\left(-1 - \sqrt{2} + (2 + \sqrt{2}) \cos\left[\frac{1}{2}(c + dx)\right]\right) \sec\left[\frac{1}{4}(c + dx)\right]^2 \sec\left[\frac{1}{2}(c + dx)\right]} \\
& \sec[c + dx] \sqrt{a(1 + \sec[c + dx])} \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c + dx)\right]^2}
\end{aligned}$$

**Problem 95: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos[c + dx] \sqrt{a + a \sec[c + dx]} dx$$

Optimal (type 3, 62 leaves, 3 steps):

$$\frac{\sqrt{a} \text{ArcTan}\left[\frac{\sqrt{a} \tan[c + dx]}{\sqrt{a + a \sec[c + dx]}}\right]}{d} + \frac{a \sin[c + dx]}{d \sqrt{a + a \sec[c + dx]}}$$

Result (type 4, 389 leaves):

$$\frac{1}{d} \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right] \sqrt{a(1+\operatorname{Sec}[c+dx])} \left(-\frac{1}{2} \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] + \frac{1}{2} \operatorname{Sin}\left[\frac{3}{2}(c+dx)\right]\right) -$$

$$\frac{1}{d} 4(-3-2\sqrt{2}) \operatorname{Cos}\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{\frac{7-5\sqrt{2}+(10-7\sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]}{1+\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]}}$$

$$\sqrt{\frac{-1+\sqrt{2}-(-2+\sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]}{1+\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]}} \left(1-\sqrt{2}+(-2+\sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right)$$

$$\left(\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] +\right.$$

$$\left.2 \operatorname{EllipticPi}\left[-3+2\sqrt{2}, -\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right]\right)$$

$$\sqrt{\left(-1-\sqrt{2}+(2+\sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right) \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]}$$

$$\operatorname{Sec}[c+dx] \sqrt{a(1+\operatorname{Sec}[c+dx])} \sqrt{3-2\sqrt{2}-\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}$$

**Problem 96: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \operatorname{Cos}[c+dx]^2 \sqrt{a+a \operatorname{Sec}[c+dx]} dx$$

Optimal (type 3, 102 leaves, 4 steps):

$$\frac{3\sqrt{a} \operatorname{ArcTan}\left[\frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{a+a \operatorname{Sec}[c+dx]}}\right]}{4d} + \frac{3a \operatorname{Sin}[c+dx]}{4d \sqrt{a+a \operatorname{Sec}[c+dx]}} + \frac{a \operatorname{Cos}[c+dx] \operatorname{Sin}[c+dx]}{2d \sqrt{a+a \operatorname{Sec}[c+dx]}}$$

Result (type 4, 401 leaves):

$$\begin{aligned}
& \frac{1}{d} \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right] \sqrt{a(1+\operatorname{Sec}[c+dx])} \\
& \left(-\frac{1}{8} \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] + \frac{1}{4} \operatorname{Sin}\left[\frac{3}{2}(c+dx)\right] + \frac{1}{8} \operatorname{Sin}\left[\frac{5}{2}(c+dx)\right]\right) + \\
& \frac{1}{d} 3 \left(2 + \frac{3}{\sqrt{2}}\right) \operatorname{Cos}\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{\frac{7-5\sqrt{2} + (10-7\sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]}{1+\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]}} \\
& \left(1-\sqrt{2} + (-2+\sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right) \left(\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] + \right. \\
& \left. 2 \operatorname{EllipticPi}\left[-3+2\sqrt{2}, -\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right]\right) \\
& \sqrt{\left(-1+\sqrt{2} - (-2+\sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right) \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2} \\
& \sqrt{\left(-1-\sqrt{2} + (2+\sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right) \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]} \\
& \operatorname{Sec}[c+dx] \sqrt{a(1+\operatorname{Sec}[c+dx])} \sqrt{3-2\sqrt{2} - \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}
\end{aligned}$$

**Problem 97: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \operatorname{Cos}[c+dx]^3 \sqrt{a+a \operatorname{Sec}[c+dx]} dx$$

Optimal (type 3, 138 leaves, 5 steps):

$$\begin{aligned}
& \frac{5\sqrt{a} \operatorname{ArcTan}\left[\frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{a+a \operatorname{Sec}[c+dx]}}\right]}{8d} + \frac{5a \operatorname{Sin}[c+dx]}{8d \sqrt{a+a \operatorname{Sec}[c+dx]}} + \\
& \frac{5a \operatorname{Cos}[c+dx] \operatorname{Sin}[c+dx]}{12d \sqrt{a+a \operatorname{Sec}[c+dx]}} + \frac{a \operatorname{Cos}[c+dx]^2 \operatorname{Sin}[c+dx]}{3d \sqrt{a+a \operatorname{Sec}[c+dx]}}
\end{aligned}$$

Result (type 4, 417 leaves):

$$\begin{aligned}
 & \frac{1}{d} \sec\left[\frac{1}{2}(c+dx)\right] \sqrt{a(1+\sec[c+dx])} \\
 & \left(-\frac{11}{48} \sin\left[\frac{1}{2}(c+dx)\right] + \frac{1}{3} \sin\left[\frac{3}{2}(c+dx)\right] + \frac{1}{16} \sin\left[\frac{5}{2}(c+dx)\right] + \frac{1}{24} \sin\left[\frac{7}{2}(c+dx)\right]\right) + \\
 & \frac{1}{4d} 5(4+3\sqrt{2}) \cos\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{\frac{7-5\sqrt{2}+(10-7\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]}{1+\cos\left[\frac{1}{2}(c+dx)\right]}} \\
 & \left(1-\sqrt{2}+(-2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]\right) \left(\text{EllipticF}\left[\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] + \right. \\
 & \left. 2 \text{EllipticPi}\left[-3+2\sqrt{2}, -\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right]\right) \\
 & \sqrt{\left(-1+\sqrt{2}-(-2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]\right) \sec\left[\frac{1}{4}(c+dx)\right]^2} \\
 & \sqrt{\left(-1-\sqrt{2}+(2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]\right) \sec\left[\frac{1}{4}(c+dx)\right]^2 \sec\left[\frac{1}{2}(c+dx)\right]} \\
 & \sec[c+dx] \sqrt{a(1+\sec[c+dx])} \sqrt{3-2\sqrt{2}-\tan\left[\frac{1}{4}(c+dx)\right]^2}
 \end{aligned}$$

**Problem 98: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos[c+dx]^4 \sqrt{a+a \sec[c+dx]} dx$$

Optimal (type 3, 174 leaves, 6 steps):

$$\begin{aligned}
 & \frac{35\sqrt{a} \text{ArcTan}\left[\frac{\sqrt{a} \tan[c+dx]}{\sqrt{a+a \sec[c+dx]}}\right]}{64d} + \frac{35a \sin[c+dx]}{64d \sqrt{a+a \sec[c+dx]}} + \\
 & \frac{35a \cos[c+dx] \sin[c+dx]}{96d \sqrt{a+a \sec[c+dx]}} + \frac{7a \cos[c+dx]^2 \sin[c+dx]}{24d \sqrt{a+a \sec[c+dx]}} + \frac{a \cos[c+dx]^3 \sin[c+dx]}{4d \sqrt{a+a \sec[c+dx]}}
 \end{aligned}$$

Result (type 4, 431 leaves):

$$\begin{aligned}
& \frac{1}{d} \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right] \sqrt{a(1+\operatorname{Sec}[c+dx])} \left( -\frac{41}{384} \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] + \right. \\
& \quad \left. \frac{11}{48} \operatorname{Sin}\left[\frac{3}{2}(c+dx)\right] + \frac{15}{128} \operatorname{Sin}\left[\frac{5}{2}(c+dx)\right] + \frac{1}{48} \operatorname{Sin}\left[\frac{7}{2}(c+dx)\right] + \frac{1}{64} \operatorname{Sin}\left[\frac{9}{2}(c+dx)\right] \right) + \\
& \frac{1}{(-64+48\sqrt{2})d} 35 \operatorname{Cos}\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{\frac{7-5\sqrt{2}+(10-7\sqrt{2})\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]}{1+\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]}} \\
& \left(1-\sqrt{2}+(-2+\sqrt{2})\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right) \left( \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] + \right. \\
& \quad \left. 2 \operatorname{EllipticPi}\left[-3+2\sqrt{2}, -\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] \right) \\
& \sqrt{\left(-1+\sqrt{2}-(-2+\sqrt{2})\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right) \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2} \\
& \sqrt{\left(-1-\sqrt{2}+(2+\sqrt{2})\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right) \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]} \\
& \operatorname{Sec}[c+dx] \sqrt{a(1+\operatorname{Sec}[c+dx])} \sqrt{3-2\sqrt{2}-\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}
\end{aligned}$$

**Problem 103: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int (a + a \operatorname{Sec}[c + dx])^{3/2} dx$$

Optimal (type 3, 66 leaves, 4 steps):

$$\frac{2 a^{3/2} \operatorname{ArcTan}\left[\frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{a+a \operatorname{Sec}[c+dx]}}\right]}{d} + \frac{2 a^2 \operatorname{Tan}[c+dx]}{d \sqrt{a+a \operatorname{Sec}[c+dx]}}$$

Result (type 4, 374 leaves):

$$\begin{aligned}
 & -\frac{1}{d} 4 (-3 - 2\sqrt{2}) \cos\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{\frac{7 - 5\sqrt{2} + (10 - 7\sqrt{2}) \cos\left[\frac{1}{2}(c+dx)\right]}{1 + \cos\left[\frac{1}{2}(c+dx)\right]}} \\
 & \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2}(c+dx)\right]}{1 + \cos\left[\frac{1}{2}(c+dx)\right]}} \left(1 - \sqrt{2} + (-2 + \sqrt{2}) \cos\left[\frac{1}{2}(c+dx)\right]\right) \\
 & \left( \text{EllipticF}\left[\text{ArcSin}\left[\frac{\text{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] + \right. \\
 & \quad \left. 2 \text{EllipticPi}\left[-3 + 2\sqrt{2}, -\text{ArcSin}\left[\frac{\text{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] \right) \\
 & \sqrt{\left(-1 - \sqrt{2} + (2 + \sqrt{2}) \cos\left[\frac{1}{2}(c+dx)\right]\right) \sec\left[\frac{1}{4}(c+dx)\right]^2 \sec\left[\frac{1}{2}(c+dx)\right]^3} \\
 & (a(1 + \sec[c+dx]))^{3/2} \sqrt{3 - 2\sqrt{2} - \text{Tan}\left[\frac{1}{4}(c+dx)\right]^2 + \frac{1}{d}} \\
 & \cos[c+dx] \sec\left[\frac{1}{2}(c+dx)\right]^2 (a(1 + \sec[c+dx]))^{3/2} \text{Tan}\left[\frac{1}{2}(c+dx)\right]
 \end{aligned}$$

**Problem 104: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos[c+dx] (a + a \sec[c+dx])^{3/2} dx$$

Optimal (type 3, 65 leaves, 5 steps):

$$\frac{3 a^{3/2} \text{ArcTan}\left[\frac{\sqrt{a} \text{Tan}[c+dx]}{\sqrt{a+a \text{Sec}[c+dx]}}\right]}{d} + \frac{a^2 \text{Sin}[c+dx]}{d \sqrt{a+a \text{Sec}[c+dx]}}$$

Result (type 4, 393 leaves):

$$\frac{1}{d} \cos [c+d x] \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^3$$

$$\left(a\left(1+\operatorname{Sec}[c+d x]\right)\right)^{3 / 2}\left(-\frac{1}{4} \sin \left[\frac{1}{2}(c+d x)\right]+\frac{1}{4} \sin \left[\frac{3}{2}(c+d x)\right]\right)-$$

$$\frac{1}{d} 6(-3-2 \sqrt{2}) \cos \left[\frac{1}{4}(c+d x)\right]^4 \sqrt{\frac{7-5 \sqrt{2}+(10-7 \sqrt{2}) \cos \left[\frac{1}{2}(c+d x)\right]}{1+\cos \left[\frac{1}{2}(c+d x)\right]}}$$

$$\sqrt{\frac{-1+\sqrt{2}-(-2+\sqrt{2}) \cos \left[\frac{1}{2}(c+d x)\right]}{1+\cos \left[\frac{1}{2}(c+d x)\right]}}\left(1-\sqrt{2}+(-2+\sqrt{2}) \cos \left[\frac{1}{2}(c+d x)\right]\right)$$

$$\left(\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan \left[\frac{1}{4}(c+d x)\right]}{\sqrt{3-2 \sqrt{2}}}\right], 17-12 \sqrt{2}\right]+2 \operatorname{EllipticPi}\left[-3+2 \sqrt{2},-\operatorname{ArcSin}\left[\frac{\tan \left[\frac{1}{4}(c+d x)\right]}{\sqrt{3-2 \sqrt{2}}}\right], 17-12 \sqrt{2}\right]\right)$$

$$\sqrt{\left(-1-\sqrt{2}+(2+\sqrt{2}) \cos \left[\frac{1}{2}(c+d x)\right]\right) \operatorname{Sec}\left[\frac{1}{4}(c+d x)\right]^2 \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^3}$$

$$\left(a\left(1+\operatorname{Sec}[c+d x]\right)\right)^{3 / 2} \sqrt{3-2 \sqrt{2}-\tan \left[\frac{1}{4}(c+d x)\right]^2}$$

**Problem 105: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos [c+d x]^2(a+a \operatorname{Sec}[c+d x])^{3 / 2} d x$$

Optimal (type 3, 106 leaves, 5 steps):

$$\frac{7 a^{3 / 2} \operatorname{ArcTan}\left[\frac{\sqrt{a} \tan [c+d x]}{\sqrt{a+a \operatorname{Sec}[c+d x]}}\right]}{4 d}+\frac{7 a^2 \sin [c+d x]}{4 d \sqrt{a+a \operatorname{Sec}[c+d x]}}+\frac{a^2 \cos [c+d x] \sin [c+d x]}{2 d \sqrt{a+a \operatorname{Sec}[c+d x]}}$$

Result (type 4, 407 leaves):



$$\begin{aligned}
 & \frac{1}{d} \cos[c+dx] \sec\left[\frac{1}{2}(c+dx)\right]^3 (a(1+\sec[c+dx]))^{3/2} \\
 & \left(-\frac{5}{16} \sin\left[\frac{1}{2}(c+dx)\right] + \frac{3}{8} \sin\left[\frac{3}{2}(c+dx)\right] + \frac{1}{16} \sin\left[\frac{5}{2}(c+dx)\right]\right) + \\
 & \frac{1}{4d} 7(4+3\sqrt{2}) \cos\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{\frac{7-5\sqrt{2}+(10-7\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]}{1+\cos\left[\frac{1}{2}(c+dx)\right]}} \\
 & \left(1-\sqrt{2}+(-2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]\right) \left(\text{EllipticF}\left[\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] + \right. \\
 & \left. 2 \text{EllipticPi}\left[-3+2\sqrt{2}, -\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right]\right) \\
 & \sqrt{\left(-1+\sqrt{2}-(-2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]\right) \sec\left[\frac{1}{4}(c+dx)\right]^2} \\
 & \sqrt{\left(-1-\sqrt{2}+(2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]\right) \sec\left[\frac{1}{4}(c+dx)\right]^2} \\
 & \sec\left[\frac{1}{2}(c+dx)\right]^3 (a(1+\sec[c+dx]))^{3/2} \sqrt{3-2\sqrt{2}-\tan\left[\frac{1}{4}(c+dx)\right]^2}
 \end{aligned}$$

**Problem 106: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos[c+dx]^3 (a+a \sec[c+dx])^{3/2} dx$$

Optimal (type 3, 144 leaves, 6 steps):

$$\begin{aligned}
 & \frac{11 a^{3/2} \text{ArcTan}\left[\frac{\sqrt{a} \tan[c+dx]}{\sqrt{a+a \sec[c+dx]}}\right]}{8 d} + \frac{11 a^2 \sin[c+dx]}{8 d \sqrt{a+a \sec[c+dx]}} + \\
 & \frac{11 a^2 \cos[c+dx] \sin[c+dx]}{12 d \sqrt{a+a \sec[c+dx]}} + \frac{a^2 \cos[c+dx]^2 \sin[c+dx]}{3 d \sqrt{a+a \sec[c+dx]}}
 \end{aligned}$$

Result (type 4, 421 leaves):

$$\begin{aligned} & \frac{1}{d} \cos [c+d x] \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^3\left(a\left(1+\operatorname{Sec}[c+d x]\right)\right)^{3 / 2} \\ & \left(-\frac{17}{96} \sin \left[\frac{1}{2}(c+d x)\right]+\frac{7}{24} \sin \left[\frac{3}{2}(c+d x)\right]+\frac{3}{32} \sin \left[\frac{5}{2}(c+d x)\right]+\frac{1}{48} \sin \left[\frac{7}{2}(c+d x)\right]\right)+ \\ & \frac{1}{8 d} 11\left(4+3 \sqrt{2}\right) \cos \left[\frac{1}{4}(c+d x)\right]^4 \sqrt{\frac{7-5 \sqrt{2}+(10-7 \sqrt{2}) \cos \left[\frac{1}{2}(c+d x)\right]}{1+\cos \left[\frac{1}{2}(c+d x)\right]}} \\ & \left(1-\sqrt{2}+(-2+\sqrt{2}) \cos \left[\frac{1}{2}(c+d x)\right]\right)\left(\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan \left[\frac{1}{4}(c+d x)\right]}{\sqrt{3-2 \sqrt{2}}}\right], 17-12 \sqrt{2}\right]+ \right. \\ & \left. 2 \operatorname{EllipticPi}\left[-3+2 \sqrt{2},-\operatorname{ArcSin}\left[\frac{\tan \left[\frac{1}{4}(c+d x)\right]}{\sqrt{3-2 \sqrt{2}}}\right], 17-12 \sqrt{2}\right]\right) \\ & \sqrt{\left(-1+\sqrt{2}-(-2+\sqrt{2}) \cos \left[\frac{1}{2}(c+d x)\right]\right) \operatorname{Sec}\left[\frac{1}{4}(c+d x)\right]^2} \\ & \sqrt{\left(-1-\sqrt{2}+(2+\sqrt{2}) \cos \left[\frac{1}{2}(c+d x)\right]\right) \operatorname{Sec}\left[\frac{1}{4}(c+d x)\right]^2} \\ & \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^3\left(a\left(1+\operatorname{Sec}[c+d x]\right)\right)^{3 / 2} \sqrt{3-2 \sqrt{2}-\tan \left[\frac{1}{4}(c+d x)\right]^2} \end{aligned}$$

**Problem 111: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int(a+a \operatorname{Sec}[c+d x])^{5 / 2} d x$$

Optimal (type 3, 98 leaves, 5 steps):

$$\frac{2 a^{5 / 2} \operatorname{ArcTan}\left[\frac{\sqrt{a} \tan [c+d x]}{\sqrt{a+a \operatorname{Sec}[c+d x]}}\right]}{d}+\frac{14 a^3 \tan [c+d x]}{3 d \sqrt{a+a \operatorname{Sec}[c+d x]}}+\frac{2 a^2 \sqrt{a+a \operatorname{Sec}[c+d x]} \tan [c+d x]}{3 d}$$

Result (type 4, 407 leaves):

$$\begin{aligned}
 & \frac{1}{d} \cos[c+dx]^2 \sec\left[\frac{1}{2}(c+dx)\right]^5 \left(a(1+\sec[c+dx])\right)^{5/2} \\
 & \left(\frac{4}{3} \sin\left[\frac{1}{2}(c+dx)\right] + \frac{1}{6} \sec[c+dx] \sin\left[\frac{1}{2}(c+dx)\right]\right) - \\
 & \frac{1}{d} 2(-3-2\sqrt{2}) \cos\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{\frac{7-5\sqrt{2}+(10-7\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]}{1+\cos\left[\frac{1}{2}(c+dx)\right]}} \\
 & \sqrt{\frac{-1+\sqrt{2}-(-2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]}{1+\cos\left[\frac{1}{2}(c+dx)\right]}} \left(1-\sqrt{2}+(-2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]\right) \\
 & \cos[c+dx] \left( \text{EllipticF}\left[\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] + \right. \\
 & \left. 2 \text{EllipticPi}\left[-3+2\sqrt{2}, -\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] \right) \\
 & \sqrt{\left(-1-\sqrt{2}+(2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]\right) \sec\left[\frac{1}{4}(c+dx)\right]^2 \sec\left[\frac{1}{2}(c+dx)\right]^5} \\
 & \left(a(1+\sec[c+dx])\right)^{5/2} \sqrt{3-2\sqrt{2}-\tan\left[\frac{1}{4}(c+dx)\right]^2}
 \end{aligned}$$

**Problem 112: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos[c+dx] (a+a \sec[c+dx])^{5/2} dx$$

Optimal (type 3, 94 leaves, 4 steps):

$$\frac{5 a^{5/2} \text{ArcTan}\left[\frac{\sqrt{a} \tan[c+dx]}{\sqrt{a+a \sec[c+dx]}}\right]}{d} - \frac{a^3 \sin[c+dx]}{d \sqrt{a+a \sec[c+dx]}} + \frac{2 a^2 \sqrt{a+a \sec[c+dx]} \sin[c+dx]}{d}$$

Result (type 4, 399 leaves):

$$\begin{aligned}
& \frac{1}{d} \cos [c+d x]^2 \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^5 \\
& \left(a\left(1+\operatorname{Sec}[c+d x]\right)\right)^{5 / 2}\left(\frac{3}{8} \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]+\frac{1}{8} \operatorname{Sin}\left[\frac{3}{2}(c+d x)\right]\right)+ \\
& \frac{1}{d} 5\left(2+\frac{3}{\sqrt{2}}\right) \cos \left[\frac{1}{4}(c+d x)\right]^4 \sqrt{\frac{7-5 \sqrt{2}+(10-7 \sqrt{2}) \cos \left[\frac{1}{2}(c+d x)\right]}{1+\cos \left[\frac{1}{2}(c+d x)\right]}} \\
& \left(\left(1-\sqrt{2}+(-2+\sqrt{2}) \cos \left[\frac{1}{2}(c+d x)\right]\right) \cos [c+d x] \right. \\
& \left.\left(\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+d x)\right]}{\sqrt{3-2 \sqrt{2}}}\right], 17-12 \sqrt{2}\right]+ \right. \right. \\
& \left. \left. 2 \operatorname{EllipticPi}\left[-3+2 \sqrt{2},-\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+d x)\right]}{\sqrt{3-2 \sqrt{2}}}\right], 17-12 \sqrt{2}\right]\right)\right) \\
& \sqrt{\left(-1+\sqrt{2}-(-2+\sqrt{2}) \cos \left[\frac{1}{2}(c+d x)\right]\right) \operatorname{Sec}\left[\frac{1}{4}(c+d x)\right]^2} \\
& \sqrt{\left(-1-\sqrt{2}+(2+\sqrt{2}) \cos \left[\frac{1}{2}(c+d x)\right]\right) \operatorname{Sec}\left[\frac{1}{4}(c+d x)\right]^2} \\
& \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^5\left(a\left(1+\operatorname{Sec}[c+d x]\right)\right)^{5 / 2} \sqrt{3-2 \sqrt{2}-\operatorname{Tan}\left[\frac{1}{4}(c+d x)\right]^2}
\end{aligned}$$

**Problem 113: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos [c+d x]^2\left(a+a \operatorname{Sec}[c+d x]\right)^{5 / 2} d x$$

Optimal (type 3, 106 leaves, 4 steps):

$$\begin{aligned}
& \frac{19 a^{5 / 2} \operatorname{ArcTan}\left[\frac{-\sqrt{a} \operatorname{Tan}[c+d x]}{\sqrt{a+a \operatorname{Sec}[c+d x]}}\right]}{4 d}+\frac{9 a^3 \operatorname{Sin}[c+d x]}{4 d \sqrt{a+a \operatorname{Sec}[c+d x]}}+ \\
& \frac{a^2 \cos [c+d x] \sqrt{a+a \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{2 d}
\end{aligned}$$

Result (type 4, 415 leaves):

$$\begin{aligned}
 & \frac{1}{d} \cos[c+dx]^2 \sec\left[\frac{1}{2}(c+dx)\right]^5 \left(a(1+\sec[c+dx])\right)^{5/2} \\
 & \left(-\frac{9}{32} \sin\left[\frac{1}{2}(c+dx)\right] + \frac{5}{16} \sin\left[\frac{3}{2}(c+dx)\right] + \frac{1}{32} \sin\left[\frac{5}{2}(c+dx)\right]\right) + \\
 & \frac{1}{8d} 19(4+3\sqrt{2}) \cos\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{\frac{7-5\sqrt{2}+(10-7\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]}{1+\cos\left[\frac{1}{2}(c+dx)\right]}} \\
 & \left(1-\sqrt{2}+(-2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]\right) \cos[c+dx] \\
 & \left(\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] + \right. \\
 & \left. 2 \operatorname{EllipticPi}\left[-3+2\sqrt{2}, -\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right]\right) \\
 & \sqrt{\left(-1+\sqrt{2}-(-2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]\right) \sec\left[\frac{1}{4}(c+dx)\right]^2} \\
 & \sqrt{\left(-1-\sqrt{2}+(2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]\right) \sec\left[\frac{1}{4}(c+dx)\right]^2} \\
 & \sec\left[\frac{1}{2}(c+dx)\right]^5 \left(a(1+\sec[c+dx])\right)^{5/2} \sqrt{3-2\sqrt{2}-\tan\left[\frac{1}{4}(c+dx)\right]^2}
 \end{aligned}$$

**Problem 114: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos[c+dx]^3 (a+a \sec[c+dx])^{5/2} dx$$

Optimal (type 3, 144 leaves, 5 steps):

$$\begin{aligned}
 & \frac{25 a^{5/2} \operatorname{ArcTan}\left[\frac{-\sqrt{a} \tan[c+dx]}{\sqrt{a+a \sec[c+dx]}}\right]}{8 d} + \frac{25 a^3 \sin[c+dx]}{8 d \sqrt{a+a \sec[c+dx]}} + \\
 & \frac{13 a^3 \cos[c+dx] \sin[c+dx]}{12 d \sqrt{a+a \sec[c+dx]}} + \frac{a^2 \cos[c+dx]^2 \sqrt{a+a \sec[c+dx]} \sin[c+dx]}{3 d}
 \end{aligned}$$

Result (type 4, 429 leaves):

$$\begin{aligned} & \frac{1}{d} \cos [c+d x]^2 \sec \left[ \frac{1}{2} (c+d x) \right]^5 \left( a \left( 1 + \sec [c+d x] \right) \right)^{5/2} \\ & \left( -\frac{47}{192} \sin \left[ \frac{1}{2} (c+d x) \right] + \frac{1}{3} \sin \left[ \frac{3}{2} (c+d x) \right] + \frac{5}{64} \sin \left[ \frac{5}{2} (c+d x) \right] + \frac{1}{96} \sin \left[ \frac{7}{2} (c+d x) \right] \right) + \\ & \frac{1}{8 d} 25 \left( 2 + \frac{3}{\sqrt{2}} \right) \cos \left[ \frac{1}{4} (c+d x) \right]^4 \sqrt{\frac{7-5 \sqrt{2} + (10-7 \sqrt{2}) \cos \left[ \frac{1}{2} (c+d x) \right]}{1+\cos \left[ \frac{1}{2} (c+d x) \right]}} \\ & \left( 1 - \sqrt{2} + (-2 + \sqrt{2}) \cos \left[ \frac{1}{2} (c+d x) \right] \right) \cos [c+d x] \\ & \left( \text{EllipticF} \left[ \text{ArcSin} \left[ \frac{\tan \left[ \frac{1}{4} (c+d x) \right]}{\sqrt{3-2 \sqrt{2}}} \right], 17-12 \sqrt{2} \right] + \right. \\ & \left. 2 \text{EllipticPi} \left[ -3+2 \sqrt{2}, -\text{ArcSin} \left[ \frac{\tan \left[ \frac{1}{4} (c+d x) \right]}{\sqrt{3-2 \sqrt{2}}} \right], 17-12 \sqrt{2} \right] \right) \\ & \sqrt{\left( -1 + \sqrt{2} - (-2 + \sqrt{2}) \cos \left[ \frac{1}{2} (c+d x) \right] \right) \sec \left[ \frac{1}{4} (c+d x) \right]^2} \\ & \sqrt{\left( -1 - \sqrt{2} + (2 + \sqrt{2}) \cos \left[ \frac{1}{2} (c+d x) \right] \right) \sec \left[ \frac{1}{4} (c+d x) \right]^2} \\ & \sec \left[ \frac{1}{2} (c+d x) \right]^5 \left( a \left( 1 + \sec [c+d x] \right) \right)^{5/2} \sqrt{3-2 \sqrt{2} - \tan \left[ \frac{1}{4} (c+d x) \right]^2} \end{aligned}$$

**Problem 115: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos [c+d x]^4 \left( a + a \sec [c+d x] \right)^{5/2} dx$$

Optimal (type 3, 182 leaves, 6 steps):

$$\begin{aligned} & \frac{163 a^{5/2} \text{ArcTan} \left[ \frac{\sqrt{a} \tan [c+d x]}{\sqrt{a+a \sec [c+d x]}} \right]}{64 d} + \frac{163 a^3 \sin [c+d x]}{64 d \sqrt{a+a \sec [c+d x]}} + \frac{163 a^3 \cos [c+d x] \sin [c+d x]}{96 d \sqrt{a+a \sec [c+d x]}} + \\ & \frac{17 a^3 \cos [c+d x]^2 \sin [c+d x]}{24 d \sqrt{a+a \sec [c+d x]}} + \frac{a^2 \cos [c+d x]^3 \sqrt{a+a \sec [c+d x]} \sin [c+d x]}{4 d} \end{aligned}$$

Result (type 4, 443 leaves):

$$\begin{aligned}
 & \frac{1}{d} \cos [c + d x]^2 \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^5 \\
 & \left( a (1 + \operatorname{Sec} [c + d x]) \right)^{5/2} \left( -\frac{265 \operatorname{Sin} \left[ \frac{1}{2} (c + d x) \right]}{1536} + \frac{55}{192} \operatorname{Sin} \left[ \frac{3}{2} (c + d x) \right] + \right. \\
 & \quad \left. \frac{47}{512} \operatorname{Sin} \left[ \frac{5}{2} (c + d x) \right] + \frac{5}{192} \operatorname{Sin} \left[ \frac{7}{2} (c + d x) \right] + \frac{1}{256} \operatorname{Sin} \left[ \frac{9}{2} (c + d x) \right] \right) + \\
 & \frac{1}{64 d} 163 \left( 2 + \frac{3}{\sqrt{2}} \right) \cos \left[ \frac{1}{4} (c + d x) \right]^4 \sqrt{\frac{7 - 5 \sqrt{2} + (10 - 7 \sqrt{2}) \cos \left[ \frac{1}{2} (c + d x) \right]}{1 + \cos \left[ \frac{1}{2} (c + d x) \right]}} \\
 & \left( 1 - \sqrt{2} + (-2 + \sqrt{2}) \cos \left[ \frac{1}{2} (c + d x) \right] \right) \cos [c + d x] \\
 & \left( \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right], 17 - 12 \sqrt{2} \right] + \right. \\
 & \quad \left. 2 \operatorname{EllipticPi} \left[ -3 + 2 \sqrt{2}, -\operatorname{ArcSin} \left[ \frac{\operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right], 17 - 12 \sqrt{2} \right] \right) \\
 & \sqrt{\left( -1 + \sqrt{2} - (-2 + \sqrt{2}) \cos \left[ \frac{1}{2} (c + d x) \right] \right) \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2} \\
 & \sqrt{\left( -1 - \sqrt{2} + (2 + \sqrt{2}) \cos \left[ \frac{1}{2} (c + d x) \right] \right) \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2} \\
 & \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^5 \left( a (1 + \operatorname{Sec} [c + d x]) \right)^{5/2} \sqrt{3 - 2 \sqrt{2} - \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2}
 \end{aligned}$$

**Problem 117: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \sqrt{a - a \operatorname{Sec} [c + d x]} dx$$

Optimal (type 3, 38 leaves, 2 steps):

$$\frac{2 \sqrt{a} \operatorname{ArcTan} \left[ \frac{\sqrt{a} \operatorname{Tan} [c + d x]}{\sqrt{a - a \operatorname{Sec} [c + d x]}} \right]}{d}$$

Result (type 3, 214 leaves):

$$\begin{aligned}
& - \left( \left( \cos [c + d x] \operatorname{Csc} \left[ \frac{1}{2} (c + d x) \right] \right. \right. \\
& \quad \left. \left( \operatorname{ArcTanh} \left[ \left( \cos \left[ \frac{c}{2} \right] + i \sin \left[ \frac{c}{2} \right] \right) \sqrt{(1 + e^{2 i d x}) \cos [c] + i (-1 + e^{2 i d x}) \sin [c]} \right] \right) + \right. \\
& \quad \left. \left. \operatorname{Log} \left[ 2 \left( e^{i d x} \cos \left[ \frac{c}{2} \right] + i e^{i d x} \sin \left[ \frac{c}{2} \right] + \sqrt{(1 + e^{2 i d x}) \cos [c] + i (-1 + e^{2 i d x}) \sin [c]} \right) \right] \right) \right) \\
& \quad \sqrt{a - a \operatorname{Sec} [c + d x]} \left( \cos \left[ \frac{d x}{2} \right] + i \sin \left[ \frac{d x}{2} \right] \right) \Bigg) / \\
& \quad \left( d \sqrt{(1 + e^{2 i d x}) \cos [c] + i (-1 + e^{2 i d x}) \sin [c]} \right) \Bigg)
\end{aligned}$$

**Problem 118: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \cos [c + d x] \sqrt{a - a \operatorname{Sec} [c + d x]} dx$$

Optimal (type 3, 65 leaves, 3 steps):

$$-\frac{\sqrt{a} \operatorname{ArcTan} \left[ \frac{\sqrt{a} \operatorname{Tan} [c + d x]}{\sqrt{a - a \operatorname{Sec} [c + d x]}} \right]}{d} + \frac{a \operatorname{Sin} [c + d x]}{d \sqrt{a - a \operatorname{Sec} [c + d x]}}$$

Result (type 3, 348 leaves):

$$\begin{aligned}
& \frac{1}{2 d \sqrt{(1 + e^{2 i d x}) \cos [c] + i (-1 + e^{2 i d x}) \sin [c]}} \\
& \cos [c + d x] \operatorname{Csc} \left[ \frac{1}{2} (c + d x) \right] \sqrt{a - a \operatorname{Sec} [c + d x]} \left( \cos \left[ \frac{d x}{2} \right] \right. \\
& \quad \left. \operatorname{Log} \left[ 2 \left( e^{i d x} \cos \left[ \frac{c}{2} \right] + i e^{i d x} \sin \left[ \frac{c}{2} \right] + \sqrt{(1 + e^{2 i d x}) \cos [c] + i (-1 + e^{2 i d x}) \sin [c]} \right) \right] \right) + \\
& \quad \operatorname{ArcTanh} \left[ \left( \cos \left[ \frac{c}{2} \right] + i \sin \left[ \frac{c}{2} \right] \right) \sqrt{(1 + e^{2 i d x}) \cos [c] + i (-1 + e^{2 i d x}) \sin [c]} \right] \\
& \quad \left( \cos \left[ \frac{d x}{2} \right] + i \sin \left[ \frac{d x}{2} \right] \right) + \\
& \quad i \operatorname{Log} \left[ 2 \left( e^{i d x} \cos \left[ \frac{c}{2} \right] + i e^{i d x} \sin \left[ \frac{c}{2} \right] + \sqrt{(1 + e^{2 i d x}) \cos [c] + i (-1 + e^{2 i d x}) \sin [c]} \right) \right] \\
& \quad \sin \left[ \frac{d x}{2} \right] - 2 \sqrt{2} \cos \left[ \frac{1}{2} (c + d x) \right] \sqrt{\cos [c + d x] \left( \cos [d x] + i \sin [d x] \right)} \Bigg)
\end{aligned}$$

**Problem 141: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec} [c + d x]}{\sqrt{a - a \operatorname{Sec} [c + d x]}} dx$$

Optimal (type 3, 48 leaves, 2 steps):



$$-\frac{\sqrt{2} \operatorname{ArcTan}\left[\frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{2} \sqrt{a-a \operatorname{Sec}[c+dx]}}\right]}{\sqrt{a} d}$$

Result (type 3, 113 leaves):

$$-\left(\left(i \sqrt{2} (-1 + e^{i(c+dx)}) \left(\operatorname{Log}[1 - e^{i(c+dx)}] - \operatorname{Log}[1 + e^{i(c+dx)} + \sqrt{2} \sqrt{1 + e^{2i(c+dx)}}]\right)\right)\right) / \left(d \sqrt{1 + e^{2i(c+dx)}} \sqrt{a - a \operatorname{Sec}[c + dx]}\right)$$

**Problem 142: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{1}{\sqrt{a - a \operatorname{Sec}[c + dx]}} dx$$

Optimal (type 3, 87 leaves, 5 steps):

$$\frac{2 \operatorname{ArcTan}\left[\frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{a-a \operatorname{Sec}[c+dx]}}\right]}{\sqrt{a} d} - \frac{\sqrt{2} \operatorname{ArcTan}\left[\frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{2} \sqrt{a-a \operatorname{Sec}[c+dx]}}\right]}{\sqrt{a} d}$$

Result (type 3, 157 leaves):

$$-\left(\left(i (-1 + e^{i(c+dx)}) \left(-i dx + \operatorname{ArcSinh}[e^{i(c+dx)}] + \sqrt{2} \operatorname{Log}[1 - e^{i(c+dx)}] + \operatorname{Log}[1 + \sqrt{1 + e^{2i(c+dx)}}]\right) - \sqrt{2} \operatorname{Log}[1 + e^{i(c+dx)} + \sqrt{2} \sqrt{1 + e^{2i(c+dx)}}]\right)\right) / \left(d \sqrt{1 + e^{2i(c+dx)}} \sqrt{a - a \operatorname{Sec}[c + dx]}\right)$$

**Problem 143: Result unnecessarily involves higher level functions.**

$$\int \operatorname{Sec}[c + dx]^3 (a + a \operatorname{Sec}[c + dx])^{2/3} dx$$

Optimal (type 4, 383 leaves, 7 steps):

$$\begin{aligned}
 & - \frac{9 (a + a \operatorname{Sec}[c + d x])^{2/3} \operatorname{Tan}[c + d x]}{40 d} + \\
 & \frac{57 (a + a \operatorname{Sec}[c + d x])^{2/3} \operatorname{Tan}[c + d x]}{80 d (1 + \operatorname{Sec}[c + d x])} + \frac{3 (a + a \operatorname{Sec}[c + d x])^{5/3} \operatorname{Tan}[c + d x]}{8 a d} - \\
 & \left( 19 \times 3^{3/4} \operatorname{EllipticF}\left[\operatorname{ArcCos}\left[\frac{2^{1/3} - (1 - \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3}}{2^{1/3} - (1 + \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3}}\right], \frac{1}{4} (2 + \sqrt{3})\right] \right) \\
 & (a + a \operatorname{Sec}[c + d x])^{2/3} (2^{1/3} - (1 + \operatorname{Sec}[c + d x])^{1/3}) \\
 & \sqrt{\frac{2^{2/3} + 2^{1/3} (1 + \operatorname{Sec}[c + d x])^{1/3} + (1 + \operatorname{Sec}[c + d x])^{2/3}}{(2^{1/3} - (1 + \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3})^2} \operatorname{Tan}[c + d x]} \Bigg/ \left( 80 \times 2^{1/3} d \right. \\
 & \left. (1 - \operatorname{Sec}[c + d x]) (1 + \operatorname{Sec}[c + d x]) \sqrt{-\frac{(1 + \operatorname{Sec}[c + d x])^{1/3} (2^{1/3} - (1 + \operatorname{Sec}[c + d x])^{1/3})}{(2^{1/3} - (1 + \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3})^2}} \right)
 \end{aligned}$$

Result (type 5, 105 leaves):

$$\begin{aligned}
 & \frac{1}{80 d} (a (1 + \operatorname{Sec}[c + d x]))^{2/3} \\
 & \left( 57 \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right] + 19 \times 2^{2/3} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]^2\right] \right) \\
 & \left( \frac{1}{1 + \operatorname{Sec}[c + d x]} \right)^{2/3} \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right] + 6 (2 + 5 \operatorname{Sec}[c + d x]) \operatorname{Tan}[c + d x]
 \end{aligned}$$

**Problem 144: Result unnecessarily involves higher level functions.**

$$\int \operatorname{Sec}[c + d x]^2 (a + a \operatorname{Sec}[c + d x])^{2/3} dx$$

Optimal (type 4, 353 leaves, 6 steps):

$$\frac{3 (a + a \operatorname{Sec}[c + d x])^{2/3} \operatorname{Tan}[c + d x]}{5 d} + \frac{3 (a + a \operatorname{Sec}[c + d x])^{2/3} \operatorname{Tan}[c + d x]}{5 d (1 + \operatorname{Sec}[c + d x])} -$$

$$\left( 3^{3/4} \operatorname{EllipticF}\left[\operatorname{ArcCos}\left[\frac{2^{1/3} - (1 - \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3}}{2^{1/3} - (1 + \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3}}\right], \frac{1}{4} (2 + \sqrt{3})\right] \right.$$

$$\left. (a + a \operatorname{Sec}[c + d x])^{2/3} (2^{1/3} - (1 + \operatorname{Sec}[c + d x])^{1/3}) \right.$$

$$\left. \sqrt{\frac{2^{2/3} + 2^{1/3} (1 + \operatorname{Sec}[c + d x])^{1/3} + (1 + \operatorname{Sec}[c + d x])^{2/3}}{(2^{1/3} - (1 + \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3})^2}} \operatorname{Tan}[c + d x] \right) / \left( 5 \times 2^{1/3} d \right.$$

$$\left. (1 - \operatorname{Sec}[c + d x]) (1 + \operatorname{Sec}[c + d x]) \sqrt{-\frac{(1 + \operatorname{Sec}[c + d x])^{1/3} (2^{1/3} - (1 + \operatorname{Sec}[c + d x])^{1/3})}{(2^{1/3} - (1 + \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3})^2}} \right)$$

Result (type 5, 97 leaves):

$$\frac{1}{5 d} (a (1 + \operatorname{Sec}[c + d x]))^{2/3}$$

$$\left( \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]^2\right] \left(\operatorname{Cos}[c + d x] \operatorname{Sec}\left[\frac{1}{2} (c + d x)\right]\right)^{2/3} \right.$$

$$\left. \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right] + 3 \left(\operatorname{Tan}\left[\frac{1}{2} (c + d x)\right] + \operatorname{Tan}[c + d x]\right) \right)$$

**Problem 145: Result unnecessarily involves higher level functions.**

$$\int \operatorname{Sec}[c + d x] (a + a \operatorname{Sec}[c + d x])^{2/3} dx$$

Optimal (type 4, 326 leaves, 5 steps):

$$\frac{3 (a + a \operatorname{Sec}[c + d x])^{2/3} \operatorname{Tan}[c + d x]}{2 d (1 + \operatorname{Sec}[c + d x])} -$$

$$\left( 3^{3/4} \operatorname{EllipticF}\left[\operatorname{ArcCos}\left[\frac{2^{1/3} - (1 - \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3}}{2^{1/3} - (1 + \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3}}\right], \frac{1}{4} (2 + \sqrt{3})\right] \right.$$

$$\left. (a + a \operatorname{Sec}[c + d x])^{2/3} (2^{1/3} - (1 + \operatorname{Sec}[c + d x])^{1/3}) \right.$$

$$\left. \sqrt{\frac{2^{2/3} + 2^{1/3} (1 + \operatorname{Sec}[c + d x])^{1/3} + (1 + \operatorname{Sec}[c + d x])^{2/3}}{(2^{1/3} - (1 + \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3})^2}} \operatorname{Tan}[c + d x] \right) / \left( 2 \times 2^{1/3} d \right.$$

$$\left. (1 - \operatorname{Sec}[c + d x]) (1 + \operatorname{Sec}[c + d x]) \sqrt{-\frac{(1 + \operatorname{Sec}[c + d x])^{1/3} (2^{1/3} - (1 + \operatorname{Sec}[c + d x])^{1/3})}{(2^{1/3} - (1 + \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3})^2}} \right)$$

Result (type 5, 75 leaves):

$$\frac{1}{2d} (a (1 + \text{Sec}[c + dx]))^{2/3} \left( 3 + 2^{2/3} \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{2}{3}, \frac{3}{2}, \text{Tan}\left[\frac{1}{2}(c + dx)\right]^2\right] \left(\frac{1}{1 + \text{Sec}[c + dx]}\right)^{2/3} \right) \text{Tan}\left[\frac{1}{2}(c + dx)\right]$$

**Problem 146: Result more than twice size of optimal antiderivative.**

$$\int (a + a \text{Sec}[c + dx])^{2/3} dx$$

Optimal (type 6, 77 leaves, 3 steps):

$$\left( 3\sqrt{2} \text{AppellF1}\left[\frac{7}{6}, \frac{1}{2}, 1, \frac{13}{6}, \frac{1}{2}(1 + \text{Sec}[c + dx]), 1 + \text{Sec}[c + dx]\right] (a + a \text{Sec}[c + dx])^{2/3} \text{Tan}[c + dx] \right) / \left( 7d\sqrt{1 - \text{Sec}[c + dx]} \right)$$

Result (type 6, 1575 leaves):

$$\begin{aligned} & \left( 9 \text{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \text{Tan}\left[\frac{1}{2}(c + dx)\right]^2, -\text{Tan}\left[\frac{1}{2}(c + dx)\right]^2\right] \right. \\ & \quad \left. (1 + \text{Sec}[c + dx])^{2/3} (a (1 + \text{Sec}[c + dx]))^{2/3} \text{Sin}[c + dx] \right) / \\ & \left( d \left( 9 \text{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \text{Tan}\left[\frac{1}{2}(c + dx)\right]^2, -\text{Tan}\left[\frac{1}{2}(c + dx)\right]^2\right] + \right. \right. \\ & \quad 2 \left( -3 \text{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(c + dx)\right]^2, -\text{Tan}\left[\frac{1}{2}(c + dx)\right]^2\right] + \right. \\ & \quad \left. \left. 2 \text{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(c + dx)\right]^2, -\text{Tan}\left[\frac{1}{2}(c + dx)\right]^2\right] \right) \text{Tan}\left[\frac{1}{2}(c + dx)\right]^2 \right) \\ & \left( \left( 9 \text{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \text{Tan}\left[\frac{1}{2}(c + dx)\right]^2, -\text{Tan}\left[\frac{1}{2}(c + dx)\right]^2\right] \right. \right. \\ & \quad \left. \left. \text{Cos}[c + dx] (1 + \text{Sec}[c + dx])^{2/3} \right) / \right. \\ & \left( 9 \text{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \text{Tan}\left[\frac{1}{2}(c + dx)\right]^2, -\text{Tan}\left[\frac{1}{2}(c + dx)\right]^2\right] + \right. \\ & \quad 2 \left( -3 \text{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(c + dx)\right]^2, -\text{Tan}\left[\frac{1}{2}(c + dx)\right]^2\right] + \right. \\ & \quad \left. \left. 2 \text{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(c + dx)\right]^2, -\text{Tan}\left[\frac{1}{2}(c + dx)\right]^2\right] \right) \text{Tan}\left[\frac{1}{2}(c + dx)\right]^2 \right) + \\ & \left( 9 (1 + \text{Sec}[c + dx])^{2/3} \text{Sin}[c + dx] \left( -\frac{1}{3} \text{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(c + dx)\right]^2, \right. \right. \right. \\ & \quad \left. \left. -\text{Tan}\left[\frac{1}{2}(c + dx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \text{Tan}\left[\frac{1}{2}(c + dx)\right] + \frac{2}{9} \text{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \right. \right. \\ & \quad \left. \left. \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(c + dx)\right]^2, -\text{Tan}\left[\frac{1}{2}(c + dx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \text{Tan}\left[\frac{1}{2}(c + dx)\right] \right) \right) / \\ & \left( 9 \text{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \text{Tan}\left[\frac{1}{2}(c + dx)\right]^2, -\text{Tan}\left[\frac{1}{2}(c + dx)\right]^2\right] + \right. \\ & \quad \left. 2 \left( -3 \text{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(c + dx)\right]^2, -\text{Tan}\left[\frac{1}{2}(c + dx)\right]^2\right] + \right. \right. \end{aligned}$$

$$\begin{aligned}
 & 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - \\
 & \left( 9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] (1 + \operatorname{Sec}[c+dx])^{2/3} \right. \\
 & \sin[c+dx] \left( 2 \left( -3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
 & \quad 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \quad \tan\left[\frac{1}{2}(c+dx)\right] + 9 \left( -\frac{1}{3} \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{2}{9} \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \right. \right. \\
 & \quad \quad \left. \left. \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) + \\
 & \quad 2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \left( -3 \left( -\frac{6}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 3, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{2}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 2, \frac{7}{2}, \right. \right. \right. \\
 & \quad \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) + \\
 & \quad 2 \left( -\frac{3}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \operatorname{AppellF1}\left[\frac{5}{2}, \frac{8}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) \Big/ \\
 & \left( 9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad 2 \left( -3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 + \\
 & \left. \left( 6 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \tan[c+dx]^2 \right) \right) \Big/ \\
 & \left( (1 + \operatorname{Sec}[c+dx])^{1/3} \left( 9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
 & \quad 2 \left( -3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \Big) \Big)
 \end{aligned}$$

**Problem 147: Result more than twice size of optimal antiderivative.**

$$\int \cos[c+dx] (a + a \operatorname{Sec}[c+dx])^{2/3} dx$$

Optimal (type 6, 77 leaves, 3 steps):

$$-\left( \left( 3\sqrt{2} \operatorname{AppellF1}\left[\frac{7}{6}, \frac{1}{2}, 2, \frac{13}{6}, \frac{1}{2} (1 + \operatorname{Sec}[c + dx]), 1 + \operatorname{Sec}[c + dx]\right] \right. \right. \\ \left. \left. (a + a \operatorname{Sec}[c + dx])^{2/3} \operatorname{Tan}[c + dx] \right) / \left( 7d\sqrt{1 - \operatorname{Sec}[c + dx]} \right) \right)$$

Result (type 6, 4011 leaves):

$$\left( \left( (1 + \operatorname{Cos}[c + dx]) \operatorname{Sec}[c + dx] \right)^{2/3} (a (1 + \operatorname{Sec}[c + dx]))^{2/3} \left( \operatorname{Sin}[c + dx] - \operatorname{Tan}\left[\frac{1}{2} (c + dx)\right] \right) \right) / \\ \left( d (1 + \operatorname{Sec}[c + dx])^{2/3} \right) - \\ \left( 2^{2/3} \operatorname{Cos}[c + dx] \left( \operatorname{Cos}\left[\frac{1}{2} (c + dx)\right]^2 \operatorname{Sec}[c + dx] \right)^{5/3} (a (1 + \operatorname{Sec}[c + dx]))^{2/3} \left( \frac{1}{6} \operatorname{Sec}\left[\frac{1}{2} (c + dx)\right]^2 \right. \right. \\ \left. \left. (1 + \operatorname{Sec}[c + dx])^{2/3} + \frac{1}{3} \operatorname{Cos}[c + dx] \operatorname{Sec}\left[\frac{1}{2} (c + dx)\right]^2 (1 + \operatorname{Sec}[c + dx])^{2/3} \right) \right. \\ \left. \operatorname{Tan}\left[\frac{1}{2} (c + dx)\right] \left( - \left( \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2} (c + dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2} (c + dx)\right]^2 \right] \right) / \right. \right. \\ \left. \left( \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2} (c + dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2} (c + dx)\right]^2 \right] + \right. \right. \\ \left. \left. \frac{2}{9} \left( -3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2} (c + dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2} (c + dx)\right]^2 \right] + 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2} (c + dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2} (c + dx)\right]^2 \right] \right) \operatorname{Tan}\left[\frac{1}{2} (c + dx)\right]^2 \right) \right) + \\ \left( 5 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2} (c + dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2} (c + dx)\right]^2 \right] \operatorname{Tan}\left[\frac{1}{2} (c + dx)\right]^2 \right) / \\ \left( 15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2} (c + dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2} (c + dx)\right]^2 \right] + \right. \\ \left. 2 \left( -3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2} (c + dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2} (c + dx)\right]^2 \right] + 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2} (c + dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2} (c + dx)\right]^2 \right] \right) \operatorname{Tan}\left[\frac{1}{2} (c + dx)\right]^2 \right) \right) / \\ \left( 3d (1 + \operatorname{Sec}[c + dx])^{2/3} \left( -\frac{1}{3 \times 2^{1/3}} \operatorname{Cos}[c + dx] \operatorname{Sec}\left[\frac{1}{2} (c + dx)\right]^2 \right. \right. \\ \left. \left( \operatorname{Cos}\left[\frac{1}{2} (c + dx)\right]^2 \operatorname{Sec}[c + dx] \right)^{5/3} \right. \\ \left. - \left( \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2} (c + dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2} (c + dx)\right]^2 \right] \right) / \right. \right. \\ \left. \left( \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2} (c + dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2} (c + dx)\right]^2 \right] + \frac{2}{9} \left( -3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2} (c + dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2} (c + dx)\right]^2 \right] + 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2} (c + dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2} (c + dx)\right]^2 \right] \right) \operatorname{Tan}\left[\frac{1}{2} (c + dx)\right]^2 \right) \right) + \\ \left( 5 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2} (c + dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2} (c + dx)\right]^2 \right] \operatorname{Tan}\left[\frac{1}{2} (c + dx)\right]^2 \right) / \\ \left( 15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2} (c + dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2} (c + dx)\right]^2 \right] + \right. \\ \left. 2 \left( -3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2} (c + dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2} (c + dx)\right]^2 \right] + 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2} (c + dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2} (c + dx)\right]^2 \right] \right) \operatorname{Tan}\left[\frac{1}{2} (c + dx)\right]^2 \right) \right)$$

$$\begin{aligned}
 & \left. \left. \left. \left. \left. \frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right) \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \right) \right) + \right. \\
 & \frac{1}{3} \times 2^{2/3} \left( \cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx] \right)^{5/3} \sin[c+dx] \tan\left[\frac{1}{2}(c+dx)\right] \\
 & \left( - \left( \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) / \right. \right. \right. \\
 & \left. \left( \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \right. \\
 & \left. \left. \frac{2}{9} \left( -3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) / \\
 & \left( 5 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) / \\
 & \left( 15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \left. 2 \left( -3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - \\
 & \frac{1}{3} \times 2^{2/3} \cos[c+dx] \left( \cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx] \right)^{5/3} \tan\left[\frac{1}{2}(c+dx)\right] \\
 & \left( - \left( \left( 3 \left( -\frac{1}{3} \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{2}{9} \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) \right) / \\
 & \left( \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \left. \frac{2}{9} \left( -3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) + \\
 & \left( 5 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) / \\
 & \left( 15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \left. 2 \left( -3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) + \\
 & \left( 5 \tan\left[\frac{1}{2}(c+dx)\right]^2 \left( -\frac{3}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right)
 \end{aligned}$$

$$\begin{aligned}
& \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{2}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \right. \\
& \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \Big) / \\
& \left( 15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& 2 \left( -3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \right. \right. \\
& \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \Big) + \\
& \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \left. \left( -\frac{1}{3} \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
& \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{2}{9} \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
& \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{2}{9} \left( -3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \right. \right. \\
& \left. \left. 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \right. \right. \\
& \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \\
& \left. \frac{2}{9} \tan\left[\frac{1}{2}(c+dx)\right]^2 \left( -3 \left( -\frac{6}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 3, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
& \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \right. \right. \\
& \left. \left. \frac{2}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right. \right. \\
& \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + 2 \left( -\frac{3}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 2, \right. \right. \right. \\
& \left. \left. \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \\
& \left. \left. \tan\left[\frac{1}{2}(c+dx)\right] + \operatorname{AppellF1}\left[\frac{5}{2}, \frac{8}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
& \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \Big) / \\
& \left( \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \frac{2}{9} \left( -3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \right. \right. \\
& \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \Big) - \\
& \left( 5 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
& \left. \left( 2 \left( -3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \right.
\end{aligned}$$



$$\begin{aligned}
 & 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \quad \left. -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \\
 & 15 \left(-\frac{3}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \quad \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \frac{2}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \right. \\
 & \quad \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \Big) + \\
 & 2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \left(-3 \left(-\frac{10}{7} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{2}{3}, 3, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \quad \left. \frac{10}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{5}{3}, 2, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) + 2 \left(-\frac{5}{7} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{5}{3}, 2, \right. \right. \\
 & \quad \left. \left. \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \quad \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \frac{25}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{8}{3}, 1, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \Big) \Big) / \\
 & \left(15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad \left. 2 \left(-3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \operatorname{AppellF1}\left[\right. \right. \right. \\
 & \quad \left. \left. \frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \Big) - \\
 & \frac{5}{9} \times 2^{2/3} \operatorname{Cos}[c+dx] \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Sec}[c+dx]\right)^{2/3} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \\
 & \left(-\left(\left(3 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right) / \right. \right. \\
 & \quad \left. \left(\operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. \frac{2}{9} \left(-3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \operatorname{AppellF1}\left[\right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \Big) + \\
 & \left(5 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) / \\
 & \left(15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad \left. 2 \left(-3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \operatorname{AppellF1}\left[\right. \right. \right.
 \end{aligned}$$

$$\left( \frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \left( -\cos\left[\frac{1}{2}(c+dx)\right] \sec[c+dx] \sin\left[\frac{1}{2}(c+dx)\right] + \cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx] \tan[c+dx] \right) \right)$$

**Problem 148: Result unnecessarily involves higher level functions.**

$$\int \sec[c+dx]^3 (a+a \sec[c+dx])^{5/3} dx$$

Optimal (type 4, 413 leaves, 8 steps):

$$\frac{147 a (a+a \sec[c+dx])^{2/3} \tan[c+dx]}{440 d} + \frac{1029 a (a+a \sec[c+dx])^{2/3} \tan[c+dx]}{880 d (1+\sec[c+dx])} - \frac{9 (a+a \sec[c+dx])^{5/3} \tan[c+dx]}{88 d} + \frac{3 (a+a \sec[c+dx])^{8/3} \tan[c+dx]}{11 a d} - \left( 343 \times 3^{3/4} a \operatorname{EllipticF}\left[\operatorname{ArcCos}\left[\frac{2^{1/3} - (1-\sqrt{3}) (1+\sec[c+dx])^{1/3}}{2^{1/3} - (1+\sqrt{3}) (1+\sec[c+dx])^{1/3}}\right], \frac{1}{4} (2+\sqrt{3})\right] (a+a \sec[c+dx])^{2/3} (2^{1/3} - (1+\sec[c+dx])^{1/3}) \sqrt{\frac{2^{2/3} + 2^{1/3} (1+\sec[c+dx])^{1/3} + (1+\sec[c+dx])^{2/3}}{(2^{1/3} - (1+\sqrt{3}) (1+\sec[c+dx])^{1/3})^2}} \tan[c+dx] \right) / \left( 880 \times 2^{1/3} d (1-\sec[c+dx]) (1+\sec[c+dx]) \sqrt{-\frac{(1+\sec[c+dx])^{1/3} (2^{1/3} - (1+\sec[c+dx])^{1/3})}{(2^{1/3} - (1+\sqrt{3}) (1+\sec[c+dx])^{1/3})^2}} \right)$$

Result (type 5, 116 leaves):

$$\frac{1}{880 d} a (a (1+\sec[c+dx]))^{2/3} \left( 1029 \tan\left[\frac{1}{2}(c+dx)\right] + 343 \times 2^{2/3} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{2}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2\right] \left(\frac{1}{1+\sec[c+dx]}\right)^{2/3} \tan\left[\frac{1}{2}(c+dx)\right] + 6 (74 + 65 \sec[c+dx] + 40 \sec[c+dx]^2) \tan[c+dx] \right)$$

**Problem 149: Result unnecessarily involves higher level functions.**

$$\int \sec[c+dx]^2 (a+a \sec[c+dx])^{5/3} dx$$

Optimal (type 4, 383 leaves, 7 steps):

$$\begin{aligned}
 & \frac{3 a (a + a \operatorname{Sec}[c + d x])^{2/3} \operatorname{Tan}[c + d x]}{8 d} + \\
 & \frac{21 a (a + a \operatorname{Sec}[c + d x])^{2/3} \operatorname{Tan}[c + d x]}{16 d (1 + \operatorname{Sec}[c + d x])} + \frac{3 (a + a \operatorname{Sec}[c + d x])^{5/3} \operatorname{Tan}[c + d x]}{8 d} - \\
 & \left( 7 \times 3^{3/4} a \operatorname{EllipticF}\left[\operatorname{ArcCos}\left[\frac{2^{1/3} - (1 - \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3}}{2^{1/3} - (1 + \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3}}\right], \frac{1}{4} (2 + \sqrt{3})\right] \right. \\
 & \quad \left. (a + a \operatorname{Sec}[c + d x])^{2/3} (2^{1/3} - (1 + \operatorname{Sec}[c + d x])^{1/3}) \right. \\
 & \quad \left. \sqrt{\frac{2^{2/3} + 2^{1/3} (1 + \operatorname{Sec}[c + d x])^{1/3} + (1 + \operatorname{Sec}[c + d x])^{2/3}}{(2^{1/3} - (1 + \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3})^2}} \operatorname{Tan}[c + d x] \right) / \left( 16 \times 2^{1/3} d \right. \\
 & \quad \left. (1 - \operatorname{Sec}[c + d x]) (1 + \operatorname{Sec}[c + d x]) \sqrt{-\frac{(1 + \operatorname{Sec}[c + d x])^{1/3} (2^{1/3} - (1 + \operatorname{Sec}[c + d x])^{1/3})}{(2^{1/3} - (1 + \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3})^2}} \right)
 \end{aligned}$$

Result (type 5, 104 leaves):

$$\begin{aligned}
 & \frac{1}{16 d} a (a (1 + \operatorname{Sec}[c + d x]))^{2/3} \\
 & \left( 21 \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right] + 7 \times 2^{2/3} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]^2\right] \right. \\
 & \quad \left. \left(\frac{1}{1 + \operatorname{Sec}[c + d x]}\right)^{2/3} \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right] + 6 (2 + \operatorname{Sec}[c + d x]) \operatorname{Tan}[c + d x] \right)
 \end{aligned}$$

**Problem 150: Result unnecessarily involves higher level functions.**

$$\int \operatorname{Sec}[c + d x] (a + a \operatorname{Sec}[c + d x])^{5/3} dx$$

Optimal (type 4, 356 leaves, 6 steps):

$$\frac{3 a (a + a \operatorname{Sec}[c + d x])^{2/3} \operatorname{Tan}[c + d x]}{5 d} + \frac{21 a (a + a \operatorname{Sec}[c + d x])^{2/3} \operatorname{Tan}[c + d x]}{10 d (1 + \operatorname{Sec}[c + d x])} -$$

$$\left( 7 \times 3^{3/4} a \operatorname{EllipticF}\left[\operatorname{ArcCos}\left[\frac{2^{1/3} - (1 - \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3}}{2^{1/3} - (1 + \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3}}\right], \frac{1}{4} (2 + \sqrt{3})\right] \right.$$

$$(a + a \operatorname{Sec}[c + d x])^{2/3} (2^{1/3} - (1 + \operatorname{Sec}[c + d x])^{1/3})$$

$$\left. \sqrt{\frac{2^{2/3} + 2^{1/3} (1 + \operatorname{Sec}[c + d x])^{1/3} + (1 + \operatorname{Sec}[c + d x])^{2/3}}{(2^{1/3} - (1 + \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3})^2} \operatorname{Tan}[c + d x]} \right) / \left( 10 \times 2^{1/3} d \right.$$

$$\left. (1 - \operatorname{Sec}[c + d x]) (1 + \operatorname{Sec}[c + d x]) \sqrt{-\frac{(1 + \operatorname{Sec}[c + d x])^{1/3} (2^{1/3} - (1 + \operatorname{Sec}[c + d x])^{1/3})}{(2^{1/3} - (1 + \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3})^2}} \right)$$

Result (type 5, 96 leaves):

$$\frac{1}{10 d} a (a (1 + \operatorname{Sec}[c + d x]))^{2/3}$$

$$\left( 21 \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right] + 7 \times 2^{2/3} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]^2\right] \right.$$

$$\left. \left(\frac{1}{1 + \operatorname{Sec}[c + d x]}\right)^{2/3} \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right] + 6 \operatorname{Tan}[c + d x] \right)$$

**Problem 151: Result more than twice size of optimal antiderivative.**

$$\int (a + a \operatorname{Sec}[c + d x])^{5/3} dx$$

Optimal (type 6, 86 leaves, 3 steps):

$$\left( 3 \sqrt{2} a \operatorname{AppellF1}\left[\frac{13}{6}, \frac{1}{2}, 1, \frac{19}{6}, \frac{1}{2} (1 + \operatorname{Sec}[c + d x]), 1 + \operatorname{Sec}[c + d x]\right] \right.$$

$$\left. (1 + \operatorname{Sec}[c + d x]) (a + a \operatorname{Sec}[c + d x])^{2/3} \operatorname{Tan}[c + d x] \right) / (13 d \sqrt{1 - \operatorname{Sec}[c + d x]})$$

Result (type 6, 3988 leaves):

$$\left( 3 ((1 + \operatorname{Cos}[c + d x]) \operatorname{Sec}[c + d x])^{2/3} (a (1 + \operatorname{Sec}[c + d x]))^{5/3} \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right] \right) /$$

$$(2 d (1 + \operatorname{Sec}[c + d x])^{5/3}) +$$

$$\left( 5 \operatorname{Cos}[c + d x] \left(\operatorname{Cos}\left[\frac{1}{2} (c + d x)\right]^2 \operatorname{Sec}[c + d x]\right)^{5/3} (a (1 + \operatorname{Sec}[c + d x]))^{5/3} \left(\frac{3}{4} \operatorname{Sec}\left[\frac{1}{2} (c + d x)\right]^2 \right.$$

$$\left. (1 + \operatorname{Sec}[c + d x])^{2/3} + \frac{1}{2} \operatorname{Cos}[c + d x] \operatorname{Sec}\left[\frac{1}{2} (c + d x)\right]^2 (1 + \operatorname{Sec}[c + d x])^{2/3} \right)$$

$$\operatorname{Tan}\left[\frac{1}{2} (c + d x)\right] \left(\operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]^2\right] \right) /$$

$$\left(\operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]^2\right] + \right.$$



$$\begin{aligned}
& 2 \left( -3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + 2 \operatorname{AppellF1} \left[ \right. \right. \\
& \quad \left. \left. \frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \Big) + \\
& \frac{1}{2^{1/3}} 5 \cos [c+dx] \left( \cos \left[ \frac{1}{2} (c+dx) \right]^2 \sec [c+dx] \right)^{5/3} \tan \left[ \frac{1}{2} (c+dx) \right] \\
& \left( \left( -\frac{1}{3} \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \right. \\
& \quad \left. \left. \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + \frac{2}{9} \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \right. \right. \right. \\
& \quad \left. \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \right) \Big) / \\
& \left( \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
& \quad \left. \frac{2}{9} \left( -3 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + 2 \operatorname{AppellF1} \left[ \right. \right. \right. \\
& \quad \left. \left. \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) + \\
& \left( \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \\
& \quad \left. \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \right) \Big) / \\
& \left( 15 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
& \quad 2 \left( -3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + 2 \operatorname{AppellF1} \left[ \right. \right. \\
& \quad \left. \left. \frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) + \\
& \left( \tan \left[ \frac{1}{2} (c+dx) \right]^2 \left( -\frac{3}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \right. \\
& \quad \left. \left. \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + \frac{2}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \right. \right. \right. \\
& \quad \left. \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \right) \right) \Big) / \\
& \left( 15 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
& \quad 2 \left( -3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + 2 \operatorname{AppellF1} \left[ \right. \right. \\
& \quad \left. \left. \frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) - \\
& \left( \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \\
& \quad \left. \left( -\frac{1}{3} \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \right. \\
& \quad \left. \left. \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + \frac{2}{9} \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
 & \left( \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{2}{9} \\
 & \left( -3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad \left. 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \\
 & \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{2}{9} \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \left( -3 \left( -\frac{6}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 3, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right. \\
 & \quad \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{2}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 2, \frac{7}{2}, \right. \\
 & \quad \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \quad \left. \tan\left[\frac{1}{2}(c+dx)\right] \right) + 2 \left( -\frac{3}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \quad \left. \operatorname{AppellF1}\left[\frac{5}{2}, \frac{8}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right. \\
 & \quad \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) / \\
 & \left( \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \frac{2}{9} \left( -3 \right. \right. \\
 & \quad \left. \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \operatorname{AppellF1}\left[ \right. \right. \\
 & \quad \left. \left. \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 - \\
 & \left( \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \quad \left. \left( 2 \left( -3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \right. \\
 & \quad \left. \left. 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right) \right. \\
 & \quad \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + 15 \left( -\frac{3}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \right. \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \right. \\
 & \quad \left. \left. \frac{2}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right. \\
 & \quad \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) + 2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \left( -3 \left( -\frac{10}{7} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{2}{3}, 3, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right. \\
 & \quad \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{10}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{5}{3}, 2, \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right) \right)
 \end{aligned}$$

$$\begin{aligned}
& \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \sec\left[\frac{1}{2}(c+dx)\right]^2 \\
& \tan\left[\frac{1}{2}(c+dx)\right] + 2 \left( -\frac{5}{7} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{5}{3}, 2, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \\
& \quad \left. \frac{25}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{8}{3}, 1, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \quad \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \Big/ \\
& \left( 15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \left( -3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \right. \right. \right. \\
& \quad \left. \left. \frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \right. \right. \\
& \quad \left. \left. 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) + \\
& \frac{1}{3 \times 2^{1/3}} 25 \cos[c+dx] \left( \cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx] \right)^{2/3} \tan\left[\frac{1}{2}(c+dx)\right] \\
& \left( \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \Big/ \right. \\
& \quad \left( \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad \left. \frac{2}{9} \left( -3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) + \\
& \quad \left. \left( \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \Big/ \right. \\
& \quad \left( 15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad \left. 2 \left( -3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \\
& \left( -\cos\left[\frac{1}{2}(c+dx)\right] \sec[c+dx] \sin\left[\frac{1}{2}(c+dx)\right] + \cos\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
& \quad \left. \left. \sec[c+dx] \tan[c+dx] \right) \right) \Big) \Big) \Big)
\end{aligned}$$

**Problem 152: Result more than twice size of optimal antiderivative.**

$$\int \cos[c+dx] (a + a \sec[c+dx])^{5/3} dx$$

Optimal (type 6, 86 leaves, 3 steps):



$$- \left( \left( 3\sqrt{2} a \operatorname{AppellF1} \left[ \frac{13}{6}, \frac{1}{2}, 2, \frac{19}{6}, \frac{1}{2} (1 + \sec[c + dx]), 1 + \sec[c + dx] \right] \right. \right. \\ \left. \left. (1 + \sec[c + dx]) (a + a \sec[c + dx])^{2/3} \tan[c + dx] \right) / (13 d \sqrt{1 - \sec[c + dx]}) \right)$$

Result (type 6, 4011 leaves):

$$\left( \left( (1 + \cos[c + dx]) \sec[c + dx] \right)^{2/3} (a (1 + \sec[c + dx]))^{5/3} \left( \sin[c + dx] - \tan \left[ \frac{1}{2} (c + dx) \right] \right) \right) / \\ \left( d (1 + \sec[c + dx])^{5/3} \right) - \\ \left( 2^{2/3} \cos[c + dx] \left( \cos \left[ \frac{1}{2} (c + dx) \right]^2 \sec[c + dx] \right)^{5/3} (a (1 + \sec[c + dx]))^{5/3} \left( \frac{2}{3} \sec \left[ \frac{1}{2} (c + dx) \right]^2 \right. \right. \\ \left. \left. (1 + \sec[c + dx])^{2/3} + \frac{5}{6} \cos[c + dx] \sec \left[ \frac{1}{2} (c + dx) \right]^2 (1 + \sec[c + dx])^{2/3} \right) \right. \\ \left. \tan \left[ \frac{1}{2} (c + dx) \right] \left( - \left( \left( 9 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] \right) / \right. \right. \right. \\ \left. \left( \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] + \right. \right. \\ \left. \left. \frac{2}{9} \left( -3 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] + 2 \operatorname{AppellF1} \left[ \right. \right. \right. \right. \\ \left. \left. \left. \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c + dx) \right]^2 \right) \right) + \\ \left( 5 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] \tan \left[ \frac{1}{2} (c + dx) \right]^2 \right) / \\ \left( 15 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] + \right. \\ \left. 2 \left( -3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] + 2 \operatorname{AppellF1} \left[ \frac{5}{2}, \right. \right. \right. \\ \left. \left. \left. \frac{5}{3}, 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c + dx) \right]^2 \right) \right) \right) / \\ \left( 3 d (1 + \sec[c + dx])^{5/3} \left( -\frac{1}{3 \times 2^{1/3}} \cos[c + dx] \sec \left[ \frac{1}{2} (c + dx) \right]^2 \right. \right. \\ \left. \left. \left( \cos \left[ \frac{1}{2} (c + dx) \right]^2 \sec[c + dx] \right)^{5/3} \right. \right. \\ \left. \left( - \left( \left( 9 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] \right) / \right. \right. \right. \\ \left. \left( \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] + \frac{2}{9} \left( -3 \operatorname{AppellF1} \left[ \right. \right. \right. \right. \\ \left. \left. \left. \frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] + 2 \operatorname{AppellF1} \left[ \frac{3}{2}, \right. \right. \right. \\ \left. \left. \left. \frac{5}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c + dx) \right]^2 \right) \right) + \\ \left( 5 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] \tan \left[ \frac{1}{2} (c + dx) \right]^2 \right) / \\ \left( 15 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] + \right. \\ \left. 2 \left( -3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] + 2 \operatorname{AppellF1} \left[ \right. \right. \right. \right. \\ \left. \left. \left. \frac{5}{3}, 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c + dx) \right]^2 \right) \right) \right) /$$





$$\begin{aligned}
& 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
& \quad \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \\
& 15 \left(-\frac{3}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \quad \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{2}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \right. \\
& \quad \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \Big) + \\
& 2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \left(-3 \left(-\frac{10}{7} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{2}{3}, 3, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \\
& \quad \left. \frac{10}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{5}{3}, 2, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \quad \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + 2 \left(-\frac{5}{7} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{5}{3}, 2, \right. \right. \\
& \quad \left. \left. \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
& \quad \left. \tan\left[\frac{1}{2}(c+dx)\right] + \frac{25}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{8}{3}, 1, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \Big) \Big) / \\
& \left(15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad \left. 2 \left(-3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \operatorname{AppellF1}\left[\right. \right. \right. \\
& \quad \left. \left. \frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \Big) - \\
& \frac{5}{9} \times 2^{2/3} \operatorname{Cos}[c+dx] \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Sec}[c+dx]\right)^{2/3} \tan\left[\frac{1}{2}(c+dx)\right] \\
& \left(-\left(\left(9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) / \right. \right. \\
& \quad \left. \left(\operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
& \quad \left. \frac{2}{9} \left(-3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \operatorname{AppellF1}\left[\right. \right. \right. \\
& \quad \left. \left. \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \Big) \Big) + \\
& \left(5 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) / \\
& \left(15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad \left. 2 \left(-3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \operatorname{AppellF1}\left[\right. \right. \right.
\end{aligned}$$

$$\left( \frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \left( -\cos\left[\frac{1}{2}(c+dx)\right] \sec[c+dx] \sin\left[\frac{1}{2}(c+dx)\right] + \cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx] \tan[c+dx] \right) \right)$$

**Problem 153: Result unnecessarily involves higher level functions.**

$$\int \frac{\sec[c+dx]^4}{(a+a \sec[c+dx])^{1/3}} dx$$

Optimal (type 4, 371 leaves, 7 steps):

$$\frac{99 \tan[c+dx]}{80 d (a+a \sec[c+dx])^{1/3}} + \frac{3 \sec[c+dx]^2 \tan[c+dx]}{8 d (a+a \sec[c+dx])^{1/3}} - \frac{3 (a+a \sec[c+dx])^{2/3} \tan[c+dx]}{40 a d} + \left( 37 \times 3^{3/4} \text{EllipticF}\left[\text{ArcCos}\left[\frac{2^{1/3} - (1-\sqrt{3}) (1+\sec[c+dx])^{1/3}}{2^{1/3} - (1+\sqrt{3}) (1+\sec[c+dx])^{1/3}}\right], \frac{1}{4} (2+\sqrt{3})\right] \right. \\ \left. (2^{1/3} - (1+\sec[c+dx])^{1/3}) \sqrt{\frac{2^{2/3} + 2^{1/3} (1+\sec[c+dx])^{1/3} + (1+\sec[c+dx])^{2/3}}{(2^{1/3} - (1+\sqrt{3}) (1+\sec[c+dx])^{1/3})^2}} \right. \\ \left. \tan[c+dx] \right) / \left( 80 \times 2^{1/3} d (1-\sec[c+dx]) (a+a \sec[c+dx])^{1/3} \sqrt{-\frac{(1+\sec[c+dx])^{1/3} (2^{1/3} - (1+\sec[c+dx])^{1/3})}{(2^{1/3} - (1+\sqrt{3}) (1+\sec[c+dx])^{1/3})^2}} \right)$$

Result (type 5, 108 leaves):

$$\frac{1}{80 a d} (a (1+\sec[c+dx]))^{2/3} \left( 129 \tan\left[\frac{1}{2}(c+dx)\right] - 37 \times 2^{2/3} \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{2}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \left( \frac{1}{1+\sec[c+dx]} \right)^{2/3} \tan\left[\frac{1}{2}(c+dx)\right] + 6 (-6+5 \sec[c+dx]) \tan[c+dx]$$

**Problem 154: Result unnecessarily involves higher level functions.**

$$\int \frac{\sec[c+dx]^3}{(a+a \sec[c+dx])^{1/3}} dx$$

Optimal (type 4, 336 leaves, 6 steps):

$$\begin{aligned}
& -\frac{9 \operatorname{Tan}[c+d x]}{10 d (a+a \operatorname{Sec}[c+d x])^{1/3}} + \frac{3 (a+a \operatorname{Sec}[c+d x])^{2/3} \operatorname{Tan}[c+d x]}{5 a d} - \\
& \left( 7 \times 3^{3/4} \operatorname{EllipticF}\left[\operatorname{ArcCos}\left[\frac{2^{1/3} - (1-\sqrt{3}) (1+\operatorname{Sec}[c+d x])^{1/3}}{2^{1/3} - (1+\sqrt{3}) (1+\operatorname{Sec}[c+d x])^{1/3}}\right], \frac{1}{4} (2+\sqrt{3})\right] \right. \\
& \left. (2^{1/3} - (1+\operatorname{Sec}[c+d x])^{1/3}) \sqrt{\frac{2^{2/3} + 2^{1/3} (1+\operatorname{Sec}[c+d x])^{1/3} + (1+\operatorname{Sec}[c+d x])^{2/3}}{(2^{1/3} - (1+\sqrt{3}) (1+\operatorname{Sec}[c+d x])^{1/3})^2}} \right. \\
& \left. \operatorname{Tan}[c+d x] \right) / \left( 10 \times 2^{1/3} d (1-\operatorname{Sec}[c+d x]) (a+a \operatorname{Sec}[c+d x])^{1/3} \right. \\
& \left. \sqrt{-\frac{(1+\operatorname{Sec}[c+d x])^{1/3} (2^{1/3} - (1+\operatorname{Sec}[c+d x])^{1/3})}{(2^{1/3} - (1+\sqrt{3}) (1+\operatorname{Sec}[c+d x])^{1/3})^2}} \right)
\end{aligned}$$

Result (type 5, 98 leaves):

$$\begin{aligned}
& \frac{1}{10 a d} (a (1+\operatorname{Sec}[c+d x]))^{2/3} \\
& \left( -9 \operatorname{Tan}\left[\frac{1}{2} (c+d x)\right] + 7 \times 2^{2/3} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2} (c+d x)\right]^2\right] \right. \\
& \left. \left(\frac{1}{1+\operatorname{Sec}[c+d x]}\right)^{2/3} \operatorname{Tan}\left[\frac{1}{2} (c+d x)\right] + 6 \operatorname{Tan}[c+d x] \right)
\end{aligned}$$

**Problem 155: Result unnecessarily involves higher level functions.**

$$\int \frac{\operatorname{Sec}[c+d x]^2}{(a+a \operatorname{Sec}[c+d x])^{1/3}} dx$$

Optimal (type 4, 306 leaves, 5 steps):

$$\frac{3 \operatorname{Tan}[c + d x]}{2 d (a + a \operatorname{Sec}[c + d x])^{1/3}} +$$

$$\left( 3^{3/4} \operatorname{EllipticF}\left[\operatorname{ArcCos}\left[\frac{2^{1/3} - (1 - \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3}}{2^{1/3} - (1 + \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3}}\right], \frac{1}{4} (2 + \sqrt{3})\right] \right.$$

$$\left. \left( 2^{1/3} - (1 + \operatorname{Sec}[c + d x])^{1/3} \right) \sqrt{\frac{2^{2/3} + 2^{1/3} (1 + \operatorname{Sec}[c + d x])^{1/3} + (1 + \operatorname{Sec}[c + d x])^{2/3}}{(2^{1/3} - (1 + \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3})^2}} \right.$$

$$\left. \operatorname{Tan}[c + d x] \right) / \left( 2 \times 2^{1/3} d (1 - \operatorname{Sec}[c + d x]) (a + a \operatorname{Sec}[c + d x])^{1/3} \right.$$

$$\left. \sqrt{-\frac{(1 + \operatorname{Sec}[c + d x])^{1/3} (2^{1/3} - (1 + \operatorname{Sec}[c + d x])^{1/3})}{(2^{1/3} - (1 + \sqrt{3}) (1 + \operatorname{Sec}[c + d x])^{1/3})^2}} \right)$$

Result(type 5, 78 leaves):

$$-\frac{1}{2 a d} (a (1 + \operatorname{Sec}[c + d x]))^{2/3}$$

$$\left( -3 + 2^{2/3} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]^2\right] \left(\frac{1}{1 + \operatorname{Sec}[c + d x]}\right)^{2/3} \right)$$

$$\operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]$$

**Problem 156: Result unnecessarily involves higher level functions.**

$$\int \frac{\operatorname{Sec}[c + d x]}{(a + a \operatorname{Sec}[c + d x])^{1/3}} dx$$

Optimal (type 4, 276 leaves, 4 steps):

$$\begin{aligned}
 & - \left( \left( 3^{3/4} \text{EllipticF} \left[ \text{ArcCos} \left[ \frac{2^{1/3} - (1 - \sqrt{3}) (1 + \text{Sec}[c + d x])^{1/3}}{2^{1/3} - (1 + \sqrt{3}) (1 + \text{Sec}[c + d x])^{1/3}} \right], \frac{1}{4} (2 + \sqrt{3}) \right] \right. \right. \\
 & \quad \left. \left. (2^{1/3} - (1 + \text{Sec}[c + d x])^{1/3}) \sqrt{\frac{2^{2/3} + 2^{1/3} (1 + \text{Sec}[c + d x])^{1/3} + (1 + \text{Sec}[c + d x])^{2/3}}{(2^{1/3} - (1 + \sqrt{3}) (1 + \text{Sec}[c + d x])^{1/3})^2}} \right. \right. \\
 & \quad \left. \left. \text{Tan}[c + d x] \right) / \left( 2^{1/3} d (1 - \text{Sec}[c + d x]) (a + a \text{Sec}[c + d x])^{1/3} \right. \right. \\
 & \quad \left. \left. \sqrt{-\frac{(1 + \text{Sec}[c + d x])^{1/3} (2^{1/3} - (1 + \text{Sec}[c + d x])^{1/3})}{(2^{1/3} - (1 + \sqrt{3}) (1 + \text{Sec}[c + d x])^{1/3})^2}} \right) \right)
 \end{aligned}$$

Result (type 5, 76 leaves):

$$\begin{aligned}
 & \frac{1}{a d} \text{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{2}{3}, \frac{3}{2}, \text{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right] \\
 & \left( \text{Cos}[c + d x] \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \right)^{2/3} (a (1 + \text{Sec}[c + d x]))^{2/3} \text{Tan} \left[ \frac{1}{2} (c + d x) \right]
 \end{aligned}$$

**Problem 157: Result more than twice size of optimal antiderivative.**

$$\int \frac{1}{(a + a \text{Sec}[c + d x])^{1/3}} dx$$

Optimal (type 6, 75 leaves, 3 steps):

$$\begin{aligned}
 & \left( 3 \sqrt{2} \text{AppellF1} \left[ \frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \frac{1}{2} (1 + \text{Sec}[c + d x]), 1 + \text{Sec}[c + d x] \right] \text{Tan}[c + d x] \right) / \\
 & \left( d \sqrt{1 - \text{Sec}[c + d x]} (a + a \text{Sec}[c + d x])^{1/3} \right)
 \end{aligned}$$

Result (type 6, 733 leaves):



$$\begin{aligned}
 & \left( 45 \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{1}{3}, 1, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \\
 & \quad \left. \operatorname{Cos} [c+dx]^2 (1+\operatorname{Cos} [c+dx]) \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 (a(1+\operatorname{Sec} [c+dx]))^{2/3} \right. \\
 & \quad \left. \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] \left( 9 \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{1}{3}, 1, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] - \right. \right. \\
 & \quad \left. \left. 2 \left( 3 \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{1}{3}, 2, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \right. \right. \\
 & \quad \left. \left. \left. \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) \Big/ \\
 & \left( a d \left( 135 \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{1}{3}, 1, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \right. \\
 & \quad \left. \left. (1+2 \operatorname{Cos} [c+dx]+3 \operatorname{Cos} [2(c+dx)]) + \right. \right. \\
 & \quad \left. \left. \frac{3}{2} \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{1}{3}, 1, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \right. \right. \\
 & \quad \left. \left. \left( 15 \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{1}{3}, 2, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \right. \right. \\
 & \quad \left. \left. \left. (8+15 \operatorname{Cos} [c+dx]+4 \operatorname{Cos} [2(c+dx)]-3 \operatorname{Cos} [3(c+dx)]) + \right. \right. \right. \\
 & \quad \left. \left. \left. 5 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \right. \right. \\
 & \quad \left. \left. \left. (8+15 \operatorname{Cos} [c+dx]+4 \operatorname{Cos} [2(c+dx)]-3 \operatorname{Cos} [3(c+dx)]) - \right. \right. \right. \\
 & \quad \left. \left. \left. 96 \left( 9 \operatorname{AppellF1} \left[ \frac{5}{2}, -\frac{1}{3}, 3, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \right. \right. \\
 & \quad \left. \left. \left. 3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] - \right. \right. \right. \\
 & \quad \left. \left. \left. \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \right. \right. \\
 & \quad \left. \left. \operatorname{Cos} [c+dx] \operatorname{Sin} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 + \right. \\
 & \quad \left. 40 \left( 3 \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{1}{3}, 2, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \operatorname{AppellF1} \left[ \frac{3}{2}, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{2}{3}, 1, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right)^2 \operatorname{Cos} [c+dx] \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^4 \right) \Big)
 \end{aligned}$$

**Problem 158: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Cos} [c+dx]}{(a+a \operatorname{Sec} [c+dx])^{1/3}} dx$$

Optimal (type 6, 75 leaves, 3 steps):

$$\begin{aligned}
 & - \left( \left( 3 \sqrt{2} \operatorname{AppellF1} \left[ \frac{1}{6}, \frac{1}{2}, 2, \frac{7}{6}, \frac{1}{2} (1+\operatorname{Sec} [c+dx]), 1+\operatorname{Sec} [c+dx] \right] \operatorname{Tan} [c+dx] \right) \Big/ \right. \\
 & \quad \left. \left( d \sqrt{1-\operatorname{Sec} [c+dx]} (a+a \operatorname{Sec} [c+dx])^{1/3} \right) \right)
 \end{aligned}$$

Result (type 6, 1986 leaves):

$$\begin{aligned}
& \left( \left( (1 + \cos[c + dx]) \sec[c + dx] \right)^{2/3} (1 + \sec[c + dx])^{1/3} \left( \sin[c + dx] - \tan\left[\frac{1}{2}(c + dx)\right] \right) \right) / \\
& \left( d (a (1 + \sec[c + dx]))^{1/3} + \right. \\
& \left( 10 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] (1 + \sec[c + dx]) \right. \\
& \left. \left( \frac{1}{6} \sec\left[\frac{1}{2}(c + dx)\right]^2 (1 + \sec[c + dx])^{2/3} - \frac{1}{6} \cos[c + dx] \sec\left[\frac{1}{2}(c + dx)\right]^2 \right. \right. \\
& \left. \left. (1 + \sec[c + dx])^{2/3} \right) \sin\left[\frac{1}{2}(c + dx)\right]^2 \tan\left[\frac{1}{2}(c + dx)\right] \right) / \\
& \left( d (a (1 + \sec[c + dx]))^{1/3} \left( 45 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] + \right. \right. \\
& \left. \left. 6 \left( -3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] + \right. \right. \right. \\
& \left. \left. \left. 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c + dx)\right]^2 \right) \right) \\
& \left( \left( 10 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] \right. \right. \\
& \left. \left. (1 + \sec[c + dx])^{2/3} \sin\left[\frac{1}{2}(c + dx)\right]^2 \right) / \right. \\
& \left( 45 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] + \right. \\
& \left. 6 \left( -3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] + 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c + dx)\right]^2 \right) + \\
& \left( 5 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] \right. \\
& \left. (1 + \sec[c + dx])^{2/3} \tan\left[\frac{1}{2}(c + dx)\right]^2 \right) / \\
& \left( 45 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] + \right. \\
& \left. 6 \left( -3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] + 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c + dx)\right]^2 \right) + \\
& \left( 10 (1 + \sec[c + dx])^{2/3} \sin\left[\frac{1}{2}(c + dx)\right]^2 \tan\left[\frac{1}{2}(c + dx)\right] \right. \\
& \left. \left( -\frac{3}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] \sec\left[\frac{1}{2}(c + dx)\right]^2 \right. \right. \\
& \left. \left. \tan\left[\frac{1}{2}(c + dx)\right] + \frac{2}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] \right. \right. \\
& \left. \left. \sec\left[\frac{1}{2}(c + dx)\right]^2 \tan\left[\frac{1}{2}(c + dx)\right] \right) \right) / \\
& \left( 45 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] + \right. \\
& \left. 6 \left( -3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] + 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] \right) \right)
\end{aligned}$$

$$\begin{aligned}
 & \left. \left( \frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 - \right. \\
 & \left. \left( 10 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \right. \\
 & \quad \left. \left( 1 + \operatorname{Sec} [c+dx] \right)^{2/3} \sin \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \right. \\
 & \quad \left( 6 \left( -3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + 2 \operatorname{AppellF1} \left[ \frac{5}{2}, \right. \right. \right. \\
 & \quad \left. \frac{5}{3}, 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} \right. \\
 & \quad \left. (c+dx) \right] + 45 \left( -\frac{3}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right. \\
 & \quad \left. \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + \frac{2}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \right) + 6 \tan \left[ \frac{1}{2} (c+dx) \right]^2 \\
 & \quad \left( -3 \left( -\frac{10}{7} \operatorname{AppellF1} \left[ \frac{7}{2}, \frac{2}{3}, 3, \frac{9}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \right. \\
 & \quad \left. \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + \frac{10}{21} \operatorname{AppellF1} \left[ \frac{7}{2}, \frac{5}{3}, 2, \frac{9}{2}, \right. \right. \\
 & \quad \left. \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \right) + \\
 & \quad \left. 2 \left( -\frac{5}{7} \operatorname{AppellF1} \left[ \frac{7}{2}, \frac{5}{3}, 2, \frac{9}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \right. \\
 & \quad \left. \left. \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + \frac{25}{21} \operatorname{AppellF1} \left[ \frac{7}{2}, \frac{8}{3}, 1, \frac{9}{2}, \tan \left[ \frac{1}{2} (c+ \right. \right. \right. \\
 & \quad \left. \left. \left. dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \right) \right) \right) \Bigg) / \\
 & \left( 45 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & \quad \left. 6 \left( -3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + 2 \operatorname{AppellF1} \left[ \right. \right. \right. \\
 & \quad \left. \frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right)^2 + \\
 & \left. \left( 20 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \operatorname{Sec} [c+dx] \right. \right. \\
 & \quad \left. \left. \sin \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \tan [c+dx] \right) \right) / \\
 & \left( 3 \left( 1 + \operatorname{Sec} [c+dx] \right)^{1/3} \left( 45 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \right. \\
 & \quad \left. \left. 6 \left( -3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + 2 \operatorname{AppellF1} \left[ \frac{5}{2}, \right. \right. \right. \\
 & \quad \left. \frac{5}{3}, 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) \right) \Bigg)
 \end{aligned}$$

Problem 159: Result unnecessarily involves higher level functions.

$$\int \frac{\text{Sec}[c + d x]^4}{(a + a \text{Sec}[c + d x])^{5/3}} dx$$

Optimal (type 4, 766 leaves, 9 steps):

$$\begin{aligned} & -\frac{33 \text{Tan}[c + d x]}{28 d (a + a \text{Sec}[c + d x])^{5/3}} + \frac{3 \text{Sec}[c + d x]^2 \text{Tan}[c + d x]}{4 d (a + a \text{Sec}[c + d x])^{5/3}} + \frac{135 \text{Tan}[c + d x]}{14 a d (a + a \text{Sec}[c + d x])^{2/3}} + \\ & \frac{375 (1 + \sqrt{3}) (a + a \text{Sec}[c + d x])^{1/3} \text{Tan}[c + d x]}{28 a^2 d (1 + \text{Sec}[c + d x])^{2/3} (2^{1/3} - (1 + \sqrt{3}) (1 + \text{Sec}[c + d x])^{1/3})} - \\ & \left( 375 \times 3^{1/4} \text{EllipticE}\left[\text{ArcCos}\left[\frac{2^{1/3} - (1 - \sqrt{3}) (1 + \text{Sec}[c + d x])^{1/3}}{2^{1/3} - (1 + \sqrt{3}) (1 + \text{Sec}[c + d x])^{1/3}}\right], \frac{1}{4} (2 + \sqrt{3})\right] \right. \\ & \quad \left. (a + a \text{Sec}[c + d x])^{1/3} (2^{1/3} - (1 + \text{Sec}[c + d x])^{1/3}) \right. \\ & \quad \left. \sqrt{\frac{2^{2/3} + 2^{1/3} (1 + \text{Sec}[c + d x])^{1/3} + (1 + \text{Sec}[c + d x])^{2/3}}{(2^{1/3} - (1 + \sqrt{3}) (1 + \text{Sec}[c + d x])^{1/3})^2}} \text{Tan}[c + d x] \right) / \left( 14 \times 2^{2/3} a^2 d \right. \\ & \quad \left. (1 - \text{Sec}[c + d x]) (1 + \text{Sec}[c + d x])^{2/3} \sqrt{-\frac{(1 + \text{Sec}[c + d x])^{1/3} (2^{1/3} - (1 + \text{Sec}[c + d x])^{1/3})}{(2^{1/3} - (1 + \sqrt{3}) (1 + \text{Sec}[c + d x])^{1/3})^2}} \right) - \\ & \left( 125 \times 3^{3/4} (1 - \sqrt{3}) \text{EllipticF}\left[\text{ArcCos}\left[\frac{2^{1/3} - (1 - \sqrt{3}) (1 + \text{Sec}[c + d x])^{1/3}}{2^{1/3} - (1 + \sqrt{3}) (1 + \text{Sec}[c + d x])^{1/3}}\right], \frac{1}{4} (2 + \sqrt{3})\right] \right. \\ & \quad \left. (a + a \text{Sec}[c + d x])^{1/3} (2^{1/3} - (1 + \text{Sec}[c + d x])^{1/3}) \right. \\ & \quad \left. \sqrt{\frac{2^{2/3} + 2^{1/3} (1 + \text{Sec}[c + d x])^{1/3} + (1 + \text{Sec}[c + d x])^{2/3}}{(2^{1/3} - (1 + \sqrt{3}) (1 + \text{Sec}[c + d x])^{1/3})^2}} \text{Tan}[c + d x] \right) / \left( 28 \times 2^{2/3} a^2 d \right. \\ & \quad \left. (1 - \text{Sec}[c + d x]) (1 + \text{Sec}[c + d x])^{2/3} \sqrt{-\frac{(1 + \text{Sec}[c + d x])^{1/3} (2^{1/3} - (1 + \text{Sec}[c + d x])^{1/3})}{(2^{1/3} - (1 + \sqrt{3}) (1 + \text{Sec}[c + d x])^{1/3})^2}} \right) \end{aligned}$$

Result (type 5, 137 leaves):

$$\begin{aligned} & \left( \frac{3}{2} \text{Sec}\left[\frac{1}{2} (c + d x)\right] \text{Sec}[c + d x]^2 \left( 3 \text{Sin}\left[\frac{1}{2} (c + d x)\right] - 12 \text{Sin}\left[\frac{3}{2} (c + d x)\right] - 23 \text{Sin}\left[\frac{5}{2} (c + d x)\right] \right) \right. \\ & \quad \left. 125 \text{Hypergeometric2F1}\left[\frac{1}{3}, \frac{1}{2}, \frac{3}{2}, \text{Tan}\left[\frac{1}{2} (c + d x)\right]^2\right] \right. \\ & \quad \left. \left( \text{Cos}[c + d x] \text{Sec}\left[\frac{1}{2} (c + d x)\right]^2 \right)^{1/3} \text{Tan}[c + d x] \right) / \left( 28 a d (a (1 + \text{Sec}[c + d x]))^{2/3} \right) \end{aligned}$$

**Problem 160: Result unnecessarily involves higher level functions.**

$$\int \frac{\sec [c+d x]^3}{(a+a \sec [c+d x])^{5/3}} d x$$

Optimal (type 4, 731 leaves, 8 steps):

$$\begin{aligned} & \frac{3 \operatorname{Tan}[c+d x]}{7 d (a+a \sec [c+d x])^{5/3}} - \frac{36 \operatorname{Tan}[c+d x]}{7 a d (a+a \sec [c+d x])^{2/3}} - \\ & \frac{57 (1+\sqrt{3}) (a+a \sec [c+d x])^{1/3} \operatorname{Tan}[c+d x]}{7 a^2 d (1+\sec [c+d x])^{2/3} (2^{1/3} - (1+\sqrt{3}) (1+\sec [c+d x])^{1/3})} + \\ & \left( 57 \times 2^{1/3} \times 3^{1/4} \operatorname{EllipticE}\left[\operatorname{ArcCos}\left[\frac{2^{1/3} - (1-\sqrt{3}) (1+\sec [c+d x])^{1/3}}{2^{1/3} - (1+\sqrt{3}) (1+\sec [c+d x])^{1/3}}\right], \frac{1}{4} (2+\sqrt{3})\right] \right) \\ & (a+a \sec [c+d x])^{1/3} (2^{1/3} - (1+\sec [c+d x])^{1/3}) \\ & \sqrt{\frac{2^{2/3} + 2^{1/3} (1+\sec [c+d x])^{1/3} + (1+\sec [c+d x])^{2/3}}{(2^{1/3} - (1+\sqrt{3}) (1+\sec [c+d x])^{1/3})^2} \operatorname{Tan}[c+d x]} \Bigg/ \left( 7 a^2 d \right. \\ & \left. (1-\sec [c+d x]) (1+\sec [c+d x])^{2/3} \sqrt{-\frac{(1+\sec [c+d x])^{1/3} (2^{1/3} - (1+\sec [c+d x])^{1/3})}{(2^{1/3} - (1+\sqrt{3}) (1+\sec [c+d x])^{1/3})^2}} \right) + \\ & \left( 19 \times 3^{3/4} (1-\sqrt{3}) \operatorname{EllipticF}\left[\operatorname{ArcCos}\left[\frac{2^{1/3} - (1-\sqrt{3}) (1+\sec [c+d x])^{1/3}}{2^{1/3} - (1+\sqrt{3}) (1+\sec [c+d x])^{1/3}}\right], \frac{1}{4} (2+\sqrt{3})\right] \right) \\ & (a+a \sec [c+d x])^{1/3} (2^{1/3} - (1+\sec [c+d x])^{1/3}) \\ & \sqrt{\frac{2^{2/3} + 2^{1/3} (1+\sec [c+d x])^{1/3} + (1+\sec [c+d x])^{2/3}}{(2^{1/3} - (1+\sqrt{3}) (1+\sec [c+d x])^{1/3})^2} \operatorname{Tan}[c+d x]} \Bigg/ \left( 7 \times 2^{2/3} a^2 d \right. \\ & \left. (1-\sec [c+d x]) (1+\sec [c+d x])^{2/3} \sqrt{-\frac{(1+\sec [c+d x])^{1/3} (2^{1/3} - (1+\sec [c+d x])^{1/3})}{(2^{1/3} - (1+\sqrt{3}) (1+\sec [c+d x])^{1/3})^2}} \right) \end{aligned}$$

Result (type 5, 135 leaves):

$$\begin{aligned} & \left( (1+\cos [c+d x]) \sec [c+d x] \left( 3 \sec \left[ \frac{1}{2} (c+d x) \right]^3 \left( 3 \sin \left[ \frac{1}{2} (c+d x) \right] + 4 \sin \left[ \frac{3}{2} (c+d x) \right] \right) \right) - \right. \\ & \left. 38 \operatorname{Hypergeometric2F1}\left[\frac{1}{3}, \frac{1}{2}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2} (c+d x)\right]^2\right] \left( \cos [c+d x] \sec \left[ \frac{1}{2} (c+d x) \right]^2 \right)^{1/3} \right. \\ & \left. \operatorname{Tan}\left[\frac{1}{2} (c+d x)\right] \right) \Bigg/ \left( 14 a d (a (1+\sec [c+d x]))^{2/3} \right) \end{aligned}$$

### Problem 161: Result unnecessarily involves higher level functions.

$$\int \frac{\text{Sec}[c + d x]^2}{(a + a \text{Sec}[c + d x])^{5/3}} dx$$

Optimal (type 4, 731 leaves, 8 steps):

$$\begin{aligned} & -\frac{3 \text{Tan}[c + d x]}{7 d (a + a \text{Sec}[c + d x])^{5/3}} + \frac{15 \text{Tan}[c + d x]}{7 a d (a + a \text{Sec}[c + d x])^{2/3}} + \\ & \frac{15 (1 + \sqrt{3}) (1 + \text{Sec}[c + d x])^{1/3} \text{Tan}[c + d x]}{7 a d (a + a \text{Sec}[c + d x])^{2/3} (2^{1/3} - (1 + \sqrt{3}) (1 + \text{Sec}[c + d x])^{1/3})} - \\ & \left( 15 \times 2^{1/3} \times 3^{3/4} \text{EllipticE}\left[\text{ArcCos}\left[\frac{2^{1/3} - (1 - \sqrt{3}) (1 + \text{Sec}[c + d x])^{1/3}}{2^{1/3} - (1 + \sqrt{3}) (1 + \text{Sec}[c + d x])^{1/3}}\right], \frac{1}{4} (2 + \sqrt{3})\right] \right) \\ & (1 + \text{Sec}[c + d x])^{1/3} (2^{1/3} - (1 + \text{Sec}[c + d x])^{1/3}) \\ & \sqrt{\frac{2^{2/3} + 2^{1/3} (1 + \text{Sec}[c + d x])^{1/3} + (1 + \text{Sec}[c + d x])^{2/3}}{(2^{1/3} - (1 + \sqrt{3}) (1 + \text{Sec}[c + d x])^{1/3})^2} \text{Tan}[c + d x]} \Bigg/ \left( 7 a d (1 - \text{Sec}[c + d x]) \right) \\ & (a + a \text{Sec}[c + d x])^{2/3} \sqrt{-\frac{(1 + \text{Sec}[c + d x])^{1/3} (2^{1/3} - (1 + \text{Sec}[c + d x])^{1/3})}{(2^{1/3} - (1 + \sqrt{3}) (1 + \text{Sec}[c + d x])^{1/3})^2}} - \\ & \left( 5 \times 3^{3/4} (1 - \sqrt{3}) \text{EllipticF}\left[\text{ArcCos}\left[\frac{2^{1/3} - (1 - \sqrt{3}) (1 + \text{Sec}[c + d x])^{1/3}}{2^{1/3} - (1 + \sqrt{3}) (1 + \text{Sec}[c + d x])^{1/3}}\right], \frac{1}{4} (2 + \sqrt{3})\right] \right) \\ & (1 + \text{Sec}[c + d x])^{1/3} (2^{1/3} - (1 + \text{Sec}[c + d x])^{1/3}) \\ & \sqrt{\frac{2^{2/3} + 2^{1/3} (1 + \text{Sec}[c + d x])^{1/3} + (1 + \text{Sec}[c + d x])^{2/3}}{(2^{1/3} - (1 + \sqrt{3}) (1 + \text{Sec}[c + d x])^{1/3})^2} \text{Tan}[c + d x]} \Bigg/ \left( 7 \times 2^{2/3} a d \right) \\ & (1 - \text{Sec}[c + d x]) (a + a \text{Sec}[c + d x])^{2/3} \sqrt{-\frac{(1 + \text{Sec}[c + d x])^{1/3} (2^{1/3} - (1 + \text{Sec}[c + d x])^{1/3})}{(2^{1/3} - (1 + \sqrt{3}) (1 + \text{Sec}[c + d x])^{1/3})^2}} \end{aligned}$$

Result (type 5, 86 leaves):

$$\begin{aligned} & \left( -3 \text{Tan}\left[\frac{1}{2} (c + d x)\right] + 5 \times 2^{1/3} \text{Hypergeometric2F1}\left[\frac{1}{3}, \frac{1}{2}, \frac{3}{2}, \text{Tan}\left[\frac{1}{2} (c + d x)\right]^2\right] \right) \\ & \left( \frac{1}{1 + \text{Sec}[c + d x]} \right)^{1/3} \text{Tan}[c + d x] \Bigg/ \left( 7 a d (a (1 + \text{Sec}[c + d x]))^{2/3} \right) \end{aligned}$$

**Problem 162: Result unnecessarily involves higher level functions.**

$$\int \frac{\text{Sec}[c + d x]}{(a + a \text{Sec}[c + d x])^{5/3}} dx$$

Optimal (type 4, 744 leaves, 8 steps):

$$\begin{aligned} & \frac{6 \text{Tan}[c + d x]}{7 a d (a + a \text{Sec}[c + d x])^{2/3}} + \frac{3 \text{Tan}[c + d x]}{7 a d (1 + \text{Sec}[c + d x]) (a + a \text{Sec}[c + d x])^{2/3}} + \\ & \frac{6 (1 + \sqrt{3}) (1 + \text{Sec}[c + d x])^{1/3} \text{Tan}[c + d x]}{7 a d (a + a \text{Sec}[c + d x])^{2/3} (2^{1/3} - (1 + \sqrt{3}) (1 + \text{Sec}[c + d x])^{1/3})} - \\ & \left( 6 \times 2^{1/3} \times 3^{1/4} \text{EllipticE}\left[\text{ArcCos}\left[\frac{2^{1/3} - (1 - \sqrt{3}) (1 + \text{Sec}[c + d x])^{1/3}}{2^{1/3} - (1 + \sqrt{3}) (1 + \text{Sec}[c + d x])^{1/3}}\right], \frac{1}{4} (2 + \sqrt{3})\right] \right. \\ & \quad \left. (1 + \text{Sec}[c + d x])^{1/3} (2^{1/3} - (1 + \text{Sec}[c + d x])^{1/3}) \right. \\ & \quad \left. \sqrt{\frac{2^{2/3} + 2^{1/3} (1 + \text{Sec}[c + d x])^{1/3} + (1 + \text{Sec}[c + d x])^{2/3}}{(2^{1/3} - (1 + \sqrt{3}) (1 + \text{Sec}[c + d x])^{1/3})^2}} \text{Tan}[c + d x] \right) / \left( 7 a d (1 - \text{Sec}[c + d x]) \right) \\ & \quad (a + a \text{Sec}[c + d x])^{2/3} \sqrt{-\frac{(1 + \text{Sec}[c + d x])^{1/3} (2^{1/3} - (1 + \text{Sec}[c + d x])^{1/3})}{(2^{1/3} - (1 + \sqrt{3}) (1 + \text{Sec}[c + d x])^{1/3})^2}} - \\ & \left( 2^{1/3} \times 3^{3/4} (1 - \sqrt{3}) \text{EllipticF}\left[\text{ArcCos}\left[\frac{2^{1/3} - (1 - \sqrt{3}) (1 + \text{Sec}[c + d x])^{1/3}}{2^{1/3} - (1 + \sqrt{3}) (1 + \text{Sec}[c + d x])^{1/3}}\right], \frac{1}{4} (2 + \sqrt{3})\right] \right. \\ & \quad \left. (1 + \text{Sec}[c + d x])^{1/3} (2^{1/3} - (1 + \text{Sec}[c + d x])^{1/3}) \right. \\ & \quad \left. \sqrt{\frac{2^{2/3} + 2^{1/3} (1 + \text{Sec}[c + d x])^{1/3} + (1 + \text{Sec}[c + d x])^{2/3}}{(2^{1/3} - (1 + \sqrt{3}) (1 + \text{Sec}[c + d x])^{1/3})^2}} \text{Tan}[c + d x] \right) / \left( 7 a d \right. \\ & \quad \left. (1 - \text{Sec}[c + d x]) (a + a \text{Sec}[c + d x])^{2/3} \sqrt{-\frac{(1 + \text{Sec}[c + d x])^{1/3} (2^{1/3} - (1 + \text{Sec}[c + d x])^{1/3})}{(2^{1/3} - (1 + \sqrt{3}) (1 + \text{Sec}[c + d x])^{1/3})^2}} \right) \end{aligned}$$

Result (type 5, 111 leaves):

$$\begin{aligned} & \left( \left( 3 \text{Cos}[c + d x] + 4 \times 2^{1/3} \text{Cos}\left[\frac{1}{2} (c + d x)\right]^2 \right. \right. \\ & \quad \left. \left. \left( \frac{\text{Cos}[c + d x]}{1 + \text{Cos}[c + d x]} \right)^{1/3} \text{Hypergeometric2F1}\left[\frac{1}{3}, \frac{1}{2}, \frac{3}{2}, \text{Tan}\left[\frac{1}{2} (c + d x)\right]^2\right] \right) \right. \\ & \quad \left. \text{Sec}[c + d x] \text{Tan}\left[\frac{1}{2} (c + d x)\right] \right) / \left( 7 a d (a (1 + \text{Sec}[c + d x]))^{2/3} \right) \end{aligned}$$

### Problem 163: Result more than twice size of optimal antiderivative.

$$\int \frac{1}{(a + a \operatorname{Sec}[c + d x])^{5/3}} dx$$

Optimal (type 6, 90 leaves, 3 steps):

$$- \left( \left( 3 \sqrt{2} \operatorname{AppellF1} \left[ -\frac{7}{6}, \frac{1}{2}, 1, -\frac{1}{6}, \frac{1}{2} (1 + \operatorname{Sec}[c + d x]), 1 + \operatorname{Sec}[c + d x] \right] \operatorname{Tan}[c + d x] \right) / \right. \\ \left. \left( 7 a d \sqrt{1 - \operatorname{Sec}[c + d x]} (1 + \operatorname{Sec}[c + d x]) (a + a \operatorname{Sec}[c + d x])^{2/3} \right) \right)$$

Result (type 6, 4638 leaves):

$$\left( \left( (1 + \operatorname{Cos}[c + d x]) \operatorname{Sec}[c + d x] \right)^{1/3} (1 + \operatorname{Sec}[c + d x])^{5/3} \right. \\ \left( \frac{27}{7} \operatorname{Sin}[c + d x] - \frac{30}{7} \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right] + \frac{3}{14} \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right] \right) / \\ \left( d (a (1 + \operatorname{Sec}[c + d x]))^{5/3} + \left( 2^{1/3} \operatorname{Cos}[c + d x] \left( \operatorname{Cos} \left[ \frac{1}{2} (c + d x) \right]^2 \operatorname{Sec}[c + d x] \right)^{1/3} \right. \right. \\ \left. \left. (1 + \operatorname{Sec}[c + d x])^{5/3} \left( \frac{16}{7} (1 + \operatorname{Sec}[c + d x])^{1/3} - \frac{27}{7} \operatorname{Cos}[c + d x] (1 + \operatorname{Sec}[c + d x])^{1/3} \right) \right. \right. \\ \left. \left. \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right] \left( -27 - \left( 5 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) / \right. \right. \right. \\ \left. \left. \left( \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right) \left( \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \right. \right. \right. \\ \left. \left. \frac{2}{9} \left( -3 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \operatorname{AppellF1} \left[ \right. \right. \right. \\ \left. \left. \left. \frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right) \right) - \right. \\ \left. \left( 45 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right] \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right) / \right. \\ \left. \left( \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right) \right. \right. \\ \left. \left( -15 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right) + \right. \right. \\ \left. \left. 2 \left( 3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right] - \operatorname{AppellF1} \left[ \frac{5}{2}, \right. \right. \right. \\ \left. \left. \left. \frac{4}{3}, 1, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right) \right) \right) / \\ \left. \left( 7 d (a (1 + \operatorname{Sec}[c + d x]))^{5/3} \left( \frac{1}{7 \times 2^{2/3}} \operatorname{Cos}[c + d x] \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \right. \right. \right. \\ \left. \left. \left( \operatorname{Cos} \left[ \frac{1}{2} (c + d x) \right]^2 \operatorname{Sec}[c + d x] \right)^{1/3} \left( -27 - \left( 5 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \right. \right. \right. \right. \\ \left. \left. \left. \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right) \right) / \left( \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right) \right) \right) \right) \right)$$



$$\begin{aligned}
 & \left( \text{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \frac{2}{9} \right. \\
 & \quad \left. \left( -3 \text{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \text{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - \\
 & \quad \left( 45 \text{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \quad \left. \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) / \left( \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \\
 & \quad \left( -15 \text{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \right. \\
 & \quad \left. \left( 3 \text{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \text{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) - \\
 & \quad \frac{1}{7} \times 2^{1/3} \left( \cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx] \right)^{1/3} \sin[c+dx] \tan\left[\frac{1}{2}(c+dx)\right] \\
 & \quad \left( -27 - \left( 5 \text{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) / \right. \\
 & \quad \left. \left( \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right. \\
 & \quad \left( \text{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad \left. \frac{2}{9} \left( -3 \text{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \text{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - \\
 & \quad \left( 45 \text{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) / \\
 & \quad \left. \left( \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right. \\
 & \quad \left( -15 \text{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad \left. 2 \left( 3 \text{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \text{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) + \\
 & \quad \frac{1}{7} \times 2^{1/3} \cos[c+dx] \left( \cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx] \right)^{1/3} \tan\left[\frac{1}{2}(c+dx)\right] \\
 & \quad \left( \left( 5 \text{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
 & \quad \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) / \left( \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right)^2 \\
 & \quad \left( \text{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right.
 \end{aligned}$$





$$\begin{aligned}
& \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \\
& \frac{1}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \\
& \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + 2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \left(\frac{5}{7} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{4}{3}, 2, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
& \tan\left[\frac{1}{2}(c+dx)\right] - \frac{20}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{7}{3}, 1, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
& \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + 3 \left(-\frac{10}{7} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{1}{3}, 3, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
& \left. \tan\left[\frac{1}{2}(c+dx)\right] + \frac{5}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{4}{3}, 2, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right)\right)\right) / \\
& \left(\left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \left(-15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \left(3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \right. \right. \right. \\
& \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \right. \right. \right. \\
& \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2\right)\right) + \\
& \frac{1}{21 \left(\cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx]\right)^{2/3}} 2^{1/3} \cos[c+dx] \tan\left[\frac{1}{2}(c+dx)\right] \\
& \left(-27 - \left(5 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right)\right) / \\
& \left(\left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \right. \\
& \left(\operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \frac{2}{9} \right. \\
& \left(-3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2\right) - \\
& \left(45 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \left. \tan\left[\frac{1}{2}(c+dx)\right]^2\right) / \left(\left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \right. \\
& \left(-15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \right. \\
& \left. \left(3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \operatorname{AppellF1}\left[\frac{5}{2}, \right.\right.\right.
\end{aligned}$$

$$\left( \frac{4}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \left( -\cos\left[\frac{1}{2}(c+dx)\right] \sec[c+dx] \sin\left[\frac{1}{2}(c+dx)\right] + \cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx] \tan[c+dx] \right) \right)$$

### Problem 164: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos[c+dx]}{(a+a \sec[c+dx])^{5/3}} dx$$

Optimal (type 6, 90 leaves, 3 steps):

$$\left( 3\sqrt{2} \operatorname{AppellF1}\left[-\frac{7}{6}, \frac{1}{2}, 2, -\frac{1}{6}, \frac{1}{2}(1+\sec[c+dx]), 1+\sec[c+dx]\right] \tan[c+dx] \right) / \left( 7ad\sqrt{1-\sec[c+dx]}(1+\sec[c+dx])(a+a \sec[c+dx])^{2/3} \right)$$

Result (type 6, 4638 leaves):

$$\left( (1+\cos[c+dx]) \sec[c+dx] \right)^{1/3} (1+\sec[c+dx])^{5/3} \left( -\frac{48}{7} \sin[c+dx] + \frac{51}{7} \tan\left[\frac{1}{2}(c+dx)\right] - \frac{3}{14} \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) / \left( d(a(1+\sec[c+dx]))^{5/3} - (5 \times 2^{1/3} \cos[c+dx] \left( \cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx] \right)^{1/3} (1+\sec[c+dx])^{5/3} \left( -\frac{30}{7} (1+\sec[c+dx])^{1/3} + \frac{55}{7} \cos[c+dx] (1+\sec[c+dx])^{1/3} \right) \tan\left[\frac{1}{2}(c+dx)\right] \left( -33 - \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right) / \left( \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right) + \frac{2}{9} \left( -3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] + \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - \left( 55 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) / \left( \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( -15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] + 2 \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] - \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) /$$

$$\begin{aligned}
& \left( 21 d (a (1 + \sec [c + d x]))^{5/3} \left( -\frac{1}{21 \times 2^{2/3}} 5 \cos [c + d x] \sec \left[ \frac{1}{2} (c + d x) \right]^2 \right. \right. \\
& \quad \left( \cos \left[ \frac{1}{2} (c + d x) \right]^2 \sec [c + d x] \right)^{1/3} \left( -33 - \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \right. \right. \right. \\
& \quad \left. \left. \left. \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) / \left( \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) \right) \right. \\
& \quad \left( \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \frac{2}{9} \right. \\
& \quad \left( -3 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \operatorname{AppellF1} \left[ \right. \right. \\
& \quad \left. \left. \frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c + d x) \right]^2 \left. \right) \right) - \\
& \quad \left( 55 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right. \\
& \quad \left. \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) / \left( \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) \left( -15 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \right. \right. \right. \\
& \quad \left. \left. \left. \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + 2 \left( 3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \right. \right. \right. \right. \\
& \quad \left. \left. \left. \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] - \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \right. \right. \right. \\
& \quad \left. \left. \left. \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) \left. \right) \right) + \\
& \quad \frac{5}{21} \times 2^{1/3} \left( \cos \left[ \frac{1}{2} (c + d x) \right]^2 \sec [c + d x] \right)^{1/3} \sin [c + d x] \tan \left[ \frac{1}{2} (c + d x) \right] \\
& \quad \left( -33 - \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) / \right. \\
& \quad \left( \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) \right) \\
& \quad \left( \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \right. \\
& \quad \left. \frac{2}{9} \left( -3 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \operatorname{AppellF1} \left[ \right. \right. \right. \\
& \quad \left. \left. \left. \frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) \left. \right) - \\
& \quad \left( 55 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) / \\
& \quad \left( \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) \right) \\
& \quad \left( -15 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \right. \\
& \quad \left. 2 \left( 3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] - \operatorname{AppellF1} \left[ \frac{5}{2}, \right. \right. \right. \\
& \quad \left. \left. \left. \frac{4}{3}, 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) \left. \right) \right) -
\end{aligned}$$



$$\begin{aligned}
& -\tan\left[\frac{1}{2}(c+dx)\right]^2 \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \\
& \frac{1}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \\
& \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \Big) \Big/ \left( \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \right. \\
& \left. \left(-15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
& \left. \left. 2 \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \operatorname{AppellF1}\left[\frac{5}{2}, \right. \right. \right. \right. \\
& \left. \left. \left. \frac{4}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) + \\
& \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \left. \left(-\frac{1}{3} \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
& \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{9} \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \right. \right. \right. \\
& \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \right. \\
& \left. \left. \frac{2}{9} \left(-3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \operatorname{AppellF1}\left[\frac{3}{2}, \right. \right. \right. \right. \\
& \left. \left. \left. \frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \sec\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \\
& \left. \left. \tan\left[\frac{1}{2}(c+dx)\right] + \frac{2}{9} \tan\left[\frac{1}{2}(c+dx)\right]^2 \left(-\frac{3}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 2, \frac{7}{2}, \right. \right. \right. \right. \\
& \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \right. \\
& \left. \left. \frac{4}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{7}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
& \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] - 3 \left(-\frac{6}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 3, \right. \right. \right. \right. \\
& \left. \left. \left. \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \\
& \left. \left. \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
& \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \Big) \Big/ \\
& \left( \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \left( \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
& \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \frac{2}{9} \left(-3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \right. \right. \right. \right. \\
& \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \right. \right. \right. \right. \\
& \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) +
\end{aligned}$$



$$\begin{aligned}
 & \left( 55 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \quad \left( 2 \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \right. \\
 & \quad \quad \left. \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right. \\
 & \quad \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] - 15 \left( -\frac{3}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \right. \right. \right. \\
 & \quad \quad \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \quad \quad \left. \frac{1}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \quad \quad \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + 2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \left( \frac{5}{7} \operatorname{AppellF1}\left[ \right. \right. \\
 & \quad \quad \left. \frac{7}{2}, \frac{4}{3}, 2, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \quad \quad \left. \tan\left[\frac{1}{2}(c+dx)\right] - \frac{20}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{7}{3}, 1, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \quad \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + 3 \left( -\frac{10}{7} \operatorname{AppellF1}\left[ \right. \right. \\
 & \quad \quad \left. \frac{7}{2}, \frac{1}{3}, 3, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \quad \quad \left. \tan\left[\frac{1}{2}(c+dx)\right] + \frac{5}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{4}{3}, 2, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) \Big/ \\
 & \left( \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( -15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right) + 2 \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \right. \right. \\
 & \quad \quad \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] - \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \right. \\
 & \quad \quad \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \Big) - \\
 & \frac{1}{63 \left( \cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx] \right)^{2/3}} 5 \times 2^{1/3} \cos[c+dx] \tan\left[\frac{1}{2}(c+dx)\right] \\
 & \left( -33 - \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right) \right) \Big/ \\
 & \left( \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right. \\
 & \quad \left( \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] + \frac{2}{9} \right. \\
 & \quad \left( -3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] + \operatorname{AppellF1}\left[ \right. \right. \\
 & \quad \quad \left. \frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \Big) -
 \end{aligned}$$

$$\left( 55 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\ \left. \tan\left[\frac{1}{2}(c+dx)\right]^2\right) / \left( \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \right) \\ \left( -15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \right. \\ \left. \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \operatorname{AppellF1}\left[\frac{5}{2}, \right. \right. \right. \\ \left. \left. \frac{4}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \\ \left( -\cos\left[\frac{1}{2}(c+dx)\right] \sec[c+dx] \sin\left[\frac{1}{2}(c+dx)\right] + \cos\left[\frac{1}{2}(c+dx)\right]^2 \right. \\ \left. \sec[c+dx] \tan[c+dx] \right) \right)$$

**Problem 172: Result unnecessarily involves higher level functions.**

$$\int \sec[c+dx]^{5/2} (a+a \sec[c+dx])^2 dx$$

Optimal (type 4, 187 leaves, 9 steps):

$$\frac{12 a^2 \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]}}{5 d} + \\ \frac{8 a^2 \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]}}{7 d} + \frac{12 a^2 \sqrt{\sec[c+dx]} \sin[c+dx]}{5 d} + \\ \frac{8 a^2 \sec[c+dx]^{3/2} \sin[c+dx]}{7 d} + \frac{4 a^2 \sec[c+dx]^{5/2} \sin[c+dx]}{5 d} + \frac{2 a^2 \sec[c+dx]^{7/2} \sin[c+dx]}{7 d}$$

Result (type 5, 287 leaves):

$$\frac{1}{70 d} a^2 \sec\left[\frac{1}{2}(c+dx)\right]^4 (1+\sec[c+dx])^2 \\ \left( -\frac{1}{-1+e^{2ic}} 2i\sqrt{2} e^{-i(c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos[c+dx]^2 \left( 21(1+e^{2i(c+dx)}) + \right. \right. \\ \left. \left. 21(-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] + 10 e^{i(c+dx)} \right. \right. \\ \left. \left. (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, \frac{1}{2}, \frac{5}{4}, -e^{2i(c+dx)}\right] \right) + \frac{1}{\sec[c+dx]^{3/2}} \right) \\ \left( 42 \cos[dx] \csc[c] + (15+14 \cos[c+dx] + 10 \cos[2(c+dx)]) \sec[c+dx]^2 \tan[c+dx] \right)$$

**Problem 173: Result unnecessarily involves higher level functions.**

$$\int \sec [c+d x]^{3 / 2} (a+a \sec [c+d x])^2 d x$$

Optimal (type 4, 161 leaves, 8 steps):

$$\begin{aligned} & -\frac{16 a^2 \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}}{5 d}+ \\ & \frac{4 a^2 \sqrt{\cos [c+d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}}{3 d}+\frac{16 a^2 \sqrt{\sec [c+d x]} \sin [c+d x]}{5 d}+ \\ & \frac{4 a^2 \sec [c+d x]^{3 / 2} \sin [c+d x]}{3 d}+\frac{2 a^2 \sec [c+d x]^{5 / 2} \sin [c+d x]}{5 d} \end{aligned}$$

Result (type 5, 269 leaves):

$$\begin{aligned} & \frac{1}{30 d} a^2 \sec \left[\frac{1}{2}(c+d x)\right]^4 (1+\sec [c+d x])^2 \\ & \left( -\frac{1}{-1+e^{2 i c}} 2^i \sqrt{2} e^{-i(c+d x)} \sqrt{\frac{e^{i(c+d x)}}{1+e^{2 i(c+d x)}}} \cos [c+d x]^2 \left( 12\left(1+e^{2 i(c+d x)}\right)+ \right. \right. \\ & \quad 12\left(-1+e^{2 i c}\right) \sqrt{1+e^{2 i(c+d x)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4},-e^{2 i(c+d x)}\right]+ \\ & \quad \left. \left. 5 e^{i(c+d x)}\left(-1+e^{2 i c}\right) \sqrt{1+e^{2 i(c+d x)}} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, \frac{1}{2}, \frac{5}{4},-e^{2 i(c+d x)}\right]\right) \right) \\ & \quad \left. \frac{24 \cos [d x] \operatorname{Csc}[c]+\left(10+3 \sec [c+d x]\right) \tan [c+d x]}{\sec [c+d x]^{3 / 2}} \right) \end{aligned}$$

**Problem 174: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \sqrt{\sec [c+d x]} (a+a \sec [c+d x])^2 d x$$

Optimal (type 4, 131 leaves, 7 steps):

$$\begin{aligned} & -\frac{4 a^2 \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}}{d}+ \\ & \frac{8 a^2 \sqrt{\cos [c+d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}}{3 d}+ \\ & \frac{4 a^2 \sqrt{\sec [c+d x]} \sin [c+d x]}{d}+\frac{2 a^2 \sec [c+d x]^{3 / 2} \sin [c+d x]}{3 d} \end{aligned}$$

Result (type 5, 264 leaves):

$$\frac{1}{3} a^2 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^4 (1+\operatorname{Sec}[c+dx])^2$$

$$\left( -\frac{1}{d(-1+e^{2ic})} i \sqrt{2} e^{-i(c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \operatorname{Cos}[c+dx]^2 \right.$$

$$\left. \left( 3(1+e^{2i(c+dx)}) + 3(-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] + \right. \right.$$

$$\left. \left. 2e^{i(c+dx)}(-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, \frac{1}{2}, \frac{5}{4}, -e^{2i(c+dx)}\right] \right) + \right.$$

$$\left. \frac{6 \operatorname{Cos}[dx] \operatorname{Csc}[c] + \operatorname{Tan}[c+dx]}{2d \operatorname{Sec}[c+dx]^{3/2}} \right)$$

**Problem 176: Result unnecessarily involves higher level functions.**

$$\int \frac{(a+a \operatorname{Sec}[c+dx])^2}{\operatorname{Sec}[c+dx]^{3/2}} dx$$

Optimal (type 4, 107 leaves, 6 steps):

$$\frac{4a^2 \sqrt{\operatorname{Cos}[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\operatorname{Sec}[c+dx]}}{d} +$$

$$\frac{8a^2 \sqrt{\operatorname{Cos}[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\operatorname{Sec}[c+dx]}}{3d} + \frac{2a^2 \operatorname{Sin}[c+dx]}{3d \sqrt{\operatorname{Sec}[c+dx]}}$$

Result (type 5, 156 leaves):

$$\left( a^2 \left( \operatorname{Cos}\left[\frac{c}{2}\right] - i \operatorname{Sin}\left[\frac{c}{2}\right] \right) \left( -i \operatorname{Cos}\left[\frac{c}{2}\right] + \operatorname{Sin}\left[\frac{c}{2}\right] \right) \right.$$

$$\left( 12 - \frac{24 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right]}{\sqrt{1+e^{2i(c+dx)}}} + \right.$$

$$\left. 8 \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, \frac{1}{2}, \frac{5}{4}, -e^{2i(c+dx)}\right] \operatorname{Sec}[c+dx] + \right.$$

$$\left. \left. 2i \operatorname{Sin}[c+dx] \right) \right) / \left( 3d \sqrt{\operatorname{Sec}[c+dx]} \right)$$

**Problem 177: Result unnecessarily involves higher level functions.**

$$\int \frac{(a+a \operatorname{Sec}[c+dx])^2}{\operatorname{Sec}[c+dx]^{5/2}} dx$$

Optimal (type 4, 135 leaves, 7 steps):

$$\frac{16 a^2 \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}}{5 d} +$$

$$\frac{4 a^2 \sqrt{\cos [c+d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}}{3 d} +$$

$$\frac{2 a^2 \sin [c+d x]}{5 d \sec [c+d x]^{3 / 2}} + \frac{4 a^2 \sin [c+d x]}{3 d \sqrt{\sec [c+d x]}}$$

Result (type 5, 136 leaves):

$$\left( a^2 \left( -96 i + \frac{192 i \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i (c+d x)}\right]}{\sqrt{1+e^{2 i (c+d x)}}} - \right. \right.$$

$$40 i \sqrt{1+e^{2 i (c+d x)}} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, \frac{1}{2}, \frac{5}{4}, -e^{2 i (c+d x)}\right] \sec [c+d x] +$$

$$\left. \left. 40 \sin [c+d x] + 6 \sin [2(c+d x)] \right) \right) / \left( 30 d \sqrt{\sec [c+d x]} \right)$$

**Problem 178: Result unnecessarily involves higher level functions.**

$$\int \frac{(a + a \sec [c+d x])^2}{\sec [c+d x]^{7 / 2}} dx$$

Optimal (type 4, 161 leaves, 8 steps):

$$\frac{12 a^2 \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}}{5 d} +$$

$$\frac{8 a^2 \sqrt{\cos [c+d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}}{7 d} +$$

$$\frac{2 a^2 \sin [c+d x]}{7 d \sec [c+d x]^{5 / 2}} + \frac{4 a^2 \sin [c+d x]}{5 d \sec [c+d x]^{3 / 2}} + \frac{8 a^2 \sin [c+d x]}{7 d \sqrt{\sec [c+d x]}}$$

Result (type 5, 149 leaves):

$$\left( a^2 \left( \frac{672 i \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i (c+d x)}\right]}{\sqrt{1+e^{2 i (c+d x)}}} + \right. \right.$$

$$2 \left( -168 i - 80 i \sqrt{1+e^{2 i (c+d x)}} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, \frac{1}{2}, \frac{5}{4}, -e^{2 i (c+d x)}\right] \sec [c+d x] + \right.$$

$$\left. \left. \left. 85 \sin [c+d x] + 28 \sin [2(c+d x)] + 5 \sin [3(c+d x)] \right) \right) \right) / \left( 140 d \sqrt{\sec [c+d x]} \right)$$

**Problem 179: Result unnecessarily involves higher level functions.**

$$\int \sec [c+d x]^{3 / 2} (a + a \sec [c+d x])^3 dx$$

Optimal (type 4, 187 leaves, 16 steps):

$$\begin{aligned} & - \frac{28 a^3 \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}}{5 d} + \\ & \frac{52 a^3 \sqrt{\cos [c+d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}}{21 d} + \frac{28 a^3 \sqrt{\sec [c+d x]} \sin [c+d x]}{5 d} + \\ & \frac{52 a^3 \sec [c+d x]^{3 / 2} \sin [c+d x]}{21 d} + \frac{6 a^3 \sec [c+d x]^{5 / 2} \sin [c+d x]}{5 d} + \frac{2 a^3 \sec [c+d x]^{7 / 2} \sin [c+d x]}{7 d} \end{aligned}$$

Result (type 5, 287 leaves):

$$\begin{aligned} & \frac{1}{420 d} a^3 \sec \left[\frac{1}{2}(c+d x)\right]^6 (1+\sec [c+d x])^3 \\ & \left( -\frac{1}{-1+e^{2 i c}} 2^i \sqrt{2} e^{-i(c+d x)} \sqrt{\frac{e^{i(c+d x)}}{1+e^{2 i(c+d x)}}} \cos [c+d x]^3 \left( 147 (1+e^{2 i(c+d x)}) + \right. \right. \\ & \quad 147 (-1+e^{2 i c}) \sqrt{1+e^{2 i(c+d x)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i(c+d x)}\right] + 65 e^{i(c+d x)} \\ & \quad \left. \left. (-1+e^{2 i c}) \sqrt{1+e^{2 i(c+d x)}} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, \frac{1}{2}, \frac{5}{4}, -e^{2 i(c+d x)}\right]\right) + \frac{1}{\sec [c+d x]^{5 / 2}} \right. \\ & \quad \left. (294 \cos [d x] \operatorname{Csc}[c] + (80+63 \cos [c+d x] + 65 \cos [2(c+d x)]) \sec [c+d x]^2 \tan [c+d x]) \right) \end{aligned}$$

**Problem 180: Result unnecessarily involves higher level functions.**

$$\int \sqrt{\sec [c+d x]} (a+a \sec [c+d x])^3 dx$$

Optimal (type 4, 157 leaves, 14 steps):

$$\begin{aligned} & - \frac{36 a^3 \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}}{5 d} + \\ & \frac{4 a^3 \sqrt{\cos [c+d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}}{d} + \frac{36 a^3 \sqrt{\sec [c+d x]} \sin [c+d x]}{5 d} + \\ & \frac{2 a^3 \sec [c+d x]^{3 / 2} \sin [c+d x]}{d} + \frac{2 a^3 \sec [c+d x]^{5 / 2} \sin [c+d x]}{5 d} \end{aligned}$$

Result (type 5, 267 leaves):

$$\frac{1}{20d} a^3 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^6 (1+\operatorname{Sec}[c+dx])^3$$

$$\left( -\frac{1}{-1+e^{2ic}} 2i\sqrt{2} e^{-i(c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \operatorname{Cos}[c+dx]^3 \right.$$

$$\left. \left( 9(1+e^{2i(c+dx)}) + 9(-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] + \right. \right.$$

$$\left. \left. 5e^{i(c+dx)} (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, \frac{1}{2}, \frac{5}{4}, -e^{2i(c+dx)}\right] \right) + \right.$$

$$\left. \frac{18 \operatorname{Cos}[dx] \operatorname{Csc}[c] + (5 + \operatorname{Sec}[c+dx]) \operatorname{Tan}[c+dx]}{\operatorname{Sec}[c+dx]^{5/2}} \right)$$

**Problem 181:** Result unnecessarily involves higher level functions.

$$\int \frac{(a + a \operatorname{Sec}[c+dx])^3}{\sqrt{\operatorname{Sec}[c+dx]}} dx$$

Optimal (type 4, 131 leaves, 12 steps):

$$-\frac{4a^3 \sqrt{\operatorname{Cos}[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\operatorname{Sec}[c+dx]}}{d} +$$

$$\frac{20a^3 \sqrt{\operatorname{Cos}[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\operatorname{Sec}[c+dx]}}{3d} +$$

$$\frac{6a^3 \sqrt{\operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]}{d} + \frac{2a^3 \operatorname{Sec}[c+dx]^{3/2} \operatorname{Sin}[c+dx]}{3d}$$

Result (type 5, 187 leaves):

$$\frac{1}{3d} a^3 e^{-2i(c+dx)} \operatorname{Sec}[c+dx]^{3/2} \left( -6 - 6 \operatorname{Cos}[2(c+dx)] + \right.$$

$$6e^{-2i(c+dx)} (1+e^{2i(c+dx)})^{3/2} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] +$$

$$20 \sqrt{1+e^{2i(c+dx)}} \operatorname{Cos}[c+dx] \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, \frac{1}{2}, \frac{5}{4}, -e^{2i(c+dx)}\right] +$$

$$\left. 2i \operatorname{Sin}[c+dx] + 9i \operatorname{Sin}[2(c+dx)] \right) (-i \operatorname{Cos}[2(c+dx)] + \operatorname{Sin}[2(c+dx)])$$

**Problem 182:** Result unnecessarily involves higher level functions.

$$\int \frac{(a + a \operatorname{Sec}[c+dx])^3}{\operatorname{Sec}[c+dx]^{3/2}} dx$$

Optimal (type 4, 131 leaves, 12 steps):

$$\frac{4 a^3 \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}}{d} +$$

$$\frac{20 a^3 \sqrt{\cos [c+d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}}{3 d} +$$

$$\frac{2 a^3 \sin [c+d x]}{3 d \sqrt{\sec [c+d x]}} + \frac{2 a^3 \sqrt{\sec [c+d x]} \sin [c+d x]}{d}$$

Result (type 5, 169 leaves):

$$\left( a^3 \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{c}{2} \right] + i \sin \left[ \frac{c}{2} \right] \right) \left( \frac{24 i \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i (c+d x)}\right]}{\sqrt{1+e^{2 i (c+d x)}}} + \right. \right.$$

$$2 \left( -6 i - 10 i \sqrt{1+e^{2 i (c+d x)}} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, \frac{1}{2}, \frac{5}{4}, -e^{2 i (c+d x)}\right] \sec [c+d x] + \right.$$

$$\left. \left. \left. \left. \sin [c+d x] + 3 \tan [c+d x] \right) \right) \right) \right) / \left( 3 d \sqrt{\sec [c+d x]} \right)$$

**Problem 183: Result unnecessarily involves higher level functions.**

$$\int \frac{(a + a \sec [c+d x])^3}{\sec [c+d x]^{5/2}} dx$$

Optimal (type 4, 131 leaves, 12 steps):

$$\frac{36 a^3 \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}}{5 d} +$$

$$\frac{4 a^3 \sqrt{\cos [c+d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}}{d} + \frac{2 a^3 \sin [c+d x]}{5 d \sec [c+d x]^{3/2}} + \frac{2 a^3 \sin [c+d x]}{d \sqrt{\sec [c+d x]}}$$

Result (type 5, 171 leaves):

$$\left( a^3 \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{c}{2} \right] + i \sin \left[ \frac{c}{2} \right] \right) \left( \frac{144 i \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i (c+d x)}\right]}{\sqrt{1+e^{2 i (c+d x)}}} + \right. \right.$$

$$2 \left( -36 i - 20 i \sqrt{1+e^{2 i (c+d x)}} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, \frac{1}{2}, \frac{5}{4}, -e^{2 i (c+d x)}\right] \sec [c+d x] + \right.$$

$$\left. \left. \left. \left. 10 \sin [c+d x] + \sin [2(c+d x)] \right) \right) \right) \right) / \left( 10 d \sqrt{\sec [c+d x]} \right)$$

**Problem 184: Result unnecessarily involves higher level functions.**

$$\int \frac{(a + a \sec [c+d x])^3}{\sec [c+d x]^{7/2}} dx$$

Optimal (type 4, 161 leaves, 14 steps):



$$\frac{28 a^3 \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}}{5 d} +$$

$$\frac{52 a^3 \sqrt{\cos [c+d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}}{21 d} +$$

$$\frac{2 a^3 \sin [c+d x]}{7 d \sec [c+d x]^{5 / 2}} + \frac{6 a^3 \sin [c+d x]}{5 d \sec [c+d x]^{3 / 2}} + \frac{52 a^3 \sin [c+d x]}{21 d \sqrt{\sec [c+d x]}}$$

Result (type 5, 146 leaves):

$$\left( a^3 \left( -2352 i + \frac{4704 i \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i(c+d x)}\right]}{\sqrt{1+e^{2 i(c+d x)}}} - \right. \right.$$

$$1040 i \sqrt{1+e^{2 i(c+d x)}} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, \frac{1}{2}, \frac{5}{4}, -e^{2 i(c+d x)}\right] \sec [c+d x] +$$

$$\left. \left. 1070 \sin [c+d x] + 252 \sin [2(c+d x)] + 30 \sin [3(c+d x)] \right) \right) / \left( 420 d \sqrt{\sec [c+d x]} \right)$$

**Problem 185: Result unnecessarily involves higher level functions.**

$$\int \frac{(a + a \sec [c+d x])^3}{\sec [c+d x]^{9 / 2}} dx$$

Optimal (type 4, 187 leaves, 16 steps):

$$\frac{68 a^3 \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}}{15 d} +$$

$$\frac{44 a^3 \sqrt{\cos [c+d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}}{21 d} +$$

$$\frac{2 a^3 \sin [c+d x]}{9 d \sec [c+d x]^{7 / 2}} + \frac{6 a^3 \sin [c+d x]}{7 d \sec [c+d x]^{5 / 2}} + \frac{68 a^3 \sin [c+d x]}{45 d \sec [c+d x]^{3 / 2}} + \frac{44 a^3 \sin [c+d x]}{21 d \sqrt{\sec [c+d x]}}$$

Result (type 5, 156 leaves):

$$\left( a^3 \left( -11424 i + \frac{22848 i \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i(c+d x)}\right]}{\sqrt{1+e^{2 i(c+d x)}}} - 5280 i \sqrt{1+e^{2 i(c+d x)}} \right. \right.$$

$$\operatorname{Hypergeometric2F1}\left[\frac{1}{4}, \frac{1}{2}, \frac{5}{4}, -e^{2 i(c+d x)}\right] \sec [c+d x] + 5820 \sin [c+d x] +$$

$$\left. \left. 2044 \sin [2(c+d x)] + 540 \sin [3(c+d x)] + 70 \sin [4(c+d x)] \right) \right) / \left( 2520 d \sqrt{\sec [c+d x]} \right)$$

**Problem 186: Result unnecessarily involves higher level functions.**

$$\int \sec [c+d x]^{3 / 2} (a + a \sec [c+d x])^4 dx$$

Optimal (type 4, 213 leaves, 21 steps):

$$\begin{aligned}
 & - \frac{152 a^4 \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}}{15 d} + \\
 & \frac{32 a^4 \sqrt{\cos [c+d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}}{7 d} + \frac{152 a^4 \sqrt{\sec [c+d x]} \sin [c+d x]}{15 d} + \\
 & \frac{32 a^4 \sec [c+d x]^{3 / 2} \sin [c+d x]}{7 d} + \frac{122 a^4 \sec [c+d x]^{5 / 2} \sin [c+d x]}{45 d} + \\
 & \frac{8 a^4 \sec [c+d x]^{7 / 2} \sin [c+d x]}{7 d} + \frac{2 a^4 \sec [c+d x]^{9 / 2} \sin [c+d x]}{9 d}
 \end{aligned}$$

Result (type 5, 396 leaves):

$$\begin{aligned}
 & - \left( \left( i e^{-i(c+d x)} \sqrt{\frac{e^{i(c+d x)}}{1+e^{2 i(c+d x)}}} \cos [c+d x]^4 \left( 133 \left( 1+e^{2 i(c+d x)} \right) + \right. \right. \right. \\
 & \quad 133 \left( -1+e^{2 i c} \right) \sqrt{1+e^{2 i(c+d x)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i(c+d x)}\right] + \\
 & \quad \left. \left. \left. 60 e^{i(c+d x)} \left( -1+e^{2 i c} \right) \sqrt{1+e^{2 i(c+d x)}} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, \frac{1}{2}, \frac{5}{4}, -e^{2 i(c+d x)}\right] \right) \right) \right) \\
 & \quad \left. \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^8 \left( a+a \sec [c+d x] \right)^4 \right) / \left( 105 \sqrt{2} d \left( -1+e^{2 i c} \right) \right) + \\
 & \frac{1}{\sec [c+d x]^{7 / 2}} \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^8 \left( a+a \sec [c+d x] \right)^4 \\
 & \left( \frac{19 \cos [d x] \operatorname{Csc}[c]}{30 d} + \frac{\sec [c] \sec [c+d x]^4 \sin [d x]}{72 d} + \right. \\
 & \quad \frac{\sec [c] \sec [c+d x]^3 \left( 7 \sin [c] + 36 \sin [d x] \right)}{504 d} + \\
 & \quad \frac{\sec [c] \sec [c+d x]^2 \left( 180 \sin [c] + 427 \sin [d x] \right)}{2520 d} + \\
 & \quad \left. \frac{\sec [c] \sec [c+d x] \left( 427 \sin [c] + 720 \sin [d x] \right)}{2520 d} + \frac{2 \tan [c]}{7 d} \right)
 \end{aligned}$$

**Problem 187: Result unnecessarily involves higher level functions.**

$$\int \sqrt{\sec [c+d x]} \left( a+a \sec [c+d x] \right)^4 d x$$

Optimal (type 4, 187 leaves, 18 steps):

$$\begin{aligned}
 & - \frac{64 a^4 \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}}{5 d} + \\
 & \frac{136 a^4 \sqrt{\cos [c+d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}}{21 d} + \frac{64 a^4 \sqrt{\sec [c+d x]} \sin [c+d x]}{5 d} + \\
 & \frac{94 a^4 \sec [c+d x]^{3 / 2} \sin [c+d x]}{21 d} + \frac{8 a^4 \sec [c+d x]^{5 / 2} \sin [c+d x]}{5 d} + \frac{2 a^4 \sec [c+d x]^{7 / 2} \sin [c+d x]}{7 d}
 \end{aligned}$$

Result (type 5, 279 leaves):

$$\begin{aligned}
 & \frac{1}{840 d} a^4 \sec \left[ \frac{1}{2}(c+d x) \right]^8 (1+\sec [c+d x])^4 \\
 & \left( -\frac{1}{-1+e^{2 i c}} 4 i \sqrt{2} e^{-i(c+d x)} \sqrt{\frac{e^{i(c+d x)}}{1+e^{2 i(c+d x)}}} \cos [c+d x]^4 \left( 168 (1+e^{2 i(c+d x)}) + \right. \right. \\
 & \quad 168 (-1+e^{2 i c}) \sqrt{1+e^{2 i(c+d x)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i(c+d x)}\right] + \\
 & \quad \left. \left. 85 e^{i(c+d x)} (-1+e^{2 i c}) \sqrt{1+e^{2 i(c+d x)}} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, \frac{1}{2}, \frac{5}{4}, -e^{2 i(c+d x)}\right] \right) + \right. \\
 & \quad \left. \frac{1}{\sec [c+d x]^{7 / 2}} (672 \cos [d x] \operatorname{Csc}[c] + (235+84 \sec [c+d x]+15 \sec [c+d x]^2) \operatorname{Tan}[c+d x]) \right)
 \end{aligned}$$

**Problem 188: Result unnecessarily involves higher level functions.**

$$\int \frac{(a+a \sec [c+d x])^4}{\sqrt{\sec [c+d x]}} dx$$

Optimal (type 4, 161 leaves, 16 steps):

$$\begin{aligned}
 & - \frac{56 a^4 \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}}{5 d} + \\
 & \frac{32 a^4 \sqrt{\cos [c+d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}}{3 d} + \frac{66 a^4 \sqrt{\sec [c+d x]} \sin [c+d x]}{5 d} + \\
 & \frac{8 a^4 \sec [c+d x]^{3 / 2} \sin [c+d x]}{3 d} + \frac{2 a^4 \sec [c+d x]^{5 / 2} \sin [c+d x]}{5 d}
 \end{aligned}$$

Result (type 5, 286 leaves):

$$\frac{1}{240 d} a^4 \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^8 (1+\operatorname{Sec}[c+d x])^4$$

$$\left( -\frac{1}{-1+e^{2 i c}} 8 i \sqrt{2} e^{-i(c+d x)} \sqrt{\frac{e^{i(c+d x)}}{1+e^{2 i(c+d x)}}} \operatorname{Cos}[c+d x]^4 \left( 21 (1+e^{2 i(c+d x)}) + \right. \right.$$

$$21 (-1+e^{2 i c}) \sqrt{1+e^{2 i(c+d x)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i(c+d x)}\right] +$$

$$20 e^{i(c+d x)} (-1+e^{2 i c}) \sqrt{1+e^{2 i(c+d x)}} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, \frac{1}{2}, \frac{5}{4}, -e^{2 i(c+d x)}\right] \left. \right) +$$

$$\frac{1}{\operatorname{Sec}[c+d x]^{7/2}} (-3(-61+5 \operatorname{Cos}[2 c]) \operatorname{Cos}[d x] \operatorname{Csc}[c] + 30 \operatorname{Cos}[c] \operatorname{Sin}[d x] +$$

$$2(20+3 \operatorname{Sec}[c+d x]) \operatorname{Tan}[c+d x] \left. \right)$$

Problem 190: Result unnecessarily involves higher level functions.

$$\int \frac{(a+a \operatorname{Sec}[c+d x])^4}{\operatorname{Sec}[c+d x]^{5/2}} dx$$

Optimal (type 4, 159 leaves, 15 steps):

$$\frac{56 a^4 \sqrt{\operatorname{Cos}[c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\operatorname{Sec}[c+d x]}}{5 d} +$$

$$\frac{32 a^4 \sqrt{\operatorname{Cos}[c+d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\operatorname{Sec}[c+d x]}}{3 d} +$$

$$\frac{2 a^4 \operatorname{Sin}[c+d x]}{5 d \operatorname{Sec}[c+d x]^{3/2}} + \frac{8 a^4 \operatorname{Sin}[c+d x]}{3 d \sqrt{\operatorname{Sec}[c+d x]}} + \frac{2 a^4 \sqrt{\operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{d}$$

Result (type 5, 184 leaves):

$$\left( a^4 \left( \operatorname{Cos}\left[\frac{c}{2}\right] - i \operatorname{Sin}\left[\frac{c}{2}\right] \right) \left( \operatorname{Cos}\left[\frac{c}{2}\right] + i \operatorname{Sin}\left[\frac{c}{2}\right] \right) \right.$$

$$\left( -336 i + \frac{672 i \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i(c+d x)}\right]}{\sqrt{1+e^{2 i(c+d x)}}} - \right.$$

$$320 i \sqrt{1+e^{2 i(c+d x)}} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, \frac{1}{2}, \frac{5}{4}, -e^{2 i(c+d x)}\right] \operatorname{Sec}[c+d x] +$$

$$\left. \left. 80 \operatorname{Sin}[c+d x] + 3 \operatorname{Sec}[c+d x] \operatorname{Sin}[3(c+d x)] + 63 \operatorname{Tan}[c+d x] \right) \right) / (30 d \sqrt{\operatorname{Sec}[c+d x]})$$

**Problem 191: Result unnecessarily involves higher level functions.**

$$\int \frac{(a + a \sec [c + d x])^4}{\sec [c + d x]^{7/2}} dx$$

Optimal (type 4, 161 leaves, 16 steps):

$$\frac{64 a^4 \sqrt{\cos [c + d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\sec [c + d x]}}{5 d} +$$

$$\frac{136 a^4 \sqrt{\cos [c + d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\sec [c + d x]}}{21 d} +$$

$$\frac{2 a^4 \sin [c + d x]}{7 d \sec [c + d x]^{5/2}} + \frac{8 a^4 \sin [c + d x]}{5 d \sec [c + d x]^{3/2}} + \frac{94 a^4 \sin [c + d x]}{21 d \sqrt{\sec [c + d x]}}$$

Result (type 5, 180 leaves):

$$\left( a^4 \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{c}{2} \right] + i \sin \left[ \frac{c}{2} \right] \right) \right.$$

$$\left( -5376 i + \frac{10752 i \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right]}{\sqrt{1 + e^{2i(c+dx)}}} - \right.$$

$$2720 i \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, \frac{1}{2}, \frac{5}{4}, -e^{2i(c+dx)}\right] \sec [c + d x] +$$

$$\left. \left. 1910 \sin [c + d x] + 336 \sin [2(c + d x)] + 30 \sin [3(c + d x)] \right) \right) / \left( 420 d \sqrt{\sec [c + d x]} \right)$$

**Problem 192: Result unnecessarily involves higher level functions.**

$$\int \frac{(a + a \sec [c + d x])^4}{\sec [c + d x]^{9/2}} dx$$

Optimal (type 4, 187 leaves, 18 steps):

$$\frac{152 a^4 \sqrt{\cos [c + d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\sec [c + d x]}}{15 d} +$$

$$\frac{32 a^4 \sqrt{\cos [c + d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\sec [c + d x]}}{7 d} +$$

$$\frac{2 a^4 \sin [c + d x]}{9 d \sec [c + d x]^{7/2}} + \frac{8 a^4 \sin [c + d x]}{7 d \sec [c + d x]^{5/2}} + \frac{122 a^4 \sin [c + d x]}{45 d \sec [c + d x]^{3/2}} + \frac{32 a^4 \sin [c + d x]}{7 d \sqrt{\sec [c + d x]}}$$

Result (type 5, 156 leaves):

$$\left( a^4 \left( -25536 i + \frac{51072 i \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right]}{\sqrt{1+e^{2i(c+dx)}}} - 11520 i \sqrt{1+e^{2i(c+dx)}} \right. \right. \\ \left. \left. \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, \frac{1}{2}, \frac{5}{4}, -e^{2i(c+dx)}\right] \operatorname{Sec}[c+dx] + 12240 \operatorname{Sin}[c+dx] + \right. \right. \\ \left. \left. 3556 \operatorname{Sin}[2(c+dx)] + 720 \operatorname{Sin}[3(c+dx)] + 70 \operatorname{Sin}[4(c+dx)] \right) \right) / \left( 2520 d \sqrt{\operatorname{Sec}[c+dx]} \right)$$

**Problem 193: Result unnecessarily involves higher level functions.**

$$\int \frac{(a + a \operatorname{Sec}[c + dx])^4}{\operatorname{Sec}[c + dx]^{11/2}} dx$$

Optimal (type 4, 213 leaves, 21 steps):

$$\frac{128 a^4 \sqrt{\operatorname{Cos}[c + dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c + dx), 2\right] \sqrt{\operatorname{Sec}[c + dx]}}{15 d} + \\ \frac{904 a^4 \sqrt{\operatorname{Cos}[c + dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] \sqrt{\operatorname{Sec}[c + dx]}}{231 d} + \frac{2 a^4 \operatorname{Sin}[c + dx]}{11 d \operatorname{Sec}[c + dx]^{9/2}} + \\ \frac{8 a^4 \operatorname{Sin}[c + dx]}{9 d \operatorname{Sec}[c + dx]^{7/2}} + \frac{150 a^4 \operatorname{Sin}[c + dx]}{77 d \operatorname{Sec}[c + dx]^{5/2}} + \frac{128 a^4 \operatorname{Sin}[c + dx]}{45 d \operatorname{Sec}[c + dx]^{3/2}} + \frac{904 a^4 \operatorname{Sin}[c + dx]}{231 d \sqrt{\operatorname{Sec}[c + dx]}}$$

Result (type 5, 306 leaves):

$$-\frac{1}{1774080 d \operatorname{Sec}[c + dx]^{7/2}} i a^4 e^{-6i(c+dx)} \\ \left( -315 - 3080 e^{i(c+dx)} - 14760 e^{2i(c+dx)} - 48664 e^{3i(c+dx)} - 137055 e^{4i(c+dx)} + 427504 e^{5i(c+dx)} + \right. \\ \left. 518672 e^{7i(c+dx)} + 137055 e^{8i(c+dx)} + 48664 e^{9i(c+dx)} + 14760 e^{10i(c+dx)} + 3080 e^{11i(c+dx)} + \right. \\ \left. 315 e^{12i(c+dx)} - 946176 e^{5i(c+dx)} \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] + \right. \\ \left. 433920 e^{6i(c+dx)} \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, \frac{1}{2}, \frac{5}{4}, -e^{2i(c+dx)}\right] \right) \\ \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^8 (1 + \operatorname{Sec}[c + dx])^4$$

**Problem 194: Result unnecessarily involves higher level functions.**

$$\int \frac{\operatorname{Sec}[c + dx]^{7/2}}{a + a \operatorname{Sec}[c + dx]} dx$$

Optimal (type 4, 164 leaves, 8 steps):

$$\frac{3 \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]}}{ad} +$$

$$\frac{5 \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]}}{3ad} -$$

$$\frac{3 \sqrt{\sec[c+dx]} \sin[c+dx]}{ad} + \frac{5 \sec[c+dx]^{3/2} \sin[c+dx]}{3ad} - \frac{\sec[c+dx]^{5/2} \sin[c+dx]}{d(a+a \sec[c+dx])}$$

Result (type 5, 291 leaves):

$$\frac{1}{3ad(1+\sec[c+dx])}$$

$$\cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx] \left( \frac{1}{-1+e^{2ic}} 2i\sqrt{2} e^{-i(c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \left( 9(1+e^{2i(c+dx)}) + \right. \right.$$

$$9(-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] - 5e^{i(c+dx)}$$

$$\left. \left. (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, \frac{1}{2}, \frac{5}{4}, -e^{2i(c+dx)}\right]\right) - \sqrt{\sec[c+dx]} \right)$$

$$\left( 18 \cos[dx] \csc[c] + \sec[c+dx] \left( -5 \sec\left[\frac{1}{2}(c+dx)\right] \sin\left[\frac{3}{2}(c+dx)\right] + \tan\left[\frac{1}{2}(c+dx)\right] \right) \right)$$

**Problem 195: Result unnecessarily involves higher level functions.**

$$\int \frac{\sec[c+dx]^{5/2}}{a+a \sec[c+dx]} dx$$

Optimal (type 4, 136 leaves, 7 steps):

$$\frac{3 \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]}}{ad} -$$

$$\frac{\sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]}}{ad} +$$

$$\frac{3 \sqrt{\sec[c+dx]} \sin[c+dx]}{ad} - \frac{\sec[c+dx]^{3/2} \sin[c+dx]}{d(a+a \sec[c+dx])}$$

Result (type 5, 262 leaves):

$$\left( \cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx] \right. \\ \left. \left( -\frac{1}{d(-1+e^{2ic})} 2i\sqrt{2} e^{-i(c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \left( 3(1+e^{2i(c+dx)}) + 3 \right. \right. \right. \\ \left. \left. \left. (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] - \right. \right. \right. \\ \left. \left. \left. e^{i(c+dx)} (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, \frac{1}{2}, \frac{5}{4}, -e^{2i(c+dx)}\right] \right) \right) + \right. \\ \left. \frac{\sqrt{\sec[c+dx]} \left( 6 \cos[dx] \operatorname{Csc}[c] - 2 \tan\left[\frac{1}{2}(c+dx)\right] \right)}{d} \right) / (a(1+\sec[c+dx]))$$

**Problem 196: Result unnecessarily involves higher level functions.**

$$\int \frac{\sec[c+dx]^{3/2}}{a+a\sec[c+dx]} dx$$

Optimal (type 4, 110 leaves, 6 steps):

$$\frac{\sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]}}{ad} + \\ \frac{\sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]}}{ad} - \frac{\sqrt{\sec[c+dx]} \sin[c+dx]}{d(a+a\sec[c+dx])}$$

Result (type 5, 201 leaves):

$$-\left( \left( 2i e^{-i(c+dx)} \cos\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \\ \left. \left. \left( 1+e^{2i(c+dx)} - (1+e^{i(c+dx)}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] + \right. \right. \right. \\ \left. \left. \left. e^{i(c+dx)} (1+e^{i(c+dx)}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, \frac{1}{2}, \frac{5}{4}, -e^{2i(c+dx)}\right] \right) \right) \right. \\ \left. \sec[c+dx]^{3/2} \right) / (ad(1+e^{i(c+dx)})(1+\sec[c+dx]))$$

**Problem 197: Result unnecessarily involves higher level functions.**

$$\int \frac{\sqrt{\sec[c+dx]}}{a+a\sec[c+dx]} dx$$

Optimal (type 4, 110 leaves, 6 steps):



$$\begin{aligned}
 & - \frac{\sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]}}{ad} + \\
 & \frac{\sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]}}{ad} + \frac{\sqrt{\sec[c+dx]} \sin[c+dx]}{d(a+a \sec[c+dx])}
 \end{aligned}$$

Result (type 5, 202 leaves):

$$\begin{aligned}
 & - \left( \left( 2i e^{-i(c+dx)} \cos\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \\
 & \quad \left( -1 - e^{2i(c+dx)} + (1 + e^{i(c+dx)}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] + \right. \\
 & \quad \left. \left. e^{i(c+dx)} (1 + e^{i(c+dx)}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, \frac{1}{2}, \frac{5}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \left. \sec[c+dx]^{3/2} \right) / \left( ad (1 + e^{i(c+dx)}) (1 + \sec[c+dx]) \right) \right)
 \end{aligned}$$

**Problem 198: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{1}{\sqrt{\sec[c+dx]} (a + a \sec[c+dx])} dx$$

Optimal (type 4, 112 leaves, 6 steps):

$$\begin{aligned}
 & \frac{3 \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]}}{ad} - \\
 & \frac{\sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]}}{ad} - \frac{\sqrt{\sec[c+dx]} \sin[c+dx]}{d(a+a \sec[c+dx])}
 \end{aligned}$$

Result (type 5, 317 leaves):

$$\begin{aligned}
 & \left( \cos\left[\frac{1}{2}(c+dx)\right]^2 \left( \frac{1}{d(-1+e^{2ic})} 2i \sqrt{2} e^{-i(c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \left( 3(1+e^{2i(c+dx)}) + \right. \right. \right. \\
 & \quad \left. \left. 3(-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] + \right. \right. \\
 & \quad \left. \left. e^{i(c+dx)} (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, \frac{1}{2}, \frac{5}{4}, -e^{2i(c+dx)}\right] \right) - \frac{1}{2d} \right. \\
 & \quad \left. \left( \cos\left[\frac{1}{2}(c-dx)\right] + 2 \cos\left[\frac{1}{2}(3c+dx)\right] + 2 \cos\left[\frac{1}{2}(c+3dx)\right] + \cos\left[\frac{1}{2}(5c+3dx)\right] \right) \right. \\
 & \quad \left. \left. \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right] \sqrt{\sec[c+dx]} \right) \operatorname{Sec}[c+dx] \right) / \left( a(1+\sec[c+dx]) \right)
 \end{aligned}$$

**Problem 199: Result unnecessarily involves higher level functions and more**

than twice size of optimal antiderivative.

$$\int \frac{1}{\text{Sec}[c + dx]^{3/2} (a + a \text{Sec}[c + dx])} dx$$

Optimal (type 4, 140 leaves, 7 steps):

$$\begin{aligned} & \frac{3 \sqrt{\text{Cos}[c + dx]} \text{EllipticE}\left[\frac{1}{2}(c + dx), 2\right] \sqrt{\text{Sec}[c + dx]}}{a d} + \\ & \frac{5 \sqrt{\text{Cos}[c + dx]} \text{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] \sqrt{\text{Sec}[c + dx]}}{3 a d} + \\ & \frac{5 \text{Sin}[c + dx]}{3 a d \sqrt{\text{Sec}[c + dx]}} - \frac{\text{Sin}[c + dx]}{d \sqrt{\text{Sec}[c + dx]} (a + a \text{Sec}[c + dx])} \end{aligned}$$

Result (type 5, 380 leaves):

$$\begin{aligned} & - \left( \left( 2 i \sqrt{2} e^{-i(c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \text{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \left( 9 (1 + e^{2i(c+dx)}) + \right. \right. \right. \\ & \quad 9 (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \text{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] + \\ & \quad \left. \left. 5 e^{i(c+dx)} (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \text{Hypergeometric2F1}\left[\frac{1}{4}, \frac{1}{2}, \frac{5}{4}, -e^{2i(c+dx)}\right] \right) \right) \\ & \quad \left. \text{Sec}[c + dx] \right) / (3 d (-1 + e^{2ic}) (a + a \text{Sec}[c + dx])) + \frac{1}{a + a \text{Sec}[c + dx]} \\ & \text{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \text{Sec}[c + dx]^{3/2} \left( \frac{(2 + \text{Cos}[2c]) \text{Cos}[dx] \text{Csc}\left[\frac{c}{2}\right] \text{Sec}\left[\frac{c}{2}\right]}{d} + \right. \\ & \quad \frac{2 \text{Cos}[2dx] \text{Sin}[2c]}{3 d} - \frac{2 \text{Sec}\left[\frac{c}{2}\right] \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right] \text{Sin}\left[\frac{dx}{2}\right]}{d} - \\ & \quad \left. \frac{4 \text{Cos}[c] \text{Sin}[dx]}{d} + \frac{2 \text{Cos}[2c] \text{Sin}[2dx]}{3 d} - \frac{2 \text{Tan}\left[\frac{c}{2}\right]}{d} \right) \end{aligned}$$

Problem 200: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{1}{\text{Sec}[c + dx]^{5/2} (a + a \text{Sec}[c + dx])} dx$$

Optimal (type 4, 168 leaves, 8 steps):

$$\frac{21 \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]}}{5ad} - \frac{5 \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]}}{3ad} + \frac{7 \sin[c+dx]}{5ad \sec[c+dx]^{3/2}} - \frac{5 \sin[c+dx]}{3ad \sqrt{\sec[c+dx]}} - \frac{\sin[c+dx]}{d \sec[c+dx]^{3/2} (a+a \sec[c+dx])}$$

Result (type 5, 347 leaves):

$$\frac{1}{60ad(1+\sec[c+dx])} \cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx] \left( \frac{1}{-1+e^{2ic}} 8i\sqrt{2} e^{-i(c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \left( 63(1+e^{2i(c+dx)}) + 63(-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] + 25e^{i(c+dx)}(-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, \frac{1}{2}, \frac{5}{4}, -e^{2i(c+dx)}\right] \right) - \sqrt{\sec[c+dx]} \left( 18(17+11\cos[2c]) \cos[dx] \operatorname{Csc}[c] + 4 \left( 10\cos[2dx] \sin[2c] - 3\cos[3dx] \sin[3c] - 30\sec\left[\frac{c}{2}\right] \sec\left[\frac{1}{2}(c+dx)\right] \sin\left[\frac{dx}{2}\right] - 99\cos[c] \sin[dx] + 10\cos[2c] \sin[2dx] - 3\cos[3c] \sin[3dx] - 30\tan\left[\frac{c}{2}\right] \right) \right) \right)$$

**Problem 201: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\sec[c+dx]^{9/2}}{(a+a \sec[c+dx])^2} dx$$

Optimal (type 4, 202 leaves, 9 steps):

$$\frac{7 \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]}}{a^2 d} + \frac{10 \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]}}{3a^2 d} - \frac{7 \sqrt{\sec[c+dx]} \sin[c+dx]}{a^2 d} + \frac{10 \sec[c+dx]^{3/2} \sin[c+dx]}{3a^2 d} - \frac{7 \sec[c+dx]^{5/2} \sin[c+dx]}{3a^2 d (1+\sec[c+dx])} - \frac{\sec[c+dx]^{7/2} \sin[c+dx]}{3d (a+a \sec[c+dx])^2}$$

Result (type 5, 451 leaves):

$$\left( 7 \sqrt{2} e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\ \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\ \left. \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx] \right) / \left( d (a + a \operatorname{Sec}[c+dx])^2 \right) + \\ \left( 20 \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sqrt{\cos[c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \operatorname{Sec}\left[\frac{c}{2}\right] \right. \\ \left. \operatorname{Sec}[c+dx]^{5/2} \sin[c] \right) / \left( 3d (a + a \operatorname{Sec}[c+dx])^2 \right) + \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Sec}[c+dx]^{5/2} \right. \\ \left. \left( -\frac{14 \cos[dx] \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right]}{d} + \frac{4 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c] (-3 \sin\left[\frac{c}{2}\right] + 5 \sin\left[\frac{3c}{2}\right])}{3d} \right. \right. \\ \left. \left. + \frac{32 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right] \sin\left[\frac{dx}{2}\right]}{3d} + \frac{2 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^3 \sin\left[\frac{dx}{2}\right]}{3d} \right. \right. \\ \left. \left. + \frac{8 \operatorname{Sec}[c] \operatorname{Sec}[c+dx] \sin[dx]}{3d} + \frac{2 \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \tan\left[\frac{c}{2}\right]}{3d} \right) \right) / (a + a \operatorname{Sec}[c+dx])^2$$

**Problem 202: Result unnecessarily involves higher level functions.**

$$\int \frac{\operatorname{Sec}[c+dx]^{7/2}}{(a + a \operatorname{Sec}[c+dx])^2} dx$$

Optimal (type 4, 176 leaves, 8 steps):

$$-\frac{4 \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\operatorname{Sec}[c+dx]}}{a^2 d} - \\ \frac{5 \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\operatorname{Sec}[c+dx]}}{3 a^2 d} + \\ \frac{4 \sqrt{\operatorname{Sec}[c+dx]} \sin[c+dx]}{a^2 d} - \frac{5 \operatorname{Sec}[c+dx]^{3/2} \sin[c+dx]}{3 a^2 d (1 + \operatorname{Sec}[c+dx])} - \frac{\operatorname{Sec}[c+dx]^{5/2} \sin[c+dx]}{3 d (a + a \operatorname{Sec}[c+dx])^2}$$

Result (type 5, 259 leaves):

$$\begin{aligned}
 & - \frac{1}{6 a^2 d (1 + \operatorname{Sec}[c + d x])^2} \\
 & e^{-i (2 c + d x)} \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] \operatorname{Sec}[c + d x]^{5/2} \left( 12 i e^{-2 i (c + d x)} (1 + e^{i (c + d x)})^3 \sqrt{1 + e^{2 i (c + d x)}} \right. \\
 & \quad \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i (c + d x)}\right] + 40 \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right]^3 \sqrt{\operatorname{Cos}[c + d x]} \\
 & \quad \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \left( \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + i \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right) - \\
 & \quad \left. i (29 + 50 \operatorname{Cos}[c + d x] + 17 \operatorname{Cos}[2(c + d x)] - 12 i \operatorname{Sin}[c + d x] - 7 i \operatorname{Sin}[2(c + d x)]) \right) \\
 & \quad \left( \operatorname{Cos}\left[\frac{1}{2}(3 c + d x)\right] + i \operatorname{Sin}\left[\frac{1}{2}(3 c + d x)\right] \right)
 \end{aligned}$$

**Problem 203: Result unnecessarily involves higher level functions.**

$$\int \frac{\operatorname{Sec}[c + d x]^{5/2}}{(a + a \operatorname{Sec}[c + d x])^2} dx$$

Optimal (type 4, 149 leaves, 7 steps):

$$\begin{aligned}
 & \frac{\sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]}}{a^2 d} + \\
 & \frac{2 \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]}}{3 a^2 d} - \\
 & \frac{\sqrt{\operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{a^2 d (1 + \operatorname{Sec}[c + d x])} - \frac{\operatorname{Sec}[c + d x]^{3/2} \operatorname{Sin}[c + d x]}{3 d (a + a \operatorname{Sec}[c + d x])^2}
 \end{aligned}$$

Result (type 5, 249 leaves):

$$\begin{aligned}
 & \frac{1}{6 a^2 d (1 + \operatorname{Sec}[c + d x])^2} e^{-i (2 c + d x)} \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] \operatorname{Sec}[c + d x]^{5/2} \\
 & \quad \left( 3 i e^{-2 i (c + d x)} (1 + e^{i (c + d x)})^3 \sqrt{1 + e^{2 i (c + d x)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i (c + d x)}\right] + \right. \\
 & \quad 16 \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right]^3 \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \\
 & \quad \left. \left( \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + i \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right) - \right. \\
 & \quad \left. i (5 + 14 \operatorname{Cos}[c + d x] + 5 \operatorname{Cos}[2(c + d x)] - i \operatorname{Sin}[2(c + d x)]) \right) \\
 & \quad \left( \operatorname{Cos}\left[\frac{1}{2}(3 c + d x)\right] + i \operatorname{Sin}\left[\frac{1}{2}(3 c + d x)\right] \right)
 \end{aligned}$$

**Problem 205: Result unnecessarily involves higher level functions.**

$$\int \frac{\sqrt{\operatorname{Sec}[c + d x]}}{(a + a \operatorname{Sec}[c + d x])^2} dx$$

Optimal (type 4, 149 leaves, 7 steps):

$$\begin{aligned}
 & - \frac{\sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}}{a^2 d} + \\
 & \frac{2 \sqrt{\cos [c+d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}}{3 a^2 d} + \\
 & \frac{\sqrt{\sec [c+d x]} \sin [c+d x]}{a^2 d(1+\sec [c+d x])} - \frac{\sec [c+d x]^{3 / 2} \sin [c+d x]}{3 d(a+a \sec [c+d x])^2}
 \end{aligned}$$

Result (type 5, 247 leaves):

$$\begin{aligned}
 & \frac{1}{6 a^2 d(1+\sec [c+d x])^2} \\
 & e^{-i(2 c+d x)} \cos \left[\frac{1}{2}(c+d x)\right] \sec [c+d x]^{5 / 2}\left(16 \cos \left[\frac{1}{2}(c+d x)\right]\right)^3 \sqrt{\cos [c+d x]} \\
 & \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]\left(\cos \left[\frac{1}{2}(c+d x)\right]+i \sin \left[\frac{1}{2}(c+d x)\right]\right)- \\
 & i\left(-7-10 \cos [c+d x]-7 \cos [2(c+d x)]+3 e^{-2 i(c+d x)}\left(1+e^{i(c+d x)}\right)^3 \sqrt{1+e^{2 i(c+d x)}}\right. \\
 & \left.\operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4},-e^{2 i(c+d x)}\right]-i \sin [2(c+d x)]\right) \\
 & \left(\cos \left[\frac{1}{2}(3 c+d x)\right]+i \sin \left[\frac{1}{2}(3 c+d x)\right]\right)
 \end{aligned}$$

**Problem 206: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{1}{\sqrt{\sec [c+d x]}(a+a \sec [c+d x])^2} d x$$

Optimal (type 4, 152 leaves, 7 steps):

$$\begin{aligned}
 & \frac{4 \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}}{a^2 d} - \\
 & \frac{5 \sqrt{\cos [c+d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}}{3 a^2 d} - \\
 & \frac{5 \sqrt{\sec [c+d x]} \sin [c+d x]}{3 a^2 d(1+\sec [c+d x])} - \frac{\sqrt{\sec [c+d x]} \sin [c+d x]}{3 d(a+a \sec [c+d x])^2}
 \end{aligned}$$

Result (type 5, 430 leaves):

$$\begin{aligned}
 & \left( 4 \sqrt{2} e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\
 & \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx]^2 \right) / \left( d (a + a \operatorname{Sec}[c+dx])^2 \right) - \\
 & \left( 10 \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sqrt{\cos[c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx]^{5/2} \sin[c] \right) / \left( 3 d (a + a \operatorname{Sec}[c+dx])^2 \right) + \\
 & \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Sec}[c+dx]^{5/2} \left( -\frac{2(3 + \cos[2c]) \cos[dx] \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right]}{d} + \right. \right. \\
 & \quad \frac{28 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right] \sin\left[\frac{dx}{2}\right]}{3 d} - \frac{2 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^3 \sin\left[\frac{dx}{2}\right]}{3 d} + \\
 & \quad \left. \left. \frac{8 \cos[c] \sin[dx]}{d} + \frac{28 \tan\left[\frac{c}{2}\right]}{3 d} - \frac{2 \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \tan\left[\frac{c}{2}\right]}{3 d} \right) \right) / (a + a \operatorname{Sec}[c+dx])^2
 \end{aligned}$$

**Problem 207: Result unnecessarily involves higher level functions.**

$$\int \frac{1}{\operatorname{Sec}[c+dx]^{3/2} (a + a \operatorname{Sec}[c+dx])^2} dx$$

Optimal (type 4, 178 leaves, 8 steps):

$$\begin{aligned}
 & - \frac{7 \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\operatorname{Sec}[c+dx]}}{a^2 d} + \\
 & \frac{10 \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\operatorname{Sec}[c+dx]}}{3 a^2 d} + \frac{10 \sin[c+dx]}{3 a^2 d \sqrt{\operatorname{Sec}[c+dx]}} - \\
 & \frac{7 \sin[c+dx]}{3 a^2 d \sqrt{\operatorname{Sec}[c+dx]} (1 + \operatorname{Sec}[c+dx])} - \frac{\sin[c+dx]}{3 d \sqrt{\operatorname{Sec}[c+dx]} (a + a \operatorname{Sec}[c+dx])^2}
 \end{aligned}$$

Result (type 5, 278 leaves):

$$\left( \cos\left[\frac{1}{2}(c+dx)\right]^4 \right. \\ \left. \left( \frac{40 \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]}}{d} + \left( 2i e^{-2i(c+dx)} \left( 1 + 33 e^{i(c+dx)} + \right. \right. \right. \right. \\ \left. \left. \left. 73 e^{2i(c+dx)} + 87 e^{3i(c+dx)} + 81 e^{4i(c+dx)} + 53 e^{5i(c+dx)} + 9 e^{6i(c+dx)} - e^{7i(c+dx)} - \right. \right. \right. \\ \left. \left. \left. 42 e^{i(c+dx)} \left( 1 + e^{i(c+dx)} \right)^3 \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right) \right. \\ \left. \sqrt{\sec[c+dx]} \right) / \left( d \left( 1 + e^{i(c+dx)} \right)^3 \right) \sec[c+dx]^2 / \left( 3 a^2 \left( 1 + \sec[c+dx] \right)^2 \right)$$

Problem 208: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{1}{\sec[c+dx]^{5/2} (a + a \sec[c+dx])^2} dx$$

Optimal (type 4, 200 leaves, 9 steps):

$$\frac{56 \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]}}{5 a^2 d} - \\ \frac{5 \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]}}{a^2 d} + \frac{56 \sin[c+dx]}{15 a^2 d \sec[c+dx]^{3/2}} - \\ \frac{5 \sin[c+dx]}{a^2 d \sqrt{\sec[c+dx]}} - \frac{3 \sin[c+dx]}{a^2 d \sec[c+dx]^{3/2} (1 + \sec[c+dx])} - \frac{\sin[c+dx]}{3 d \sec[c+dx]^{3/2} (a + a \sec[c+dx])^2}$$

Result (type 5, 500 leaves):



$$\begin{aligned}
 & \left( 56 \sqrt{2} e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\
 & \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx]^2 \right) / \left( 5d (a + a \operatorname{Sec}[c+dx])^2 \right) - \\
 & \left( 10 \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sqrt{\cos[c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx]^{5/2} \sin[c] \right) / \left( d (a + a \operatorname{Sec}[c+dx])^2 \right) + \\
 & \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Sec}[c+dx]^{5/2} \left( -\frac{(151 + 73 \cos[2c]) \cos[dx] \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right]}{10d} - \right. \right. \\
 & \quad \frac{8 \cos[2dx] \sin[2c]}{3d} + \frac{2 \cos[3dx] \sin[3c]}{5d} + \frac{52 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right] \sin\left[\frac{dx}{2}\right]}{3d} - \\
 & \quad \frac{2 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^3 \sin\left[\frac{dx}{2}\right]}{3d} + \frac{146 \cos[c] \sin[dx]}{5d} - \frac{8 \cos[2c] \sin[2dx]}{3d} + \\
 & \quad \left. \left. \frac{2 \cos[3c] \sin[3dx]}{5d} + \frac{52 \tan\left[\frac{c}{2}\right]}{3d} - \frac{2 \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \tan\left[\frac{c}{2}\right]}{3d} \right) \right) / (a + a \operatorname{Sec}[c+dx])^2
 \end{aligned}$$

**Problem 209: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec}[c+dx]^{11/2}}{(a + a \operatorname{Sec}[c+dx])^3} dx$$

Optimal (type 4, 247 leaves, 10 steps):

$$\begin{aligned}
 & \frac{119 \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\operatorname{Sec}[c+dx]}}{10 a^3 d} + \\
 & \frac{11 \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\operatorname{Sec}[c+dx]}}{2 a^3 d} - \\
 & \frac{119 \sqrt{\operatorname{Sec}[c+dx]} \sin[c+dx]}{10 a^3 d} + \frac{11 \operatorname{Sec}[c+dx]^{3/2} \sin[c+dx]}{2 a^3 d} - \\
 & \frac{\operatorname{Sec}[c+dx]^{9/2} \sin[c+dx]}{5d (a + a \operatorname{Sec}[c+dx])^3} - \frac{2 \operatorname{Sec}[c+dx]^{7/2} \sin[c+dx]}{3ad (a + a \operatorname{Sec}[c+dx])^2} - \frac{119 \operatorname{Sec}[c+dx]^{5/2} \sin[c+dx]}{30d (a^3 + a^3 \operatorname{Sec}[c+dx])}
 \end{aligned}$$

Result (type 5, 516 leaves):

$$\left( 119 \sqrt{2} e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\ \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\ \left. \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx]^3 \right) / \left( 5d (a + a \operatorname{Sec}[c+dx])^3 \right) + \\ \left( 22 \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \sqrt{\cos[c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \operatorname{Sec}\left[\frac{c}{2}\right] \right. \\ \left. \operatorname{Sec}[c+dx]^{7/2} \sin[c] \right) / \left( d (a + a \operatorname{Sec}[c+dx])^3 \right) + \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Sec}[c+dx]^{7/2} \right. \\ \left. \left( -\frac{238 \cos[dx] \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right]}{5d} + \frac{2 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c] (-25 \sin\left[\frac{c}{2}\right] + 33 \sin\left[\frac{3c}{2}\right])}{3d} \right) \right. \\ \left. \frac{116 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right] \sin\left[\frac{dx}{2}\right]}{3d} + \frac{52 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^3 \sin\left[\frac{dx}{2}\right]}{15d} \right. \\ \left. \frac{2 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^5 \sin\left[\frac{dx}{2}\right]}{5d} + \frac{16 \operatorname{Sec}[c] \operatorname{Sec}[c+dx] \sin[dx]}{3d} \right. \\ \left. \left. \frac{52 \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \tan\left[\frac{c}{2}\right]}{15d} + \frac{2 \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \tan\left[\frac{c}{2}\right]}{5d} \right) \right) / (a + a \operatorname{Sec}[c+dx])^3$$

**Problem 210: Result unnecessarily involves higher level functions.**

$$\int \frac{\operatorname{Sec}[c+dx]^{9/2}}{(a + a \operatorname{Sec}[c+dx])^3} dx$$

Optimal (type 4, 221 leaves, 9 steps):

$$-\frac{49 \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\operatorname{Sec}[c+dx]}}{10 a^3 d} - \\ \frac{13 \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\operatorname{Sec}[c+dx]}}{6 a^3 d} + \frac{49 \sqrt{\operatorname{Sec}[c+dx]} \sin[c+dx]}{10 a^3 d} - \\ \frac{\operatorname{Sec}[c+dx]^{7/2} \sin[c+dx]}{5d (a + a \operatorname{Sec}[c+dx])^3} - \frac{8 \operatorname{Sec}[c+dx]^{5/2} \sin[c+dx]}{15 a d (a + a \operatorname{Sec}[c+dx])^2} - \frac{13 \operatorname{Sec}[c+dx]^{3/2} \sin[c+dx]}{6d (a^3 + a^3 \operatorname{Sec}[c+dx])}$$

Result (type 5, 371 leaves):

$$\frac{1}{15 a^3 d (1 + \operatorname{Sec}[c + d x])^3}$$

$$2 \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right]^6 \left( -\frac{1}{-1 + e^{2 i c}} 2 i \sqrt{2} e^{-i(c+d x)} \sqrt{\frac{e^{i(c+d x)}}{1 + e^{2 i(c+d x)}}} \left( 147 (1 + e^{2 i(c+d x)}) + \right. \right.$$

$$147 (-1 + e^{2 i c}) \sqrt{1 + e^{2 i(c+d x)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i(c+d x)}\right] -$$

$$\left. \left. 65 e^{i(c+d x)} (-1 + e^{2 i c}) \sqrt{1 + e^{2 i(c+d x)}} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, \frac{1}{2}, \frac{5}{4}, -e^{2 i(c+d x)}\right]\right) + \right.$$

$$\frac{1}{32} \left( 1284 \operatorname{Cos}\left[\frac{1}{2}(c - d x)\right] + 921 \operatorname{Cos}\left[\frac{1}{2}(3 c + d x)\right] + 1243 \operatorname{Cos}\left[\frac{1}{2}(c + 3 d x)\right] + \right.$$

$$374 \operatorname{Cos}\left[\frac{1}{2}(5 c + 3 d x)\right] + 670 \operatorname{Cos}\left[\frac{1}{2}(3 c + 5 d x)\right] + 65 \operatorname{Cos}\left[\frac{1}{2}(7 c + 5 d x)\right] +$$

$$\left. \left. 147 \operatorname{Cos}\left[\frac{1}{2}(5 c + 7 d x)\right]\right) \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^5 \sqrt{\operatorname{Sec}[c + d x]} \right) \operatorname{Sec}[c + d x]^3$$

**Problem 211: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec}[c + d x]^{7/2}}{(a + a \operatorname{Sec}[c + d x])^3} dx$$

Optimal (type 4, 195 leaves, 8 steps):

$$\frac{9 \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]}}{10 a^3 d} +$$

$$\frac{\sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]}}{2 a^3 d} - \frac{\operatorname{Sec}[c + d x]^{5/2} \operatorname{Sin}[c + d x]}{5 d (a + a \operatorname{Sec}[c + d x])^3} -$$

$$\frac{2 \operatorname{Sec}[c + d x]^{3/2} \operatorname{Sin}[c + d x]}{5 a d (a + a \operatorname{Sec}[c + d x])^2} - \frac{9 \sqrt{\operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{10 d (a^3 + a^3 \operatorname{Sec}[c + d x])}$$

Result (type 5, 474 leaves):

$$\left( 9 \sqrt{2} e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\ \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\ \left. \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx] \right)^3 \Big/ \left( 5d (a + a \operatorname{Sec}[c+dx])^3 \right) + \\ \left( 2 \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \sqrt{\cos[c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \right. \\ \left. \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx]^{7/2} \sin[c] \right) \Big/ \left( d (a + a \operatorname{Sec}[c+dx])^3 \right) + \\ \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Sec}[c+dx]^{7/2} \left( -\frac{18 \cos[dx] \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right]}{5d} + \frac{4 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right] \sin\left[\frac{dx}{2}\right]}{d} \right. \right. \\ \left. \left. + \frac{4 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^3 \sin\left[\frac{dx}{2}\right]}{5d} + \frac{2 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^5 \sin\left[\frac{dx}{2}\right]}{5d} + \frac{4 \operatorname{Tan}\left[\frac{c}{2}\right]}{d} \right. \right. \\ \left. \left. + \frac{4 \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \operatorname{Tan}\left[\frac{c}{2}\right]}{5d} + \frac{2 \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Tan}\left[\frac{c}{2}\right]}{5d} \right) \right) \Big/ (a + a \operatorname{Sec}[c+dx])^3$$

**Problem 212: Result unnecessarily involves higher level functions.**

$$\int \frac{\operatorname{Sec}[c+dx]^{5/2}}{(a + a \operatorname{Sec}[c+dx])^3} dx$$

Optimal (type 4, 195 leaves, 8 steps):

$$\frac{\sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\operatorname{Sec}[c+dx]}}{10 a^3 d} + \\ \frac{\sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\operatorname{Sec}[c+dx]}}{6 a^3 d} - \frac{\operatorname{Sec}[c+dx]^{3/2} \sin[c+dx]}{5d (a + a \operatorname{Sec}[c+dx])^3} - \\ \frac{4 \sqrt{\operatorname{Sec}[c+dx]} \sin[c+dx]}{15 a d (a + a \operatorname{Sec}[c+dx])^2} + \frac{\sqrt{\operatorname{Sec}[c+dx]} \sin[c+dx]}{6 d (a^3 + a^3 \operatorname{Sec}[c+dx])}$$

Result (type 5, 371 leaves):

$$\begin{aligned}
 & \frac{1}{15 a^3 d (1 + \operatorname{Sec}[c + d x])^3} 2 \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right]^6 \left( \frac{1}{-1 + e^{2 i c}} 2 i \sqrt{2} e^{-i(c+d x)} \sqrt{\frac{e^{i(c+d x)}}{1 + e^{2 i(c+d x)}}} \right. \\
 & \left. \left( 3 (1 + e^{2 i(c+d x)}) + 3 (-1 + e^{2 i c}) \sqrt{1 + e^{2 i(c+d x)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i(c+d x)}\right] - \right. \right. \\
 & \left. \left. 5 e^{i(c+d x)} (-1 + e^{2 i c}) \sqrt{1 + e^{2 i(c+d x)}} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, \frac{1}{2}, \frac{5}{4}, -e^{2 i(c+d x)}\right] \right) - \right. \\
 & \left. \frac{1}{32} \left( 36 \operatorname{Cos}\left[\frac{1}{2}(c - d x)\right] + 9 \operatorname{Cos}\left[\frac{1}{2}(3 c + d x)\right] + 7 \operatorname{Cos}\left[\frac{1}{2}(c + 3 d x)\right] + 26 \operatorname{Cos}\left[\frac{1}{2}(5 c + 3 d x)\right] + \right. \right. \\
 & \left. \left. 10 \operatorname{Cos}\left[\frac{1}{2}(3 c + 5 d x)\right] + 5 \operatorname{Cos}\left[\frac{1}{2}(7 c + 5 d x)\right] + 3 \operatorname{Cos}\left[\frac{1}{2}(5 c + 7 d x)\right] \right) \right. \\
 & \left. \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^5 \sqrt{\operatorname{Sec}[c + d x]} \right) \operatorname{Sec}[c + d x]^3
 \end{aligned}$$

**Problem 213: Result unnecessarily involves higher level functions.**

$$\int \frac{\operatorname{Sec}[c + d x]^{3/2}}{(a + a \operatorname{Sec}[c + d x])^3} dx$$

Optimal (type 4, 195 leaves, 8 steps):

$$\begin{aligned}
 & - \frac{\sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]}}{10 a^3 d} + \\
 & \frac{\sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]}}{6 a^3 d} + \\
 & \frac{\operatorname{Sec}[c + d x]^{3/2} \operatorname{Sin}[c + d x]}{5 d (a + a \operatorname{Sec}[c + d x])^3} - \frac{\sqrt{\operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{15 a d (a + a \operatorname{Sec}[c + d x])^2} + \frac{\sqrt{\operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{6 d (a^3 + a^3 \operatorname{Sec}[c + d x])}
 \end{aligned}$$

Result (type 5, 371 leaves):

$$\frac{1}{15 a^3 d (1 + \operatorname{Sec}[c + d x])^3} 2 \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right]^6 \left( -\frac{1}{-1 + e^{2 i c}} 2 i \sqrt{2} e^{-i(c+d x)} \sqrt{\frac{e^{i(c+d x)}}{1 + e^{2 i(c+d x)}}} \left( 3 (1 + e^{2 i(c+d x)}) + 3 (-1 + e^{2 i c}) \sqrt{1 + e^{2 i(c+d x)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i(c+d x)}\right] + 5 e^{i(c+d x)} (-1 + e^{2 i c}) \sqrt{1 + e^{2 i(c+d x)}} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, \frac{1}{2}, \frac{5}{4}, -e^{2 i(c+d x)}\right] \right) + \frac{1}{32} \left( 36 \operatorname{Cos}\left[\frac{1}{2}(c - d x)\right] + 9 \operatorname{Cos}\left[\frac{1}{2}(3 c + d x)\right] + 17 \operatorname{Cos}\left[\frac{1}{2}(c + 3 d x)\right] + 16 \operatorname{Cos}\left[\frac{1}{2}(5 c + 3 d x)\right] + 20 \operatorname{Cos}\left[\frac{1}{2}(3 c + 5 d x)\right] - 5 \operatorname{Cos}\left[\frac{1}{2}(7 c + 5 d x)\right] + 3 \operatorname{Cos}\left[\frac{1}{2}(5 c + 7 d x)\right] \right) \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^5 \sqrt{\operatorname{Sec}[c + d x]} \right) \operatorname{Sec}[c + d x]^3$$

**Problem 214: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\sqrt{\operatorname{Sec}[c + d x]}}{(a + a \operatorname{Sec}[c + d x])^3} dx$$

Optimal (type 4, 195 leaves, 8 steps):

$$-\frac{9 \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]}}{10 a^3 d} + \frac{\sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]}}{2 a^3 d} - \frac{\operatorname{Sec}[c + d x]^{3/2} \operatorname{Sin}[c + d x]}{5 d (a + a \operatorname{Sec}[c + d x])^3} + \frac{2 \sqrt{\operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{5 a d (a + a \operatorname{Sec}[c + d x])^2} + \frac{\sqrt{\operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{2 d (a^3 + a^3 \operatorname{Sec}[c + d x])}$$

Result (type 5, 474 leaves):

$$\begin{aligned}
 & - \left( \left( 9 \sqrt{2} e^{-i(c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right] \right. \right. \\
 & \quad \left. \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \right. \\
 & \quad \left. \left. \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx]^3 \right) / \left( 5d (a + a \operatorname{Sec}[c+dx])^3 \right) \right) + \\
 & \left( 2 \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \sqrt{\cos[c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \operatorname{Sec}\left[\frac{c}{2}\right] \right. \\
 & \quad \left. \operatorname{Sec}[c+dx]^{7/2} \sin[c] \right) / \left( d (a + a \operatorname{Sec}[c+dx])^3 \right) + \\
 & \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Sec}[c+dx]^{7/2} \left( \frac{18 \cos[dx] \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right]}{5d} - \frac{12 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right] \sin\left[\frac{dx}{2}\right]}{d} \right. \right. \\
 & \quad \left. \left. + \frac{16 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^3 \sin\left[\frac{dx}{2}\right]}{5d} - \frac{2 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^5 \sin\left[\frac{dx}{2}\right]}{5d} - \frac{12 \tan\left[\frac{c}{2}\right]}{d} \right. \right. \\
 & \quad \left. \left. + \frac{16 \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \tan\left[\frac{c}{2}\right]}{5d} - \frac{2 \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \tan\left[\frac{c}{2}\right]}{5d} \right) \right) / \left( a + a \operatorname{Sec}[c+dx] \right)^3
 \end{aligned}$$

**Problem 215: Result unnecessarily involves higher level functions.**

$$\int \frac{1}{\sqrt{\operatorname{Sec}[c+dx]} (a + a \operatorname{Sec}[c+dx])^3} dx$$

Optimal (type 4, 195 leaves, 8 steps):

$$\begin{aligned}
 & \frac{49 \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\operatorname{Sec}[c+dx]}}{10 a^3 d} - \\
 & \frac{13 \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\operatorname{Sec}[c+dx]}}{6 a^3 d} - \frac{\sqrt{\operatorname{Sec}[c+dx]} \sin[c+dx]}{5d (a + a \operatorname{Sec}[c+dx])^3} - \\
 & \frac{8 \sqrt{\operatorname{Sec}[c+dx]} \sin[c+dx]}{15 a d (a + a \operatorname{Sec}[c+dx])^2} - \frac{13 \sqrt{\operatorname{Sec}[c+dx]} \sin[c+dx]}{6 d (a^3 + a^3 \operatorname{Sec}[c+dx])}
 \end{aligned}$$

Result (type 5, 386 leaves):

$$\frac{1}{15 a^3 d (1 + \operatorname{Sec}[c + d x])^3} \\ 2 \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right]^6 \left( \frac{1}{-1 + e^{2 i c}} 2 i \sqrt{2} e^{-i(c+d x)} \sqrt{\frac{e^{i(c+d x)}}{1 + e^{2 i(c+d x)}}} \left( 147 (1 + e^{2 i(c+d x)}) + \right. \right. \\ \left. 147 (-1 + e^{2 i c}) \sqrt{1 + e^{2 i(c+d x)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i(c+d x)}\right] + \right. \\ \left. 65 e^{i(c+d x)} (-1 + e^{2 i c}) \sqrt{1 + e^{2 i(c+d x)}} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, \frac{1}{2}, \frac{5}{4}, -e^{2 i(c+d x)}\right] \right) - \\ \frac{1}{32} \left( 1134 \operatorname{Cos}\left[\frac{1}{2}(c - d x)\right] + 1071 \operatorname{Cos}\left[\frac{1}{2}(3 c + d x)\right] + 923 \operatorname{Cos}\left[\frac{1}{2}(c + 3 d x)\right] + \right. \\ \left. 694 \operatorname{Cos}\left[\frac{1}{2}(5 c + 3 d x)\right] + 470 \operatorname{Cos}\left[\frac{1}{2}(3 c + 5 d x)\right] + \right. \\ \left. 265 \operatorname{Cos}\left[\frac{1}{2}(7 c + 5 d x)\right] + 117 \operatorname{Cos}\left[\frac{1}{2}(5 c + 7 d x)\right] + 30 \operatorname{Cos}\left[\frac{1}{2}(9 c + 7 d x)\right] \right) \\ \left. \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^5 \sqrt{\operatorname{Sec}[c + d x]} \right) \operatorname{Sec}[c + d x]^3$$

Problem 216: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{1}{\operatorname{Sec}[c + d x]^{3/2} (a + a \operatorname{Sec}[c + d x])^3} dx$$

Optimal (type 4, 221 leaves, 9 steps):

$$\frac{119 \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]}}{10 a^3 d} + \\ \frac{11 \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]}}{2 a^3 d} + \\ \frac{11 \operatorname{Sin}[c + d x]}{2 a^3 d \sqrt{\operatorname{Sec}[c + d x]}} - \frac{\operatorname{Sin}[c + d x]}{5 d \sqrt{\operatorname{Sec}[c + d x]} (a + a \operatorname{Sec}[c + d x])^3} - \\ \frac{2 \operatorname{Sin}[c + d x]}{3 a d \sqrt{\operatorname{Sec}[c + d x]} (a + a \operatorname{Sec}[c + d x])^2} - \frac{119 \operatorname{Sin}[c + d x]}{30 d \sqrt{\operatorname{Sec}[c + d x]} (a^3 + a^3 \operatorname{Sec}[c + d x])}$$

Result (type 5, 529 leaves):



$$\begin{aligned}
 & - \left( \left( 119 \sqrt{2} e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right] \right. \right. \\
 & \quad \left. \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \right. \\
 & \quad \left. \left. \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx]^3 \right) / \left( 5d (a + a \operatorname{Sec}[c+dx])^3 \right) \right) + \\
 & \left( 22 \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \sqrt{\cos[c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx]^{7/2} \sin[c] \right) / \\
 & \left( d (a + a \operatorname{Sec}[c+dx])^3 + \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Sec}[c+dx]^{7/2} \right. \right. \\
 & \quad \left. \left( \frac{2(89 + 30 \cos[2c]) \cos[dx] \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right]}{5d} + \frac{8 \cos[2dx] \sin[2c]}{3d} - \right. \right. \\
 & \quad \left. \frac{172 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right] \sin\left[\frac{dx}{2}\right]}{3d} + \frac{88 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^3 \sin\left[\frac{dx}{2}\right]}{15d} - \right. \\
 & \quad \left. \frac{2 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^5 \sin\left[\frac{dx}{2}\right]}{5d} - \frac{48 \cos[c] \sin[dx]}{d} + \frac{8 \cos[2c] \sin[2dx]}{3d} - \right. \\
 & \quad \left. \left. \left. \frac{172 \tan\left[\frac{c}{2}\right]}{3d} + \frac{88 \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \tan\left[\frac{c}{2}\right]}{15d} - \frac{2 \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \tan\left[\frac{c}{2}\right]}{5d} \right) \right) \right) / (a + a \operatorname{Sec}[c+dx])^3
 \end{aligned}$$

**Problem 217: Result unnecessarily involves higher level functions.**

$$\int \frac{1}{\operatorname{Sec}[c+dx]^{5/2} (a + a \operatorname{Sec}[c+dx])^3} dx$$

Optimal (type 4, 247 leaves, 10 steps):

$$\begin{aligned}
 & \frac{231 \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\operatorname{Sec}[c+dx]}}{10 a^3 d} - \\
 & \frac{21 \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\operatorname{Sec}[c+dx]}}{2 a^3 d} + \frac{77 \sin[c+dx]}{10 a^3 d \operatorname{Sec}[c+dx]^{3/2}} - \\
 & \frac{21 \sin[c+dx]}{2 a^3 d \sqrt{\operatorname{Sec}[c+dx]}} - \frac{\sin[c+dx]}{5 d \operatorname{Sec}[c+dx]^{3/2} (a + a \operatorname{Sec}[c+dx])^3} - \\
 & \frac{4 \sin[c+dx]}{5 a d \operatorname{Sec}[c+dx]^{3/2} (a + a \operatorname{Sec}[c+dx])^2} - \frac{63 \sin[c+dx]}{10 d \operatorname{Sec}[c+dx]^{3/2} (a^3 + a^3 \operatorname{Sec}[c+dx])}
 \end{aligned}$$

Result (type 5, 332 leaves):

$$\begin{aligned}
 & - \frac{1}{5 a^3 d (1 + e^{i(c+dx)})^5 (1 + \text{Sec}[c + dx])^3} 2 i e^{-3 i(c+dx)} \text{Cos}\left[\frac{1}{2}(c + dx)\right]^6 \\
 & \left( -1 + 5 e^{i(c+dx)} + 369 e^{2 i(c+dx)} + 1505 e^{3 i(c+dx)} + 2900 e^{4 i(c+dx)} + 3590 e^{5 i(c+dx)} + \right. \\
 & \quad 3340 e^{6 i(c+dx)} + 2182 e^{7 i(c+dx)} + 805 e^{8 i(c+dx)} + 93 e^{9 i(c+dx)} - 5 e^{10 i(c+dx)} + e^{11 i(c+dx)} - \\
 & \quad 210 i e^{3 i(c+dx)} (1 + e^{i(c+dx)})^5 \sqrt{\text{Cos}[c + dx]} \text{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] - 462 e^{2 i(c+dx)} \\
 & \quad \left. (1 + e^{i(c+dx)})^5 \sqrt{1 + e^{2 i(c+dx)}} \text{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i(c+dx)}\right] \right) \text{Sec}[c + dx]^{7/2}
 \end{aligned}$$

**Problem 218: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \text{Sec}[c + dx]^{5/2} \sqrt{a + a \text{Sec}[c + dx]} dx$$

Optimal (type 3, 116 leaves, 4 steps):

$$\frac{3 \sqrt{a} \text{ArcSinh}\left[\frac{\sqrt{a} \text{Tan}[c+dx]}{\sqrt{a+a \text{Sec}[c+dx]}}\right]}{4 d} + \frac{3 a \text{Sec}[c + dx]^{3/2} \text{Sin}[c + dx]}{4 d \sqrt{a + a \text{Sec}[c + dx]}} + \frac{a \text{Sec}[c + dx]^{5/2} \text{Sin}[c + dx]}{2 d \sqrt{a + a \text{Sec}[c + dx]}}$$

Result (type 3, 434 leaves):

$$\begin{aligned}
 & \frac{1}{32 \sqrt{2} d \sqrt{\text{Sec}[c + dx]}} \text{Sec}\left[\frac{1}{2}(c + dx)\right] \sqrt{a (1 + \text{Sec}[c + dx])} \\
 & \left( -12 i \text{ArcTan}\left[\frac{\text{Cos}\left[\frac{1}{4}(c + dx)\right] - (-1 + \sqrt{2}) \text{Sin}\left[\frac{1}{4}(c + dx)\right]}{(1 + \sqrt{2}) \text{Cos}\left[\frac{1}{4}(c + dx)\right] - \text{Sin}\left[\frac{1}{4}(c + dx)\right]}\right] - \right. \\
 & \quad 12 i \text{ArcTan}\left[\frac{\text{Cos}\left[\frac{1}{4}(c + dx)\right] - (1 + \sqrt{2}) \text{Sin}\left[\frac{1}{4}(c + dx)\right]}{(-1 + \sqrt{2}) \text{Cos}\left[\frac{1}{4}(c + dx)\right] - \text{Sin}\left[\frac{1}{4}(c + dx)\right]}\right] + \text{Sec}[c + dx]^2 \\
 & \quad \left( 6 \text{Log}\left[\sqrt{2} + 2 \text{Sin}\left[\frac{1}{2}(c + dx)\right]\right] - 3 \text{Log}\left[2 - \sqrt{2} \text{Cos}\left[\frac{1}{2}(c + dx)\right] - \sqrt{2} \text{Sin}\left[\frac{1}{2}(c + dx)\right]\right] - \right. \\
 & \quad 3 \text{Log}\left[2 + \sqrt{2} \text{Cos}\left[\frac{1}{2}(c + dx)\right] - \sqrt{2} \text{Sin}\left[\frac{1}{2}(c + dx)\right]\right] + \\
 & \quad \text{Cos}[2(c + dx)] \left( 6 \text{Log}\left[\sqrt{2} + 2 \text{Sin}\left[\frac{1}{2}(c + dx)\right]\right] - \right. \\
 & \quad \left. 3 \left( \text{Log}\left[2 - \sqrt{2} \text{Cos}\left[\frac{1}{2}(c + dx)\right] - \sqrt{2} \text{Sin}\left[\frac{1}{2}(c + dx)\right]\right] + \text{Log}\left[2 + \sqrt{2} \text{Cos}\left[\frac{1}{2}(c + dx)\right] - \right. \right. \\
 & \quad \left. \left. \sqrt{2} \text{Sin}\left[\frac{1}{2}(c + dx)\right]\right] \right) \right) \left. \right) + 4 \sqrt{2} \text{Sin}\left[\frac{1}{2}(c + dx)\right] + 12 \sqrt{2} \text{Sin}\left[\frac{3}{2}(c + dx)\right] \left. \right)
 \end{aligned}$$

**Problem 219: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \text{Sec}[c + dx]^{3/2} \sqrt{a + a \text{Sec}[c + dx]} \, dx$$

Optimal (type 3, 72 leaves, 3 steps):

$$\frac{\sqrt{a} \text{ArcSinh}\left[\frac{\sqrt{a} \text{Tan}[c+dx]}{\sqrt{a+a \text{Sec}[c+dx]}}\right]}{d} + \frac{a \text{Sec}[c + dx]^{3/2} \text{Sin}[c + dx]}{d \sqrt{a + a \text{Sec}[c + dx]}}$$

Result (type 3, 306 leaves):

$$\begin{aligned} & \frac{1}{4 \sqrt{2} d \sqrt{\text{Sec}[c + dx]}} \text{Sec}\left[\frac{1}{2}(c + dx)\right] \sqrt{a(1 + \text{Sec}[c + dx])} \\ & \left( -2 i \text{ArcTan}\left[\frac{\cos\left[\frac{1}{4}(c + dx)\right] - (-1 + \sqrt{2}) \sin\left[\frac{1}{4}(c + dx)\right]}{(1 + \sqrt{2}) \cos\left[\frac{1}{4}(c + dx)\right] - \sin\left[\frac{1}{4}(c + dx)\right]}\right] - \right. \\ & \quad \left. 2 i \text{ArcTan}\left[\frac{\cos\left[\frac{1}{4}(c + dx)\right] - (1 + \sqrt{2}) \sin\left[\frac{1}{4}(c + dx)\right]}{(-1 + \sqrt{2}) \cos\left[\frac{1}{4}(c + dx)\right] - \sin\left[\frac{1}{4}(c + dx)\right]}\right] + \right. \\ & \quad \left. 2 \text{Log}\left[\sqrt{2} + 2 \sin\left[\frac{1}{2}(c + dx)\right]\right] - \text{Log}\left[2 - \sqrt{2} \cos\left[\frac{1}{2}(c + dx)\right] - \sqrt{2} \sin\left[\frac{1}{2}(c + dx)\right]\right] - \right. \\ & \quad \left. \text{Log}\left[2 + \sqrt{2} \cos\left[\frac{1}{2}(c + dx)\right] - \sqrt{2} \sin\left[\frac{1}{2}(c + dx)\right]\right] + 4 \sqrt{2} \text{Sec}[c + dx] \text{Sin}\left[\frac{1}{2}(c + dx)\right] \right) \end{aligned}$$

**Problem 220: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \sqrt{\text{Sec}[c + dx]} \sqrt{a + a \text{Sec}[c + dx]} \, dx$$

Optimal (type 3, 37 leaves, 2 steps):

$$\frac{2 \sqrt{a} \text{ArcSinh}\left[\frac{\sqrt{a} \text{Tan}[c+dx]}{\sqrt{a+a \text{Sec}[c+dx]}}\right]}{d}$$

Result (type 3, 283 leaves):

$$\left( \left( -2 \operatorname{ArcTan} \left[ \frac{\cos \left[ \frac{1}{4} (c + d x) \right] - (-1 + \sqrt{2}) \sin \left[ \frac{1}{4} (c + d x) \right]}{(1 + \sqrt{2}) \cos \left[ \frac{1}{4} (c + d x) \right] - \sin \left[ \frac{1}{4} (c + d x) \right]} \right] - \right. \right. \\ \left. \left. 2 \operatorname{ArcTan} \left[ \frac{\cos \left[ \frac{1}{4} (c + d x) \right] - (1 + \sqrt{2}) \sin \left[ \frac{1}{4} (c + d x) \right]}{(-1 + \sqrt{2}) \cos \left[ \frac{1}{4} (c + d x) \right] - \sin \left[ \frac{1}{4} (c + d x) \right]} \right] + \right. \\ \left. 2 \operatorname{Log} \left[ \sqrt{2} + 2 \sin \left[ \frac{1}{2} (c + d x) \right] \right] - \operatorname{Log} \left[ 2 - \sqrt{2} \cos \left[ \frac{1}{2} (c + d x) \right] - \sqrt{2} \sin \left[ \frac{1}{2} (c + d x) \right] \right] - \right. \\ \left. \operatorname{Log} \left[ 2 + \sqrt{2} \cos \left[ \frac{1}{2} (c + d x) \right] - \sqrt{2} \sin \left[ \frac{1}{2} (c + d x) \right] \right] \right) \\ \left. \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right] \sqrt{a (1 + \operatorname{Sec} [c + d x])} \right) / (2 \sqrt{2} d \sqrt{\operatorname{Sec} [c + d x]})$$

**Problem 225: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \operatorname{Sec} [c + d x]^{5/2} (a + a \operatorname{Sec} [c + d x])^{3/2} dx$$

Optimal (type 3, 160 leaves, 6 steps):

$$\frac{11 a^{3/2} \operatorname{ArcSinh} \left[ \frac{\sqrt{a} \operatorname{Tan} [c + d x]}{\sqrt{a + a \operatorname{Sec} [c + d x]}} \right]}{8 d} + \frac{11 a^2 \operatorname{Sec} [c + d x]^{3/2} \operatorname{Sin} [c + d x]}{8 d \sqrt{a + a \operatorname{Sec} [c + d x]}} + \\ \frac{11 a^2 \operatorname{Sec} [c + d x]^{5/2} \operatorname{Sin} [c + d x]}{12 d \sqrt{a + a \operatorname{Sec} [c + d x]}} + \frac{a^2 \operatorname{Sec} [c + d x]^{7/2} \operatorname{Sin} [c + d x]}{3 d \sqrt{a + a \operatorname{Sec} [c + d x]}}$$

Result (type 3, 456 leaves):

$$\frac{1}{384 \sqrt{2} d \sqrt{\sec [c+d x]}} a \sec \left[ \frac{1}{2} (c+d x) \right] \sqrt{a \left( 1 + \sec [c+d x] \right)}$$

$$\left( -264 i \operatorname{ArcTan} \left[ \frac{\cos \left[ \frac{1}{4} (c+d x) \right] - (-1 + \sqrt{2}) \sin \left[ \frac{1}{4} (c+d x) \right]}{(1 + \sqrt{2}) \cos \left[ \frac{1}{4} (c+d x) \right] - \sin \left[ \frac{1}{4} (c+d x) \right]} \right] - \right.$$

$$\left. 264 i \operatorname{ArcTan} \left[ \frac{\cos \left[ \frac{1}{4} (c+d x) \right] - (1 + \sqrt{2}) \sin \left[ \frac{1}{4} (c+d x) \right]}{(-1 + \sqrt{2}) \cos \left[ \frac{1}{4} (c+d x) \right] - \sin \left[ \frac{1}{4} (c+d x) \right]} \right] + \right.$$

$$\left. \sec [c+d x]^3 \left( 99 \cos [c+d x] \left( 2 \operatorname{Log} [\sqrt{2} + 2 \sin \left[ \frac{1}{2} (c+d x) \right]] - \operatorname{Log} [2 - \sqrt{2} \cos \left[ \frac{1}{2} (c+d x) \right] - \right. \right. \right.$$

$$\left. \left. \sqrt{2} \sin \left[ \frac{1}{2} (c+d x) \right] \right] - \operatorname{Log} [2 + \sqrt{2} \cos \left[ \frac{1}{2} (c+d x) \right] - \sqrt{2} \sin \left[ \frac{1}{2} (c+d x) \right]] \right) + \right.$$

$$\left. 33 \cos [3 (c+d x)] \left( 2 \operatorname{Log} [\sqrt{2} + 2 \sin \left[ \frac{1}{2} (c+d x) \right]] - \operatorname{Log} [2 - \sqrt{2} \cos \left[ \frac{1}{2} (c+d x) \right] - \right. \right.$$

$$\left. \left. \sqrt{2} \sin \left[ \frac{1}{2} (c+d x) \right] \right] - \operatorname{Log} [2 + \sqrt{2} \cos \left[ \frac{1}{2} (c+d x) \right] - \sqrt{2} \sin \left[ \frac{1}{2} (c+d x) \right]] \right) + \right.$$

$$\left. 4 \sqrt{2} \left( 54 \sin \left[ \frac{1}{2} (c+d x) \right] + 11 \sin \left[ \frac{3}{2} (c+d x) \right] + 33 \sin \left[ \frac{5}{2} (c+d x) \right] \right) \right)$$

**Problem 226: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \sec [c+d x]^{3/2} (a + a \sec [c+d x])^{3/2} dx$$

Optimal (type 3, 120 leaves, 5 steps):

$$\frac{7 a^{3/2} \operatorname{ArcSinh} \left[ \frac{\sqrt{a} \tan [c+d x]}{\sqrt{a+a \sec [c+d x]}} \right]}{4 d} + \frac{7 a^2 \sec [c+d x]^{3/2} \sin [c+d x]}{4 d \sqrt{a+a \sec [c+d x]}} + \frac{a^2 \sec [c+d x]^{5/2} \sin [c+d x]}{2 d \sqrt{a+a \sec [c+d x]}}$$

Result (type 3, 432 leaves):

$$\begin{aligned}
 & - \frac{1}{32 \sqrt{2} d \sqrt{\text{Sec}[c+dx]}} a \text{Sec}\left[\frac{1}{2}(c+dx)\right] \sqrt{a(1+\text{Sec}[c+dx])} \\
 & \left( 28 i \text{ArcTan}\left[\frac{\text{Cos}\left[\frac{1}{4}(c+dx)\right] - (-1+\sqrt{2}) \text{Sin}\left[\frac{1}{4}(c+dx)\right]}{(1+\sqrt{2}) \text{Cos}\left[\frac{1}{4}(c+dx)\right] - \text{Sin}\left[\frac{1}{4}(c+dx)\right]}\right] + \right. \\
 & 28 i \text{ArcTan}\left[\frac{\text{Cos}\left[\frac{1}{4}(c+dx)\right] - (1+\sqrt{2}) \text{Sin}\left[\frac{1}{4}(c+dx)\right]}{(-1+\sqrt{2}) \text{Cos}\left[\frac{1}{4}(c+dx)\right] - \text{Sin}\left[\frac{1}{4}(c+dx)\right]}\right] + \text{Sec}[c+dx]^2 \\
 & \left. \left( 7 \text{Cos}[2(c+dx)] \left( -2 \text{Log}[\sqrt{2} + 2 \text{Sin}\left[\frac{1}{2}(c+dx)\right]] + \text{Log}[2 - \sqrt{2} \text{Cos}\left[\frac{1}{2}(c+dx)\right] - \right. \right. \right. \\
 & \left. \left. \left. \sqrt{2} \text{Sin}\left[\frac{1}{2}(c+dx)\right]\right] + \text{Log}[2 + \sqrt{2} \text{Cos}\left[\frac{1}{2}(c+dx)\right] - \sqrt{2} \text{Sin}\left[\frac{1}{2}(c+dx)\right]] \right) \right) + \right. \\
 & 12 \sqrt{2} \text{Sin}\left[\frac{1}{2}(c+dx)\right] + 7 \left( -2 \text{Log}[\sqrt{2} + 2 \text{Sin}\left[\frac{1}{2}(c+dx)\right]] + \right. \\
 & \left. \text{Log}[2 - \sqrt{2} \text{Cos}\left[\frac{1}{2}(c+dx)\right] - \sqrt{2} \text{Sin}\left[\frac{1}{2}(c+dx)\right]] + \right. \\
 & \left. \left. \left. \text{Log}[2 + \sqrt{2} \text{Cos}\left[\frac{1}{2}(c+dx)\right] - \sqrt{2} \text{Sin}\left[\frac{1}{2}(c+dx)\right]] - 4 \sqrt{2} \text{Sin}\left[\frac{3}{2}(c+dx)\right] \right) \right) \right)
 \end{aligned}$$

**Problem 227: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \sqrt{\text{Sec}[c+dx]} (a + a \text{Sec}[c+dx])^{3/2} dx$$

Optimal (type 3, 75 leaves, 4 steps):

$$\frac{3 a^{3/2} \text{ArcSinh}\left[\frac{\sqrt{a} \text{Tan}[c+dx]}{\sqrt{a+a \text{Sec}[c+dx]}}\right]}{d} + \frac{a^2 \text{Sec}[c+dx]^{3/2} \text{Sin}[c+dx]}{d \sqrt{a+a \text{Sec}[c+dx]}}$$

Result (type 3, 307 leaves):

$$\begin{aligned}
 & \frac{1}{4 \sqrt{2} d \sqrt{\text{Sec}[c+dx]}} a \text{Sec}\left[\frac{1}{2}(c+dx)\right] \sqrt{a(1+\text{Sec}[c+dx])} \\
 & \left( -6 i \text{ArcTan}\left[\frac{\text{Cos}\left[\frac{1}{4}(c+dx)\right] - (-1+\sqrt{2}) \text{Sin}\left[\frac{1}{4}(c+dx)\right]}{(1+\sqrt{2}) \text{Cos}\left[\frac{1}{4}(c+dx)\right] - \text{Sin}\left[\frac{1}{4}(c+dx)\right]}\right] - \right. \\
 & 6 i \text{ArcTan}\left[\frac{\text{Cos}\left[\frac{1}{4}(c+dx)\right] - (1+\sqrt{2}) \text{Sin}\left[\frac{1}{4}(c+dx)\right]}{(-1+\sqrt{2}) \text{Cos}\left[\frac{1}{4}(c+dx)\right] - \text{Sin}\left[\frac{1}{4}(c+dx)\right]}\right] + \\
 & 6 \text{Log}[\sqrt{2} + 2 \text{Sin}\left[\frac{1}{2}(c+dx)\right]] - 3 \text{Log}[2 - \sqrt{2} \text{Cos}\left[\frac{1}{2}(c+dx)\right] - \sqrt{2} \text{Sin}\left[\frac{1}{2}(c+dx)\right]] - \\
 & \left. \left. \left. 3 \text{Log}[2 + \sqrt{2} \text{Cos}\left[\frac{1}{2}(c+dx)\right] - \sqrt{2} \text{Sin}\left[\frac{1}{2}(c+dx)\right]] + 4 \sqrt{2} \text{Sec}[c+dx] \text{Sin}\left[\frac{1}{2}(c+dx)\right] \right) \right) \right)
 \end{aligned}$$

**Problem 228: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{(a + a \operatorname{Sec}[c + d x])^{3/2}}{\sqrt{\operatorname{Sec}[c + d x]}} dx$$

Optimal (type 3, 76 leaves, 4 steps):

$$\frac{2 a^{3/2} \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c+d x]}{\sqrt{a+a \operatorname{Sec}[c+d x]}}\right]}{d} + \frac{2 a^2 \sqrt{\operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{d \sqrt{a+a \operatorname{Sec}[c+d x]}}$$

Result (type 3, 301 leaves):

$$\begin{aligned} & \frac{1}{2 \sqrt{2} d \sqrt{\operatorname{Sec}[c+d x]}} a \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right] \sqrt{a(1+\operatorname{Sec}[c+d x])} \\ & \left( -2 i \operatorname{ArcTan}\left[\frac{\operatorname{Cos}\left[\frac{1}{4}(c+d x)\right] - (-1+\sqrt{2}) \operatorname{Sin}\left[\frac{1}{4}(c+d x)\right]}{(1+\sqrt{2}) \operatorname{Cos}\left[\frac{1}{4}(c+d x)\right] - \operatorname{Sin}\left[\frac{1}{4}(c+d x)\right]}\right] - \right. \\ & \quad \left. 2 i \operatorname{ArcTan}\left[\frac{\operatorname{Cos}\left[\frac{1}{4}(c+d x)\right] - (1+\sqrt{2}) \operatorname{Sin}\left[\frac{1}{4}(c+d x)\right]}{(-1+\sqrt{2}) \operatorname{Cos}\left[\frac{1}{4}(c+d x)\right] - \operatorname{Sin}\left[\frac{1}{4}(c+d x)\right]}\right] + \right. \\ & \quad \left. 2 \operatorname{Log}\left[\sqrt{2} + 2 \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right] - \operatorname{Log}\left[2 - \sqrt{2} \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] - \sqrt{2} \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right] - \right. \\ & \quad \left. \operatorname{Log}\left[2 + \sqrt{2} \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] - \sqrt{2} \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right] + 4 \sqrt{2} \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] \right) \end{aligned}$$

**Problem 233: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \operatorname{Sec}[c+d x]^{5/2} (a + a \operatorname{Sec}[c+d x])^{5/2} dx$$

Optimal (type 3, 200 leaves, 6 steps):

$$\begin{aligned} & \frac{163 a^{5/2} \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c+d x]}{\sqrt{a+a \operatorname{Sec}[c+d x]}}\right]}{64 d} + \frac{163 a^3 \operatorname{Sec}[c+d x]^{3/2} \operatorname{Sin}[c+d x]}{64 d \sqrt{a+a \operatorname{Sec}[c+d x]}} + \\ & \frac{163 a^3 \operatorname{Sec}[c+d x]^{5/2} \operatorname{Sin}[c+d x]}{96 d \sqrt{a+a \operatorname{Sec}[c+d x]}} + \frac{17 a^3 \operatorname{Sec}[c+d x]^{7/2} \operatorname{Sin}[c+d x]}{24 d \sqrt{a+a \operatorname{Sec}[c+d x]}} + \\ & \frac{a^2 \operatorname{Sec}[c+d x]^{7/2} \sqrt{a+a \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{4 d} \end{aligned}$$

Result (type 3, 582 leaves):

$$\begin{aligned}
 & - \frac{1}{6144 \sqrt{2} d \sqrt{\sec [c+d x]}} a^2 \sec \left[ \frac{1}{2} (c+d x) \right] \sqrt{a (1+\sec [c+d x])} \\
 & \left( 7824 \operatorname{ArcTan} \left[ \frac{\cos \left[ \frac{1}{4} (c+d x) \right] - (-1+\sqrt{2}) \sin \left[ \frac{1}{4} (c+d x) \right]}{(1+\sqrt{2}) \cos \left[ \frac{1}{4} (c+d x) \right] - \sin \left[ \frac{1}{4} (c+d x) \right]} \right] + \right. \\
 & 7824 \operatorname{ArcTan} \left[ \frac{\cos \left[ \frac{1}{4} (c+d x) \right] - (1+\sqrt{2}) \sin \left[ \frac{1}{4} (c+d x) \right]}{(-1+\sqrt{2}) \cos \left[ \frac{1}{4} (c+d x) \right] - \sin \left[ \frac{1}{4} (c+d x) \right]} \right] + \\
 & \sec [c+d x]^4 \left( -2934 \operatorname{Log} \left[ \sqrt{2} + 2 \sin \left[ \frac{1}{2} (c+d x) \right] \right] + \right. \\
 & 1467 \operatorname{Log} \left[ 2 - \sqrt{2} \cos \left[ \frac{1}{2} (c+d x) \right] - \sqrt{2} \sin \left[ \frac{1}{2} (c+d x) \right] \right] - 1956 \cos [2 (c+d x)] \\
 & \left( 2 \operatorname{Log} \left[ \sqrt{2} + 2 \sin \left[ \frac{1}{2} (c+d x) \right] \right] - \operatorname{Log} \left[ 2 - \sqrt{2} \cos \left[ \frac{1}{2} (c+d x) \right] - \sqrt{2} \sin \left[ \frac{1}{2} (c+d x) \right] \right] - \right. \\
 & \left. \operatorname{Log} \left[ 2 + \sqrt{2} \cos \left[ \frac{1}{2} (c+d x) \right] - \sqrt{2} \sin \left[ \frac{1}{2} (c+d x) \right] \right] \right) - 489 \cos [4 (c+d x)] \\
 & \left( 2 \operatorname{Log} \left[ \sqrt{2} + 2 \sin \left[ \frac{1}{2} (c+d x) \right] \right] - \operatorname{Log} \left[ 2 - \sqrt{2} \cos \left[ \frac{1}{2} (c+d x) \right] - \sqrt{2} \sin \left[ \frac{1}{2} (c+d x) \right] \right] - \right. \\
 & \left. \operatorname{Log} \left[ 2 + \sqrt{2} \cos \left[ \frac{1}{2} (c+d x) \right] - \sqrt{2} \sin \left[ \frac{1}{2} (c+d x) \right] \right] \right) + \\
 & 1467 \operatorname{Log} \left[ 2 + \sqrt{2} \cos \left[ \frac{1}{2} (c+d x) \right] - \sqrt{2} \sin \left[ \frac{1}{2} (c+d x) \right] \right] + 2060 \sqrt{2} \sin \left[ \frac{1}{2} (c+d x) \right] - \\
 & \left. \left. 6204 \sqrt{2} \sin \left[ \frac{3}{2} (c+d x) \right] - 652 \sqrt{2} \sin \left[ \frac{5}{2} (c+d x) \right] - 1956 \sqrt{2} \sin \left[ \frac{7}{2} (c+d x) \right] \right) \right)
 \end{aligned}$$

**Problem 234: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \sec [c+d x]^{3/2} (a+a \sec [c+d x])^{5/2} dx$$

Optimal (type 3, 160 leaves, 5 steps):

$$\begin{aligned}
 & \frac{25 a^{5/2} \operatorname{ArcSinh} \left[ \frac{\sqrt{a} \tan [c+d x]}{\sqrt{a+a \sec [c+d x]}} \right]}{8 d} + \frac{25 a^3 \sec [c+d x]^{3/2} \sin [c+d x]}{8 d \sqrt{a+a \sec [c+d x]}} + \\
 & \frac{13 a^3 \sec [c+d x]^{5/2} \sin [c+d x]}{12 d \sqrt{a+a \sec [c+d x]}} + \frac{a^2 \sec [c+d x]^{5/2} \sqrt{a+a \sec [c+d x]} \sin [c+d x]}{3 d}
 \end{aligned}$$

Result (type 3, 458 leaves):



$$\begin{aligned}
 & \frac{1}{384 \sqrt{2} d \sqrt{\sec [c+d x]}} a^2 \sec \left[ \frac{1}{2} (c+d x) \right] \sqrt{a \left( 1 + \sec [c+d x] \right)} \\
 & \left( -600 i \operatorname{ArcTan} \left[ \frac{\cos \left[ \frac{1}{4} (c+d x) \right] - (-1 + \sqrt{2}) \sin \left[ \frac{1}{4} (c+d x) \right]}{(1 + \sqrt{2}) \cos \left[ \frac{1}{4} (c+d x) \right] - \sin \left[ \frac{1}{4} (c+d x) \right]} \right] - \right. \\
 & \left. 600 i \operatorname{ArcTan} \left[ \frac{\cos \left[ \frac{1}{4} (c+d x) \right] - (1 + \sqrt{2}) \sin \left[ \frac{1}{4} (c+d x) \right]}{(-1 + \sqrt{2}) \cos \left[ \frac{1}{4} (c+d x) \right] - \sin \left[ \frac{1}{4} (c+d x) \right]} \right] + \right. \\
 & \left. \sec [c+d x]^3 \left( 225 \cos [c+d x] \left( 2 \log [\sqrt{2} + 2 \sin \left[ \frac{1}{2} (c+d x) \right]] - \log [2 - \sqrt{2} \cos \left[ \frac{1}{2} (c+d x) \right]] - \right. \right. \right. \\
 & \quad \left. \left. \sqrt{2} \sin \left[ \frac{1}{2} (c+d x) \right] \right) - \log [2 + \sqrt{2} \cos \left[ \frac{1}{2} (c+d x) \right]] - \sqrt{2} \sin \left[ \frac{1}{2} (c+d x) \right] \right) + \right. \\
 & \quad \left. 75 \cos [3 (c+d x)] \left( 2 \log [\sqrt{2} + 2 \sin \left[ \frac{1}{2} (c+d x) \right]] - \log [2 - \sqrt{2} \cos \left[ \frac{1}{2} (c+d x) \right]] - \right. \right. \\
 & \quad \left. \left. \sqrt{2} \sin \left[ \frac{1}{2} (c+d x) \right] \right) - \log [2 + \sqrt{2} \cos \left[ \frac{1}{2} (c+d x) \right]] - \sqrt{2} \sin \left[ \frac{1}{2} (c+d x) \right] \right) + \right. \\
 & \quad \left. \left. 4 \sqrt{2} \left( 114 \sin \left[ \frac{1}{2} (c+d x) \right] - 7 \sin \left[ \frac{3}{2} (c+d x) \right] + 75 \sin \left[ \frac{5}{2} (c+d x) \right] \right) \right) \right)
 \end{aligned}$$

**Problem 235: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \sqrt{\sec [c+d x]} (a + a \sec [c+d x])^{5/2} dx$$

Optimal (type 3, 120 leaves, 4 steps):

$$\begin{aligned}
 & \frac{19 a^{5/2} \operatorname{ArcSinh} \left[ \frac{\sqrt{a} \tan [c+d x]}{\sqrt{a+a \sec [c+d x]}} \right]}{4 d} + \frac{9 a^3 \sec [c+d x]^{3/2} \sin [c+d x]}{4 d \sqrt{a+a \sec [c+d x]}} + \\
 & \frac{a^2 \sec [c+d x]^{3/2} \sqrt{a+a \sec [c+d x]} \sin [c+d x]}{2 d}
 \end{aligned}$$

Result (type 3, 435 leaves):

$$\begin{aligned}
& - \frac{1}{32 \sqrt{2} d \sqrt{\text{Sec}[c+dx]}} a^2 \text{Sec}\left[\frac{1}{2}(c+dx)\right] \sqrt{a(1+\text{Sec}[c+dx])} \\
& \left( 76 i \text{ArcTan}\left[\frac{\text{Cos}\left[\frac{1}{4}(c+dx)\right] - (-1+\sqrt{2}) \text{Sin}\left[\frac{1}{4}(c+dx)\right]}{(1+\sqrt{2}) \text{Cos}\left[\frac{1}{4}(c+dx)\right] - \text{Sin}\left[\frac{1}{4}(c+dx)\right]}\right] + \right. \\
& 76 i \text{ArcTan}\left[\frac{\text{Cos}\left[\frac{1}{4}(c+dx)\right] - (1+\sqrt{2}) \text{Sin}\left[\frac{1}{4}(c+dx)\right]}{(-1+\sqrt{2}) \text{Cos}\left[\frac{1}{4}(c+dx)\right] - \text{Sin}\left[\frac{1}{4}(c+dx)\right]}\right] + \\
& \text{Sec}[c+dx]^2 \left( -38 \text{Log}\left[\sqrt{2} + 2 \text{Sin}\left[\frac{1}{2}(c+dx)\right]\right] + 19 \text{Log}\left[2 - \sqrt{2} \text{Cos}\left[\frac{1}{2}(c+dx)\right] - \right. \\
& \left. \sqrt{2} \text{Sin}\left[\frac{1}{2}(c+dx)\right]\right] + 19 \text{Log}\left[2 + \sqrt{2} \text{Cos}\left[\frac{1}{2}(c+dx)\right] - \sqrt{2} \text{Sin}\left[\frac{1}{2}(c+dx)\right]\right] + \\
& 19 \text{Cos}\left[2(c+dx)\right] \left( -2 \text{Log}\left[\sqrt{2} + 2 \text{Sin}\left[\frac{1}{2}(c+dx)\right]\right] + \text{Log}\left[2 - \sqrt{2} \text{Cos}\left[\frac{1}{2}(c+dx)\right] - \right. \\
& \left. \sqrt{2} \text{Sin}\left[\frac{1}{2}(c+dx)\right]\right] + \text{Log}\left[2 + \sqrt{2} \text{Cos}\left[\frac{1}{2}(c+dx)\right] - \sqrt{2} \text{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \right) + \\
& \left. \left. 28 \sqrt{2} \text{Sin}\left[\frac{1}{2}(c+dx)\right] - 44 \sqrt{2} \text{Sin}\left[\frac{3}{2}(c+dx)\right] \right) \right)
\end{aligned}$$

**Problem 236: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{(a + a \text{Sec}[c+dx])^{5/2}}{\sqrt{\text{Sec}[c+dx]}} dx$$

Optimal (type 3, 112 leaves, 4 steps):

$$\frac{5 a^{5/2} \text{ArcSinh}\left[\frac{-\sqrt{a} \text{Tan}[c+dx]}{\sqrt{a+a \text{Sec}[c+dx]}}\right]}{d} + \frac{a^3 \sqrt{\text{Sec}[c+dx]} \text{Sin}[c+dx]}{d \sqrt{a+a \text{Sec}[c+dx]}} + \frac{a^2 \sqrt{\text{Sec}[c+dx]} \sqrt{a+a \text{Sec}[c+dx]} \text{Sin}[c+dx]}{d}$$

Result (type 3, 309 leaves):

$$\frac{1}{4\sqrt{2}d\sqrt{\sec[c+dx]}} a^2 \sec\left[\frac{1}{2}(c+dx)\right] \sqrt{a(1+\sec[c+dx])} \left( -10i \operatorname{ArcTan}\left[\frac{\cos\left[\frac{1}{4}(c+dx)\right] - (-1+\sqrt{2})\sin\left[\frac{1}{4}(c+dx)\right]}{(1+\sqrt{2})\cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]}\right] - 10i \operatorname{ArcTan}\left[\frac{\cos\left[\frac{1}{4}(c+dx)\right] - (1+\sqrt{2})\sin\left[\frac{1}{4}(c+dx)\right]}{(-1+\sqrt{2})\cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]}\right] + 10 \operatorname{Log}\left[\sqrt{2} + 2\sin\left[\frac{1}{2}(c+dx)\right]\right] - 5 \operatorname{Log}\left[2 - \sqrt{2}\cos\left[\frac{1}{2}(c+dx)\right] - \sqrt{2}\sin\left[\frac{1}{2}(c+dx)\right]\right] - 5 \operatorname{Log}\left[2 + \sqrt{2}\cos\left[\frac{1}{2}(c+dx)\right] - \sqrt{2}\sin\left[\frac{1}{2}(c+dx)\right]\right] + 4\sqrt{2}\sec[c+dx]\sin\left[\frac{3}{2}(c+dx)\right] \right)$$

**Problem 237: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{(a + a \sec[c + dx])^{5/2}}{\sec[c + dx]^{3/2}} dx$$

Optimal (type 3, 118 leaves, 4 steps):

$$\frac{2a^{5/2} \operatorname{ArcSinh}\left[\frac{\sqrt{a} \tan[c+dx]}{\sqrt{a+a\sec[c+dx]}}\right]}{d} + \frac{14a^3 \sqrt{\sec[c+dx]} \sin[c+dx]}{3d\sqrt{a+a\sec[c+dx]}} + \frac{2a^2 \sqrt{a+a\sec[c+dx]} \sin[c+dx]}{3d\sqrt{\sec[c+dx]}}$$

Result (type 3, 320 leaves):

$$\frac{1}{6\sqrt{2}d\sqrt{\sec[c+dx]}} a^2 \sec\left[\frac{1}{2}(c+dx)\right] \sqrt{a(1+\sec[c+dx])} \left( -6i \operatorname{ArcTan}\left[\frac{\cos\left[\frac{1}{4}(c+dx)\right] - (-1+\sqrt{2})\sin\left[\frac{1}{4}(c+dx)\right]}{(1+\sqrt{2})\cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]}\right] - 6i \operatorname{ArcTan}\left[\frac{\cos\left[\frac{1}{4}(c+dx)\right] - (1+\sqrt{2})\sin\left[\frac{1}{4}(c+dx)\right]}{(-1+\sqrt{2})\cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]}\right] + 6 \operatorname{Log}\left[\sqrt{2} + 2\sin\left[\frac{1}{2}(c+dx)\right]\right] - 3 \operatorname{Log}\left[2 - \sqrt{2}\cos\left[\frac{1}{2}(c+dx)\right] - \sqrt{2}\sin\left[\frac{1}{2}(c+dx)\right]\right] - 3 \operatorname{Log}\left[2 + \sqrt{2}\cos\left[\frac{1}{2}(c+dx)\right] - \sqrt{2}\sin\left[\frac{1}{2}(c+dx)\right]\right] + 30\sqrt{2}\sin\left[\frac{1}{2}(c+dx)\right] + 2\sqrt{2}\sin\left[\frac{3}{2}(c+dx)\right] \right)$$

**Problem 243: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \sqrt{\sec[e+fx]} \sqrt{a+a \sec[e+fx]} dx$$

Optimal (type 3, 37 leaves, 2 steps):

$$\frac{2 \sqrt{a} \operatorname{ArcSinh}\left[\frac{\sqrt{a} \tan[e+fx]}{\sqrt{a+a \sec[e+fx]}}\right]}{f}$$

Result (type 3, 283 leaves):

$$\left( \left( -2 i \operatorname{ArcTan}\left[ \frac{\cos\left[\frac{1}{4}(e+fx)\right] - (-1+\sqrt{2}) \sin\left[\frac{1}{4}(e+fx)\right]}{(1+\sqrt{2}) \cos\left[\frac{1}{4}(e+fx)\right] - \sin\left[\frac{1}{4}(e+fx)\right]} \right] - \right. \right. \\ \left. \left. 2 i \operatorname{ArcTan}\left[ \frac{\cos\left[\frac{1}{4}(e+fx)\right] - (1+\sqrt{2}) \sin\left[\frac{1}{4}(e+fx)\right]}{(-1+\sqrt{2}) \cos\left[\frac{1}{4}(e+fx)\right] - \sin\left[\frac{1}{4}(e+fx)\right]} \right] + \right. \right. \\ \left. \left. 2 \operatorname{Log}\left[\sqrt{2} + 2 \sin\left[\frac{1}{2}(e+fx)\right]\right] - \operatorname{Log}\left[2 - \sqrt{2} \cos\left[\frac{1}{2}(e+fx)\right] - \sqrt{2} \sin\left[\frac{1}{2}(e+fx)\right]\right] - \right. \right. \\ \left. \left. \operatorname{Log}\left[2 + \sqrt{2} \cos\left[\frac{1}{2}(e+fx)\right] - \sqrt{2} \sin\left[\frac{1}{2}(e+fx)\right]\right] \right) \right) \\ \left. \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right] \sqrt{a(1+\sec[e+fx])} \right) / (2 \sqrt{2} f \sqrt{\sec[e+fx]})$$

**Problem 244: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \sqrt{-\sec[e+fx]} \sqrt{a-a \sec[e+fx]} dx$$

Optimal (type 3, 38 leaves, 2 steps):

$$\frac{2 \sqrt{a} \operatorname{ArcSinh}\left[\frac{\sqrt{a} \tan[e+fx]}{\sqrt{a-a \sec[e+fx]}}\right]}{f}$$

Result (type 3, 299 leaves):

$$\frac{1}{2\sqrt{2} f \sqrt{-\text{Sec}[e + f x]}}$$

$$\text{Csc}\left[\frac{1}{2}(e + f x)\right] \left( -2 \text{i ArcTan}\left[\frac{\text{Cos}\left[\frac{1}{4}(e + f x)\right] - (-1 + \sqrt{2}) \text{Sin}\left[\frac{1}{4}(e + f x)\right]}{(1 + \sqrt{2}) \text{Cos}\left[\frac{1}{4}(e + f x)\right] - \text{Sin}\left[\frac{1}{4}(e + f x)\right]}\right] + \right.$$

$$\left. 2 \text{i ArcTan}\left[\frac{\text{Cos}\left[\frac{1}{4}(e + f x)\right] - (1 + \sqrt{2}) \text{Sin}\left[\frac{1}{4}(e + f x)\right]}{(-1 + \sqrt{2}) \text{Cos}\left[\frac{1}{4}(e + f x)\right] - \text{Sin}\left[\frac{1}{4}(e + f x)\right]}\right] - \right.$$

$$4 \text{ArcTanh}\left[\sqrt{2} \text{Cos}\left[\frac{1}{4}(2e + f x)\right] \text{Sec}\left[\frac{f x}{4}\right] + \text{Tan}\left[\frac{f x}{4}\right]\right] +$$

$$\text{Log}\left[2 - \sqrt{2} \text{Cos}\left[\frac{1}{2}(e + f x)\right] - \sqrt{2} \text{Sin}\left[\frac{1}{2}(e + f x)\right]\right] -$$

$$\left. \text{Log}\left[2 + \sqrt{2} \text{Cos}\left[\frac{1}{2}(e + f x)\right] - \sqrt{2} \text{Sin}\left[\frac{1}{2}(e + f x)\right]\right] \right) \sqrt{a - a \text{Sec}[e + f x]}$$

**Problem 245: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\text{Sec}[c + d x]^{5/2}}{\sqrt{a + a \text{Sec}[c + d x]}} dx$$

Optimal (type 3, 128 leaves, 6 steps):

$$-\frac{\text{ArcSinh}\left[\frac{\sqrt{a} \text{Tan}[c + d x]}{\sqrt{a + a \text{Sec}[c + d x]}}\right]}{\sqrt{a} d} + \frac{\sqrt{2} \text{ArcTanh}\left[\frac{\sqrt{a} \sqrt{\text{Sec}[c + d x]} \text{Sin}[c + d x]}{\sqrt{2} \sqrt{a + a \text{Sec}[c + d x]}}\right]}{\sqrt{a} d} + \frac{\text{Sec}[c + d x]^{3/2} \text{Sin}[c + d x]}{d \sqrt{a + a \text{Sec}[c + d x]}}$$

Result (type 3, 362 leaves):

$$\frac{1}{2\sqrt{2} d \sqrt{a(1 + \text{Sec}[c + d x])}}$$

$$\text{Cos}\left[\frac{1}{2}(c + d x)\right] \sqrt{\text{Sec}[c + d x]} \left( 2 \text{i ArcTan}\left[\frac{\text{Cos}\left[\frac{1}{4}(c + d x)\right] - (-1 + \sqrt{2}) \text{Sin}\left[\frac{1}{4}(c + d x)\right]}{(1 + \sqrt{2}) \text{Cos}\left[\frac{1}{4}(c + d x)\right] - \text{Sin}\left[\frac{1}{4}(c + d x)\right]}\right] + \right.$$

$$\left. 2 \text{i ArcTan}\left[\frac{\text{Cos}\left[\frac{1}{4}(c + d x)\right] - (1 + \sqrt{2}) \text{Sin}\left[\frac{1}{4}(c + d x)\right]}{(-1 + \sqrt{2}) \text{Cos}\left[\frac{1}{4}(c + d x)\right] - \text{Sin}\left[\frac{1}{4}(c + d x)\right]}\right] - 4 \sqrt{2} \right.$$

$$\text{Log}\left[\text{Cos}\left[\frac{1}{4}(c + d x)\right] - \text{Sin}\left[\frac{1}{4}(c + d x)\right]\right] + 4 \sqrt{2} \text{Log}\left[\text{Cos}\left[\frac{1}{4}(c + d x)\right] + \text{Sin}\left[\frac{1}{4}(c + d x)\right]\right] -$$

$$2 \text{Log}\left[\sqrt{2} + 2 \text{Sin}\left[\frac{1}{2}(c + d x)\right]\right] + \text{Log}\left[2 - \sqrt{2} \text{Cos}\left[\frac{1}{2}(c + d x)\right] - \sqrt{2} \text{Sin}\left[\frac{1}{2}(c + d x)\right]\right] +$$

$$\left. \text{Log}\left[2 + \sqrt{2} \text{Cos}\left[\frac{1}{2}(c + d x)\right] - \sqrt{2} \text{Sin}\left[\frac{1}{2}(c + d x)\right]\right] + 4 \sqrt{2} \text{Sec}[c + d x] \text{Sin}\left[\frac{1}{2}(c + d x)\right] \right)$$

**Problem 246:** Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\text{Sec}[c + d x]^{3/2}}{\sqrt{a + a \text{Sec}[c + d x]}} dx$$

Optimal (type 3, 95 leaves, 5 steps):

$$\frac{2 \text{ArcSinh}\left[\frac{\sqrt{a} \text{Tan}[c+dx]}{\sqrt{a+a \text{Sec}[c+dx]}}\right]}{\sqrt{a} d} - \frac{\sqrt{2} \text{ArcTanh}\left[\frac{\sqrt{a} \sqrt{\text{Sec}[c+dx]} \text{Sin}[c+dx]}{\sqrt{2} \sqrt{a+a \text{Sec}[c+dx]}}\right]}{\sqrt{a} d}$$

Result (type 3, 394 leaves):

$$\frac{1}{((-1 + i) + \sqrt{2}) d \sqrt{a} (1 + \text{Sec}[c + d x])} \left( \frac{1}{2} + \frac{i}{2} \right) \text{Cos}\left[\frac{1}{2} (c + d x)\right] \\ \left( 2 \left( (-1 - i) + \sqrt{2} \right) \text{ArcTan}\left[\frac{\text{Cos}\left[\frac{1}{4} (c + d x)\right] - (-1 + \sqrt{2}) \text{Sin}\left[\frac{1}{4} (c + d x)\right]}{(1 + \sqrt{2}) \text{Cos}\left[\frac{1}{4} (c + d x)\right] - \text{Sin}\left[\frac{1}{4} (c + d x)\right]}\right] + \right. \\ \left. 2 \left( (-1 - i) + \sqrt{2} \right) \text{ArcTan}\left[\frac{\text{Cos}\left[\frac{1}{4} (c + d x)\right] - (1 + \sqrt{2}) \text{Sin}\left[\frac{1}{4} (c + d x)\right]}{(-1 + \sqrt{2}) \text{Cos}\left[\frac{1}{4} (c + d x)\right] - \text{Sin}\left[\frac{1}{4} (c + d x)\right]}\right] - \right. \\ \left. i \left( (-4 + (2 + 2 i) \sqrt{2}) \text{Log}\left[\text{Cos}\left[\frac{1}{4} (c + d x)\right] - \text{Sin}\left[\frac{1}{4} (c + d x)\right]\right] + \right. \right. \\ \left. \left. (4 - (2 + 2 i) \sqrt{2}) \text{Log}\left[\text{Cos}\left[\frac{1}{4} (c + d x)\right] + \text{Sin}\left[\frac{1}{4} (c + d x)\right]\right] - ((-1 - i) + \sqrt{2}) \right. \right. \\ \left. \left. \left( 2 \text{Log}\left[\sqrt{2} + 2 \text{Sin}\left[\frac{1}{2} (c + d x)\right]\right] - \text{Log}\left[2 - \sqrt{2} \text{Cos}\left[\frac{1}{2} (c + d x)\right] - \sqrt{2} \text{Sin}\left[\frac{1}{2} (c + d x)\right]\right] - \right. \right. \\ \left. \left. \left. \left. \text{Log}\left[2 + \sqrt{2} \text{Cos}\left[\frac{1}{2} (c + d x)\right] - \sqrt{2} \text{Sin}\left[\frac{1}{2} (c + d x)\right]\right]\right] \right) \right) \right) \sqrt{\text{Sec}[c + d x]}$$

**Problem 251:** Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\text{Sec}[c + d x]^{7/2}}{(a + a \text{Sec}[c + d x])^{3/2}} dx$$

Optimal (type 3, 174 leaves, 7 steps):

$$\frac{3 \text{ArcSinh}\left[\frac{\sqrt{a} \text{Tan}[c+dx]}{\sqrt{a+a \text{Sec}[c+dx]}}\right]}{a^{3/2} d} + \frac{9 \text{ArcTanh}\left[\frac{\sqrt{a} \sqrt{\text{Sec}[c+dx]} \text{Sin}[c+dx]}{\sqrt{2} \sqrt{a+a \text{Sec}[c+dx]}}\right]}{2 \sqrt{2} a^{3/2} d} \\ \frac{\text{Sec}[c + d x]^{5/2} \text{Sin}[c + d x]}{2 d (a + a \text{Sec}[c + d x])^{3/2}} + \frac{3 \text{Sec}[c + d x]^{3/2} \text{Sin}[c + d x]}{2 a d \sqrt{a + a \text{Sec}[c + d x]}}$$

Result (type 3, 457 leaves):

$$\frac{1}{2 d (a (1 + \operatorname{Sec}[c + d x]))^{3/2}} \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right]^3 \operatorname{Sec}[c + d x]^{3/2} \left( 6 \sqrt{2} \operatorname{ArcTan}\left[\frac{\operatorname{Cos}\left[\frac{1}{4}(c + d x)\right] - (-1 + \sqrt{2}) \operatorname{Sin}\left[\frac{1}{4}(c + d x)\right]}{(1 + \sqrt{2}) \operatorname{Cos}\left[\frac{1}{4}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{4}(c + d x)\right]}\right] + 6 \sqrt{2} \operatorname{ArcTan}\left[\frac{\operatorname{Cos}\left[\frac{1}{4}(c + d x)\right] - (1 + \sqrt{2}) \operatorname{Sin}\left[\frac{1}{4}(c + d x)\right]}{(-1 + \sqrt{2}) \operatorname{Cos}\left[\frac{1}{4}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{4}(c + d x)\right]}\right] - 18 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{4}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{4}(c + d x)\right]\right] + 18 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{4}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{4}(c + d x)\right]\right] - 6 \sqrt{2} \operatorname{Log}\left[\sqrt{2} + 2 \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] + 3 \sqrt{2} \operatorname{Log}\left[2 - \sqrt{2} \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \sqrt{2} \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] + 3 \sqrt{2} \operatorname{Log}\left[2 + \sqrt{2} \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \sqrt{2} \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] + \frac{1}{\left(\operatorname{Cos}\left[\frac{1}{4}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{4}(c + d x)\right]\right)^2} - \frac{1}{\left(\operatorname{Cos}\left[\frac{1}{4}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{4}(c + d x)\right]\right)^2} + \frac{4}{\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]} - \frac{4}{\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]} \right)$$

**Problem 252: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec}[c + d x]^{5/2}}{(a + a \operatorname{Sec}[c + d x])^{3/2}} dx$$

Optimal (type 3, 134 leaves, 6 steps):

$$\frac{2 \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c + d x]}{\sqrt{a + a \operatorname{Sec}[c + d x]}}\right]}{a^{3/2} d} - \frac{5 \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{\operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{\sqrt{2} \sqrt{a + a \operatorname{Sec}[c + d x]}}\right]}{2 \sqrt{2} a^{3/2} d} - \frac{\operatorname{Sec}[c + d x]^{3/2} \operatorname{Sin}[c + d x]}{2 d (a + a \operatorname{Sec}[c + d x])^{3/2}}$$

Result (type 3, 437 leaves):

$$\frac{1}{2 d (a (1 + \sec [c + d x]))^{3/2}} \cos \left[ \frac{1}{2} (c + d x) \right]^3 \sec [c + d x]^{3/2}$$

$$\left( \frac{(4 + 4 i) \left( (-1 - i) + \sqrt{2} \right) \operatorname{ArcTan} \left[ \frac{\cos \left[ \frac{1}{4} (c + d x) \right] - (-1 + \sqrt{2}) \sin \left[ \frac{1}{4} (c + d x) \right]}{(1 + \sqrt{2}) \cos \left[ \frac{1}{4} (c + d x) \right] - \sin \left[ \frac{1}{4} (c + d x) \right]} \right)}{(-1 + i) + \sqrt{2}} - \right.$$

$$4 i \sqrt{2} \operatorname{ArcTan} \left[ \frac{\cos \left[ \frac{1}{4} (c + d x) \right] - (1 + \sqrt{2}) \sin \left[ \frac{1}{4} (c + d x) \right]}{(-1 + \sqrt{2}) \cos \left[ \frac{1}{4} (c + d x) \right] - \sin \left[ \frac{1}{4} (c + d x) \right]} \right] +$$

$$10 \operatorname{Log} \left[ \cos \left[ \frac{1}{4} (c + d x) \right] - \sin \left[ \frac{1}{4} (c + d x) \right] \right] -$$

$$10 \operatorname{Log} \left[ \cos \left[ \frac{1}{4} (c + d x) \right] + \sin \left[ \frac{1}{4} (c + d x) \right] \right] + 4 \sqrt{2} \operatorname{Log} \left[ \sqrt{2} + 2 \sin \left[ \frac{1}{2} (c + d x) \right] \right] -$$

$$2 \sqrt{2} \operatorname{Log} \left[ 2 - \sqrt{2} \cos \left[ \frac{1}{2} (c + d x) \right] - \sqrt{2} \sin \left[ \frac{1}{2} (c + d x) \right] \right] + \frac{1}{(-1 + i) + \sqrt{2}}$$

$$(2 - 2 i) \left( (-1 - i) + \sqrt{2} \right) \operatorname{Log} \left[ 2 + \sqrt{2} \cos \left[ \frac{1}{2} (c + d x) \right] - \sqrt{2} \sin \left[ \frac{1}{2} (c + d x) \right] \right] -$$

$$\left. \frac{1}{\left( \cos \left[ \frac{1}{4} (c + d x) \right] - \sin \left[ \frac{1}{4} (c + d x) \right] \right)^2} + \frac{1}{\left( \cos \left[ \frac{1}{4} (c + d x) \right] + \sin \left[ \frac{1}{4} (c + d x) \right] \right)^2} \right)$$

**Problem 258: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\sec [c + d x]^{9/2}}{(a + a \sec [c + d x])^{5/2}} dx$$

Optimal (type 3, 214 leaves, 8 steps):

$$-\frac{5 \operatorname{ArcSinh} \left[ \frac{\sqrt{a} \tan [c + d x]}{\sqrt{a + a \sec [c + d x]}} \right]}{a^{5/2} d} + \frac{115 \operatorname{ArcTanh} \left[ \frac{\sqrt{a} \sqrt{\sec [c + d x]} \sin [c + d x]}{\sqrt{2} \sqrt{a + a \sec [c + d x]}} \right]}{16 \sqrt{2} a^{5/2} d} -$$

$$\frac{\sec [c + d x]^{7/2} \sin [c + d x]}{4 d (a + a \sec [c + d x])^{5/2}} - \frac{15 \sec [c + d x]^{5/2} \sin [c + d x]}{16 a d (a + a \sec [c + d x])^{3/2}} + \frac{35 \sec [c + d x]^{3/2} \sin [c + d x]}{16 a^2 d \sqrt{a + a \sec [c + d x]}}$$

Result (type 3, 1042 leaves):

$$\left( 10 i \sqrt{2} \operatorname{ArcTan} \left[ \frac{\cos \left[ \frac{1}{4} (c + d x) \right] - \sin \left[ \frac{1}{4} (c + d x) \right] - \sqrt{2} \sin \left[ \frac{1}{4} (c + d x) \right]}{-\cos \left[ \frac{1}{4} (c + d x) \right] + \sqrt{2} \cos \left[ \frac{1}{4} (c + d x) \right] - \sin \left[ \frac{1}{4} (c + d x) \right]} \right] \right.$$

$$\left. \cos \left[ \frac{1}{2} (c + d x) \right]^5 \sec [c + d x]^{5/2} \right) / (d (a (1 + \sec [c + d x]))^{5/2}) +$$



$$\begin{aligned}
 & \left( 10 i \sqrt{2} \operatorname{ArcTan} \left[ \frac{\cos \left[ \frac{1}{4} (c+dx) \right] + \sin \left[ \frac{1}{4} (c+dx) \right] - \sqrt{2} \sin \left[ \frac{1}{4} (c+dx) \right]}{\cos \left[ \frac{1}{4} (c+dx) \right] + \sqrt{2} \cos \left[ \frac{1}{4} (c+dx) \right] - \sin \left[ \frac{1}{4} (c+dx) \right]} \right] \right. \\
 & \quad \left. \cos \left[ \frac{1}{2} (c+dx) \right]^5 \operatorname{Sec}[c+dx]^{5/2} \right) / \left( d (a (1 + \operatorname{Sec}[c+dx]))^{5/2} \right) - \\
 & \left( 115 \cos \left[ \frac{1}{2} (c+dx) \right]^5 \operatorname{Log} \left[ \cos \left[ \frac{1}{4} (c+dx) \right] - \sin \left[ \frac{1}{4} (c+dx) \right] \right] \operatorname{Sec}[c+dx]^{5/2} \right) / \\
 & \quad \left( 4 d (a (1 + \operatorname{Sec}[c+dx]))^{5/2} \right) + \\
 & \left( 115 \cos \left[ \frac{1}{2} (c+dx) \right]^5 \operatorname{Log} \left[ \cos \left[ \frac{1}{4} (c+dx) \right] + \sin \left[ \frac{1}{4} (c+dx) \right] \right] \operatorname{Sec}[c+dx]^{5/2} \right) / \\
 & \quad \left( 4 d (a (1 + \operatorname{Sec}[c+dx]))^{5/2} \right) - \\
 & \frac{40 i \cos \left[ \frac{1}{2} (c+dx) \right]^5 \operatorname{Log} \left[ \sqrt{2} + 2 \sin \left[ \frac{1}{2} (c+dx) \right] \right] \operatorname{Sec}[c+dx]^{5/2}}{\left( (-1+i) + \sqrt{2} \right) \left( (1+i) + \sqrt{2} \right) d (a (1 + \operatorname{Sec}[c+dx]))^{5/2}} + \\
 & \left( 5 \sqrt{2} \cos \left[ \frac{1}{2} (c+dx) \right]^5 \operatorname{Log} \left[ 2 - \sqrt{2} \cos \left[ \frac{1}{2} (c+dx) \right] - \sqrt{2} \sin \left[ \frac{1}{2} (c+dx) \right] \right] \operatorname{Sec}[c+dx]^{5/2} \right) / \\
 & \quad \left( d (a (1 + \operatorname{Sec}[c+dx]))^{5/2} \right) + \\
 & \left( 5 \sqrt{2} \cos \left[ \frac{1}{2} (c+dx) \right]^5 \operatorname{Log} \left[ 2 + \sqrt{2} \cos \left[ \frac{1}{2} (c+dx) \right] - \sqrt{2} \sin \left[ \frac{1}{2} (c+dx) \right] \right] \operatorname{Sec}[c+dx]^{5/2} \right) / \\
 & \quad \left( d (a (1 + \operatorname{Sec}[c+dx]))^{5/2} \right) + \frac{\cos \left[ \frac{1}{2} (c+dx) \right]^5 \operatorname{Sec}[c+dx]^{5/2}}{8 d (a (1 + \operatorname{Sec}[c+dx]))^{5/2} \left( \cos \left[ \frac{1}{4} (c+dx) \right] - \sin \left[ \frac{1}{4} (c+dx) \right] \right)^4} + \\
 & \frac{19 \cos \left[ \frac{1}{2} (c+dx) \right]^5 \operatorname{Sec}[c+dx]^{5/2}}{8 d (a (1 + \operatorname{Sec}[c+dx]))^{5/2} \left( \cos \left[ \frac{1}{4} (c+dx) \right] - \sin \left[ \frac{1}{4} (c+dx) \right] \right)^2} - \\
 & \frac{\cos \left[ \frac{1}{2} (c+dx) \right]^5 \operatorname{Sec}[c+dx]^{5/2}}{8 d (a (1 + \operatorname{Sec}[c+dx]))^{5/2} \left( \cos \left[ \frac{1}{4} (c+dx) \right] + \sin \left[ \frac{1}{4} (c+dx) \right] \right)^4} - \\
 & \frac{19 \cos \left[ \frac{1}{2} (c+dx) \right]^5 \operatorname{Sec}[c+dx]^{5/2}}{8 d (a (1 + \operatorname{Sec}[c+dx]))^{5/2} \left( \cos \left[ \frac{1}{4} (c+dx) \right] + \sin \left[ \frac{1}{4} (c+dx) \right] \right)^2} + \\
 & \frac{4 \cos \left[ \frac{1}{2} (c+dx) \right]^5 \operatorname{Sec}[c+dx]^{5/2}}{d (a (1 + \operatorname{Sec}[c+dx]))^{5/2} \left( \cos \left[ \frac{1}{2} (c+dx) \right] - \sin \left[ \frac{1}{2} (c+dx) \right] \right)} - \\
 & \frac{4 \cos \left[ \frac{1}{2} (c+dx) \right]^5 \operatorname{Sec}[c+dx]^{5/2}}{d (a (1 + \operatorname{Sec}[c+dx]))^{5/2} \left( \cos \left[ \frac{1}{2} (c+dx) \right] + \sin \left[ \frac{1}{2} (c+dx) \right] \right)}
 \end{aligned}$$

**Problem 259:** Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\text{Sec}[c + d x]^{7/2}}{(a + a \text{Sec}[c + d x])^{5/2}} dx$$

Optimal (type 3, 174 leaves, 7 steps):

$$\frac{2 \text{ArcSinh}\left[\frac{\sqrt{a} \text{Tan}[c+dx]}{\sqrt{a+a \text{Sec}[c+dx]}}\right]}{a^{5/2} d} - \frac{43 \text{ArcTanh}\left[\frac{\sqrt{a} \sqrt{\text{Sec}[c+dx]} \text{Sin}[c+dx]}{\sqrt{2} \sqrt{a+a \text{Sec}[c+dx]}}\right]}{16 \sqrt{2} a^{5/2} d} - \frac{\text{Sec}[c + d x]^{5/2} \text{Sin}[c + d x]}{4 d (a + a \text{Sec}[c + d x])^{5/2}} - \frac{11 \text{Sec}[c + d x]^{3/2} \text{Sin}[c + d x]}{16 a d (a + a \text{Sec}[c + d x])^{3/2}}$$

Result (type 3, 925 leaves):

$$\begin{aligned}
 & - \left( \left( 4 i \sqrt{2} \operatorname{ArcTan} \left[ \frac{\cos \left[ \frac{1}{4} (c+d x) \right] - \sin \left[ \frac{1}{4} (c+d x) \right] - \sqrt{2} \sin \left[ \frac{1}{4} (c+d x) \right]}{-\cos \left[ \frac{1}{4} (c+d x) \right] + \sqrt{2} \cos \left[ \frac{1}{4} (c+d x) \right] - \sin \left[ \frac{1}{4} (c+d x) \right]} \right) \right. \right. \\
 & \quad \left. \left. \cos \left[ \frac{1}{2} (c+d x) \right]^5 \operatorname{Sec}[c+d x]^{5/2} \right) / \left( d (a (1 + \operatorname{Sec}[c+d x]))^{5/2} \right) + \right. \\
 & \left( (4+4 i) \left( (-1-i) + \sqrt{2} \right) \operatorname{ArcTan} \left[ \frac{\cos \left[ \frac{1}{4} (c+d x) \right] + \sin \left[ \frac{1}{4} (c+d x) \right] - \sqrt{2} \sin \left[ \frac{1}{4} (c+d x) \right]}{\cos \left[ \frac{1}{4} (c+d x) \right] + \sqrt{2} \cos \left[ \frac{1}{4} (c+d x) \right] - \sin \left[ \frac{1}{4} (c+d x) \right]} \right) \right. \\
 & \quad \left. \cos \left[ \frac{1}{2} (c+d x) \right]^5 \operatorname{Sec}[c+d x]^{5/2} \right) / \left( \left( (-1+i) + \sqrt{2} \right) d (a (1 + \operatorname{Sec}[c+d x]))^{5/2} \right) + \\
 & \left( 43 \cos \left[ \frac{1}{2} (c+d x) \right]^5 \operatorname{Log} \left[ \cos \left[ \frac{1}{4} (c+d x) \right] - \sin \left[ \frac{1}{4} (c+d x) \right] \right] \operatorname{Sec}[c+d x]^{5/2} \right) / \\
 & \quad \left( 4 d (a (1 + \operatorname{Sec}[c+d x]))^{5/2} \right) - \\
 & \left( 43 \cos \left[ \frac{1}{2} (c+d x) \right]^5 \operatorname{Log} \left[ \cos \left[ \frac{1}{4} (c+d x) \right] + \sin \left[ \frac{1}{4} (c+d x) \right] \right] \operatorname{Sec}[c+d x]^{5/2} \right) / \\
 & \quad \left( 4 d (a (1 + \operatorname{Sec}[c+d x]))^{5/2} \right) + \\
 & \frac{4 \sqrt{2} \cos \left[ \frac{1}{2} (c+d x) \right]^5 \operatorname{Log} \left[ \sqrt{2} + 2 \sin \left[ \frac{1}{2} (c+d x) \right] \right] \operatorname{Sec}[c+d x]^{5/2}}{d (a (1 + \operatorname{Sec}[c+d x]))^{5/2}} - \\
 & \left( 2 \sqrt{2} \cos \left[ \frac{1}{2} (c+d x) \right]^5 \operatorname{Log} \left[ 2 - \sqrt{2} \cos \left[ \frac{1}{2} (c+d x) \right] - \sqrt{2} \sin \left[ \frac{1}{2} (c+d x) \right] \right] \operatorname{Sec}[c+d x]^{5/2} \right) / \\
 & \quad \left( d (a (1 + \operatorname{Sec}[c+d x]))^{5/2} \right) + \\
 & \left( (2-2 i) \left( (-1-i) + \sqrt{2} \right) \cos \left[ \frac{1}{2} (c+d x) \right]^5 \operatorname{Log} \left[ 2 + \sqrt{2} \cos \left[ \frac{1}{2} (c+d x) \right] - \sqrt{2} \sin \left[ \frac{1}{2} (c+d x) \right] \right] \right. \\
 & \quad \left. \operatorname{Sec}[c+d x]^{5/2} \right) / \left( \left( (-1+i) + \sqrt{2} \right) d (a (1 + \operatorname{Sec}[c+d x]))^{5/2} \right) - \\
 & \frac{\cos \left[ \frac{1}{2} (c+d x) \right]^5 \operatorname{Sec}[c+d x]^{5/2}}{8 d (a (1 + \operatorname{Sec}[c+d x]))^{5/2} \left( \cos \left[ \frac{1}{4} (c+d x) \right] - \sin \left[ \frac{1}{4} (c+d x) \right] \right)^4} - \\
 & \frac{11 \cos \left[ \frac{1}{2} (c+d x) \right]^5 \operatorname{Sec}[c+d x]^{5/2}}{8 d (a (1 + \operatorname{Sec}[c+d x]))^{5/2} \left( \cos \left[ \frac{1}{4} (c+d x) \right] - \sin \left[ \frac{1}{4} (c+d x) \right] \right)^2} + \\
 & \frac{\cos \left[ \frac{1}{2} (c+d x) \right]^5 \operatorname{Sec}[c+d x]^{5/2}}{8 d (a (1 + \operatorname{Sec}[c+d x]))^{5/2} \left( \cos \left[ \frac{1}{4} (c+d x) \right] + \sin \left[ \frac{1}{4} (c+d x) \right] \right)^4} + \\
 & \frac{11 \cos \left[ \frac{1}{2} (c+d x) \right]^5 \operatorname{Sec}[c+d x]^{5/2}}{8 d (a (1 + \operatorname{Sec}[c+d x]))^{5/2} \left( \cos \left[ \frac{1}{4} (c+d x) \right] + \sin \left[ \frac{1}{4} (c+d x) \right] \right)^2}
 \end{aligned}$$

**Problem 265: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\text{Sec}[c + d x]^{7/2}}{\sqrt{1 + \text{Sec}[c + d x]}} dx$$

Optimal (type 3, 126 leaves, 7 steps):

$$-\frac{\sqrt{2} \text{ArcSinh}\left[\frac{\text{Tan}[c+dx]}{1+\text{Sec}[c+dx]}\right]}{d} + \frac{7 \text{ArcSinh}\left[\frac{\text{Tan}[c+dx]}{\sqrt{1+\text{Sec}[c+dx]}}\right]}{4d} - \frac{\text{Sec}[c+dx]^{3/2} \text{Sin}[c+dx]}{4d\sqrt{1+\text{Sec}[c+dx]}} + \frac{\text{Sec}[c+dx]^{5/2} \text{Sin}[c+dx]}{2d\sqrt{1+\text{Sec}[c+dx]}}$$

Result (type 3, 542 leaves):

$$\begin{aligned} & \frac{1}{32d} \text{Cos}\left[\frac{1}{2}(c+dx)\right] \sqrt{\text{Sec}\left[\frac{1}{2}(c+dx)\right]^2} \\ & \left( -28i \text{ArcTan}\left[\frac{\text{Cos}\left[\frac{1}{4}(c+dx)\right] - (-1+\sqrt{2}) \text{Sin}\left[\frac{1}{4}(c+dx)\right]}{(1+\sqrt{2}) \text{Cos}\left[\frac{1}{4}(c+dx)\right] - \text{Sin}\left[\frac{1}{4}(c+dx)\right]}\right] - \right. \\ & \quad \left. 28i \text{ArcTan}\left[\frac{\text{Cos}\left[\frac{1}{4}(c+dx)\right] - (1+\sqrt{2}) \text{Sin}\left[\frac{1}{4}(c+dx)\right]}{(-1+\sqrt{2}) \text{Cos}\left[\frac{1}{4}(c+dx)\right] - \text{Sin}\left[\frac{1}{4}(c+dx)\right]}\right] + \right. \\ & \quad \text{Sec}[c+dx]^2 \left( 16\sqrt{2} \text{Log}\left[\text{Cos}\left[\frac{1}{4}(c+dx)\right] - \text{Sin}\left[\frac{1}{4}(c+dx)\right]\right] - \right. \\ & \quad \quad 16\sqrt{2} \text{Log}\left[\text{Cos}\left[\frac{1}{4}(c+dx)\right] + \text{Sin}\left[\frac{1}{4}(c+dx)\right]\right] + 14 \text{Log}\left[\sqrt{2} + 2 \text{Sin}\left[\frac{1}{2}(c+dx)\right]\right] - \\ & \quad \quad 7 \text{Log}\left[2 - \sqrt{2} \text{Cos}\left[\frac{1}{2}(c+dx)\right] - \sqrt{2} \text{Sin}\left[\frac{1}{2}(c+dx)\right]\right] + \\ & \quad \quad \text{Cos}[2(c+dx)] \left( 16\sqrt{2} \text{Log}\left[\text{Cos}\left[\frac{1}{4}(c+dx)\right] - \text{Sin}\left[\frac{1}{4}(c+dx)\right]\right] - \right. \\ & \quad \quad \quad 16\sqrt{2} \text{Log}\left[\text{Cos}\left[\frac{1}{4}(c+dx)\right] + \text{Sin}\left[\frac{1}{4}(c+dx)\right]\right] + 14 \text{Log}\left[\sqrt{2} + 2 \text{Sin}\left[\frac{1}{2}(c+dx)\right]\right] - \\ & \quad \quad \quad 7 \text{Log}\left[2 - \sqrt{2} \text{Cos}\left[\frac{1}{2}(c+dx)\right] - \sqrt{2} \text{Sin}\left[\frac{1}{2}(c+dx)\right]\right] - \\ & \quad \quad \quad \left. \left. 7 \text{Log}\left[2 + \sqrt{2} \text{Cos}\left[\frac{1}{2}(c+dx)\right] - \sqrt{2} \text{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \right) - \right. \\ & \quad \quad \quad \left. 7 \text{Log}\left[2 + \sqrt{2} \text{Cos}\left[\frac{1}{2}(c+dx)\right] - \sqrt{2} \text{Sin}\left[\frac{1}{2}(c+dx)\right]\right] + \right. \\ & \quad \quad \quad \left. \left. 20\sqrt{2} \text{Sin}\left[\frac{1}{2}(c+dx)\right] - 4\sqrt{2} \text{Sin}\left[\frac{3}{2}(c+dx)\right] \right) \right) \end{aligned}$$

**Problem 266: Result unnecessarily involves complex numbers and more than**

twice size of optimal antiderivative.

$$\int \frac{\text{Sec}[c + d x]^{5/2}}{\sqrt{1 + \text{Sec}[c + d x]}} dx$$

Optimal (type 3, 85 leaves, 6 steps):

$$\frac{\sqrt{2} \text{ArcSinh}\left[\frac{\text{Tan}[c+dx]}{1+\text{Sec}[c+dx]}\right]}{d} - \frac{\text{ArcSinh}\left[\frac{\text{Tan}[c+dx]}{\sqrt{1+\text{Sec}[c+dx]}}\right]}{d} + \frac{\text{Sec}[c+dx]^{3/2} \text{Sin}[c+dx]}{d \sqrt{1 + \text{Sec}[c+dx]}}$$

Result (type 3, 349 leaves):

$$\begin{aligned} & \frac{1}{4d} \text{Cos}\left[\frac{1}{2}(c+dx)\right] \sqrt{\text{Sec}\left[\frac{1}{2}(c+dx)\right]^2} \\ & \left( 2 \text{i ArcTan}\left[\frac{\text{Cos}\left[\frac{1}{4}(c+dx)\right] - (-1 + \sqrt{2}) \text{Sin}\left[\frac{1}{4}(c+dx)\right]}{(1 + \sqrt{2}) \text{Cos}\left[\frac{1}{4}(c+dx)\right] - \text{Sin}\left[\frac{1}{4}(c+dx)\right]}\right] + \right. \\ & 2 \text{i ArcTan}\left[\frac{\text{Cos}\left[\frac{1}{4}(c+dx)\right] - (1 + \sqrt{2}) \text{Sin}\left[\frac{1}{4}(c+dx)\right]}{(-1 + \sqrt{2}) \text{Cos}\left[\frac{1}{4}(c+dx)\right] - \text{Sin}\left[\frac{1}{4}(c+dx)\right]}\right] - 4 \sqrt{2} \\ & \text{Log}\left[\text{Cos}\left[\frac{1}{4}(c+dx)\right] - \text{Sin}\left[\frac{1}{4}(c+dx)\right]\right] + 4 \sqrt{2} \text{Log}\left[\text{Cos}\left[\frac{1}{4}(c+dx)\right] + \text{Sin}\left[\frac{1}{4}(c+dx)\right]\right] - \\ & 2 \text{Log}\left[\sqrt{2} + 2 \text{Sin}\left[\frac{1}{2}(c+dx)\right]\right] + \text{Log}\left[2 - \sqrt{2} \text{Cos}\left[\frac{1}{2}(c+dx)\right] - \sqrt{2} \text{Sin}\left[\frac{1}{2}(c+dx)\right]\right] + \\ & \left. \text{Log}\left[2 + \sqrt{2} \text{Cos}\left[\frac{1}{2}(c+dx)\right] - \sqrt{2} \text{Sin}\left[\frac{1}{2}(c+dx)\right]\right] + 4 \sqrt{2} \text{Sec}[c+dx] \text{Sin}\left[\frac{1}{2}(c+dx)\right] \right) \end{aligned}$$

Problem 267: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\text{Sec}[c + d x]^{3/2}}{\sqrt{1 + \text{Sec}[c + d x]}} dx$$

Optimal (type 3, 54 leaves, 5 steps):

$$-\frac{\sqrt{2} \text{ArcSinh}\left[\frac{\text{Tan}[c+dx]}{1+\text{Sec}[c+dx]}\right]}{d} + \frac{2 \text{ArcSinh}\left[\frac{\text{Tan}[c+dx]}{\sqrt{1+\text{Sec}[c+dx]}}\right]}{d}$$

Result (type 3, 384 leaves):

$$\frac{1}{((-1+i) + \sqrt{2}) d} \left( \frac{1}{2} + \frac{i}{2} \right) \cos\left[\frac{1}{2}(c+dx)\right] \sqrt{\frac{1}{1+\cos[c+dx]}}$$

$$\left( 2 \left( (-1-i) + \sqrt{2} \right) \operatorname{ArcTan}\left[ \frac{\cos\left[\frac{1}{4}(c+dx)\right] - (-1+\sqrt{2}) \sin\left[\frac{1}{4}(c+dx)\right]}{(1+\sqrt{2}) \cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]} \right] + \right.$$

$$2 \left( (-1-i) + \sqrt{2} \right) \operatorname{ArcTan}\left[ \frac{\cos\left[\frac{1}{4}(c+dx)\right] - (1+\sqrt{2}) \sin\left[\frac{1}{4}(c+dx)\right]}{(-1+\sqrt{2}) \cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]} \right] -$$

$$i \left( (-4 + (2+2i)\sqrt{2}) \operatorname{Log}\left[\cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]\right] + \right.$$

$$\left. (4 - (2+2i)\sqrt{2}) \operatorname{Log}\left[\cos\left[\frac{1}{4}(c+dx)\right] + \sin\left[\frac{1}{4}(c+dx)\right]\right] - \left( (-1-i) + \sqrt{2} \right) \right.$$

$$\left. \left( 2 \operatorname{Log}\left[\sqrt{2} + 2 \sin\left[\frac{1}{2}(c+dx)\right]\right] - \operatorname{Log}\left[2 - \sqrt{2} \cos\left[\frac{1}{2}(c+dx)\right] - \sqrt{2} \sin\left[\frac{1}{2}(c+dx)\right]\right] - \right.$$

$$\left. \left. \operatorname{Log}\left[2 + \sqrt{2} \cos\left[\frac{1}{2}(c+dx)\right] - \sqrt{2} \sin\left[\frac{1}{2}(c+dx)\right]\right] \right) \right)$$

**Problem 268: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sqrt{\sec[c+dx]}}{\sqrt{1+\sec[c+dx]}} dx$$

Optimal (type 3, 27 leaves, 2 steps):

$$\frac{\sqrt{2} \operatorname{ArcSinh}\left[\frac{\tan[c+dx]}{1+\sec[c+dx]}\right]}{d}$$

Result (type 3, 78 leaves):

$$\frac{1}{d} 2 \cos\left[\frac{1}{2}(c+dx)\right] \sqrt{\frac{1}{1+\cos[c+dx]}}$$

$$\left( -\operatorname{Log}\left[\cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]\right] + \operatorname{Log}\left[\cos\left[\frac{1}{4}(c+dx)\right] + \sin\left[\frac{1}{4}(c+dx)\right]\right] \right)$$

**Problem 272: Result unnecessarily involves higher level functions.**

$$\int (e \sec[c+dx])^{4/3} \sqrt{a+a \sec[c+dx]} dx$$

Optimal (type 4, 325 leaves, 4 steps):

$$\frac{6 a e (e \operatorname{Sec}[c+d x])^{1/3} \operatorname{Tan}[c+d x]}{5 d \sqrt{a+a \operatorname{Sec}[c+d x]}} +$$

$$\left( 4 \times 3^{3/4} \sqrt{2+\sqrt{3}} a^2 e \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{(1-\sqrt{3}) e^{1/3}-(e \operatorname{Sec}[c+d x])^{1/3}}{(1+\sqrt{3}) e^{1/3}-(e \operatorname{Sec}[c+d x])^{1/3}}\right], -7-4 \sqrt{3}\right] \right.$$

$$\left. \left( e^{1/3}-(e \operatorname{Sec}[c+d x])^{1/3} \right) \sqrt{\frac{e^{2/3}+e^{1/3}(e \operatorname{Sec}[c+d x])^{1/3}+(e \operatorname{Sec}[c+d x])^{2/3}}{\left((1+\sqrt{3}) e^{1/3}-(e \operatorname{Sec}[c+d x])^{1/3}\right)^2}} \operatorname{Tan}[c+d x]} \right) /$$

$$\left( 5 d (a-a \operatorname{Sec}[c+d x]) \sqrt{a+a \operatorname{Sec}[c+d x]} \sqrt{\frac{e^{1/3}\left(e^{1/3}-(e \operatorname{Sec}[c+d x])^{1/3}\right)}{\left((1+\sqrt{3}) e^{1/3}-(e \operatorname{Sec}[c+d x])^{1/3}\right)^2}} \right)$$

Result (type 5, 160 leaves):

$$-\left( \left( 3 i e^{-4+4 e^{i(c+d x)}}+4\left(1+e^{2 i(c+d x)}\right)^{5/6} \operatorname{Hypergeometric2F1}\left[\frac{1}{6}, \frac{5}{6}, \frac{7}{6},-e^{2 i(c+d x)}\right]+e^{i(c+d x)}\left(1+e^{2 i(c+d x)}\right)^{5/6} \operatorname{Hypergeometric2F1}\left[\frac{2}{3}, \frac{5}{6}, \frac{5}{3},-e^{2 i(c+d x)}\right]\right)\left(e \operatorname{Sec}[c+d x]\right)^{1/3} \sqrt{a(1+\operatorname{Sec}[c+d x])} \right) / \left( 10 d\left(1+e^{i(c+d x)}\right)\right)$$

**Problem 273: Result unnecessarily involves higher level functions.**

$$\int (e \operatorname{Sec}[c+d x])^{1/3} \sqrt{a+a \operatorname{Sec}[c+d x]} dx$$

Optimal (type 4, 280 leaves, 3 steps):

$$\left( 2 \times 3^{3/4} \sqrt{2+\sqrt{3}} a^2 \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{(1-\sqrt{3}) e^{1/3}-(e \operatorname{Sec}[c+d x])^{1/3}}{(1+\sqrt{3}) e^{1/3}-(e \operatorname{Sec}[c+d x])^{1/3}}\right], -7-4 \sqrt{3}\right] \right.$$

$$\left. \left( e^{1/3}-(e \operatorname{Sec}[c+d x])^{1/3} \right) \sqrt{\frac{e^{2/3}+e^{1/3}(e \operatorname{Sec}[c+d x])^{1/3}+(e \operatorname{Sec}[c+d x])^{2/3}}{\left((1+\sqrt{3}) e^{1/3}-(e \operatorname{Sec}[c+d x])^{1/3}\right)^2}} \operatorname{Tan}[c+d x]} \right) /$$

$$\left( d (a-a \operatorname{Sec}[c+d x]) \sqrt{a+a \operatorname{Sec}[c+d x]} \sqrt{\frac{e^{1/3}\left(e^{1/3}-(e \operatorname{Sec}[c+d x])^{1/3}\right)}{\left((1+\sqrt{3}) e^{1/3}-(e \operatorname{Sec}[c+d x])^{1/3}\right)^2}} \right)$$

Result (type 5, 153 leaves):

$$- \left( \left( 3 i \left( \frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}} \right)^{1/3} (1+e^{2i(c+dx)})^{5/6} \left( 4 \operatorname{Hypergeometric2F1} \left[ \frac{1}{6}, \frac{5}{6}, \frac{7}{6}, -e^{2i(c+dx)} \right] + e^{i(c+dx)} \operatorname{Hypergeometric2F1} \left[ \frac{2}{3}, \frac{5}{6}, \frac{5}{3}, -e^{2i(c+dx)} \right] \right) \sqrt{a(1+\operatorname{Sec}[c+dx])} \right) / (2 \times 2^{2/3} d (1+e^{i(c+dx)})) \right)$$

**Problem 274: Result unnecessarily involves higher level functions.**

$$\int \frac{\sqrt{a+a \operatorname{Sec}[c+dx]}}{(e \operatorname{Sec}[c+dx])^{2/3}} dx$$

Optimal (type 4, 326 leaves, 4 steps):

$$\frac{3 a \operatorname{Tan}[c+dx]}{2 d (e \operatorname{Sec}[c+dx])^{2/3} \sqrt{a+a \operatorname{Sec}[c+dx]}} + \left( 3^{3/4} \sqrt{2+\sqrt{3}} a^2 \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{(1-\sqrt{3}) e^{1/3} - (e \operatorname{Sec}[c+dx])^{1/3}}{(1+\sqrt{3}) e^{1/3} - (e \operatorname{Sec}[c+dx])^{1/3}} \right], -7-4\sqrt{3} \right] \left( e^{1/3} - (e \operatorname{Sec}[c+dx])^{1/3} \right) \sqrt{\frac{e^{2/3} + e^{1/3} (e \operatorname{Sec}[c+dx])^{1/3} + (e \operatorname{Sec}[c+dx])^{2/3}}{\left( (1+\sqrt{3}) e^{1/3} - (e \operatorname{Sec}[c+dx])^{1/3} \right)^2}} \operatorname{Tan}[c+dx] \right) / \left( 2 d e (a-a \operatorname{Sec}[c+dx]) \sqrt{a+a \operatorname{Sec}[c+dx]} \sqrt{\frac{e^{1/3} (e^{1/3} - (e \operatorname{Sec}[c+dx])^{1/3})}{\left( (1+\sqrt{3}) e^{1/3} - (e \operatorname{Sec}[c+dx])^{1/3} \right)^2}} \right)$$

Result (type 5, 231 leaves):

$$\frac{1}{16 \times 2^{2/3} d e} 3 e^{-2i(c+dx)} \left( \frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}} \right)^{1/3} \left( 4 (-1+e^{i(c+dx)} - e^{2i(c+dx)} + e^{3i(c+dx)}) + 4 e^{i(c+dx)} (1+e^{2i(c+dx)})^{5/6} \operatorname{Hypergeometric2F1} \left[ \frac{1}{6}, \frac{5}{6}, \frac{7}{6}, -e^{2i(c+dx)} \right] + e^{2i(c+dx)} (1+e^{2i(c+dx)})^{5/6} \operatorname{Hypergeometric2F1} \left[ \frac{2}{3}, \frac{5}{6}, \frac{5}{3}, -e^{2i(c+dx)} \right] \right) \sqrt{a(1+\operatorname{Sec}[c+dx])} \left( -i + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] \right)$$

**Problem 275: Result unnecessarily involves higher level functions.**

$$\int (e \operatorname{Sec}[c+dx])^{8/3} \sqrt{a+a \operatorname{Sec}[c+dx]} dx$$

Optimal (type 4, 716 leaves, 7 steps):



$$\begin{aligned}
 & \frac{60 a e^2 (e \operatorname{Sec}[c+d x])^{2/3} \operatorname{Tan}[c+d x]}{91 d \sqrt{a+a \operatorname{Sec}[c+d x]}} + \frac{6 a e (e \operatorname{Sec}[c+d x])^{5/3} \operatorname{Tan}[c+d x]}{13 d \sqrt{a+a \operatorname{Sec}[c+d x]}} - \\
 & \frac{240 a e^3 \operatorname{Tan}[c+d x]}{91 d \sqrt{a+a \operatorname{Sec}[c+d x]} \left( (1+\sqrt{3}) e^{1/3} - (e \operatorname{Sec}[c+d x])^{1/3} \right)} + \\
 & \left( 120 \times 3^{1/4} \sqrt{2-\sqrt{3}} a^2 e^{7/3} \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{(1-\sqrt{3}) e^{1/3} - (e \operatorname{Sec}[c+d x])^{1/3}}{(1+\sqrt{3}) e^{1/3} - (e \operatorname{Sec}[c+d x])^{1/3}}\right], -7-4\sqrt{3}\right] \right. \\
 & \left. (e^{1/3} - (e \operatorname{Sec}[c+d x])^{1/3}) \sqrt{\frac{e^{2/3} + e^{1/3} (e \operatorname{Sec}[c+d x])^{1/3} + (e \operatorname{Sec}[c+d x])^{2/3} \operatorname{Tan}[c+d x]}{\left( (1+\sqrt{3}) e^{1/3} - (e \operatorname{Sec}[c+d x])^{1/3} \right)^2}} \right) / \\
 & \left( 91 d (a - a \operatorname{Sec}[c+d x]) \sqrt{a+a \operatorname{Sec}[c+d x]} \sqrt{\frac{e^{1/3} (e^{1/3} - (e \operatorname{Sec}[c+d x])^{1/3})}{\left( (1+\sqrt{3}) e^{1/3} - (e \operatorname{Sec}[c+d x])^{1/3} \right)^2}} \right) - \\
 & \left( 80 \sqrt{2} 3^{3/4} a^2 e^{7/3} \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{(1-\sqrt{3}) e^{1/3} - (e \operatorname{Sec}[c+d x])^{1/3}}{(1+\sqrt{3}) e^{1/3} - (e \operatorname{Sec}[c+d x])^{1/3}}\right], -7-4\sqrt{3}\right] \right. \\
 & \left. (e^{1/3} - (e \operatorname{Sec}[c+d x])^{1/3}) \sqrt{\frac{e^{2/3} + e^{1/3} (e \operatorname{Sec}[c+d x])^{1/3} + (e \operatorname{Sec}[c+d x])^{2/3} \operatorname{Tan}[c+d x]}{\left( (1+\sqrt{3}) e^{1/3} - (e \operatorname{Sec}[c+d x])^{1/3} \right)^2}} \right) / \\
 & \left( 91 d (a - a \operatorname{Sec}[c+d x]) \sqrt{a+a \operatorname{Sec}[c+d x]} \sqrt{\frac{e^{1/3} (e^{1/3} - (e \operatorname{Sec}[c+d x])^{1/3})}{\left( (1+\sqrt{3}) e^{1/3} - (e \operatorname{Sec}[c+d x])^{1/3} \right)^2}} \right)
 \end{aligned}$$

Result(type 5, 221 leaves):

$$\begin{aligned}
 & \frac{1}{91 d} 3^i e^{-\frac{5}{2} i (c+d x)} \left( 10 - 5 e^{i (c+d x)} + 22 e^{2 i (c+d x)} - 22 e^{3 i (c+d x)} + 5 e^{4 i (c+d x)} - \right. \\
 & 10 e^{5 i (c+d x)} - 10 (1 + e^{2 i (c+d x)})^{13/6} \operatorname{Hypergeometric2F1}\left[-\frac{1}{6}, \frac{1}{6}, \frac{5}{6}, -e^{2 i (c+d x)}\right] + \\
 & \left. 5 e^{i (c+d x)} (1 + e^{2 i (c+d x)})^{13/6} \operatorname{Hypergeometric2F1}\left[\frac{1}{6}, \frac{1}{3}, \frac{4}{3}, -e^{2 i (c+d x)}\right] \right) \\
 & \operatorname{Sec}\left[\frac{1}{2} (c+d x)\right] (e \operatorname{Sec}[c+d x])^{5/3} \sqrt{a (1 + \operatorname{Sec}[c+d x])}
 \end{aligned}$$

**Problem 276: Result unnecessarily involves higher level functions.**

$$\int (e \operatorname{Sec}[c+d x])^{5/3} \sqrt{a+a \operatorname{Sec}[c+d x]} dx$$

Optimal (type 4, 673 leaves, 6 steps):

$$\frac{6 a e (e \operatorname{Sec}[c+d x])^{2/3} \operatorname{Tan}[c+d x]}{7 d \sqrt{a+a \operatorname{Sec}[c+d x]}} - \frac{24 a e^2 \operatorname{Tan}[c+d x]}{7 d \sqrt{a+a \operatorname{Sec}[c+d x]} \left( (1+\sqrt{3}) e^{1/3} - (e \operatorname{Sec}[c+d x])^{1/3} \right)} +$$

$$\left( 12 \times 3^{1/4} \sqrt{2-\sqrt{3}} a^2 e^{4/3} \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{(1-\sqrt{3}) e^{1/3} - (e \operatorname{Sec}[c+d x])^{1/3}}{(1+\sqrt{3}) e^{1/3} - (e \operatorname{Sec}[c+d x])^{1/3}}\right], -7-4 \sqrt{3}\right] \right.$$

$$\left. (e^{1/3} - (e \operatorname{Sec}[c+d x])^{1/3}) \sqrt{\frac{e^{2/3} + e^{1/3} (e \operatorname{Sec}[c+d x])^{1/3} + (e \operatorname{Sec}[c+d x])^{2/3}}{\left( (1+\sqrt{3}) e^{1/3} - (e \operatorname{Sec}[c+d x])^{1/3} \right)^2}} \operatorname{Tan}[c+d x] \right) /$$

$$\left( 7 d (a - a \operatorname{Sec}[c+d x]) \sqrt{a+a \operatorname{Sec}[c+d x]} \sqrt{\frac{e^{1/3} (e^{1/3} - (e \operatorname{Sec}[c+d x])^{1/3})}{\left( (1+\sqrt{3}) e^{1/3} - (e \operatorname{Sec}[c+d x])^{1/3} \right)^2}} \right) -$$

$$\left( 8 \sqrt{2} 3^{3/4} a^2 e^{4/3} \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{(1-\sqrt{3}) e^{1/3} - (e \operatorname{Sec}[c+d x])^{1/3}}{(1+\sqrt{3}) e^{1/3} - (e \operatorname{Sec}[c+d x])^{1/3}}\right], -7-4 \sqrt{3}\right] \right.$$

$$\left. (e^{1/3} - (e \operatorname{Sec}[c+d x])^{1/3}) \sqrt{\frac{e^{2/3} + e^{1/3} (e \operatorname{Sec}[c+d x])^{1/3} + (e \operatorname{Sec}[c+d x])^{2/3}}{\left( (1+\sqrt{3}) e^{1/3} - (e \operatorname{Sec}[c+d x])^{1/3} \right)^2}} \operatorname{Tan}[c+d x] \right) /$$

$$\left( 7 d (a - a \operatorname{Sec}[c+d x]) \sqrt{a+a \operatorname{Sec}[c+d x]} \sqrt{\frac{e^{1/3} (e^{1/3} - (e \operatorname{Sec}[c+d x])^{1/3})}{\left( (1+\sqrt{3}) e^{1/3} - (e \operatorname{Sec}[c+d x])^{1/3} \right)^2}} \right)$$

Result (type 5, 192 leaves):

$$\frac{1}{7 d} 3^i e^{-\frac{3}{2} i (c+d x)} \left( 2 - e^i (c+d x) + e^{2 i (c+d x)} - 2 e^{3 i (c+d x)} - \right.$$

$$2 \left( 1 + e^{2 i (c+d x)} \right)^{7/6} \operatorname{Hypergeometric2F1}\left[-\frac{1}{6}, \frac{1}{6}, \frac{5}{6}, -e^{2 i (c+d x)}\right] +$$

$$e^i (c+d x) \left( 1 + e^{2 i (c+d x)} \right)^{7/6} \operatorname{Hypergeometric2F1}\left[\frac{1}{6}, \frac{1}{3}, \frac{4}{3}, -e^{2 i (c+d x)}\right] \Big)$$

$$\operatorname{Sec}\left[\frac{1}{2} (c+d x)\right] (e \operatorname{Sec}[c+d x])^{2/3} \sqrt{a (1+\operatorname{Sec}[c+d x])}$$

**Problem 277: Result unnecessarily involves higher level functions.**

$$\int (e \operatorname{Sec}[c+d x])^{2/3} \sqrt{a+a \operatorname{Sec}[c+d x]} dx$$

Optimal (type 4, 624 leaves, 5 steps):

$$\begin{aligned}
 & - \frac{6 a e \operatorname{Tan}[c+d x]}{d \sqrt{a+a \operatorname{Sec}[c+d x]} \left( (1+\sqrt{3}) e^{1/3} - (e \operatorname{Sec}[c+d x])^{1/3} \right)^2} + \\
 & \left( 3 \times 3^{1/4} \sqrt{2-\sqrt{3}} a^2 e^{1/3} \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{(1-\sqrt{3}) e^{1/3} - (e \operatorname{Sec}[c+d x])^{1/3}}{(1+\sqrt{3}) e^{1/3} - (e \operatorname{Sec}[c+d x])^{1/3}}\right], -7-4 \sqrt{3}\right] \right. \\
 & \left. (e^{1/3} - (e \operatorname{Sec}[c+d x])^{1/3}) \sqrt{\frac{e^{2/3} + e^{1/3} (e \operatorname{Sec}[c+d x])^{1/3} + (e \operatorname{Sec}[c+d x])^{2/3}}{\left( (1+\sqrt{3}) e^{1/3} - (e \operatorname{Sec}[c+d x])^{1/3} \right)^2}} \operatorname{Tan}[c+d x]} \right) / \\
 & \left( d (a - a \operatorname{Sec}[c+d x]) \sqrt{a+a \operatorname{Sec}[c+d x]} \sqrt{\frac{e^{1/3} \left( e^{1/3} - (e \operatorname{Sec}[c+d x])^{1/3} \right)}{\left( (1+\sqrt{3}) e^{1/3} - (e \operatorname{Sec}[c+d x])^{1/3} \right)^2}} \right) - \\
 & \left( 2 \sqrt{2} 3^{3/4} a^2 e^{1/3} \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{(1-\sqrt{3}) e^{1/3} - (e \operatorname{Sec}[c+d x])^{1/3}}{(1+\sqrt{3}) e^{1/3} - (e \operatorname{Sec}[c+d x])^{1/3}}\right], -7-4 \sqrt{3}\right] \right. \\
 & \left. (e^{1/3} - (e \operatorname{Sec}[c+d x])^{1/3}) \sqrt{\frac{e^{2/3} + e^{1/3} (e \operatorname{Sec}[c+d x])^{1/3} + (e \operatorname{Sec}[c+d x])^{2/3}}{\left( (1+\sqrt{3}) e^{1/3} - (e \operatorname{Sec}[c+d x])^{1/3} \right)^2}} \operatorname{Tan}[c+d x]} \right) / \\
 & \left( d (a - a \operatorname{Sec}[c+d x]) \sqrt{a+a \operatorname{Sec}[c+d x]} \sqrt{\frac{e^{1/3} \left( e^{1/3} - (e \operatorname{Sec}[c+d x])^{1/3} \right)}{\left( (1+\sqrt{3}) e^{1/3} - (e \operatorname{Sec}[c+d x])^{1/3} \right)^2}} \right)
 \end{aligned}$$

Result (type 5, 158 leaves):

$$\begin{aligned}
 & \left( 3 i e \left( 2 - 2 e^{i(c+d x)} - 2 \left( 1 + e^{2 i(c+d x)} \right)^{1/6} \operatorname{Hypergeometric2F1}\left[-\frac{1}{6}, \frac{1}{6}, \frac{5}{6}, -e^{2 i(c+d x)}\right] + \right. \right. \\
 & \left. \left. e^{i(c+d x)} \left( 1 + e^{2 i(c+d x)} \right)^{1/6} \operatorname{Hypergeometric2F1}\left[\frac{1}{6}, \frac{1}{3}, \frac{4}{3}, -e^{2 i(c+d x)}\right] \right) \right) / \\
 & \left( d \left( 1 + e^{i(c+d x)} \right) \left( e \operatorname{Sec}[c+d x] \right)^{1/3} \right)
 \end{aligned}$$

**Problem 278: Result unnecessarily involves higher level functions.**

$$\int \frac{\sqrt{a+a \operatorname{Sec}[c+d x]}}{(e \operatorname{Sec}[c+d x])^{1/3}} dx$$

Optimal (type 4, 662 leaves, 6 steps):

$$\frac{3 a \operatorname{Tan}[c+d x]}{d \left(e \operatorname{Sec}[c+d x]\right)^{1 / 3} \sqrt{a+a \operatorname{Sec}[c+d x]}} +$$

$$\frac{3 a \operatorname{Tan}[c+d x]}{d \sqrt{a+a \operatorname{Sec}[c+d x]}\left(\left(1+\sqrt{3}\right) e^{1 / 3}-\left(e \operatorname{Sec}[c+d x]\right)^{1 / 3}\right)} -$$

$$\left(3 \times 3^{1 / 4} \sqrt{2-\sqrt{3}} a^2 \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\left(1-\sqrt{3}\right) e^{1 / 3}-\left(e \operatorname{Sec}[c+d x]\right)^{1 / 3}}{\left(1+\sqrt{3}\right) e^{1 / 3}-\left(e \operatorname{Sec}[c+d x]\right)^{1 / 3}}\right],-7-4 \sqrt{3}\right]\right.$$

$$\left.\left(e^{1 / 3}-\left(e \operatorname{Sec}[c+d x]\right)^{1 / 3}\right) \sqrt{\frac{e^{2 / 3}+e^{1 / 3}\left(e \operatorname{Sec}[c+d x]\right)^{1 / 3}+\left(e \operatorname{Sec}[c+d x]\right)^{2 / 3}}{\left(\left(1+\sqrt{3}\right) e^{1 / 3}-\left(e \operatorname{Sec}[c+d x]\right)^{1 / 3}\right)^2} \operatorname{Tan}[c+d x]}\right) /$$

$$\left(2 d e^{2 / 3}\left(a-a \operatorname{Sec}[c+d x]\right) \sqrt{a+a \operatorname{Sec}[c+d x]}\sqrt{\frac{e^{1 / 3}\left(e^{1 / 3}-\left(e \operatorname{Sec}[c+d x]\right)^{1 / 3}\right)}{\left(\left(1+\sqrt{3}\right) e^{1 / 3}-\left(e \operatorname{Sec}[c+d x]\right)^{1 / 3}\right)^2}}\right) +$$

$$\left(\sqrt{2} 3^{3 / 4} a^2 \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\left(1-\sqrt{3}\right) e^{1 / 3}-\left(e \operatorname{Sec}[c+d x]\right)^{1 / 3}}{\left(1+\sqrt{3}\right) e^{1 / 3}-\left(e \operatorname{Sec}[c+d x]\right)^{1 / 3}}\right],-7-4 \sqrt{3}\right]\right.$$

$$\left.\left(e^{1 / 3}-\left(e \operatorname{Sec}[c+d x]\right)^{1 / 3}\right) \sqrt{\frac{e^{2 / 3}+e^{1 / 3}\left(e \operatorname{Sec}[c+d x]\right)^{1 / 3}+\left(e \operatorname{Sec}[c+d x]\right)^{2 / 3}}{\left(\left(1+\sqrt{3}\right) e^{1 / 3}-\left(e \operatorname{Sec}[c+d x]\right)^{1 / 3}\right)^2} \operatorname{Tan}[c+d x]}\right) /$$

$$\left(d e^{2 / 3}\left(a-a \operatorname{Sec}[c+d x]\right) \sqrt{a+a \operatorname{Sec}[c+d x]}\sqrt{\frac{e^{1 / 3}\left(e^{1 / 3}-\left(e \operatorname{Sec}[c+d x]\right)^{1 / 3}\right)}{\left(\left(1+\sqrt{3}\right) e^{1 / 3}-\left(e \operatorname{Sec}[c+d x]\right)^{1 / 3}\right)^2}}\right)$$

Result (type 5, 153 leaves):

$$-\left(\left(3 i\left(1+e^{2 i(c+d x)}\right)^{1 / 6}\left(-2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{6}, \frac{1}{6}, \frac{5}{6},-e^{2 i(c+d x)}\right]+e^{i(c+d x)} \operatorname{Hypergeometric2F1}\left[\frac{1}{6}, \frac{1}{3}, \frac{4}{3},-e^{2 i(c+d x)}\right]\right) \sqrt{a\left(1+\operatorname{Sec}[c+d x]\right)}\right) / \left(2 \times 2^{1 / 3} d\left(1+e^{i(c+d x)}\right)\left(\frac{e e^{i(c+d x)}}{1+e^{2 i(c+d x)}}\right)^{1 / 3}\right)$$

**Problem 279: Result unnecessarily involves higher level functions.**

$$\int \frac{\sqrt{a+a \operatorname{Sec}[c+d x]}}{\left(e \operatorname{Sec}[c+d x]\right)^{4 / 3}} d x$$

Optimal (type 4, 715 leaves, 7 steps):

$$\begin{aligned}
 & \frac{3 a \operatorname{Tan}[c+d x]}{4 d \left(e \operatorname{Sec}[c+d x]\right)^{4 / 3} \sqrt{a+a \operatorname{Sec}[c+d x]}} + \frac{15 a \operatorname{Tan}[c+d x]}{8 d e \left(e \operatorname{Sec}[c+d x]\right)^{1 / 3} \sqrt{a+a \operatorname{Sec}[c+d x]}} + \\
 & \frac{15 a \operatorname{Tan}[c+d x]}{8 d e \sqrt{a+a \operatorname{Sec}[c+d x]} \left(\left(1+\sqrt{3}\right) e^{1 / 3}-\left(e \operatorname{Sec}[c+d x]\right)^{1 / 3}\right)} - \\
 & \left(15 \times 3^{1 / 4} \sqrt{2-\sqrt{3}} a^2 \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\left(1-\sqrt{3}\right) e^{1 / 3}-\left(e \operatorname{Sec}[c+d x]\right)^{1 / 3}}{\left(1+\sqrt{3}\right) e^{1 / 3}-\left(e \operatorname{Sec}[c+d x]\right)^{1 / 3}}\right],-7-4 \sqrt{3}\right]\right. \\
 & \left.\left(e^{1 / 3}-\left(e \operatorname{Sec}[c+d x]\right)^{1 / 3}\right) \sqrt{\frac{e^{2 / 3}+e^{1 / 3}\left(e \operatorname{Sec}[c+d x]\right)^{1 / 3}+\left(e \operatorname{Sec}[c+d x]\right)^{2 / 3}}{\left(\left(1+\sqrt{3}\right) e^{1 / 3}-\left(e \operatorname{Sec}[c+d x]\right)^{1 / 3}\right)^2} \operatorname{Tan}[c+d x]}\right) / \\
 & \left(16 d e^{5 / 3}(a-a \operatorname{Sec}[c+d x]) \sqrt{a+a \operatorname{Sec}[c+d x]} \sqrt{\frac{e^{1 / 3}\left(e^{1 / 3}-\left(e \operatorname{Sec}[c+d x]\right)^{1 / 3}\right)}{\left(\left(1+\sqrt{3}\right) e^{1 / 3}-\left(e \operatorname{Sec}[c+d x]\right)^{1 / 3}\right)^2}}\right) + \\
 & \left(5 \times 3^{3 / 4} a^2 \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\left(1-\sqrt{3}\right) e^{1 / 3}-\left(e \operatorname{Sec}[c+d x]\right)^{1 / 3}}{\left(1+\sqrt{3}\right) e^{1 / 3}-\left(e \operatorname{Sec}[c+d x]\right)^{1 / 3}}\right],-7-4 \sqrt{3}\right]\right. \\
 & \left.\left(e^{1 / 3}-\left(e \operatorname{Sec}[c+d x]\right)^{1 / 3}\right) \sqrt{\frac{e^{2 / 3}+e^{1 / 3}\left(e \operatorname{Sec}[c+d x]\right)^{1 / 3}+\left(e \operatorname{Sec}[c+d x]\right)^{2 / 3}}{\left(\left(1+\sqrt{3}\right) e^{1 / 3}-\left(e \operatorname{Sec}[c+d x]\right)^{1 / 3}\right)^2} \operatorname{Tan}[c+d x]}\right) / \\
 & \left(4 \sqrt{2} d e^{5 / 3}(a-a \operatorname{Sec}[c+d x]) \sqrt{a+a \operatorname{Sec}[c+d x]} \sqrt{\frac{e^{1 / 3}\left(e^{1 / 3}-\left(e \operatorname{Sec}[c+d x]\right)^{1 / 3}\right)}{\left(\left(1+\sqrt{3}\right) e^{1 / 3}-\left(e \operatorname{Sec}[c+d x]\right)^{1 / 3}\right)^2}}\right)
 \end{aligned}$$

Result (type 5, 248 leaves):

$$\begin{aligned}
 & \left(3 e^{-2 i(c+d x)}\left(2\left(-1+e^{i(c+d x)}-e^{2 i(c+d x)}+e^{3 i(c+d x)}\right)-\right.\right. \\
 & \quad 10 e^{i(c+d x)}\left(1+e^{2 i(c+d x)}\right)^{1 / 6} \operatorname{Hypergeometric2F1}\left[-\frac{1}{6}, \frac{1}{6}, \frac{5}{6},-e^{2 i(c+d x)}\right]+ \\
 & \quad \left.5 e^{2 i(c+d x)}\left(1+e^{2 i(c+d x)}\right)^{1 / 6} \operatorname{Hypergeometric2F1}\left[\frac{1}{6}, \frac{1}{3}, \frac{4}{3},-e^{2 i(c+d x)}\right]\right) \\
 & \left.\sqrt{a(1+\operatorname{Sec}[c+d x])}\left(-i+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right)\right) / \\
 & \left(16 \times 2^{5 / 6} d\left(e^{-i(c+d x)}\left(1+e^{2 i(c+d x)}\right)\right)^{1 / 6} \operatorname{Cos}[c+d x]^{5 / 6}\left(e \operatorname{Sec}[c+d x]\right)^{4 / 3}\right)
 \end{aligned}$$

**Problem 280: Result more than twice size of optimal antiderivative.**

$$\int \frac{\left(e \operatorname{Sec}[c+d x]\right)^{2 / 3}}{\sqrt{a+a \operatorname{Sec}[c+d x]}} d x$$

Optimal (type 6, 78 leaves, 4 steps):

$$-\left(\left(3 \operatorname{AppellF1}\left[\frac{2}{3}, \frac{1}{2}, 1, \frac{5}{3}, \operatorname{Sec}[c+dx], -\operatorname{Sec}[c+dx]\right] \left(e \operatorname{Sec}[c+dx]\right)^{2/3} \operatorname{Tan}[c+dx]\right) / \left(2 d \sqrt{1-\operatorname{Sec}[c+dx]} \sqrt{a+a \operatorname{Sec}[c+dx]}\right)\right)$$

Result (type 6, 1975 leaves):

$$\begin{aligned} & \left(9 \times 2^{5/6} \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{6}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\ & \quad \left. \left(e \operatorname{Sec}[c+dx]\right)^{2/3} \left(1+\operatorname{Sec}[c+dx]\right)^{1/6} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right) / \left(d \left(\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2\right)^{1/3} \right. \\ & \quad \sqrt{a \left(1+\operatorname{Sec}[c+dx]\right)} \left(9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{6}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\ & \quad \left. \left(-2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{6}, \frac{4}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\ & \quad \left. \left. \operatorname{AppellF1}\left[\frac{3}{2}, \frac{7}{6}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \\ & \quad \left. \left(\left(9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{6}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \right. \\ & \quad \left. \left. \left(\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2\right)^{2/3} \left(1+\operatorname{Sec}[c+dx]\right)^{1/6}\right) / \right. \right. \\ & \quad \left. \left(2^{1/6} \left(9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{6}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \right. \\ & \quad \left. \left. \left(-2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{6}, \frac{4}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + \operatorname{AppellF1}\left[\frac{3}{2}, \right. \right. \right. \right. \\ & \quad \left. \left. \left. \frac{7}{6}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \right) - \\ & \quad \left. \left(3 \times 2^{5/6} \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{6}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\ & \quad \left. \left. \left(1+\operatorname{Sec}[c+dx]\right)^{1/6} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) / \right. \right. \\ & \quad \left. \left(\left(\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2\right)^{1/3} \left(9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{6}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \right. \\ & \quad \left. \left. \left(-2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{6}, \frac{4}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + \operatorname{AppellF1}\left[\frac{3}{2}, \right. \right. \right. \right. \\ & \quad \left. \left. \left. \frac{7}{6}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \right) + \\ & \quad \left. \left(9 \times 2^{5/6} \left(1+\operatorname{Sec}[c+dx]\right)^{1/6} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \left(-\frac{1}{9} \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{6}, \frac{4}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\ & \quad \left. \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \frac{1}{18} \operatorname{AppellF1}\left[\frac{3}{2}, \frac{7}{6}, \frac{1}{3}, \right. \right. \right. \right. \\ & \quad \left. \left. \left. \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right) \right) / \right. \\ & \quad \left. \left(\left(\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2\right)^{1/3} \left(9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{6}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \right. \\ & \quad \left. \left. \left(-2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{6}, \frac{4}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + \operatorname{AppellF1}\left[\frac{3}{2}, \right. \right. \right. \right. \end{aligned}$$

$$\begin{aligned}
 & \left. \left. \left. \left. \left. \frac{7}{6}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) - \right. \\
 & \left( 9 \times 2^{5/6} \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{6}, \frac{1}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] (1 + \operatorname{Sec}[c+dx])^{1/6} \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{2}(c+dx)\right] \left( \left( -2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{6}, \frac{4}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \operatorname{AppellF1}\left[\frac{3}{2}, \frac{7}{6}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{2}(c+dx)\right] + 9 \left( -\frac{1}{9} \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{6}, \frac{4}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{18} \operatorname{AppellF1}\left[\frac{3}{2}, \frac{7}{6}, \frac{1}{3}, \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) \right. \\
 & \left. \tan\left[\frac{1}{2}(c+dx)\right]^2 \left( -\frac{1}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{7}{6}, \frac{4}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{7}{10} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{13}{6}, \frac{1}{3}, \frac{7}{2}, \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] - \right. \\
 & \left. 2 \left( -\frac{4}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{6}, \frac{7}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{10} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{7}{6}, \frac{4}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+ \right. \right. \right. \\
 & \left. \left. \left. \left. dx\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) \right) \right) / \\
 & \left( \left( \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right)^{1/3} \left( 9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{6}, \frac{1}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
 & \left. \left( -2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{6}, \frac{4}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \operatorname{AppellF1}\left[\frac{3}{2}, \right. \right. \right. \\
 & \left. \left. \left. \left. \frac{7}{6}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) + \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{6}, \frac{1}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}[c+dx] \right. \\
 & \left. \tan\left[\frac{1}{2}(c+dx)\right] \tan[c+dx] \right) / \\
 & \left( 2^{1/6} \left( \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right)^{1/3} (1 + \operatorname{Sec}[c+dx])^{5/6} \right. \\
 & \left( 9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{6}, \frac{1}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \left( -2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{6}, \frac{4}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \operatorname{AppellF1}\left[\frac{3}{2}, \right. \right. \\
 & \left. \left. \left. \left. \frac{7}{6}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) \right) \right)
 \end{aligned}$$

Problem 281: Result more than twice size of optimal antiderivative.

$$\int \frac{(e \operatorname{Sec}[c + d x])^{1/3}}{\sqrt{a + a \operatorname{Sec}[c + d x]}} dx$$

Optimal (type 6, 76 leaves, 4 steps):

$$- \left( \left( 3 \operatorname{AppellF1} \left[ \frac{1}{3}, \frac{1}{2}, 1, \frac{4}{3}, \operatorname{Sec}[c + d x], -\operatorname{Sec}[c + d x] \right] (e \operatorname{Sec}[c + d x])^{1/3} \operatorname{Tan}[c + d x] \right) / \left( d \sqrt{1 - \operatorname{Sec}[c + d x]} \sqrt{a + a \operatorname{Sec}[c + d x]} \right) \right)$$

Result (type 6, 749 leaves):

$$\begin{aligned} & \left( 720 e \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{1}{6}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right. \\ & \quad \left. \operatorname{Cos} \left[ \frac{1}{2} (c + d x) \right] (1 + \operatorname{Cos}[c + d x])^2 \operatorname{Sin} \left[ \frac{1}{2} (c + d x) \right] \right. \\ & \quad \left( 9 \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{1}{6}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right] - \right. \\ & \quad \left( 4 \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{1}{6}, \frac{5}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \right. \\ & \quad \left. \left. \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{6}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right) \left. \right) / \\ & \left( d (e \operatorname{Sec}[c + d x])^{2/3} \sqrt{a (1 + \operatorname{Sec}[c + d x])} \right. \\ & \quad \left( 4320 \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{1}{6}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right]^2 \right. \\ & \quad \left. \operatorname{Cos} \left[ \frac{1}{2} (c + d x) \right]^6 (-1 + 4 \operatorname{Cos}[c + d x]) + \right. \\ & \quad 160 \left( 4 \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{1}{6}, \frac{5}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \operatorname{AppellF1} \left[ \frac{3}{2}, \right. \right. \\ & \quad \left. \left. \frac{5}{6}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right)^2 \operatorname{Cos}[c + d x] \operatorname{Sin} \left[ \frac{1}{2} (c + d x) \right]^4 + \\ & \quad 12 \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{1}{6}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right] \operatorname{Sin} \left[ \frac{1}{2} (c + d x) \right]^2 \\ & \quad \left( 20 \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{1}{6}, \frac{5}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right. \\ & \quad \left. (7 + 14 \operatorname{Cos}[c + d x] + 5 \operatorname{Cos}[2(c + d x)] - 2 \operatorname{Cos}[3(c + d x)]) + \right. \\ & \quad 5 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{6}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right] \\ & \quad \left. (7 + 14 \operatorname{Cos}[c + d x] + 5 \operatorname{Cos}[2(c + d x)] - 2 \operatorname{Cos}[3(c + d x)]) - \right. \\ & \quad 24 \left( 40 \operatorname{AppellF1} \left[ \frac{5}{2}, -\frac{1}{6}, \frac{8}{3}, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \right. \\ & \quad \left. 8 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{6}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right] - 5 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{11}{6}, \right. \right. \\ & \quad \left. \left. \frac{2}{3}, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) \operatorname{Cos}[c + d x] \operatorname{Sin} \left[ \frac{1}{2} (c + d x) \right]^2 \right) \left. \right) \end{aligned}$$



### Problem 282: Result more than twice size of optimal antiderivative.

$$\int \frac{1}{\left(e \operatorname{Sec}[c+dx]\right)^{1/3} \sqrt{a+a \operatorname{Sec}[c+dx]}} dx$$

Optimal (type 6, 76 leaves, 4 steps):

$$\frac{3 \operatorname{AppellF1}\left[-\frac{1}{3}, \frac{1}{2}, 1, \frac{2}{3}, \operatorname{Sec}[c+dx], -\operatorname{Sec}[c+dx]\right] \operatorname{Tan}[c+dx]}{d \sqrt{1-\operatorname{Sec}[c+dx]} \left(e \operatorname{Sec}[c+dx]\right)^{1/3} \sqrt{a+a \operatorname{Sec}[c+dx]}}$$

Result (type 6, 5151 leaves):

$$\begin{aligned} & - \left( \left( 3 \left( \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Sec}[c+dx] \right)^{1/6} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \right. \right. \\ & \quad \left. \left( 1 + \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{6}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right) / \right. \\ & \quad \left. \left( \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \right. \right. \\ & \quad \left. \left( 9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{6}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\ & \quad \left. \left( -2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{6}, \frac{4}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + \operatorname{AppellF1}\left[\frac{3}{2}, \right. \right. \\ & \quad \left. \left. \frac{7}{6}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) - \\ & \quad \left. \left( 10 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{6}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) / \right. \\ & \quad \left. \left( \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \right. \right. \\ & \quad \left. \left( 15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{6}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\ & \quad \left. \left( -2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{6}, \frac{4}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + \operatorname{AppellF1}\left[\frac{5}{2}, \right. \right. \\ & \quad \left. \left. \frac{7}{6}, \frac{1}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) / \\ & \left( d \left( \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right)^{1/3} \left(e \operatorname{Sec}[c+dx]\right)^{1/3} \sqrt{a(1+\operatorname{Sec}[c+dx])} \right) \\ & \left( -3 \left( \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right)^{2/3} \left( \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Sec}[c+dx] \right)^{1/6} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right. \\ & \quad \left. \left( 1 + \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{6}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right) / \right. \\ & \quad \left. \left( \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \right. \right. \\ & \quad \left. \left( 9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{6}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \end{aligned}$$



$$\begin{aligned}
 & \left( \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right) + \text{AppellF1}\left[\frac{3}{2}, \frac{7}{6}, \frac{1}{3}, \frac{5}{2}, \right. \\
 & \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - \\
 & \left( 10 \text{AppellF1}\left[\frac{3}{2}, \frac{1}{6}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \left. \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) / \left( \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( 15 \text{AppellF1}\left[\frac{3}{2}, \frac{1}{6}, \frac{1}{3}, \frac{5}{2}, \right. \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] + \left( -2 \text{AppellF1}\left[\frac{5}{2}, \frac{1}{6}, \frac{4}{3}, \frac{7}{2}, \right. \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] + \text{AppellF1}\left[\frac{5}{2}, \frac{7}{6}, \frac{1}{3}, \frac{7}{2}, \right. \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) - \\
 & \frac{1}{\left( \sec\left[\frac{1}{2}(c+dx)\right]^2 \right)^{1/3}} 3 \left( \cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx] \right)^{1/6} \tan\left[\frac{1}{2}(c+dx)\right] \\
 & \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \\
 & \left( - \left( \left( 3 \text{AppellF1}\left[\frac{1}{2}, \frac{1}{6}, \frac{1}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{2}(c+dx)\right] \right) / \left( \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \left( 9 \text{AppellF1}\left[\frac{1}{2}, \frac{1}{6}, \frac{1}{3}, \frac{3}{2}, \right. \right. \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] + \left( -2 \text{AppellF1}\left[\frac{3}{2}, \frac{1}{6}, \frac{4}{3}, \frac{5}{2}, \right. \right. \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] + \text{AppellF1}\left[\frac{3}{2}, \frac{7}{6}, \frac{1}{3}, \frac{5}{2}, \right. \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) + \\
 & \left( 3 \left( -\frac{1}{9} \text{AppellF1}\left[\frac{3}{2}, \frac{1}{6}, \frac{4}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right. \right. \\
 & \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{18} \text{AppellF1}\left[\frac{3}{2}, \frac{7}{6}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) / \\
 & \left( \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( 9 \text{AppellF1}\left[\frac{1}{2}, \frac{1}{6}, \frac{1}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] + \left( -2 \text{AppellF1}\left[\frac{3}{2}, \frac{1}{6}, \frac{4}{3}, \frac{5}{2}, \right. \right. \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] + \text{AppellF1}\left[\frac{3}{2}, \frac{7}{6}, \frac{1}{3}, \frac{5}{2}, \right. \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) + \\
 & \left( 10 \text{AppellF1}\left[\frac{3}{2}, \frac{1}{6}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right. \\
 & \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^3 \right) / \left( \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \left( 15 \text{AppellF1}\left[\frac{3}{2}, \right. \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \begin{aligned}
 & \frac{1}{6}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 + \left(-2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{6}, \frac{4}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \operatorname{AppellF1}\left[\frac{5}{2}, \frac{7}{6}, \frac{1}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - \\
 & \left(10 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{6}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right) / \left(\left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)\right) \\
 & \left(15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{6}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \left. \left(-2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{6}, \frac{4}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
 & \left. \left. \operatorname{AppellF1}\left[\frac{5}{2}, \frac{7}{6}, \frac{1}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \right) \right. \\
 & \left. \tan\left[\frac{1}{2}(c+dx)\right]^2\right) - \left(10 \tan\left[\frac{1}{2}(c+dx)\right]^2 \left(-\frac{1}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{6}, \frac{4}{3}, \frac{7}{2}, \right. \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \right. \\
 & \left. \left. \frac{1}{10} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{7}{6}, \frac{1}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
 & \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right) \right) / \left(\left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)\right) \left(15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{6}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
 & \left. \left. \left(-2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{6}, \frac{4}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \operatorname{AppellF1}\left[\frac{5}{2}, \frac{7}{6}, \frac{1}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \right) - \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{6}, \frac{1}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \left. \left(\left(-2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{6}, \frac{4}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \operatorname{AppellF1}\left[\frac{3}{2}, \frac{7}{6}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{2}(c+dx)\right] + 9 \left(-\frac{1}{9} \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{6}, \frac{4}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \right. \\
 & \left. \left. \left. - \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{18} \operatorname{AppellF1}\left[\frac{3}{2}, \frac{7}{6}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]\right) + \tan\left[\frac{1}{2}(c+dx)\right]^2 \left(-\frac{1}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{7}{6}, \frac{4}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \right. \\
 & \left. \left. \frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \\
 \end{aligned}
 \end{aligned}$$

$$\begin{aligned}
 & \frac{7}{10} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{13}{6}, \frac{1}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \\
 & \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] - 2\left(-\frac{4}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{6}, \frac{7}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \left. \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{10} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{7}{6}, \frac{4}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right)\right) \Big/ \\
 & \left(\left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)\left(9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{6}, \frac{1}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \left(-2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{6}, \frac{4}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \operatorname{AppellF1}\left[\frac{3}{2}, \frac{7}{6}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2 + \right. \\
 & \left. \left(10 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{6}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \tan\left[\frac{1}{2}(c+dx)\right]^2\right)\right. \\
 & \left.\left(\left(-2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{6}, \frac{4}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \operatorname{AppellF1}\left[\frac{5}{2}, \frac{7}{6}, \frac{1}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + 15\left(-\frac{1}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{6}, \frac{4}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{10} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{7}{6}, \frac{1}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right)\right) + \\
 & \tan\left[\frac{1}{2}(c+dx)\right]^2\left(-\frac{5}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{7}{6}, \frac{4}{3}, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \left. \frac{5}{6} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{13}{6}, \frac{1}{3}, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] - 2\left(-\frac{20}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{1}{6}, \frac{7}{3}, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{2}(c+dx)\right] + \frac{5}{42} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{7}{6}, \frac{4}{3}, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right)\right)\right) \Big/
 \end{aligned}$$

$$\begin{aligned}
 & \left( \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( 15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{6}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right] + \left( -2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{6}, \frac{4}{3}, \frac{7}{2}, \right. \right. \right. \\
 & \quad \quad \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right] + \operatorname{AppellF1}\left[\frac{5}{2}, \frac{7}{6}, \frac{1}{3}, \frac{7}{2}, \right. \right. \\
 & \quad \quad \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \Bigg) - \\
 & \frac{1}{2 \left( \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right)^{1/3} \left( \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Sec}[c+dx] \right)^{5/6}} \\
 & \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \\
 & \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \\
 & \left( 1 + \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{6}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right] \right) \Bigg) / \right. \\
 & \left( \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( 9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{6}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right] + \left( -2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{6}, \frac{4}{3}, \frac{5}{2}, \right. \right. \right. \\
 & \quad \quad \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right] + \operatorname{AppellF1}\left[\frac{3}{2}, \frac{7}{6}, \frac{1}{3}, \frac{5}{2}, \right. \right. \\
 & \quad \quad \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \Bigg) - \\
 & \left( 10 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{6}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right] \right. \\
 & \quad \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) / \left( \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right. \\
 & \quad \left( 15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{6}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right] + \right. \\
 & \quad \left( -2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{6}, \frac{4}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right] + \right. \\
 & \quad \quad \left. \operatorname{AppellF1}\left[\frac{5}{2}, \frac{7}{6}, \frac{1}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \Bigg) \\
 & \left( -\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] \operatorname{Sec}[c+dx] \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \quad \left. \operatorname{Sec}[c+dx] \operatorname{Tan}[c+dx] \right) \Bigg) \Bigg) \Bigg) \Bigg) \Bigg)
 \end{aligned}$$

Problem 283: Result more than twice size of optimal antiderivative.

$$\int \frac{1}{(e \operatorname{Sec}[c + d x])^{2/3} \sqrt{a + a \operatorname{Sec}[c + d x]}} dx$$

Optimal (type 6, 78 leaves, 4 steps):

$$\frac{3 \operatorname{AppellF1}\left[-\frac{2}{3}, \frac{1}{2}, 1, \frac{1}{3}, \operatorname{Sec}[c + d x], -\operatorname{Sec}[c + d x]\right] \operatorname{Tan}[c + d x]}{2 d \sqrt{1 - \operatorname{Sec}[c + d x]} (e \operatorname{Sec}[c + d x])^{2/3} \sqrt{a + a \operatorname{Sec}[c + d x]}}$$

Result (type 6, 2819 leaves):

$$\begin{aligned} & \left( \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] \operatorname{Sec}[c + d x]^2 \left( -\frac{3}{2} \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] + \frac{3}{2} \operatorname{Sin}\left[\frac{3}{2}(c + d x)\right] \right) \right) / \\ & \left( d (e \operatorname{Sec}[c + d x])^{2/3} \sqrt{a (1 + \operatorname{Sec}[c + d x])} \right) + \\ & \left( \left( -\frac{3}{4 \operatorname{Sec}[c + d x]^{1/6}} + \frac{1}{4} \operatorname{Sec}[c + d x]^{5/6} \right) \operatorname{Sec}[c + d x]^{7/6} \right. \\ & \left( \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right]^2 \operatorname{Sec}[c + d x] \right)^{5/6} \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] \\ & \left( -\operatorname{Cos}[c + d x]^{5/6} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{5}{6}, \frac{3}{2}, 2 \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^2 + \right. \\ & \left. \left( 10 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{6}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2\right] \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2 \right) / \right. \\ & \left. \left( 15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{6}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2\right] + \right. \right. \\ & \left. \left( -4 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{6}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2\right] + 5 \operatorname{AppellF1}\left[\frac{5}{2}, \right. \right. \right. \\ & \left. \left. \left. \frac{11}{6}, \frac{2}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2\right] \right) \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2 \right) \right) / \\ & \left( d \left( \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^2 \right)^{2/3} (e \operatorname{Sec}[c + d x])^{2/3} \sqrt{a (1 + \operatorname{Sec}[c + d x])} \right) \\ & \left( \frac{1}{2} \left( \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^2 \right)^{1/3} \left( \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right]^2 \operatorname{Sec}[c + d x] \right)^{5/6} \right. \\ & \left( -\operatorname{Cos}[c + d x]^{5/6} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{5}{6}, \frac{3}{2}, 2 \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^2 + \right. \\ & \left. \left( 10 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{6}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2\right] \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2 \right) / \right. \\ & \left. \left( 15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{6}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2\right] + \right. \right. \\ & \left. \left( -4 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{6}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2\right] + 5 \operatorname{AppellF1}\left[\frac{5}{2}, \right. \right. \right. \\ & \left. \left. \left. \frac{11}{6}, \frac{2}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2\right] \right) \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2 \right) \right) - \\ & \frac{1}{3 \left( \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^2 \right)^{2/3}} 2 \left( \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right]^2 \operatorname{Sec}[c + d x] \right)^{5/6} \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2 \end{aligned}$$

$$\begin{aligned}
 & \left( -\text{Cos}[c+dx]^{5/6} \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{5}{6}, \frac{3}{2}, 2 \text{Sin}\left[\frac{1}{2}(c+dx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 + \right. \\
 & \left. \left( 10 \text{AppellF1}\left[\frac{3}{2}, \frac{5}{6}, \frac{2}{3}, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
 & \quad \left. \left. \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) / \right. \\
 & \left. \left( 15 \text{AppellF1}\left[\frac{3}{2}, \frac{5}{6}, \frac{2}{3}, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
 & \quad \left. \left( -4 \text{AppellF1}\left[\frac{5}{2}, \frac{5}{6}, \frac{5}{3}, \frac{7}{2}, \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + 5 \text{AppellF1}\left[\frac{5}{2}, \right. \right. \right. \\
 & \quad \quad \left. \left. \frac{11}{6}, \frac{2}{3}, \frac{7}{2}, \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) + \\
 & \frac{1}{\left(\text{Sec}\left[\frac{1}{2}(c+dx)\right]^2\right)^{2/3}} \left( \text{Cos}\left[\frac{1}{2}(c+dx)\right]^2 \text{Sec}[c+dx] \right)^{5/6} \text{Tan}\left[\frac{1}{2}(c+dx)\right] \\
 & \left( -\frac{1}{2} \text{Cos}[c+dx]^{5/6} \text{Csc}\left[\frac{1}{2}(c+dx)\right] \text{Sec}\left[\frac{1}{2}(c+dx)\right] \right. \\
 & \left. \left( -\text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{5}{6}, \frac{3}{2}, 2 \text{Sin}\left[\frac{1}{2}(c+dx)\right]^2\right] + \frac{1}{\left(1-2 \text{Sin}\left[\frac{1}{2}(c+dx)\right]^2\right)^{5/6}} \right) + \right. \\
 & \left. \left( 5 \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{5}{6}, \frac{3}{2}, 2 \text{Sin}\left[\frac{1}{2}(c+dx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \text{Sin}[c+dx] \right) / \right. \\
 & \left. \left( 6 \text{Cos}[c+dx]^{1/6} \right) - \text{Cos}[c+dx]^{5/6} \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{5}{6}, \frac{3}{2}, 2 \text{Sin}\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \text{Tan}\left[\frac{1}{2}(c+dx)\right] + \left( 10 \text{AppellF1}\left[\frac{3}{2}, \frac{5}{6}, \frac{2}{3}, \frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \text{Tan}\left[\frac{1}{2}(c+dx)\right] \right) / \\
 & \left( 15 \text{AppellF1}\left[\frac{3}{2}, \frac{5}{6}, \frac{2}{3}, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad \left. \left( -4 \text{AppellF1}\left[\frac{5}{2}, \frac{5}{6}, \frac{5}{3}, \frac{7}{2}, \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + 5 \text{AppellF1}\left[\frac{5}{2}, \right. \right. \right. \\
 & \quad \quad \left. \left. \frac{11}{6}, \frac{2}{3}, \frac{7}{2}, \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) + \\
 & \left( 10 \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \left( -\frac{2}{5} \text{AppellF1}\left[\frac{5}{2}, \frac{5}{6}, \frac{5}{3}, \frac{7}{2}, \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
 & \quad \left. \left. \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \text{Tan}\left[\frac{1}{2}(c+dx)\right] + \frac{1}{2} \text{AppellF1}\left[\frac{5}{2}, \frac{11}{6}, \frac{2}{3}, \frac{7}{2}, \right. \right. \right. \\
 & \quad \quad \left. \left. \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \text{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \right) / \\
 & \left( 15 \text{AppellF1}\left[\frac{3}{2}, \frac{5}{6}, \frac{2}{3}, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad \left. \left( -4 \text{AppellF1}\left[\frac{5}{2}, \frac{5}{6}, \frac{5}{3}, \frac{7}{2}, \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + 5 \text{AppellF1}\left[\frac{5}{2}, \right. \right. \right. \\
 & \quad \quad \left. \left. \frac{11}{6}, \frac{2}{3}, \frac{7}{2}, \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right)
 \end{aligned}$$



$$\begin{aligned}
 & \left. \left( \frac{11}{6}, \frac{2}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - \right. \\
 & \left( 10 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{6}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \left. \left( \left( -4 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{6}, \frac{5}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \right. \\
 & \left. \left. \left. 5 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{11}{6}, \frac{2}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right. \right. \\
 & \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + 15 \left( -\frac{2}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{6}, \frac{5}{3}, \frac{7}{2}, \right. \right. \right. \right. \\
 & \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \right. \right. \\
 & \left. \left. \frac{1}{2} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{11}{6}, \frac{2}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
 & \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \left. \left( -4 \left( -\frac{25}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{5}{6}, \frac{8}{3}, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \right. \\
 & \left. \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \right. \right. \\
 & \left. \left. \frac{25}{42} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{11}{6}, \frac{5}{3}, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
 & \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + 5 \left( -\frac{10}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{11}{6}, \right. \right. \right. \\
 & \left. \left. \left. \frac{5}{3}, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{2}(c+dx)\right] + \frac{55}{42} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{17}{6}, \frac{2}{3}, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) \Big/ \\
 & \left( 15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{6}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \left( -4 \operatorname{AppellF1}\left[ \right. \right. \right. \\
 & \left. \left. \left. \frac{5}{2}, \frac{5}{6}, \frac{5}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] + 5 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{11}{6}, \right. \right. \right. \\
 & \left. \left. \left. \frac{2}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \Big) + \\
 & \frac{1}{6 \left( \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right)^{2/3} \left( \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Sec}[c+dx] \right)^{1/6}} 5 \tan\left[\frac{1}{2}(c+dx)\right] \\
 & \left( -\operatorname{Cos}[c+dx]^{5/6} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{5}{6}, \frac{3}{2}, 2 \sin\left[\frac{1}{2}(c+dx)\right]^2 \right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 + \right. \\
 & \left. \left( 10 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{6}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \Big/ \right)
 \end{aligned}$$

$$\left( \begin{aligned} & \left( 15 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{6}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\ & \left( -4 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{6}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] + 5 \operatorname{AppellF1} \left[ \frac{5}{2}, \right. \right. \\ & \left. \left. \frac{11}{6}, \frac{2}{3}, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \\ & \left( -\operatorname{Cos} \left[ \frac{1}{2} (c+dx) \right] \operatorname{Sec} [c+dx] \operatorname{Sin} \left[ \frac{1}{2} (c+dx) \right] + \operatorname{Cos} \left[ \frac{1}{2} (c+dx) \right]^2 \right. \\ & \left. \left. \operatorname{Sec} [c+dx] \operatorname{Tan} [c+dx] \right) \right) \end{aligned} \right)$$

**Problem 284: Result more than twice size of optimal antiderivative.**

$$\int \operatorname{Sec} [c+dx]^{4/3} (a+a \operatorname{Sec} [c+dx])^{1/3} dx$$

Optimal (type 6, 78 leaves, 3 steps):

$$\left( 2^{5/6} \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{1}{3}, \frac{1}{6}, \frac{3}{2}, 1-\operatorname{Sec} [c+dx], \frac{1}{2} (1-\operatorname{Sec} [c+dx]) \right] \right) \left( a+a \operatorname{Sec} [c+dx] \right)^{1/3} \operatorname{Tan} [c+dx] \Big/ \left( d (1+\operatorname{Sec} [c+dx])^{5/6} \right)$$

Result (type 6, 1982 leaves):

$$\left( \begin{aligned} & \left( 3 \operatorname{Sec} [c+dx]^{1/3} \left( (1+\operatorname{Cos} [c+dx]) \operatorname{Sec} [c+dx] \right)^{1/3} (a(1+\operatorname{Sec} [c+dx]))^{1/3} \operatorname{Sin} [c+dx] \right) \Big/ \\ & \left( 2d(1+\operatorname{Sec} [c+dx])^{1/3} \right) + \\ & \left( 3(a(1+\operatorname{Sec} [c+dx]))^{1/3} \left( -\frac{(1+\operatorname{Sec} [c+dx])^{1/3}}{\operatorname{Sec} [c+dx]^{2/3}} + \frac{1}{2} \operatorname{Sec} [c+dx]^{1/3} (1+\operatorname{Sec} [c+dx])^{1/3} \right) \right. \\ & \left. \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] \left( -1 + \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \right) \Big/ \right. \\ & \left( 9 \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] - \right. \\ & \left. 2 \left( 2 \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \right. \\ & \left. \left. \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{2}{3}, \frac{3}{4} \right\}, \left\{ \frac{7}{4} \right\}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^4 \right] \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) \Big/ \right. \\ & \left( 2^{2/3} d \left( \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \right)^{2/3} \left( \operatorname{Cos} \left[ \frac{1}{2} (c+dx) \right]^2 \operatorname{Sec} [c+dx] \right)^{1/3} (1+\operatorname{Sec} [c+dx])^{1/3} \right. \\ & \left. \left( 3 \left( \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \right)^{1/3} \right. \right. \\ & \left. \left. \left( -1 + \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \right) \right) \Big/ \right) \end{aligned} \right)$$

$$\begin{aligned}
& \left( 9 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \\
& \quad \left. 2 \left( 2 \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
& \quad \quad \left. \left. \operatorname{HypergeometricPFQ}\left[\left\{\frac{2}{3}, \frac{3}{4}\right\}, \left\{\frac{7}{4}\right\}, \tan\left[\frac{1}{2}(c+dx)\right]^4\right]\right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) / \\
& \left( 2 \times 2^{2/3} \left( \cos\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Sec}[c+dx] \right)^{1/3} \right) - \left( 2^{1/3} \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \\
& \quad \left( -1 + \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right) / \\
& \quad \left( 9 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \\
& \quad \quad \left. 2 \left( 2 \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
& \quad \quad \quad \left. \left. \operatorname{HypergeometricPFQ}\left[\left\{\frac{2}{3}, \frac{3}{4}\right\}, \left\{\frac{7}{4}\right\}, \tan\left[\frac{1}{2}(c+dx)\right]^4\right]\right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) / \\
& \left( \left( \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right)^{2/3} \left( \cos\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Sec}[c+dx] \right)^{1/3} \right) + \right. \\
& \quad \left. 1 \right) \\
& \frac{2^{2/3} \left( \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right)^{2/3} \left( \cos\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Sec}[c+dx] \right)^{1/3}}{3 \tan\left[\frac{1}{2}(c+dx)\right] \left( \left( 3 \left( -\frac{2}{9} \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \right. \right. \\
& \quad \left. \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] - \frac{1}{9} \operatorname{HypergeometricPFQ}\left[ \right. \right. \right. \right. \right. \\
& \quad \left. \left. \left. \left. \left\{\frac{2}{3}, \frac{3}{4}\right\}, \left\{\frac{7}{4}\right\}, \tan\left[\frac{1}{2}(c+dx)\right]^4 \right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) \right) / \\
& \quad \left( 9 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \\
& \quad \quad \left. 2 \left( 2 \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
& \quad \quad \quad \left. \left. \operatorname{HypergeometricPFQ}\left[\left\{\frac{2}{3}, \frac{3}{4}\right\}, \left\{\frac{7}{4}\right\}, \tan\left[\frac{1}{2}(c+dx)\right]^4\right]\right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - \right. \\
& \quad \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \\
& \quad \left( -2 \left( 2 \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
& \quad \quad \left. \left. \operatorname{HypergeometricPFQ}\left[\left\{\frac{2}{3}, \frac{3}{4}\right\}, \left\{\frac{7}{4}\right\}, \tan\left[\frac{1}{2}(c+dx)\right]^4\right]\right) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right) \\
& \quad \tan\left[\frac{1}{2}(c+dx)\right] + 9 \left( -\frac{2}{9} \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] - \right.
\end{aligned}$$

$$\begin{aligned}
 & \frac{1}{9} \text{HypergeometricPFQ}\left[\left\{\frac{2}{3}, \frac{3}{4}\right\}, \left\{\frac{7}{4}\right\}, \tan\left[\frac{1}{2}(c+dx)\right]^4\right] \\
 & \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] - 2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \left(2 \left(-\text{AppellF1}\left[\frac{5}{2}, -\frac{1}{3}, \frac{8}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right.\right. \\
 & \quad \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] - \frac{1}{5} \text{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{5}{3}, \frac{7}{2}, \right. \\
 & \quad \left.\tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right. \\
 & \quad \left. + \frac{3}{2} \text{Csc}\left[\frac{1}{2}(c+dx)\right] \text{Sec}\left[\frac{1}{2}(c+dx)\right] \left(-\text{HypergeometricPFQ}\left[\right.\right. \\
 & \quad \left.\left.\left\{\frac{2}{3}, \frac{3}{4}\right\}, \left\{\frac{7}{4}\right\}, \tan\left[\frac{1}{2}(c+dx)\right]^4\right] + \frac{1}{\left(1 - \tan\left[\frac{1}{2}(c+dx)\right]^4\right)^{2/3}}\right)\right)\right) / \\
 & \left(9 \text{AppellF1}\left[\frac{1}{2}, -\frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \right. \\
 & \quad \left(2 \text{AppellF1}\left[\frac{3}{2}, -\frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad \left. \text{HypergeometricPFQ}\left[\left\{\frac{2}{3}, \frac{3}{4}\right\}, \left\{\frac{7}{4}\right\}, \tan\left[\frac{1}{2}(c+dx)\right]^4\right] \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2 \right) - \\
 & \left(\tan\left[\frac{1}{2}(c+dx)\right] \left(-1 + \left(3 \text{AppellF1}\left[\frac{1}{2}, -\frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right.\right.\right. \right. \\
 & \quad \left.\left.\left.-\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right)\right) / \right. \\
 & \quad \left(9 \text{AppellF1}\left[\frac{1}{2}, -\frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \\
 & \quad \left. 2 \left(2 \text{AppellF1}\left[\frac{3}{2}, -\frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right.\right. \\
 & \quad \left. \left. \text{HypergeometricPFQ}\left[\left\{\frac{2}{3}, \frac{3}{4}\right\}, \left\{\frac{7}{4}\right\}, \tan\left[\frac{1}{2}(c+dx)\right]^4\right] \tan\left[\frac{1}{2}(c+dx)\right]^2\right)\right) \right. \\
 & \quad \left(-\cos\left[\frac{1}{2}(c+dx)\right] \text{Sec}[c+dx] \sin\left[\frac{1}{2}(c+dx)\right] + \cos\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \quad \left. \text{Sec}[c+dx] \tan[c+dx]\right) \right) / \\
 & \left(2^{2/3} \left(\text{Sec}\left[\frac{1}{2}(c+dx)\right]^2\right)^{2/3} \left(\cos\left[\frac{1}{2}(c+dx)\right]^2 \text{Sec}[c+dx]\right)^{4/3}\right) \right)
 \end{aligned}$$

**Problem 285:** Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \text{Sec}[c + d x]^{4/3} (a + a \text{Sec}[c + d x])^{2/3} dx$$

Optimal (type 6, 79 leaves, 3 steps):

$$\left( 2 \times 2^{1/6} \text{AppellF1}\left[\frac{1}{2}, -\frac{1}{3}, -\frac{1}{6}, \frac{3}{2}, 1 - \text{Sec}[c + d x], \frac{1}{2} (1 - \text{Sec}[c + d x])\right] \right. \\ \left. (a + a \text{Sec}[c + d x])^{2/3} \text{Tan}[c + d x] \right) / \left( d (1 + \text{Sec}[c + d x])^{7/6} \right)$$

Result (type 6, 3726 leaves):

$$\left( \text{Sec}[c + d x]^{1/3} \left( (1 + \text{Cos}[c + d x]) \text{Sec}[c + d x] \right)^{2/3} (a (1 + \text{Sec}[c + d x]))^{2/3} \text{Tan}\left[\frac{1}{2} (c + d x)\right] \right) / \\ \left( d (1 + \text{Sec}[c + d x])^{2/3} \right) + \\ \left( 15 \times 2^{2/3} \text{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \text{Tan}\left[\frac{1}{4} (c + d x)\right]^2, -\text{Tan}\left[\frac{1}{4} (c + d x)\right]^2\right] \right. \\ \text{Sec}\left[\frac{1}{2} (c + d x)\right] (a (1 + \text{Sec}[c + d x]))^{2/3} \\ \left( 9 \text{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \text{Tan}\left[\frac{1}{4} (c + d x)\right]^2, -\text{Tan}\left[\frac{1}{4} (c + d x)\right]^2\right] - 2 \text{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \right. \right. \\ \left. \left. \text{Tan}\left[\frac{1}{4} (c + d x)\right]^2, -\text{Tan}\left[\frac{1}{4} (c + d x)\right]^2\right] \text{Tan}\left[\frac{1}{4} (c + d x)\right]^2 + 4 \text{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \right. \right. \\ \left. \left. \frac{5}{2}, \text{Tan}\left[\frac{1}{4} (c + d x)\right]^2, -\text{Tan}\left[\frac{1}{4} (c + d x)\right]^2\right] \text{Tan}\left[\frac{1}{4} (c + d x)\right]^2 \right) \right) / \\ \left( d \text{Sec}[c + d x]^{2/3} \left( 9 \text{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \text{Tan}\left[\frac{1}{4} (c + d x)\right]^2, -\text{Tan}\left[\frac{1}{4} (c + d x)\right]^2\right] - \right. \right. \\ \left. \left. 2 \left( \text{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \text{Tan}\left[\frac{1}{4} (c + d x)\right]^2, -\text{Tan}\left[\frac{1}{4} (c + d x)\right]^2\right] - \right. \right. \right. \\ \left. \left. \left. 2 \text{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \text{Tan}\left[\frac{1}{4} (c + d x)\right]^2, -\text{Tan}\left[\frac{1}{4} (c + d x)\right]^2\right] \right) \text{Tan}\left[\frac{1}{4} (c + d x)\right]^2 \right) \right) \\ \left( 405 \times 2^{2/3} \text{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \text{Tan}\left[\frac{1}{4} (c + d x)\right]^2, -\text{Tan}\left[\frac{1}{4} (c + d x)\right]^2\right]^2 \text{Cos}\left[\frac{1}{2} (c + d x)\right] + \right. \\ \left. 90 \times 2^{2/3} \text{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \text{Tan}\left[\frac{1}{4} (c + d x)\right]^2, -\text{Tan}\left[\frac{1}{4} (c + d x)\right]^2\right] \right. \\ \left. \text{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \text{Tan}\left[\frac{1}{4} (c + d x)\right]^2, -\text{Tan}\left[\frac{1}{4} (c + d x)\right]^2\right] \right. \\ \left. \text{Sec}\left[\frac{1}{4} (c + d x)\right]^2 \text{Sin}\left[\frac{1}{2} (c + d x)\right] \text{Tan}\left[\frac{1}{4} (c + d x)\right] - \right. \\ \left. 180 \times 2^{2/3} \text{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \text{Tan}\left[\frac{1}{4} (c + d x)\right]^2, -\text{Tan}\left[\frac{1}{4} (c + d x)\right]^2\right] \right. \\ \left. \text{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \text{Tan}\left[\frac{1}{4} (c + d x)\right]^2, -\text{Tan}\left[\frac{1}{4} (c + d x)\right]^2\right] \right. \\ \left. \text{Sec}\left[\frac{1}{4} (c + d x)\right]^2 \text{Sin}\left[\frac{1}{2} (c + d x)\right] \text{Tan}\left[\frac{1}{4} (c + d x)\right] - \right. \\ \left. 90 \times 2^{2/3} \text{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \text{Tan}\left[\frac{1}{4} (c + d x)\right]^2, -\text{Tan}\left[\frac{1}{4} (c + d x)\right]^2\right] \text{AppellF1}\left[\frac{3}{2}, \right. \right. \\ \left. \left. \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \text{Tan}\left[\frac{1}{4} (c + d x)\right]^2, -\text{Tan}\left[\frac{1}{4} (c + d x)\right]^2\right] \text{Cos}\left[\frac{1}{2} (c + d x)\right] \text{Tan}\left[\frac{1}{4} (c + d x)\right]^2 + \right.$$



$$\begin{aligned}
 & \text{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{4}(c+dx)\right]^2, -\tan\left[\frac{1}{4}(c+dx)\right]^2\right] \\
 & \sin\left[\frac{1}{2}(c+dx)\right] \tan\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \Big) - \\
 & \left( \left( \sec\left[\frac{1}{2}(c+dx)\right]^2 \right)^{4/3} \sec[c+dx]^{1/3} (a(1+\sec[c+dx]))^{2/3} \right. \\
 & \left. \frac{\text{AppellF1}\left[-\frac{2}{3}, -\frac{1}{3}, -\frac{1}{3}, \frac{1}{3}, -\frac{1+i}{-1+\tan\left[\frac{1}{2}(c+dx)\right]}, -\frac{1-i}{-1+\tan\left[\frac{1}{2}(c+dx)\right]}\right]}{\left(\frac{-i+\tan\left[\frac{1}{2}(c+dx)\right]}{-1+\tan\left[\frac{1}{2}(c+dx)\right]}\right)^{1/3} \left(\frac{i+\tan\left[\frac{1}{2}(c+dx)\right]}{-1+\tan\left[\frac{1}{2}(c+dx)\right]}\right)^{1/3}} \right. \\
 & \left. \frac{\text{AppellF1}\left[-\frac{2}{3}, -\frac{1}{3}, -\frac{1}{3}, \frac{1}{3}, \frac{1-i}{1+\tan\left[\frac{1}{2}(c+dx)\right]}, \frac{1+i}{1+\tan\left[\frac{1}{2}(c+dx)\right]}\right]}{\left(\frac{-i+\tan\left[\frac{1}{2}(c+dx)\right]}{1+\tan\left[\frac{1}{2}(c+dx)\right]}\right)^{1/3} \left(\frac{i+\tan\left[\frac{1}{2}(c+dx)\right]}{1+\tan\left[\frac{1}{2}(c+dx)\right]}\right)^{1/3}} \right) \Big) / \\
 & \left( 2^{1/3} d \left( -\frac{1}{2^{1/3}} \left( \sec\left[\frac{1}{2}(c+dx)\right]^2 \right)^{1/3} \tan\left[\frac{1}{2}(c+dx)\right] \right. \right. \\
 & \left. \left. \frac{\text{AppellF1}\left[-\frac{2}{3}, -\frac{1}{3}, -\frac{1}{3}, \frac{1}{3}, -\frac{1+i}{-1+\tan\left[\frac{1}{2}(c+dx)\right]}, -\frac{1-i}{-1+\tan\left[\frac{1}{2}(c+dx)\right]}\right]}{\left(\frac{-i+\tan\left[\frac{1}{2}(c+dx)\right]}{-1+\tan\left[\frac{1}{2}(c+dx)\right]}\right)^{1/3} \left(\frac{i+\tan\left[\frac{1}{2}(c+dx)\right]}{-1+\tan\left[\frac{1}{2}(c+dx)\right]}\right)^{1/3}} \right. \right. \\
 & \left. \left. \frac{\text{AppellF1}\left[-\frac{2}{3}, -\frac{1}{3}, -\frac{1}{3}, \frac{1}{3}, \frac{1-i}{1+\tan\left[\frac{1}{2}(c+dx)\right]}, \frac{1+i}{1+\tan\left[\frac{1}{2}(c+dx)\right]}\right]}{\left(\frac{-i+\tan\left[\frac{1}{2}(c+dx)\right]}{1+\tan\left[\frac{1}{2}(c+dx)\right]}\right)^{1/3} \left(\frac{i+\tan\left[\frac{1}{2}(c+dx)\right]}{1+\tan\left[\frac{1}{2}(c+dx)\right]}\right)^{1/3}} \right) \right) - \\
 & \frac{1}{2^{1/3}} 3 \left( \sec\left[\frac{1}{2}(c+dx)\right]^2 \right)^{1/3} \left( \left( \left( \frac{1-i}{3} \right) \text{AppellF1}\left[\frac{1}{3}, -\frac{1}{3}, \frac{2}{3}, \frac{4}{3}, -\frac{1+i}{-1+\tan\left[\frac{1}{2}(c+dx)\right]}, \right. \right. \right. \\
 & \left. \left. \left. -\frac{1-i}{-1+\tan\left[\frac{1}{2}(c+dx)\right]}\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \right) / \left( -1+\tan\left[\frac{1}{2}(c+dx)\right] \right)^2 + \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( \left( \frac{1}{3} + \frac{i}{3} \right) \text{AppellF1} \left[ \frac{1}{3}, \frac{2}{3}, -\frac{1}{3}, \frac{4}{3}, -\frac{1+i}{-1+\tan\left[\frac{1}{2}(c+dx)\right]}, \right. \right. \\
 & \quad \left. \left. -\frac{1-i}{-1+\tan\left[\frac{1}{2}(c+dx)\right]} \right] \text{Sec} \left[ \frac{1}{2}(c+dx) \right]^2 \right) / \left( -1 + \tan \left[ \frac{1}{2}(c+dx) \right] \right)^2 \Big/ \\
 & \left( \left( \frac{-i+\tan\left[\frac{1}{2}(c+dx)\right]}{-1+\tan\left[\frac{1}{2}(c+dx)\right]} \right)^{1/3} \left( \frac{i+\tan\left[\frac{1}{2}(c+dx)\right]}{-1+\tan\left[\frac{1}{2}(c+dx)\right]} \right)^{1/3} \right) - \\
 & \left( \text{AppellF1} \left[ -\frac{2}{3}, -\frac{1}{3}, -\frac{1}{3}, \frac{1}{3}, -\frac{1+i}{-1+\tan\left[\frac{1}{2}(c+dx)\right]}, -\frac{1-i}{-1+\tan\left[\frac{1}{2}(c+dx)\right]} \right] \right. \\
 & \quad \left. \left( \frac{\text{Sec} \left[ \frac{1}{2}(c+dx) \right]^2}{2 \left( -1 + \tan \left[ \frac{1}{2}(c+dx) \right] \right)} - \frac{\text{Sec} \left[ \frac{1}{2}(c+dx) \right]^2 \left( -i + \tan \left[ \frac{1}{2}(c+dx) \right] \right)}{2 \left( -1 + \tan \left[ \frac{1}{2}(c+dx) \right] \right)^2} \right) \right) \Big/ \\
 & \left( 3 \left( \frac{-i+\tan\left[\frac{1}{2}(c+dx)\right]}{-1+\tan\left[\frac{1}{2}(c+dx)\right]} \right)^{4/3} \left( \frac{i+\tan\left[\frac{1}{2}(c+dx)\right]}{-1+\tan\left[\frac{1}{2}(c+dx)\right]} \right)^{1/3} \right) - \\
 & \left( \text{AppellF1} \left[ -\frac{2}{3}, -\frac{1}{3}, -\frac{1}{3}, \frac{1}{3}, -\frac{1+i}{-1+\tan\left[\frac{1}{2}(c+dx)\right]}, -\frac{1-i}{-1+\tan\left[\frac{1}{2}(c+dx)\right]} \right] \right. \\
 & \quad \left. \left( \frac{\text{Sec} \left[ \frac{1}{2}(c+dx) \right]^2}{2 \left( -1 + \tan \left[ \frac{1}{2}(c+dx) \right] \right)} - \frac{\text{Sec} \left[ \frac{1}{2}(c+dx) \right]^2 \left( i + \tan \left[ \frac{1}{2}(c+dx) \right] \right)}{2 \left( -1 + \tan \left[ \frac{1}{2}(c+dx) \right] \right)^2} \right) \right) \Big/ \\
 & \left( 3 \left( \frac{-i+\tan\left[\frac{1}{2}(c+dx)\right]}{-1+\tan\left[\frac{1}{2}(c+dx)\right]} \right)^{1/3} \left( \frac{i+\tan\left[\frac{1}{2}(c+dx)\right]}{-1+\tan\left[\frac{1}{2}(c+dx)\right]} \right)^{4/3} \right) - \\
 & \left( - \left( \left( \left( \frac{1}{3} + \frac{i}{3} \right) \text{AppellF1} \left[ \frac{1}{3}, -\frac{1}{3}, \frac{2}{3}, \frac{4}{3}, \frac{1-i}{1+\tan\left[\frac{1}{2}(c+dx)\right]}, \frac{1+i}{1+\tan\left[\frac{1}{2}(c+dx)\right]} \right] \right. \right. \right. \\
 & \quad \left. \left. \text{Sec} \left[ \frac{1}{2}(c+dx) \right]^2 \right) / \left( 1 + \tan \left[ \frac{1}{2}(c+dx) \right] \right)^2 - \left( \left( \frac{1}{3} - \frac{i}{3} \right) \text{AppellF1} \left[ \frac{1}{3}, \frac{2}{3}, \right. \right. \right. \\
 & \quad \left. \left. -\frac{1}{3}, \frac{4}{3}, \frac{1-i}{1+\tan\left[\frac{1}{2}(c+dx)\right]}, \frac{1+i}{1+\tan\left[\frac{1}{2}(c+dx)\right]} \right] \text{Sec} \left[ \frac{1}{2}(c+dx) \right]^2 \right) \Big/ \\
 & \quad \left( 1 + \tan \left[ \frac{1}{2}(c+dx) \right] \right)^2 \right) / \left( \left( \frac{-i+\tan\left[\frac{1}{2}(c+dx)\right]}{1+\tan\left[\frac{1}{2}(c+dx)\right]} \right)^{1/3} \left( \frac{i+\tan\left[\frac{1}{2}(c+dx)\right]}{1+\tan\left[\frac{1}{2}(c+dx)\right]} \right)^{1/3} \right) + \\
 & \left( \text{AppellF1} \left[ -\frac{2}{3}, -\frac{1}{3}, -\frac{1}{3}, \frac{1}{3}, \frac{1-i}{1+\tan\left[\frac{1}{2}(c+dx)\right]}, \frac{1+i}{1+\tan\left[\frac{1}{2}(c+dx)\right]} \right] \right.
 \end{aligned}$$



$$\left( -\frac{\sec\left[\frac{1}{2}(c+dx)\right]^2 \left(-i + \tan\left[\frac{1}{2}(c+dx)\right]\right)}{2 \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]\right)^2} + \frac{\sec\left[\frac{1}{2}(c+dx)\right]^2}{2 \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]\right)} \right) /$$

$$\left( 3 \left( \frac{-i + \tan\left[\frac{1}{2}(c+dx)\right]}{1 + \tan\left[\frac{1}{2}(c+dx)\right]} \right)^{4/3} \left( \frac{i + \tan\left[\frac{1}{2}(c+dx)\right]}{1 + \tan\left[\frac{1}{2}(c+dx)\right]} \right)^{1/3} \right) +$$

$$\left( \text{AppellF1}\left[-\frac{2}{3}, -\frac{1}{3}, -\frac{1}{3}, \frac{1}{3}, \frac{1-i}{1 + \tan\left[\frac{1}{2}(c+dx)\right]}, \frac{1+i}{1 + \tan\left[\frac{1}{2}(c+dx)\right]}\right] \right.$$

$$\left. \left( -\frac{\sec\left[\frac{1}{2}(c+dx)\right]^2 \left(i + \tan\left[\frac{1}{2}(c+dx)\right]\right)}{2 \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]\right)^2} + \frac{\sec\left[\frac{1}{2}(c+dx)\right]^2}{2 \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]\right)} \right) / \right.$$

$$\left. \left( 3 \left( \frac{-i + \tan\left[\frac{1}{2}(c+dx)\right]}{1 + \tan\left[\frac{1}{2}(c+dx)\right]} \right)^{1/3} \left( \frac{i + \tan\left[\frac{1}{2}(c+dx)\right]}{1 + \tan\left[\frac{1}{2}(c+dx)\right]} \right)^{4/3} \right) \right)$$

**Problem 287: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{(a + a \sec[c + dx])^{4/3}}{\sec[c + dx]^{1/3}} dx$$

Optimal (type 6, 80 leaves, 3 steps):

$$\left( 2 \times 2^{5/6} a \text{AppellF1}\left[\frac{1}{2}, \frac{4}{3}, -\frac{5}{6}, \frac{3}{2}, 1 - \sec[c + dx], \frac{1}{2}(1 - \sec[c + dx])\right] \right.$$

$$\left. (a + a \sec[c + dx])^{1/3} \tan[c + dx] \right) / (d (1 + \sec[c + dx])^{5/6})$$

Result (type 6, 2325 leaves):

$$- \left( 3 (a (1 + \sec[c + dx]))^{4/3} \right.$$

$$\left. \left( \frac{(1 + \sec[c + dx])^{1/3}}{\sec[c + dx]^{1/3}} + \sec[c + dx]^{2/3} (1 + \sec[c + dx])^{1/3} \right) \left( -8 \tan\left[\frac{1}{2}(c + dx)\right] + \right.$$

$$\left. \left( \text{AppellF1}\left[-\frac{4}{3}, -\frac{2}{3}, -\frac{2}{3}, -\frac{1}{3}, -\frac{1+i}{-1 + \tan\left[\frac{1}{2}(c+dx)\right]}, -\frac{1-i}{-1 + \tan\left[\frac{1}{2}(c+dx)\right]}\right] \right) \right.$$

$$\left. \left. \sec\left[\frac{1}{2}(c + dx)\right]^2 \right) / \left( \left( \frac{-i + \tan\left[\frac{1}{2}(c + dx)\right]}{-1 + \tan\left[\frac{1}{2}(c + dx)\right]} \right)^{2/3} \left( \frac{i + \tan\left[\frac{1}{2}(c + dx)\right]}{-1 + \tan\left[\frac{1}{2}(c + dx)\right]} \right)^{2/3} \right) \right)$$

$$\begin{aligned}
 & \text{AppellF1}\left[-\frac{4}{3}, -\frac{2}{3}, -\frac{2}{3}, -\frac{1}{3}, \frac{1-i}{1+\tan\left[\frac{1}{2}(c+dx)\right]}, \frac{1+i}{1+\tan\left[\frac{1}{2}(c+dx)\right]}\right] \\
 & \left(\frac{-i+\tan\left[\frac{1}{2}(c+dx)\right]}{1+\tan\left[\frac{1}{2}(c+dx)\right]}\right)^{1/3} \left(\frac{i+\tan\left[\frac{1}{2}(c+dx)\right]}{1+\tan\left[\frac{1}{2}(c+dx)\right]}\right)^{1/3} \left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right)^2 \Bigg) / \\
 & \left(4 \times 2^{2/3} d \left(\sec\left[\frac{1}{2}(c+dx)\right]\right)^2\right)^{1/3} (1+\sec[c+dx])^{4/3} \\
 & \left(\left(\tan\left[\frac{1}{2}(c+dx)\right]\right) \left(-8 \tan\left[\frac{1}{2}(c+dx)\right] + \left(\text{AppellF1}\left[-\frac{4}{3}, -\frac{2}{3}, -\frac{2}{3}, -\frac{1}{3}, \right.\right.\right. \right. \\
 & \left.\left.\left.\frac{1+i}{-1+\tan\left[\frac{1}{2}(c+dx)\right]}, -\frac{1-i}{-1+\tan\left[\frac{1}{2}(c+dx)\right]}\right] \sec\left[\frac{1}{2}(c+dx)\right]^2\right)\right) / \\
 & \left(\left(\frac{-i+\tan\left[\frac{1}{2}(c+dx)\right]}{-1+\tan\left[\frac{1}{2}(c+dx)\right]}\right)^{2/3} \left(\frac{i+\tan\left[\frac{1}{2}(c+dx)\right]}{-1+\tan\left[\frac{1}{2}(c+dx)\right]}\right)^{2/3}\right) - \\
 & \text{AppellF1}\left[-\frac{4}{3}, -\frac{2}{3}, -\frac{2}{3}, -\frac{1}{3}, \frac{1-i}{1+\tan\left[\frac{1}{2}(c+dx)\right]}, \frac{1+i}{1+\tan\left[\frac{1}{2}(c+dx)\right]}\right] \\
 & \left(\frac{-i+\tan\left[\frac{1}{2}(c+dx)\right]}{1+\tan\left[\frac{1}{2}(c+dx)\right]}\right)^{1/3} \left(\frac{i+\tan\left[\frac{1}{2}(c+dx)\right]}{1+\tan\left[\frac{1}{2}(c+dx)\right]}\right)^{1/3} \left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right)^2 \Bigg) / \\
 & \left(4 \times 2^{2/3} \left(\sec\left[\frac{1}{2}(c+dx)\right]\right)^2\right)^{1/3} - \frac{1}{4 \times 2^{2/3} \left(\sec\left[\frac{1}{2}(c+dx)\right]\right)^{1/3}} 3 \left(-4 \sec\left[\frac{1}{2}(c+dx)\right]\right)^2 + \\
 & \left(\sec\left[\frac{1}{2}(c+dx)\right]\right)^2 \left(-\left(\left(\left(\frac{4}{3} - \frac{4i}{3}\right) \text{AppellF1}\left[-\frac{1}{3}, -\frac{2}{3}, \frac{1}{3}, \frac{2}{3}, -\frac{1+i}{-1+\tan\left[\frac{1}{2}(c+dx)\right]}, \right.\right.\right. \right. \right. \\
 & \left.\left.\left.\frac{1-i}{-1+\tan\left[\frac{1}{2}(c+dx)\right]}\right] \sec\left[\frac{1}{2}(c+dx)\right]^2\right) / \left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)^2\right) - \\
 & \left(\left(\frac{4}{3} + \frac{4i}{3}\right) \text{AppellF1}\left[-\frac{1}{3}, \frac{1}{3}, -\frac{2}{3}, \frac{2}{3}, -\frac{1+i}{-1+\tan\left[\frac{1}{2}(c+dx)\right]}, \right.\right. \right. \\
 & \left.\left.\frac{1-i}{-1+\tan\left[\frac{1}{2}(c+dx)\right]}\right] \sec\left[\frac{1}{2}(c+dx)\right]^2\right) / \left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)^2 \Bigg) / \\
 & \left(\left(\frac{-i+\tan\left[\frac{1}{2}(c+dx)\right]}{-1+\tan\left[\frac{1}{2}(c+dx)\right]}\right)^{2/3} \left(\frac{i+\tan\left[\frac{1}{2}(c+dx)\right]}{-1+\tan\left[\frac{1}{2}(c+dx)\right]}\right)^{2/3}\right) + \left(\text{AppellF1}\left[-\frac{4}{3}, \right.\right. \\
 & \left.\left.-\frac{2}{3}, -\frac{2}{3}, -\frac{1}{3}, -\frac{1+i}{-1+\tan\left[\frac{1}{2}(c+dx)\right]}, -\frac{1-i}{-1+\tan\left[\frac{1}{2}(c+dx)\right]}\right] \sec\left[\frac{1}{2}(c+dx)\right]^2\right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \tan\left[\frac{1}{2}(c+dx)\right] \right/ \left( \left( \frac{-i + \tan\left[\frac{1}{2}(c+dx)\right]}{-1 + \tan\left[\frac{1}{2}(c+dx)\right]} \right)^{2/3} \left( \frac{i + \tan\left[\frac{1}{2}(c+dx)\right]}{-1 + \tan\left[\frac{1}{2}(c+dx)\right]} \right)^{2/3} \right) - \\
 & \text{AppellF1}\left[-\frac{4}{3}, -\frac{2}{3}, -\frac{2}{3}, -\frac{1}{3}, \frac{1-i}{1 + \tan\left[\frac{1}{2}(c+dx)\right]}, \frac{1+i}{1 + \tan\left[\frac{1}{2}(c+dx)\right]}\right] \\
 & \sec\left[\frac{1}{2}(c+dx)\right]^2 \left( \frac{-i + \tan\left[\frac{1}{2}(c+dx)\right]}{1 + \tan\left[\frac{1}{2}(c+dx)\right]} \right)^{1/3} \left( \frac{i + \tan\left[\frac{1}{2}(c+dx)\right]}{1 + \tan\left[\frac{1}{2}(c+dx)\right]} \right)^{1/3} \\
 & \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right] \right) - \left( 2 \text{AppellF1}\left[-\frac{4}{3}, -\frac{2}{3}, -\frac{2}{3}, -\frac{1}{3}, \right. \right. \\
 & \quad \left. \left. -\frac{1+i}{-1 + \tan\left[\frac{1}{2}(c+dx)\right]}, -\frac{1-i}{-1 + \tan\left[\frac{1}{2}(c+dx)\right]}\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \quad \left. \left( \frac{\sec\left[\frac{1}{2}(c+dx)\right]^2}{2(-1 + \tan\left[\frac{1}{2}(c+dx)\right])} - \frac{\sec\left[\frac{1}{2}(c+dx)\right]^2(-i + \tan\left[\frac{1}{2}(c+dx)\right])}{2(-1 + \tan\left[\frac{1}{2}(c+dx)\right])^2} \right) \right) \right/ \\
 & \left( 3 \left( \frac{-i + \tan\left[\frac{1}{2}(c+dx)\right]}{-1 + \tan\left[\frac{1}{2}(c+dx)\right]} \right)^{5/3} \left( \frac{i + \tan\left[\frac{1}{2}(c+dx)\right]}{-1 + \tan\left[\frac{1}{2}(c+dx)\right]} \right)^{2/3} \right) - \left( 2 \text{AppellF1}\left[-\frac{4}{3}, \right. \right. \\
 & \quad \left. \left. -\frac{2}{3}, -\frac{2}{3}, -\frac{1}{3}, -\frac{1+i}{-1 + \tan\left[\frac{1}{2}(c+dx)\right]}, -\frac{1-i}{-1 + \tan\left[\frac{1}{2}(c+dx)\right]}\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \quad \left. \left( \frac{\sec\left[\frac{1}{2}(c+dx)\right]^2}{2(-1 + \tan\left[\frac{1}{2}(c+dx)\right])} - \frac{\sec\left[\frac{1}{2}(c+dx)\right]^2(i + \tan\left[\frac{1}{2}(c+dx)\right])}{2(-1 + \tan\left[\frac{1}{2}(c+dx)\right])^2} \right) \right) \right/ \\
 & \left( 3 \left( \frac{-i + \tan\left[\frac{1}{2}(c+dx)\right]}{-1 + \tan\left[\frac{1}{2}(c+dx)\right]} \right)^{2/3} \left( \frac{i + \tan\left[\frac{1}{2}(c+dx)\right]}{-1 + \tan\left[\frac{1}{2}(c+dx)\right]} \right)^{5/3} \right) - \\
 & \left( \frac{-i + \tan\left[\frac{1}{2}(c+dx)\right]}{1 + \tan\left[\frac{1}{2}(c+dx)\right]} \right)^{1/3} \left( \frac{i + \tan\left[\frac{1}{2}(c+dx)\right]}{1 + \tan\left[\frac{1}{2}(c+dx)\right]} \right)^{1/3} \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right] \right)^2 \\
 & \left( \left( \left( \frac{4}{3} + \frac{4i}{3} \right) \text{AppellF1}\left[-\frac{1}{3}, -\frac{2}{3}, \frac{1}{3}, \frac{2}{3}, \frac{1-i}{1 + \tan\left[\frac{1}{2}(c+dx)\right]}, \frac{1+i}{1 + \tan\left[\frac{1}{2}(c+dx)\right]}\right] \right. \right. \\
 & \quad \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \right) \right/ \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right] \right)^2 + \\
 & \left( \left( \frac{4}{3} - \frac{4i}{3} \right) \text{AppellF1}\left[-\frac{1}{3}, \frac{1}{3}, -\frac{2}{3}, \frac{2}{3}, \frac{1-i}{1 + \tan\left[\frac{1}{2}(c+dx)\right]}, \right. \right. \\
 & \quad \left. \left. \frac{1+i}{1 + \tan\left[\frac{1}{2}(c+dx)\right]}\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \right) \right/ \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right] \right)^2 \right) -
 \end{aligned}$$

$$\left( \text{AppellF1}\left[-\frac{4}{3}, -\frac{2}{3}, -\frac{2}{3}, -\frac{1}{3}, \frac{1-i}{1+\tan\left[\frac{1}{2}(c+dx)\right]}, \frac{1+i}{1+\tan\left[\frac{1}{2}(c+dx)\right]}\right] \right. \\ \left. \left( \frac{i+\tan\left[\frac{1}{2}(c+dx)\right]}{1+\tan\left[\frac{1}{2}(c+dx)\right]} \right)^{1/3} \left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right)^2 \right. \\ \left. \left( -\frac{\text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \left(-i+\tan\left[\frac{1}{2}(c+dx)\right]\right)}{2\left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right)^2} + \frac{\text{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{2\left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right)} \right) \right) / \\ \left( 3 \left( \frac{-i+\tan\left[\frac{1}{2}(c+dx)\right]}{1+\tan\left[\frac{1}{2}(c+dx)\right]} \right)^{2/3} \right) - \left( \text{AppellF1}\left[-\frac{4}{3}, -\frac{2}{3}, -\frac{2}{3}, -\frac{1}{3}, \right. \right. \\ \left. \left. \frac{1-i}{1+\tan\left[\frac{1}{2}(c+dx)\right]}, \frac{1+i}{1+\tan\left[\frac{1}{2}(c+dx)\right]}\right] \left( \frac{-i+\tan\left[\frac{1}{2}(c+dx)\right]}{1+\tan\left[\frac{1}{2}(c+dx)\right]} \right)^{1/3} \right. \\ \left. \left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right)^2 \left( -\frac{\text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \left(i+\tan\left[\frac{1}{2}(c+dx)\right]\right)}{2\left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right)^2} + \right. \right. \\ \left. \left. \frac{\text{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{2\left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right)} \right) \right) / \left( 3 \left( \frac{i+\tan\left[\frac{1}{2}(c+dx)\right]}{1+\tan\left[\frac{1}{2}(c+dx)\right]} \right)^{2/3} \right) \right) \right)$$

**Problem 288: Unable to integrate problem.**

$$\int \text{Sec}[e+fx]^n (a+a \text{Sec}[e+fx])^4 dx$$

Optimal (type 5, 304 leaves, 8 steps):

$$\frac{a^4 (30+21n+4n^2) \text{Sec}[e+fx]^{1+n} \text{Sin}[e+fx]}{f(1+n)(2+n)(3+n)} + \frac{\text{Sec}[e+fx]^{1+n} (a^2+a^2 \text{Sec}[e+fx])^2 \text{Sin}[e+fx]}{f(3+n)} + \\ \frac{2(4+n) \text{Sec}[e+fx]^{1+n} (a^4+a^4 \text{Sec}[e+fx]) \text{Sin}[e+fx]}{f(2+n)(3+n)} - \\ \left( a^4 (3+24n+8n^2) \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1-n}{2}, \frac{3-n}{2}, \text{Cos}[e+fx]^2\right] \right. \\ \left. \text{Sec}[e+fx]^{-1+n} \text{Sin}[e+fx] \right) / \left( f(1-n)(1+n)(3+n) \sqrt{\text{Sin}[e+fx]^2} \right) + \\ \left( 4a^4 (3+2n) \text{Hypergeometric2F1}\left[\frac{1}{2}, -\frac{n}{2}, \frac{2-n}{2}, \text{Cos}[e+fx]^2\right] \text{Sec}[e+fx]^n \text{Sin}[e+fx] \right) / \\ \left( fn(2+n) \sqrt{\text{Sin}[e+fx]^2} \right)$$

Result (type 8, 23 leaves):

$$\int \text{Sec}[e+fx]^n (a+a \text{Sec}[e+fx])^4 dx$$

### Problem 289: Unable to integrate problem.

$$\int \text{Sec}[e + f x]^n (a + a \text{Sec}[e + f x])^3 dx$$

Optimal (type 5, 230 leaves, 7 steps):

$$\frac{a^3 (5 + 2n) \text{Sec}[e + f x]^{1+n} \text{Sin}[e + f x]}{f (1+n) (2+n)} + \frac{\text{Sec}[e + f x]^{1+n} (a^3 + a^3 \text{Sec}[e + f x]) \text{Sin}[e + f x]}{f (2+n)} -$$

$$\left( a^3 (1 + 4n) \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1-n}{2}, \frac{3-n}{2}, \text{Cos}[e + f x]^2\right] \text{Sec}[e + f x]^{-1+n} \text{Sin}[e + f x] \right) /$$

$$\left( f (1 - n^2) \sqrt{\text{Sin}[e + f x]^2} \right) +$$

$$\left( a^3 (7 + 4n) \text{Hypergeometric2F1}\left[\frac{1}{2}, -\frac{n}{2}, \frac{2-n}{2}, \text{Cos}[e + f x]^2\right] \text{Sec}[e + f x]^n \text{Sin}[e + f x] \right) /$$

$$\left( f n (2+n) \sqrt{\text{Sin}[e + f x]^2} \right)$$

Result (type 8, 23 leaves):

$$\int \text{Sec}[e + f x]^n (a + a \text{Sec}[e + f x])^3 dx$$

### Problem 290: Unable to integrate problem.

$$\int \text{Sec}[e + f x]^n (a + a \text{Sec}[e + f x])^2 dx$$

Optimal (type 5, 172 leaves, 6 steps):

$$\frac{a^2 \text{Sec}[e + f x]^{1+n} \text{Sin}[e + f x]}{f (1+n)} -$$

$$\left( a^2 (1 + 2n) \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1-n}{2}, \frac{3-n}{2}, \text{Cos}[e + f x]^2\right] \text{Sec}[e + f x]^{-1+n} \text{Sin}[e + f x] \right) /$$

$$\left( f (1 - n^2) \sqrt{\text{Sin}[e + f x]^2} \right) +$$

$$\left( 2 a^2 \text{Hypergeometric2F1}\left[\frac{1}{2}, -\frac{n}{2}, \frac{2-n}{2}, \text{Cos}[e + f x]^2\right] \text{Sec}[e + f x]^n \text{Sin}[e + f x] \right) /$$

$$\left( f n \sqrt{\text{Sin}[e + f x]^2} \right)$$

Result (type 8, 23 leaves):

$$\int \text{Sec}[e + f x]^n (a + a \text{Sec}[e + f x])^2 dx$$

### Problem 291: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \text{Sec}[e + f x]^n (a + a \text{Sec}[e + f x]) dx$$

Optimal (type 5, 132 leaves, 5 steps):

$$- \left( \left( a \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{1-n}{2}, \frac{3-n}{2}, \cos[e+fx]^2 \right] \operatorname{Sec}[e+fx]^{-1+n} \sin[e+fx] \right) / \right. \\ \left. \left( f(1-n) \sqrt{\sin[e+fx]^2} \right) \right) + \\ \left( a \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, -\frac{n}{2}, \frac{2-n}{2}, \cos[e+fx]^2 \right] \operatorname{Sec}[e+fx]^n \sin[e+fx] \right) / \\ \left( f n \sqrt{\sin[e+fx]^2} \right)$$

Result (type 6, 3990 leaves):

$$- \left( \left( a \operatorname{Sec}[e+fx]^{2n} (1 + \operatorname{Sec}[e+fx]) \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right] \right. \right. \\ \left( \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, n, 1-n, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right] \cos[e+fx] \right) / \right. \\ \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, n, 1-n, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right] + 2 \left( (-1+n) \right. \right. \\ \left. \left. \operatorname{AppellF1} \left[ \frac{3}{2}, n, 2-n, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right] + n \operatorname{AppellF1} \left[ \frac{3}{2}, \right. \right. \right. \\ \left. \left. \left. 1+n, 1-n, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right) \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right) + \\ \operatorname{AppellF1} \left[ \frac{1}{2}, 1+n, -n, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right) / \\ \left( \operatorname{AppellF1} \left[ \frac{1}{2}, 1+n, -n, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right] + \right. \\ \left. \frac{2}{3} \left( n \operatorname{AppellF1} \left[ \frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right] + \right. \right. \\ \left. \left. (1+n) \operatorname{AppellF1} \left[ \frac{3}{2}, 2+n, -n, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right) \right) \\ \left. \left. \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right) \right) \right) / \left( f \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right) \right) \\ \left( \frac{1}{\left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right)^2} \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \operatorname{Sec}[e+fx]^n \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right. \right. \\ \left( \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, n, 1-n, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right] \cos[e+fx] \right) / \right. \\ \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, n, 1-n, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right] + \right. \\ \left. 2 \left( (-1+n) \operatorname{AppellF1} \left[ \frac{3}{2}, n, 2-n, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right] + \right. \right. \\ \left. \left. n \operatorname{AppellF1} \left[ \frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, \right. \right. \right. \\ \left. \left. \left. -\operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right) \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right) + \right. \\ \left. \left. \left. \left. \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right) \right) \right) \right) \right)$$

$$\begin{aligned}
 & \text{AppellF1}\left[\frac{1}{2}, 1+n, -n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] / \\
 & \left( \text{AppellF1}\left[\frac{1}{2}, 1+n, -n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \frac{2}{3} \left( n \text{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \quad \left. (1+n) \text{AppellF1}\left[\frac{3}{2}, 2+n, -n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \\
 & \quad \left. \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) - \frac{1}{2(-1+\tan\left[\frac{1}{2}(e+fx)\right]^2)} \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \text{Sec}[e+fx]^n \\
 & \left( \left( 3 \text{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \cos[e+fx] \right) / \right. \\
 & \quad \left( 3 \text{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad 2 \left( (-1+n) \text{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \quad n \text{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) + \\
 & \text{AppellF1}\left[\frac{1}{2}, 1+n, -n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] / \\
 & \left( \text{AppellF1}\left[\frac{1}{2}, 1+n, -n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \frac{2}{3} \left( n \text{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \quad \left. (1+n) \text{AppellF1}\left[\frac{3}{2}, 2+n, -n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) - \\
 & \frac{1}{-1+\tan\left[\frac{1}{2}(e+fx)\right]^2} n \text{Sec}[e+fx]^{1+n} \text{Sin}[e+fx] \tan\left[\frac{1}{2}(e+fx)\right] \\
 & \left( \left( 3 \text{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \cos[e+fx] \right) / \right. \\
 & \quad \left( 3 \text{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad 2 \left( (-1+n) \text{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \quad n \text{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) + \\
 & \text{AppellF1}\left[\frac{1}{2}, 1+n, -n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] /
 \end{aligned}$$

$$\begin{aligned}
& \left( \text{AppellF1}\left[\frac{1}{2}, 1+n, -n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
& \quad \frac{2}{3} \left( n \text{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
& \quad \quad \left. (1+n) \text{AppellF1}\left[\frac{3}{2}, 2+n, -n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \\
& \quad \left. \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) - \frac{1}{-1 + \tan\left[\frac{1}{2}(e+fx)\right]^2} \text{Sec}[e+fx]^n \tan\left[\frac{1}{2}(e+fx)\right] \\
& \left( - \left( \left( 3 \text{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sin[e+fx] \right) \right) / \right. \\
& \quad \left( 3 \text{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
& \quad \quad 2 \left( (-1+n) \text{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
& \quad \quad \quad \left. n \text{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \\
& \quad \quad \left. \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) + \left( 3 \cos[e+fx] \left( -\frac{1}{3} (1-n) \text{AppellF1}\left[\frac{3}{2}, n, \right. \right. \right. \\
& \quad \quad \left. \left. \left. 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \right. \right. \\
& \quad \quad \left. \left. \tan\left[\frac{1}{2}(e+fx)\right] + \frac{1}{3} n \text{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \\
& \quad \quad \left. \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) \right) \right) / \\
& \left( 3 \text{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
& \quad 2 \left( (-1+n) \text{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
& \quad \quad \left. n \text{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
& \quad \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 + \right. \\
& \quad \left. \left( \frac{1}{3} n \text{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \\
& \quad \quad \left. \left. \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \frac{1}{3} (1+n) \text{AppellF1}\left[\frac{3}{2}, 2+n, -n, \frac{5}{2}, \right. \right. \right. \\
& \quad \quad \left. \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) \right) / \\
& \left( \text{AppellF1}\left[\frac{1}{2}, 1+n, -n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
& \quad \frac{2}{3} \left( n \text{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
& \quad \quad \left. (1+n) \text{AppellF1}\left[\frac{3}{2}, 2+n, -n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
& \quad \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 - \right.
\end{aligned}$$



$$\begin{aligned}
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \cos[e+fx] \right. \\
 & \quad \left( 2 \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \right. \\
 & \quad \quad \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \\
 & \quad \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + 3 \left( -\frac{1}{3}(1-n) \operatorname{AppellF1}\left[\frac{3}{2}, n, \right. \right. \\
 & \quad \quad \left. \left. 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \right. \\
 & \quad \quad \left. \tan\left[\frac{1}{2}(e+fx)\right] + \frac{1}{3} n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) \right) + \\
 & \quad 2 \tan\left[\frac{1}{2}(e+fx)\right]^2 \left( (-1+n) \left( -\frac{3}{5}(2-n) \operatorname{AppellF1}\left[\frac{5}{2}, n, 3-n, \frac{7}{2}, \right. \right. \right. \\
 & \quad \quad \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \right. \right. \\
 & \quad \quad \left. \tan\left[\frac{1}{2}(e+fx)\right] + \frac{3}{5} n \operatorname{AppellF1}\left[\frac{5}{2}, 1+n, 2-n, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) \right) + \\
 & \quad n \left( -\frac{3}{5}(1-n) \operatorname{AppellF1}\left[\frac{5}{2}, 1+n, 2-n, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \right. \\
 & \quad \quad \left. \frac{3}{5}(1+n) \operatorname{AppellF1}\left[\frac{5}{2}, 2+n, 1-n, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) \right) \Bigg) / \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad 2 \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \right. \\
 & \quad \quad \left. n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) - \\
 & \left( \operatorname{AppellF1}\left[\frac{1}{2}, 1+n, -n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \quad \left( \frac{1}{3} n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \\
 & \quad \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \frac{1}{3}(1+n) \operatorname{AppellF1}\left[\frac{3}{2}, 2+n, -n, \frac{5}{2}, \right. \\
 & \quad \quad \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \frac{2}{3} \left( n \operatorname{AppellF1} \left[ \frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+f x) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (e+f x) \right]^2 \right] + \right. \\
 & \quad \left. (1+n) \operatorname{AppellF1} \left[ \frac{3}{2}, 2+n, -n, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+f x) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (e+f x) \right]^2 \right] \right) \\
 & \operatorname{Sec} \left[ \frac{1}{2} (e+f x) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (e+f x) \right] + \frac{2}{3} \operatorname{Tan} \left[ \frac{1}{2} (e+f x) \right]^2 \\
 & \left( n \left( -\frac{3}{5} (1-n) \operatorname{AppellF1} \left[ \frac{5}{2}, 1+n, 2-n, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+f x) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\operatorname{Tan} \left[ \frac{1}{2} (e+f x) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (e+f x) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (e+f x) \right] + \right. \right. \\
 & \quad \left. \frac{3}{5} (1+n) \operatorname{AppellF1} \left[ \frac{5}{2}, 2+n, 1-n, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+f x) \right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan} \left[ \frac{1}{2} (e+f x) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (e+f x) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (e+f x) \right] \right) + \right. \\
 & \quad \left. (1+n) \left( \frac{3}{5} n \operatorname{AppellF1} \left[ \frac{5}{2}, 2+n, 1-n, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+f x) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\operatorname{Tan} \left[ \frac{1}{2} (e+f x) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (e+f x) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (e+f x) \right] + \right. \right. \\
 & \quad \left. \frac{3}{5} (2+n) \operatorname{AppellF1} \left[ \frac{5}{2}, 3+n, -n, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+f x) \right]^2, \right. \right. \\
 & \quad \left. \left. \left. -\operatorname{Tan} \left[ \frac{1}{2} (e+f x) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (e+f x) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (e+f x) \right] \right) \right) \right) \Bigg/ \\
 & \left( \operatorname{AppellF1} \left[ \frac{1}{2}, 1+n, -n, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+f x) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (e+f x) \right]^2 \right] + \right. \\
 & \quad \frac{2}{3} \left( n \operatorname{AppellF1} \left[ \frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+f x) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (e+f x) \right]^2 \right] + \right. \\
 & \quad \left. (1+n) \operatorname{AppellF1} \left[ \frac{3}{2}, 2+n, -n, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+f x) \right]^2, \right. \right. \\
 & \quad \left. \left. \left. -\operatorname{Tan} \left[ \frac{1}{2} (e+f x) \right]^2 \right] \operatorname{Tan} \left[ \frac{1}{2} (e+f x) \right]^2 \right) \right) \right) \Bigg) \Bigg) \Bigg) \Bigg)
 \end{aligned}$$

**Problem 292: Unable to integrate problem.**

$$\int \frac{\operatorname{Sec} [e+f x]^n}{a+a \operatorname{Sec} [e+f x]} dx$$

Optimal (type 5, 174 leaves, 6 steps):

$$\frac{\text{Sec}[e + f x]^n \text{Sin}[e + f x]}{f (a + a \text{Sec}[e + f x])} +$$

$$\left( (1 - n) \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{2 - n}{2}, \frac{4 - n}{2}, \text{Cos}[e + f x]^2\right] \text{Sec}[e + f x]^{-2+n} \text{Sin}[e + f x] \right) /$$

$$\left( a f (2 - n) \sqrt{\text{Sin}[e + f x]^2} \right) -$$

$$\left( \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1 - n}{2}, \frac{3 - n}{2}, \text{Cos}[e + f x]^2\right] \text{Sec}[e + f x]^{-1+n} \text{Sin}[e + f x] \right) /$$

$$\left( a f \sqrt{\text{Sin}[e + f x]^2} \right)$$

Result (type 8, 23 leaves):

$$\int \frac{\text{Sec}[e + f x]^n}{a + a \text{Sec}[e + f x]} dx$$

**Problem 293: Unable to integrate problem.**

$$\int \frac{\text{Sec}[e + f x]^n}{(a + a \text{Sec}[e + f x])^2} dx$$

Optimal (type 5, 217 leaves, 7 steps):

$$-\frac{2(2-n)\text{Sec}[e+fx]^{1+n}\text{Sin}[e+fx]}{3a^2f(1+\text{Sec}[e+fx])} - \frac{\text{Sec}[e+fx]^{1+n}\text{Sin}[e+fx]}{3f(a+a\text{Sec}[e+fx])^2}$$

$$\left( (3-2n) \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1-n}{2}, \frac{3-n}{2}, \text{Cos}[e + f x]^2\right] \text{Sec}[e + f x]^{-1+n} \text{Sin}[e + f x] \right) /$$

$$\left( 3 a^2 f \sqrt{\text{Sin}[e + f x]^2} \right) +$$

$$\left( 2(2-n) \text{Hypergeometric2F1}\left[\frac{1}{2}, -\frac{n}{2}, \frac{2-n}{2}, \text{Cos}[e + f x]^2\right] \text{Sec}[e + f x]^n \text{Sin}[e + f x] \right) /$$

$$\left( 3 a^2 f \sqrt{\text{Sin}[e + f x]^2} \right)$$

Result (type 8, 23 leaves):

$$\int \frac{\text{Sec}[e + f x]^n}{(a + a \text{Sec}[e + f x])^2} dx$$

**Problem 294: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \text{Sec}[e + f x]^n (1 + \text{Sec}[e + f x])^{5/2} dx$$

Optimal (type 5, 162 leaves, 4 steps):

$$\frac{2(7+4n)\operatorname{Sec}[e+fx]^{1+n}\operatorname{Sin}[e+fx]}{f(1+2n)(3+2n)\sqrt{1+\operatorname{Sec}[e+fx]}} + \frac{2\operatorname{Sec}[e+fx]^{1+n}\sqrt{1+\operatorname{Sec}[e+fx]}\operatorname{Sin}[e+fx]}{f(3+2n)} + \left( \frac{2(3+24n+16n^2)\operatorname{Hypergeometric2F1}\left[\frac{1}{2}, 1-n, \frac{3}{2}, 1-\operatorname{Sec}[e+fx]\right]\operatorname{Tan}[e+fx]}{f(1+2n)(3+2n)\sqrt{1+\operatorname{Sec}[e+fx]}} \right) /$$

Result (type 5, 433 leaves):

$$-\frac{1}{f\operatorname{Sec}[e+fx]^{5/2}} \int 2^{-\frac{5}{2}+n} e^{-i\left(\frac{1}{2}+n\right)(e+fx)} \left( \frac{e^{i(e+fx)}}{1+e^{2i(e+fx)}} \right)^{\frac{1}{2}+n} \left( 1+e^{2i(e+fx)} \right)^{\frac{1}{2}+n} \left( \frac{1}{2+n} 10 e^{i(2+n)(e+fx)} \operatorname{Hypergeometric2F1}\left[1+\frac{n}{2}, \frac{5}{2}+n, 2+\frac{n}{2}, -e^{2i(e+fx)}\right] + \frac{1}{4+n} 5 e^{i(4+n)(e+fx)} \operatorname{Hypergeometric2F1}\left[2+\frac{n}{2}, \frac{5}{2}+n, 3+\frac{n}{2}, -e^{2i(e+fx)}\right] + \frac{e^{in(e+fx)} \operatorname{Hypergeometric2F1}\left[\frac{n}{2}, \frac{5}{2}+n, 1+\frac{n}{2}, -e^{2i(e+fx)}\right]}{n} + \frac{5 e^{i(1+n)(e+fx)} \operatorname{Hypergeometric2F1}\left[\frac{1+n}{2}, \frac{5}{2}+n, \frac{3+n}{2}, -e^{2i(e+fx)}\right]}{1+n} + \frac{10 e^{i(3+n)(e+fx)} \operatorname{Hypergeometric2F1}\left[\frac{5}{2}+n, \frac{3+n}{2}, \frac{5+n}{2}, -e^{2i(e+fx)}\right]}{3+n} + \frac{e^{i(5+n)(e+fx)} \operatorname{Hypergeometric2F1}\left[\frac{5}{2}+n, \frac{5+n}{2}, \frac{7+n}{2}, -e^{2i(e+fx)}\right]}{5+n} \right) \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^5 (1+\operatorname{Sec}[e+fx])^{5/2} dx$$

**Problem 295: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \operatorname{Sec}[e+fx]^n (1+\operatorname{Sec}[e+fx])^{3/2} dx$$

Optimal (type 5, 98 leaves, 4 steps):

$$\frac{2\operatorname{Sec}[e+fx]^{1+n}\operatorname{Sin}[e+fx]}{f(1+2n)\sqrt{1+\operatorname{Sec}[e+fx]}} + \left( \frac{2(1+4n)\operatorname{Hypergeometric2F1}\left[\frac{1}{2}, 1-n, \frac{3}{2}, 1-\operatorname{Sec}[e+fx]\right]\operatorname{Tan}[e+fx]}{f(1+2n)\sqrt{1+\operatorname{Sec}[e+fx]}} \right) /$$

Result (type 5, 6367 leaves):

$$\left( 14 \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^3 \left( \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \right)^n \right)$$

$$\begin{aligned}
 & \left( \cos \left[ \frac{1}{2} (e + f x) \right]^2 \sec[e + f x] \right)^{-\frac{3}{2}+n} (1 + \sec[e + f x])^{3/2} \left( \cos \left[ \frac{3}{2} (e + f x) \right] \right. \\
 & \quad \left( \frac{1}{8} \sec[e + f x]^{-\frac{3}{2}+n} + \frac{3}{8} \sec[e + f x]^{\frac{1}{2}+n} + \frac{3}{4} i \sec[e + f x]^{\frac{1}{2}+n} \sin[e + f x] - \frac{3}{8} \sec[e + f x]^{\frac{1}{2}+n} \right. \\
 & \quad \left. \sin[e + f x]^2 + \cos[e + f x] \left( \frac{3}{8} \sec[e + f x]^{\frac{1}{2}+n} + \frac{3}{8} i \sec[e + f x]^{\frac{1}{2}+n} \sin[e + f x] \right) + \right. \\
 & \quad \left. \sec[e + f x] \left( \frac{1}{8} \sec[e + f x]^{\frac{1}{2}+n} + \frac{3}{8} i \sec[e + f x]^{\frac{1}{2}+n} \sin[e + f x] - \right. \right. \\
 & \quad \left. \left. \frac{3}{8} \sec[e + f x]^{\frac{1}{2}+n} \sin[e + f x]^2 - \frac{1}{8} i \sec[e + f x]^{\frac{1}{2}+n} \sin[e + f x]^3 \right) \right) - \\
 & \quad \frac{1}{8} i \sec[e + f x]^{-\frac{3}{2}+n} \sin \left[ \frac{3}{2} (e + f x) \right] - \frac{3}{8} i \sec[e + f x]^{\frac{1}{2}+n} \sin \left[ \frac{3}{2} (e + f x) \right] + \\
 & \quad \frac{3}{4} \sec[e + f x]^{\frac{1}{2}+n} \sin[e + f x] \sin \left[ \frac{3}{2} (e + f x) \right] + \\
 & \quad \frac{3}{8} i \sec[e + f x]^{\frac{1}{2}+n} \sin[e + f x]^2 \sin \left[ \frac{3}{2} (e + f x) \right] + \cos[e + f x] \\
 & \quad \left( -\frac{3}{8} i \sec[e + f x]^{\frac{1}{2}+n} \sin \left[ \frac{3}{2} (e + f x) \right] + \frac{3}{8} \sec[e + f x]^{\frac{1}{2}+n} \sin[e + f x] \sin \left[ \frac{3}{2} (e + f x) \right] \right) + \\
 & \quad \sec[e + f x] \left( -\frac{1}{8} i \sec[e + f x]^{\frac{1}{2}+n} \sin \left[ \frac{3}{2} (e + f x) \right] + \frac{3}{8} \sec[e + f x]^{\frac{1}{2}+n} \sin[e + f x] \right. \\
 & \quad \left. \sin \left[ \frac{3}{2} (e + f x) \right] + \frac{3}{8} i \sec[e + f x]^{\frac{1}{2}+n} \sin[e + f x]^2 \sin \left[ \frac{3}{2} (e + f x) \right] - \right. \\
 & \quad \left. \frac{1}{8} \sec[e + f x]^{\frac{1}{2}+n} \sin[e + f x]^3 \sin \left[ \frac{3}{2} (e + f x) \right] \right) \tan \left[ \frac{1}{2} (e + f x) \right] \\
 & \quad \left( 8 \operatorname{Gamma} \left[ \frac{5}{2} + n \right] \operatorname{Hypergeometric2F1} \left[ 2, \frac{5}{2} + n, \frac{7}{2}, -2 \sec[e + f x] \sin \left[ \frac{1}{2} (e + f x) \right]^2 \right] \right. \\
 & \quad \left. \sec \left[ \frac{1}{2} (e + f x) \right]^2 \tan \left[ \frac{1}{2} (e + f x) \right]^2 + \right. \\
 & \quad \left. 5 \operatorname{Gamma} \left[ \frac{3}{2} + n \right] \operatorname{Hypergeometric2F1} \left[ 1, \frac{3}{2} + n, \frac{5}{2}, -2 \sec[e + f x] \sin \left[ \frac{1}{2} (e + f x) \right]^2 \right] \right. \\
 & \quad \left. \left( -3 + \tan \left[ \frac{1}{2} (e + f x) \right]^2 + 2 \tan \left[ \frac{1}{2} (e + f x) \right]^4 \right) \right) \Bigg) / \\
 & \quad \left( f \sec[e + f x]^{3/2} \left( -1 + \tan \left[ \frac{1}{2} (e + f x) \right]^2 \right) \left( 8 \operatorname{Gamma} \left[ \frac{5}{2} + n \right] \sec \left[ \frac{1}{2} (e + f x) \right]^4 \right. \right. \\
 & \quad \left. \left. \tan \left[ \frac{1}{2} (e + f x) \right]^2 \left( 7 \cos[e + f x] (-5 - 2n + 2(1+n) \cos[e + f x]) \right. \right. \right. \\
 & \quad \left. \left. \operatorname{Hypergeometric2F1} \left[ 2, \frac{5}{2} + n, \frac{7}{2}, -2 \sec[e + f x] \sin \left[ \frac{1}{2} (e + f x) \right]^2 \right] \sec \left[ \frac{1}{2} (e + f x) \right]^2 + \right. \right. \\
 & \quad \left. \left. 8(5+2n) \operatorname{Hypergeometric2F1} \left[ 3, \frac{7}{2} + n, \frac{9}{2}, -2 \sec[e + f x] \sin \left[ \frac{1}{2} (e + f x) \right]^2 \right] \right. \right. \\
 & \quad \left. \left. \tan \left[ \frac{1}{2} (e + f x) \right]^2 \right) + 7 \operatorname{Gamma} \left[ \frac{3}{2} + n \right] \left( -1 + \tan \left[ \frac{1}{2} (e + f x) \right]^2 \right) \right. \\
 & \quad \left. \left( \frac{5}{2} \cos[e + f x] (-15 - 9n + (9+8n) \cos[e + f x] + n \cos[2(e + f x)]) \right. \right. \\
 & \quad \left. \left. \operatorname{Hypergeometric2F1} \left[ 1, \frac{3}{2} + n, \frac{5}{2}, -2 \sec[e + f x] \sin \left[ \frac{1}{2} (e + f x) \right]^2 \right] \sec \left[ \frac{1}{2} (e + f x) \right]^6 + \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & 2 (3 + 2 n) (5 + \text{Cos}[e + f x]) \text{Hypergeometric2F1}\left[2, \frac{5}{2} + n, \frac{7}{2}, \right. \\
 & \quad \left. -2 \text{Sec}[e + f x] \text{Sin}\left[\frac{1}{2} (e + f x)\right]^2\right] \text{Sec}\left[\frac{1}{2} (e + f x)\right]^4 \text{Tan}\left[\frac{1}{2} (e + f x)\right]^2\left.\right) \\
 & \left(-\left(\left(14 \left(\text{Sec}\left[\frac{1}{2} (e + f x)\right]^2\right)^{1+n} \left(\text{Cos}\left[\frac{1}{2} (e + f x)\right]^2 \text{Sec}[e + f x]\right)^{-\frac{3}{2}+n} \text{Tan}\left[\frac{1}{2} (e + f x)\right]^2\right.\right.\right. \\
 & \quad \left(\left.8 \text{Gamma}\left[\frac{5}{2} + n\right] \text{Hypergeometric2F1}\left[2, \frac{5}{2} + n, \frac{7}{2}, -2 \text{Sec}[e + f x] \text{Sin}\left[\frac{1}{2} (e + f x)\right]^2\right]\right.\right. \\
 & \quad \left.\left.\text{Sec}\left[\frac{1}{2} (e + f x)\right]^2 \text{Tan}\left[\frac{1}{2} (e + f x)\right]^2 +\right.\right. \\
 & \quad \left.\left.5 \text{Gamma}\left[\frac{3}{2} + n\right] \text{Hypergeometric2F1}\left[1, \frac{3}{2} + n, \frac{5}{2}, -2 \text{Sec}[e + f x] \text{Sin}\left[\frac{1}{2} (e + f x)\right]^2\right]\right.\right. \\
 & \quad \left.\left.\left(-3 + \text{Tan}\left[\frac{1}{2} (e + f x)\right]^2 + 2 \text{Tan}\left[\frac{1}{2} (e + f x)\right]^4\right)\right)\right)\right) / \\
 & \left(\left(-1 + \text{Tan}\left[\frac{1}{2} (e + f x)\right]^2\right)^2 \left(8 \text{Gamma}\left[\frac{5}{2} + n\right] \text{Sec}\left[\frac{1}{2} (e + f x)\right]^4 \text{Tan}\left[\frac{1}{2} (e + f x)\right]^2\right.\right. \\
 & \quad \left(\left.7 \text{Cos}[e + f x] (-5 - 2 n + 2 (1 + n) \text{Cos}[e + f x]) \text{Hypergeometric2F1}\left[2, \frac{5}{2} + n, \right.\right. \\
 & \quad \left.\left.\frac{7}{2}, -2 \text{Sec}[e + f x] \text{Sin}\left[\frac{1}{2} (e + f x)\right]^2\right] \text{Sec}\left[\frac{1}{2} (e + f x)\right]^2 + 8 (5 + 2 n)\right.\right. \\
 & \quad \left.\left.\text{Hypergeometric2F1}\left[3, \frac{7}{2} + n, \frac{9}{2}, -2 \text{Sec}[e + f x] \text{Sin}\left[\frac{1}{2} (e + f x)\right]^2\right]\right.\right. \\
 & \quad \left.\left.\text{Tan}\left[\frac{1}{2} (e + f x)\right]^2\right) + 7 \text{Gamma}\left[\frac{3}{2} + n\right] \left(-1 + \text{Tan}\left[\frac{1}{2} (e + f x)\right]^2\right)\right.\right. \\
 & \quad \left(\left.\frac{5}{2} \text{Cos}[e + f x] (-15 - 9 n + (9 + 8 n) \text{Cos}[e + f x] + n \text{Cos}[2 (e + f x)])\right)\right.\right. \\
 & \quad \left.\left.\text{Hypergeometric2F1}\left[1, \frac{3}{2} + n, \frac{5}{2}, -2 \text{Sec}[e + f x] \text{Sin}\left[\frac{1}{2} (e + f x)\right]^2\right]\right.\right. \\
 & \quad \left.\left.\text{Sec}\left[\frac{1}{2} (e + f x)\right]^6 + 2 (3 + 2 n) (5 + \text{Cos}[e + f x]) \text{Hypergeometric2F1}\left[2, \frac{5}{2} + n, \frac{7}{2}, \right.\right. \\
 & \quad \left.\left.-2 \text{Sec}[e + f x] \text{Sin}\left[\frac{1}{2} (e + f x)\right]^2\right] \text{Sec}\left[\frac{1}{2} (e + f x)\right]^4 \text{Tan}\left[\frac{1}{2} (e + f x)\right]^2\right)\right)\right) + \\
 & \left(7 \left(\text{Sec}\left[\frac{1}{2} (e + f x)\right]^2\right)^{1+n} \left(\text{Cos}\left[\frac{1}{2} (e + f x)\right]^2 \text{Sec}[e + f x]\right)^{-\frac{3}{2}+n}\right. \\
 & \quad \left(\left.8 \text{Gamma}\left[\frac{5}{2} + n\right] \text{Hypergeometric2F1}\left[2, \frac{5}{2} + n, \frac{7}{2}, -2 \text{Sec}[e + f x] \text{Sin}\left[\frac{1}{2} (e + f x)\right]^2\right]\right.\right. \\
 & \quad \left.\left.\text{Sec}\left[\frac{1}{2} (e + f x)\right]^2 \text{Tan}\left[\frac{1}{2} (e + f x)\right]^2 + 5 \text{Gamma}\left[\frac{3}{2} + n\right] \text{Hypergeometric2F1}\left[1, \frac{3}{2} + n, \frac{5}{2}, \right.\right. \\
 & \quad \left.\left.-2 \text{Sec}[e + f x] \text{Sin}\left[\frac{1}{2} (e + f x)\right]^2\right] \left(-3 + \text{Tan}\left[\frac{1}{2} (e + f x)\right]^2 + 2 \text{Tan}\left[\frac{1}{2} (e + f x)\right]^4\right)\right)\right)\right) / \\
 & \left(\left(-1 + \text{Tan}\left[\frac{1}{2} (e + f x)\right]^2\right)\right) \left(8 \text{Gamma}\left[\frac{5}{2} + n\right] \text{Sec}\left[\frac{1}{2} (e + f x)\right]^4 \text{Tan}\left[\frac{1}{2} (e + f x)\right]^2\right. \\
 & \quad \left(\left.7 \text{Cos}[e + f x] (-5 - 2 n + 2 (1 + n) \text{Cos}[e + f x]) \text{Hypergeometric2F1}\left[2, \frac{5}{2} + \right.\right.
 \end{aligned}$$

$$\begin{aligned}
 & n, \frac{7}{2}, -2 \operatorname{Sec}[e + f x] \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right]^2 \operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^2 + \\
 & 8(5 + 2n) \operatorname{Hypergeometric2F1}\left[3, \frac{7}{2} + n, \frac{9}{2}, -2 \operatorname{Sec}[e + f x] \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \\
 & \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2 + 7 \operatorname{Gamma}\left[\frac{3}{2} + n\right] \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right) \\
 & \left(\frac{5}{2} \operatorname{Cos}[e + f x] (-15 - 9n + (9 + 8n) \operatorname{Cos}[e + f x] + n \operatorname{Cos}[2(e + f x)])\right) \\
 & \operatorname{Hypergeometric2F1}\left[1, \frac{3}{2} + n, \frac{5}{2}, -2 \operatorname{Sec}[e + f x] \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \\
 & \operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^6 + 2(3 + 2n)(5 + \operatorname{Cos}[e + f x]) \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2} + n, \frac{7}{2}, -2 \operatorname{Sec}[e + f x] \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^4 \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2 \right) + \\
 & \left(14n \left(\operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^2\right)^n \left(\operatorname{Cos}\left[\frac{1}{2}(e + f x)\right]^2 \operatorname{Sec}[e + f x]\right)^{-\frac{3}{2}+n} \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2 \right. \\
 & \left. \left(8 \operatorname{Gamma}\left[\frac{5}{2} + n\right] \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2} + n, \frac{7}{2}, -2 \operatorname{Sec}[e + f x] \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \right. \right. \\
 & \left. \left. \operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2 + 5 \operatorname{Gamma}\left[\frac{3}{2} + n\right] \operatorname{Hypergeometric2F1}\left[1, \frac{3}{2} + n, \frac{5}{2}, -2 \operatorname{Sec}[e + f x] \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \left(-3 + \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2 + 2 \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^4\right)\right)\right) / \\
 & \left(\left(-1 + \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right) \left(8 \operatorname{Gamma}\left[\frac{5}{2} + n\right] \operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^4 \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2 \right. \right. \\
 & \left. \left. \left(7 \operatorname{Cos}[e + f x] (-5 - 2n + 2(1 + n) \operatorname{Cos}[e + f x]) \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2} + n, \frac{7}{2}, -2 \operatorname{Sec}[e + f x] \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^2 + \right. \right. \right. \\
 & \left. \left. 8(5 + 2n) \operatorname{Hypergeometric2F1}\left[3, \frac{7}{2} + n, \frac{9}{2}, -2 \operatorname{Sec}[e + f x] \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2 + 7 \operatorname{Gamma}\left[\frac{3}{2} + n\right] \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right) \right. \right. \\
 & \left. \left. \left(\frac{5}{2} \operatorname{Cos}[e + f x] (-15 - 9n + (9 + 8n) \operatorname{Cos}[e + f x] + n \operatorname{Cos}[2(e + f x)])\right) \right. \right. \\
 & \left. \left. \operatorname{Hypergeometric2F1}\left[1, \frac{3}{2} + n, \frac{5}{2}, -2 \operatorname{Sec}[e + f x] \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \right. \right. \\
 & \left. \left. \operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^6 + 2(3 + 2n)(5 + \operatorname{Cos}[e + f x]) \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2} + n, \frac{7}{2}, -2 \operatorname{Sec}[e + f x] \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^4 \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right)\right) + \\
 & \left(14 \left(-\frac{3}{2} + n\right) \left(\operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^2\right)^n \left(\operatorname{Cos}\left[\frac{1}{2}(e + f x)\right]^2 \operatorname{Sec}[e + f x]\right)^{-\frac{5}{2}+n} \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right] \right. \\
 & \left. \left(8 \operatorname{Gamma}\left[\frac{5}{2} + n\right] \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2} + n, \frac{7}{2}, -2 \operatorname{Sec}[e + f x] \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \right) \right)
 \end{aligned}$$

$$\begin{aligned}
& \left( \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2 + 5 \text{Gamma}\left[\frac{3}{2}+n\right] \text{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2}, \right. \right. \\
& \quad \left. \left. -2 \text{Sec}[e+fx] \text{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \left(-3 + \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2 + 2 \text{Tan}\left[\frac{1}{2}(e+fx)\right]^4\right)\right) \\
& \left(-\text{Cos}\left[\frac{1}{2}(e+fx)\right]\right) \text{Sec}[e+fx] \text{Sin}\left[\frac{1}{2}(e+fx)\right] + \\
& \quad \left. \text{Cos}\left[\frac{1}{2}(e+fx)\right]^2 \text{Sec}[e+fx] \text{Tan}[e+fx]\right) \Bigg) / \\
& \left( \left(-1 + \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right) \left(8 \text{Gamma}\left[\frac{5}{2}+n\right] \text{Sec}\left[\frac{1}{2}(e+fx)\right]^4 \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right. \right. \\
& \quad \left. \left(7 \text{Cos}[e+fx] (-5 - 2n + 2(1+n) \text{Cos}[e+fx]) \text{Hypergeometric2F1}\left[2, \frac{5}{2}+ \right. \right. \right. \\
& \quad \quad \left. \left. n, \frac{7}{2}, -2 \text{Sec}[e+fx] \text{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 + \right. \right. \\
& \quad \left. \left. 8(5+2n) \text{Hypergeometric2F1}\left[3, \frac{7}{2}+n, \frac{9}{2}, -2 \text{Sec}[e+fx] \text{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \\
& \quad \left. \left. \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right) + 7 \text{Gamma}\left[\frac{3}{2}+n\right] \left(-1 + \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right) \right. \right. \\
& \quad \left. \left(\frac{5}{2} \text{Cos}[e+fx] (-15 - 9n + (9+8n) \text{Cos}[e+fx] + n \text{Cos}[2(e+fx)])\right) \right. \\
& \quad \left. \text{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2}, -2 \text{Sec}[e+fx] \text{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
& \quad \left. \text{Sec}\left[\frac{1}{2}(e+fx)\right]^6 + 2(3+2n)(5+\text{Cos}[e+fx]) \text{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \right. \right. \\
& \quad \left. \left. \frac{7}{2}, -2 \text{Sec}[e+fx] \text{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(e+fx)\right]^4 \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right) \Bigg) \right) + \\
& \left(14 \left(\text{Sec}\left[\frac{1}{2}(e+fx)\right]^2\right)^n \left(\text{Cos}\left[\frac{1}{2}(e+fx)\right]^2 \text{Sec}[e+fx]\right)^{-\frac{3}{2}+n} \text{Tan}\left[\frac{1}{2}(e+fx)\right] \right. \\
& \quad \left(8 \text{Gamma}\left[\frac{5}{2}+n\right] \text{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2 \text{Sec}[e+fx] \text{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
& \quad \left. \text{Sec}\left[\frac{1}{2}(e+fx)\right]^4 \text{Tan}\left[\frac{1}{2}(e+fx)\right] + 8 \text{Gamma}\left[\frac{5}{2}+n\right] \text{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \right. \right. \\
& \quad \left. \left. \frac{7}{2}, -2 \text{Sec}[e+fx] \text{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \text{Tan}\left[\frac{1}{2}(e+fx)\right]^3 + \right. \\
& \quad \left. 5 \text{Gamma}\left[\frac{3}{2}+n\right] \text{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2}, -2 \text{Sec}[e+fx] \text{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
& \quad \left. \left(\text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \text{Tan}\left[\frac{1}{2}(e+fx)\right] + 4 \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \text{Tan}\left[\frac{1}{2}(e+fx)\right]^3\right) + \right. \\
& \quad \left. \frac{32}{7} \left(\frac{5}{2}+n\right) \text{Gamma}\left[\frac{5}{2}+n\right] \text{Hypergeometric2F1}\left[3, \frac{7}{2}+n, \frac{9}{2}, \right. \right. \\
& \quad \left. \left. -2 \text{Sec}[e+fx] \text{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \right. \\
& \quad \left. \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \left(-2 \text{Cos}\left[\frac{1}{2}(e+fx)\right]\right) \text{Sec}[e+fx] \text{Sin}\left[\frac{1}{2}(e+fx)\right] - \right. \\
& \quad \left. \left. 2 \text{Sec}[e+fx] \text{Sin}\left[\frac{1}{2}(e+fx)\right]^2 \text{Tan}[e+fx]\right) + 2 \left(\frac{3}{2}+n\right) \text{Gamma}\left[\frac{3}{2}+n\right] \right)
\end{aligned}$$



$$\begin{aligned}
 & \text{Hypergeometric2F1}\left[2, \frac{5}{2} + n, \frac{7}{2}, -2 \text{Sec}[e + f x] \text{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \\
 & \left(-3 + \text{Tan}\left[\frac{1}{2}(e + f x)\right]^2 + 2 \text{Tan}\left[\frac{1}{2}(e + f x)\right]^4\right) \left(-2 \text{Cos}\left[\frac{1}{2}(e + f x)\right] \text{Sec}[e + f x] \right. \\
 & \quad \left. \text{Sin}\left[\frac{1}{2}(e + f x)\right] - 2 \text{Sec}[e + f x] \text{Sin}\left[\frac{1}{2}(e + f x)\right]^2 \text{Tan}[e + f x]\right) \Bigg) / \\
 & \left(\left(-1 + \text{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right) \left(8 \text{Gamma}\left[\frac{5}{2} + n\right] \text{Sec}\left[\frac{1}{2}(e + f x)\right]^4 \text{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right.\right. \\
 & \quad \left.\left. \left(7 \text{Cos}[e + f x] (-5 - 2n + 2(1+n) \text{Cos}[e + f x]) \text{Hypergeometric2F1}\left[2, \frac{5}{2} +\right.\right.\right. \right. \\
 & \quad \quad \left.\left.\left.\frac{7}{2}, -2 \text{Sec}[e + f x] \text{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \text{Sec}\left[\frac{1}{2}(e + f x)\right]^2 +\right.\right.\right. \\
 & \quad \left.8(5 + 2n) \text{Hypergeometric2F1}\left[3, \frac{7}{2} + n, \frac{9}{2}, -2 \text{Sec}[e + f x] \text{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \right. \\
 & \quad \left. \text{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right) + 7 \text{Gamma}\left[\frac{3}{2} + n\right] \left(-1 + \text{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right) \\
 & \quad \left.\left(\frac{5}{2} \text{Cos}[e + f x] (-15 - 9n + (9 + 8n) \text{Cos}[e + f x] + n \text{Cos}[2(e + f x)])\right)\right) \\
 & \quad \text{Hypergeometric2F1}\left[1, \frac{3}{2} + n, \frac{5}{2}, -2 \text{Sec}[e + f x] \text{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \\
 & \quad \left.\text{Sec}\left[\frac{1}{2}(e + f x)\right]^6 + 2(3 + 2n)(5 + \text{Cos}[e + f x]) \text{Hypergeometric2F1}\left[2, \frac{5}{2} + n,\right.\right. \\
 & \quad \left.\left.\frac{7}{2}, -2 \text{Sec}[e + f x] \text{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \text{Sec}\left[\frac{1}{2}(e + f x)\right]^4 \text{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right)\right) \Bigg) - \\
 & \left(14 \left(\text{Sec}\left[\frac{1}{2}(e + f x)\right]^2\right)^n \left(\text{Cos}\left[\frac{1}{2}(e + f x)\right] \text{Sec}[e + f x]\right)^{-\frac{3}{2}+n} \text{Tan}\left[\frac{1}{2}(e + f x)\right] \right. \\
 & \quad \left(8 \text{Gamma}\left[\frac{5}{2} + n\right] \text{Hypergeometric2F1}\left[2, \frac{5}{2} + n, \frac{7}{2}, -2 \text{Sec}[e + f x] \text{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \right. \\
 & \quad \left. \text{Sec}\left[\frac{1}{2}(e + f x)\right]^2 \text{Tan}\left[\frac{1}{2}(e + f x)\right]^2 + 5 \text{Gamma}\left[\frac{3}{2} + n\right] \text{Hypergeometric2F1}\left[1, \frac{3}{2} + n, \frac{5}{2},\right.\right. \\
 & \quad \left.\left.-2 \text{Sec}[e + f x] \text{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \left(-3 + \text{Tan}\left[\frac{1}{2}(e + f x)\right]^2 + 2 \text{Tan}\left[\frac{1}{2}(e + f x)\right]^4\right)\right) \\
 & \quad \left. \left(8 \text{Gamma}\left[\frac{5}{2} + n\right] \text{Sec}\left[\frac{1}{2}(e + f x)\right]^6 \text{Tan}\left[\frac{1}{2}(e + f x)\right] \right. \right. \\
 & \quad \left. \left(7 \text{Cos}[e + f x] (-5 - 2n + 2(1+n) \text{Cos}[e + f x]) \text{Hypergeometric2F1}\left[2, \frac{5}{2} +\right.\right. \right. \\
 & \quad \quad \left.\left.\frac{7}{2}, -2 \text{Sec}[e + f x] \text{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \text{Sec}\left[\frac{1}{2}(e + f x)\right]^2 +\right.\right. \\
 & \quad \left.8(5 + 2n) \text{Hypergeometric2F1}\left[3, \frac{7}{2} + n, \frac{9}{2}, -2 \text{Sec}[e + f x] \text{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \right. \\
 & \quad \left. \text{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right) + 16 \text{Gamma}\left[\frac{5}{2} + n\right] \text{Sec}\left[\frac{1}{2}(e + f x)\right]^4 \text{Tan}\left[\frac{1}{2}(e + f x)\right]^3 \\
 & \quad \left.\left(7 \text{Cos}[e + f x] (-5 - 2n + 2(1+n) \text{Cos}[e + f x]) \text{Hypergeometric2F1}\left[2, \frac{5}{2} +\right.\right. \right. \\
 & \quad \quad \left.\left.\frac{7}{2}, -2 \text{Sec}[e + f x] \text{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \text{Sec}\left[\frac{1}{2}(e + f x)\right]^2 +\right.
 \end{aligned}$$

$$\begin{aligned}
& 8 (5 + 2 n) \operatorname{Hypergeometric2F1}\left[3, \frac{7}{2} + n, \frac{9}{2}, -2 \operatorname{Sec}[e + f x] \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \\
& \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right) + 7 \operatorname{Gamma}\left[\frac{3}{2} + n\right] \operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right] \\
& \left(\frac{5}{2} \operatorname{Cos}[e + f x] (-15 - 9 n + (9 + 8 n) \operatorname{Cos}[e + f x] + n \operatorname{Cos}[2(e + f x)])\right) \\
& \operatorname{Hypergeometric2F1}\left[1, \frac{3}{2} + n, \frac{5}{2}, -2 \operatorname{Sec}[e + f x] \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \\
& \operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^6 + 2(3 + 2 n)(5 + \operatorname{Cos}[e + f x]) \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2} + \right. \\
& \left. n, \frac{7}{2}, -2 \operatorname{Sec}[e + f x] \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^4 \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right) + \\
& 8 \operatorname{Gamma}\left[\frac{5}{2} + n\right] \operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^4 \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2 \left(-14(1 + n) \operatorname{Cos}[e + f x] \right. \\
& \left. \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2} + n, \frac{7}{2}, -2 \operatorname{Sec}[e + f x] \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \right. \\
& \left. \operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^2 \operatorname{Sin}[e + f x] - 7(-5 - 2 n + 2(1 + n) \operatorname{Cos}[e + f x]) \right. \\
& \left. \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2} + n, \frac{7}{2}, -2 \operatorname{Sec}[e + f x] \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \right. \\
& \left. \operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^2 \operatorname{Sin}[e + f x] + 7 \operatorname{Cos}[e + f x](-5 - 2 n + 2(1 + n) \operatorname{Cos}[e + f x]) \right. \\
& \left. \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2} + n, \frac{7}{2}, -2 \operatorname{Sec}[e + f x] \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \right. \\
& \left. \operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right] + 8(5 + 2 n) \operatorname{Hypergeometric2F1}\left[3, \frac{7}{2} + \right. \right. \\
& \left. \left. n, \frac{9}{2}, -2 \operatorname{Sec}[e + f x] \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right] + \right. \\
& \left. 4\left(\frac{5}{2} + n\right) \operatorname{Cos}[e + f x](-5 - 2 n + 2(1 + n) \operatorname{Cos}[e + f x]) \operatorname{Hypergeometric2F1}\left[3, \frac{7}{2} + \right. \right. \\
& \left. \left. n, \frac{9}{2}, -2 \operatorname{Sec}[e + f x] \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^2 \left(-2 \operatorname{Cos}\left[\frac{1}{2}(e + f x)\right] \right. \right. \\
& \left. \left. \operatorname{Sec}[e + f x] \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right] - 2 \operatorname{Sec}[e + f x] \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right]^2 \operatorname{Tan}[e + f x]\right)\right) + \\
& \frac{16}{3} \left(\frac{7}{2} + n\right) (5 + 2 n) \operatorname{Hypergeometric2F1}\left[4, \frac{9}{2} + n, \frac{11}{2}, -2 \operatorname{Sec}[e + f x] \right. \\
& \left. \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2 \left(-2 \operatorname{Cos}\left[\frac{1}{2}(e + f x)\right] \operatorname{Sec}[e + f x] \right. \\
& \left. \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right] - 2 \operatorname{Sec}[e + f x] \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right]^2 \operatorname{Tan}[e + f x]\right)\right) + \\
& 7 \operatorname{Gamma}\left[\frac{3}{2} + n\right] \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right) \left(-\frac{5}{2}(-15 - 9 n + (9 + 8 n) \operatorname{Cos}[e + f x] + \right. \\
& \left. n \operatorname{Cos}[2(e + f x)])\right) \operatorname{Hypergeometric2F1}\left[1, \frac{3}{2} + n, \frac{5}{2}, -2 \right. \\
& \left. \operatorname{Sec}[e + f x] \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^6 \operatorname{Sin}[e + f x] +
\end{aligned}$$

$$\begin{aligned}
 & \frac{5}{2} \cos [e+f x] \operatorname{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2}, -2 \operatorname{Sec}[e+f x] \sin \left[\frac{1}{2}(e+f x)\right]^2\right] \\
 & \operatorname{Sec}\left[\frac{1}{2}(e+f x)\right]^6\left(-\left(9+8 n\right) \sin [e+f x]-2 n \sin [2(e+f x)]\right)+ \\
 & \frac{15}{2} \cos [e+f x]\left(-15-9 n+\left(9+8 n\right) \cos [e+f x]+n \cos [2(e+f x)]\right) \\
 & \operatorname{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2}, -2 \operatorname{Sec}[e+f x] \sin \left[\frac{1}{2}(e+f x)\right]^2\right] \\
 & \operatorname{Sec}\left[\frac{1}{2}(e+f x)\right]^6 \tan \left[\frac{1}{2}(e+f x)\right]+2(3+2 n)\left(5+\cos [e+f x]\right) \\
 & \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2 \operatorname{Sec}[e+f x] \sin \left[\frac{1}{2}(e+f x)\right]^2\right] \\
 & \operatorname{Sec}\left[\frac{1}{2}(e+f x)\right]^6 \tan \left[\frac{1}{2}(e+f x)\right]-2(3+2 n) \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2\right. \\
 & \left.\operatorname{Sec}[e+f x] \sin \left[\frac{1}{2}(e+f x)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+f x)\right]^4 \sin [e+f x] \tan \left[\frac{1}{2}(e+f x)\right]^2+ \\
 & 4(3+2 n)\left(5+\cos [e+f x]\right) \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2\right. \\
 & \left.\operatorname{Sec}[e+f x] \sin \left[\frac{1}{2}(e+f x)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+f x)\right]^4 \tan \left[\frac{1}{2}(e+f x)\right]^3+ \\
 & \left(\frac{3}{2}+n\right) \cos [e+f x]\left(-15-9 n+\left(9+8 n\right) \cos [e+f x]+n \cos [2(e+f x)]\right) \\
 & \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2 \operatorname{Sec}[e+f x] \sin \left[\frac{1}{2}(e+f x)\right]^2\right] \\
 & \operatorname{Sec}\left[\frac{1}{2}(e+f x)\right]^6\left(-2 \cos \left[\frac{1}{2}(e+f x)\right] \operatorname{Sec}[e+f x] \sin \left[\frac{1}{2}(e+f x)\right]-2 \operatorname{Sec}[e+f x] \right. \\
 & \left. \sin \left[\frac{1}{2}(e+f x)\right]^2 \tan [e+f x]\right)+\frac{8}{7}\left(\frac{5}{2}+n\right)(3+2 n)\left(5+\cos [e+f x]\right) \\
 & \operatorname{Hypergeometric2F1}\left[3, \frac{7}{2}+n, \frac{9}{2}, -2 \operatorname{Sec}[e+f x] \sin \left[\frac{1}{2}(e+f x)\right]^2\right] \\
 & \operatorname{Sec}\left[\frac{1}{2}(e+f x)\right]^4 \tan \left[\frac{1}{2}(e+f x)\right]^2\left(-2 \cos \left[\frac{1}{2}(e+f x)\right] \operatorname{Sec}[e+f x] \right. \\
 & \left.\sin \left[\frac{1}{2}(e+f x)\right]-2 \operatorname{Sec}[e+f x] \sin \left[\frac{1}{2}(e+f x)\right]^2 \tan [e+f x]\right)\right)\right) / \\
 & \left(\left(-1+\tan \left[\frac{1}{2}(e+f x)\right]^2\right)\left(8 \operatorname{Gamma}\left[\frac{5}{2}+n\right] \operatorname{Sec}\left[\frac{1}{2}(e+f x)\right]^4 \tan \left[\frac{1}{2}(e+f x)\right]^2\right.\right. \\
 & \left.\left.(7 \cos [e+f x]\left(-5-2 n+2(1+n) \cos [e+f x]\right) \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2 \operatorname{Sec}[e+f x] \sin \left[\frac{1}{2}(e+f x)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+f x)\right]^2+8(5+2 n)\right.\right. \\
 & \left.\left.\operatorname{Hypergeometric2F1}\left[3, \frac{7}{2}+n, \frac{9}{2}, -2 \operatorname{Sec}[e+f x] \sin \left[\frac{1}{2}(e+f x)\right]^2\right] \tan \left[\frac{1}{2}(e+f x)\right]^2\right)+7 \operatorname{Gamma}\left[\frac{3}{2}+n\right]\left(-1+\tan \left[\frac{1}{2}(e+f x)\right]^2\right)\right) \\
 & \left.\left(\frac{5}{2} \cos [e+f x]\left(-15-9 n+\left(9+8 n\right) \cos [e+f x]+n \cos [2(e+f x)]\right)\right)\right)
 \end{aligned}$$

$$\text{Hypergeometric2F1}\left[1, \frac{3}{2} + n, \frac{5}{2}, -2 \text{Sec}[e + f x] \text{Sin}\left[\frac{1}{2} (e + f x)\right]^2\right]$$

$$\text{Sec}\left[\frac{1}{2} (e + f x)\right]^6 + 2 (3 + 2 n) (5 + \text{Cos}[e + f x]) \text{Hypergeometric2F1}\left[2, \frac{5}{2} + n, \frac{7}{2}, -2 \text{Sec}[e + f x] \text{Sin}\left[\frac{1}{2} (e + f x)\right]^2\right] \text{Sec}\left[\frac{1}{2} (e + f x)\right]^4 \text{Tan}\left[\frac{1}{2} (e + f x)\right]^2\right]^2\right)$$

**Problem 296: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \text{Sec}[e + f x]^n \sqrt{1 + \text{Sec}[e + f x]} \, dx$$

Optimal (type 5, 45 leaves, 2 steps):

$$\frac{2 \text{Hypergeometric2F1}\left[\frac{1}{2}, 1 - n, \frac{3}{2}, 1 - \text{Sec}[e + f x]\right] \text{Tan}[e + f x]}{f \sqrt{1 + \text{Sec}[e + f x]}}$$

Result (type 5, 211 leaves):

$$-\frac{1}{f n (1 + n)} i^{2^{-\frac{1}{2}+n}} e^{\frac{1}{2} i (e+fx)} (1 + e^{2 i (e+fx)})^{-\frac{1}{2}+n} (e^{-i (e+fx)} (1 + e^{2 i (e+fx)}))^{\frac{1}{2}-n}$$

$$\text{Cos}[e + f x]^{\frac{1}{2}+n} \left( (1 + n) \text{Hypergeometric2F1}\left[\frac{n}{2}, \frac{1}{2} + n, \frac{2 + n}{2}, -e^{2 i (e+fx)}\right] + \right.$$

$$\left. e^{i (e+fx)} n \text{Hypergeometric2F1}\left[\frac{1}{2} + n, \frac{1 + n}{2}, \frac{3 + n}{2}, -e^{2 i (e+fx)}\right] \right)$$

$$\text{Sec}\left[\frac{1}{2} (e + f x)\right] \text{Sec}[e + f x]^n \sqrt{1 + \text{Sec}[e + f x]}$$

**Problem 297: Result more than twice size of optimal antiderivative.**

$$\int \frac{\text{Sec}[e + f x]^n}{\sqrt{1 + \text{Sec}[e + f x]}} \, dx$$

Optimal (type 6, 59 leaves, 3 steps):

$$\frac{\left(\text{AppellF1}\left[\frac{1}{2}, 1 - n, 1, \frac{3}{2}, 1 - \text{Sec}[e + f x], \frac{1}{2} (1 - \text{Sec}[e + f x])\right] \text{Tan}[e + f x]\right)}{\left(f \sqrt{1 + \text{Sec}[e + f x]}\right)}$$

Result (type 6, 2938 leaves):

$$\left(3 \sqrt{2} \text{AppellF1}\left[\frac{1}{2}, -\frac{1}{2} + n, 1 - n, \frac{3}{2}, \text{Tan}\left[\frac{1}{2} (e + f x)\right]^2, -\text{Tan}\left[\frac{1}{2} (e + f x)\right]^2\right] \left(\text{Sec}\left[\frac{1}{2} (e + f x)\right]^2\right)^n\right.$$

$$\left. \text{Sec}[e + f x]^{-\frac{1}{2}+\frac{1}{2}(-1+2n)} \left(\text{Cos}\left[\frac{1}{2} (e + f x)\right]^2 \text{Sec}[e + f x]\right)^n \text{Tan}\left[\frac{1}{2} (e + f x)\right]\right) /$$

$$\left(f \left(3 \text{AppellF1}\left[\frac{1}{2}, -\frac{1}{2} + n, 1 - n, \frac{3}{2}, \text{Tan}\left[\frac{1}{2} (e + f x)\right]^2, -\text{Tan}\left[\frac{1}{2} (e + f x)\right]^2\right] + \right.\right)$$

$$\begin{aligned}
 & \left( 2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left. (-1+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \\
 & \left( \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \cos[e+fx] \right. \right. \\
 & \quad \left. \left. \left( \sec\left[\frac{1}{2}(e+fx)\right]^2 \right)^{1+n} \left( \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \right)^n \sqrt{1+\sec[e+fx]} \right) \right) / \\
 & \quad \left( \sqrt{2} \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \\
 & \quad \left. \left( 2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \\
 & \quad \quad \left. \left. (-1+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \right) \right) \\
 & \quad \left. \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) - \left( 3\sqrt{2} \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, 1-n, \frac{3}{2}, \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \left( \sec\left[\frac{1}{2}(e+fx)\right]^2 \right)^n \right. \\
 & \quad \left. \left( \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \right)^n \sqrt{1+\sec[e+fx]} \sin[e+fx] \tan\left[\frac{1}{2}(e+fx)\right] \right) \right) / \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left( 2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \quad \left. (-1+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \\
 & \quad \left. \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) + \left( 3\sqrt{2} n \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \cos[e+fx] \left( \sec\left[\frac{1}{2}(e+fx)\right]^2 \right)^n \right. \\
 & \quad \left. \left( \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \right)^n \sqrt{1+\sec[e+fx]} \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \right) / \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left( 2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \quad \left. (-1+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \\
 & \quad \left. \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) + \left( 3\sqrt{2} \cos[e+fx] \left( \sec\left[\frac{1}{2}(e+fx)\right]^2 \right)^n \right. \\
 & \quad \left. \left( \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \right)^n \sqrt{1+\sec[e+fx]} \tan\left[\frac{1}{2}(e+fx)\right] \right) \right) \\
 & \quad \left( -\frac{1}{3}(1-n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right)
 \end{aligned}$$

$$\begin{aligned}
 & \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] + \frac{1}{3}\left(-\frac{1}{2}+n\right) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+n, 1-n, \frac{5}{2}, \right. \\
 & \left. \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\Big) / \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, 1-n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \left(2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 2-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \left. (-1+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+n, 1-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right]\right) \\
 & \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 - \left(3\sqrt{2} \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, 1-n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Cos}[e+fx] \left(\operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2\right)^n \right. \\
 & \left. \left(\operatorname{Cos}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Sec}[e+fx]\right)^n \sqrt{1+\operatorname{Sec}[e+fx]} \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \right. \\
 & \left. \left(\left(2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 2-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \right. \\
 & \left. \left. (-1+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+n, 1-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right]\right)\right) \\
 & \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] + \\
 & 3\left(-\frac{1}{3}(1-n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 2-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] + \frac{1}{3}\left(-\frac{1}{2}+n\right) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+n, 1-n, \frac{5}{2}, \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right) + \\
 & \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \left(2(-1+n)\left(-\frac{3}{5}(2-n) \operatorname{AppellF1}\left[\frac{5}{2}, -\frac{1}{2}+n, 3-n, \frac{7}{2}, \right. \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] + \frac{3}{5} \right. \\
 & \left. \left(-\frac{1}{2}+n\right) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{2}+n, 2-n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right) + (-1+2n)\left(-\frac{3}{5}(1-n) \operatorname{AppellF1}\left[\frac{5}{2}, \right. \right. \\
 & \left. \left. \frac{1}{2}+n, 2-n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \right. \\
 & \left. \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] + \frac{3}{5}\left(\frac{1}{2}+n\right) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{3}{2}+n, 1-n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)\Big) / \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, 1-n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \left. \left(2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 2-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & (-1+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \\
 & \quad \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \tan\left[\frac{1}{2}(e+fx)\right]^2 + \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \quad \left. \left(\sec\left[\frac{1}{2}(e+fx)\right]^2\right)^n \left(\cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx]\right)^n \right. \\
 & \quad \left. \tan\left[\frac{1}{2}(e+fx)\right] \tan[e+fx]\right) / \left(\sqrt{2} \sqrt{1+\sec[e+fx]}\right) \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left. \left(2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \\
 & \quad \quad \left. \left. (-1+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \tan\left[\frac{1}{2}(e+fx)\right]^2\right) + \right. \\
 & \left. \left(3\sqrt{2}n \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \\
 & \quad \left. \left. \cos[e+fx] \left(\sec\left[\frac{1}{2}(e+fx)\right]^2\right)^n \left(\cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx]\right)^{-1+n} \right. \right. \\
 & \quad \left. \left. \sqrt{1+\sec[e+fx]} \tan\left[\frac{1}{2}(e+fx)\right] \left(-\cos\left[\frac{1}{2}(e+fx)\right] \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right] + \right. \right. \right. \\
 & \quad \left. \left. \left. \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \tan[e+fx]\right)\right)\right) / \right. \\
 & \left. \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \\
 & \quad \left. \left(2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \\
 & \quad \quad \left. \left. (-1+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \tan\left[\frac{1}{2}(e+fx)\right]^2\right) \right)
 \end{aligned}$$

**Problem 298: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sec[e+fx]^n}{(1+\sec[e+fx])^{3/2}} dx$$

Optimal (type 6, 62 leaves, 3 steps):

$$\left( \operatorname{AppellF1}\left[\frac{1}{2}, 1-n, 2, \frac{3}{2}, 1-\sec[e+fx], \frac{1}{2}(1-\sec[e+fx])\right] \tan[e+fx] \right) / \left(2f\sqrt{1+\sec[e+fx]}\right)$$

Result (type 6, 2990 leaves):

$$\begin{aligned}
& \left( 6 \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{3}{2} + n, 1 - n, \frac{3}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] \right. \\
& \quad \left( \operatorname{Sec} \left[ \frac{1}{2} (e + f x) \right]^2 \right)^n \operatorname{Sec} [e + f x]^{\frac{1}{2} + \frac{1}{2} (-3+2n)} \left( \cos \left[ \frac{1}{2} (e + f x) \right]^2 \operatorname{Sec} [e + f x] \right)^{\frac{3}{2} + n} \\
& \quad \left. \tan \left[ \frac{1}{2} (e + f x) \right] \left( -1 + \tan \left[ \frac{1}{2} (e + f x) \right]^2 \right) \right) / \\
& \left( f (1 + \operatorname{Sec} [e + f x])^{3/2} \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{3}{2} + n, 1 - n, \frac{3}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] \right) + \right. \\
& \quad \left( 2 (-1 + n) \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{3}{2} + n, 2 - n, \frac{5}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] + \right. \\
& \quad \left. (-3 + 2n) \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{1}{2} + n, 1 - n, \frac{5}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] \right) \\
& \quad \tan \left[ \frac{1}{2} (e + f x) \right]^2 \left( \left( 12 \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{3}{2} + n, 1 - n, \frac{3}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, \right. \right. \right. \\
& \quad \left. \left. -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] \cos [e + f x] \left( \operatorname{Sec} \left[ \frac{1}{2} (e + f x) \right]^2 \right)^{1+n} \right. \right. \\
& \quad \left. \left. \left( \cos \left[ \frac{1}{2} (e + f x) \right]^2 \operatorname{Sec} [e + f x] \right)^{\frac{3}{2} + n} \tan \left[ \frac{1}{2} (e + f x) \right]^2 \left( -1 + \tan \left[ \frac{1}{2} (e + f x) \right]^2 \right) \right) \right) / \\
& \quad \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{3}{2} + n, 1 - n, \frac{3}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] + \right. \\
& \quad \left( 2 (-1 + n) \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{3}{2} + n, 2 - n, \frac{5}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] + \right. \\
& \quad \left. (-3 + 2n) \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{1}{2} + n, 1 - n, \frac{5}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, \right. \right. \\
& \quad \left. \left. -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (e + f x) \right]^2 \right) + \\
& \quad \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{3}{2} + n, 1 - n, \frac{3}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] \cos [e + f x] \right. \\
& \quad \left. \left( \operatorname{Sec} \left[ \frac{1}{2} (e + f x) \right]^2 \right)^{1+n} \left( \cos \left[ \frac{1}{2} (e + f x) \right]^2 \operatorname{Sec} [e + f x] \right)^{\frac{3}{2} + n} \left( -1 + \tan \left[ \frac{1}{2} (e + f x) \right]^2 \right)^2 \right) / \\
& \quad \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{3}{2} + n, 1 - n, \frac{3}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] + \right. \\
& \quad \left( 2 (-1 + n) \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{3}{2} + n, 2 - n, \frac{5}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] + \right. \\
& \quad \left. (-3 + 2n) \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{1}{2} + n, 1 - n, \frac{5}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] \right) \\
& \quad \tan \left[ \frac{1}{2} (e + f x) \right]^2 \right) - \left( 6 \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{3}{2} + n, 1 - n, \frac{3}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, \right. \right. \\
& \quad \left. \left. -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] \left( \operatorname{Sec} \left[ \frac{1}{2} (e + f x) \right]^2 \right)^n \left( \cos \left[ \frac{1}{2} (e + f x) \right]^2 \operatorname{Sec} [e + f x] \right)^{\frac{3}{2} + n} \right)
\end{aligned}$$



$$\begin{aligned}
 & \sin[e + f x] \tan\left[\frac{1}{2}(e + f x)\right] \left(-1 + \tan\left[\frac{1}{2}(e + f x)\right]\right)^2 \Big/ \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2} + n, 1 - n, \frac{3}{2}, \tan\left[\frac{1}{2}(e + f x)\right]^2, -\tan\left[\frac{1}{2}(e + f x)\right]^2\right] + \right. \\
 & \quad \left(2(-1 + n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{3}{2} + n, 2 - n, \frac{5}{2}, \tan\left[\frac{1}{2}(e + f x)\right]^2, -\tan\left[\frac{1}{2}(e + f x)\right]^2\right] + \right. \\
 & \quad \quad \left. (-3 + 2n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2} + n, 1 - n, \frac{5}{2}, \tan\left[\frac{1}{2}(e + f x)\right]^2, -\tan\left[\frac{1}{2}(e + f x)\right]^2\right]\right) \\
 & \quad \tan\left[\frac{1}{2}(e + f x)\right]^2 \Big) + \left(6n \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2} + n, 1 - n, \frac{3}{2}, \tan\left[\frac{1}{2}(e + f x)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(e + f x)\right]^2\right] \cos[e + f x] \left(\sec\left[\frac{1}{2}(e + f x)\right]\right)^n \right. \\
 & \quad \left. \left(\cos\left[\frac{1}{2}(e + f x)\right]^2 \sec[e + f x]\right)^{\frac{3}{2}+n} \tan\left[\frac{1}{2}(e + f x)\right]^2 \left(-1 + \tan\left[\frac{1}{2}(e + f x)\right]\right)^2 \Big) \Big/ \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2} + n, 1 - n, \frac{3}{2}, \tan\left[\frac{1}{2}(e + f x)\right]^2, -\tan\left[\frac{1}{2}(e + f x)\right]^2\right] + \right. \\
 & \quad \left(2(-1 + n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{3}{2} + n, 2 - n, \frac{5}{2}, \tan\left[\frac{1}{2}(e + f x)\right]^2, -\tan\left[\frac{1}{2}(e + f x)\right]^2\right] + \right. \\
 & \quad \quad \left. (-3 + 2n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2} + n, 1 - n, \frac{5}{2}, \tan\left[\frac{1}{2}(e + f x)\right]^2, -\tan\left[\frac{1}{2}(e + f x)\right]^2\right]\right) \\
 & \quad \tan\left[\frac{1}{2}(e + f x)\right]^2 \Big) + \left(6 \cos[e + f x] \left(\sec\left[\frac{1}{2}(e + f x)\right]\right)^n \right. \\
 & \quad \left. \left(\cos\left[\frac{1}{2}(e + f x)\right]^2 \sec[e + f x]\right)^{\frac{3}{2}+n} \tan\left[\frac{1}{2}(e + f x)\right] \left(-\frac{1}{3}(1 - n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{3}{2} + n, \right. \right. \right. \\
 & \quad \left. \left. 2 - n, \frac{5}{2}, \tan\left[\frac{1}{2}(e + f x)\right]^2, -\tan\left[\frac{1}{2}(e + f x)\right]^2\right] \sec\left[\frac{1}{2}(e + f x)\right]^2 \tan\left[\frac{1}{2}(e + f x)\right] \right) + \right. \\
 & \quad \left. \frac{1}{3} \left(-\frac{3}{2} + n\right) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2} + n, 1 - n, \frac{5}{2}, \tan\left[\frac{1}{2}(e + f x)\right]^2, -\tan\left[\frac{1}{2}(e + f x)\right]^2\right] \right. \\
 & \quad \left. \sec\left[\frac{1}{2}(e + f x)\right]^2 \tan\left[\frac{1}{2}(e + f x)\right] \right) \left(-1 + \tan\left[\frac{1}{2}(e + f x)\right]\right)^2 \Big) \Big/ \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2} + n, 1 - n, \frac{3}{2}, \tan\left[\frac{1}{2}(e + f x)\right]^2, -\tan\left[\frac{1}{2}(e + f x)\right]^2\right] + \right. \\
 & \quad \left(2(-1 + n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{3}{2} + n, 2 - n, \frac{5}{2}, \tan\left[\frac{1}{2}(e + f x)\right]^2, -\tan\left[\frac{1}{2}(e + f x)\right]^2\right] + \right. \\
 & \quad \quad \left. (-3 + 2n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2} + n, 1 - n, \frac{5}{2}, \tan\left[\frac{1}{2}(e + f x)\right]^2, -\tan\left[\frac{1}{2}(e + f x)\right]^2\right]\right) \\
 & \quad \tan\left[\frac{1}{2}(e + f x)\right]^2 \Big) - \left(6 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2} + n, 1 - n, \frac{3}{2}, \tan\left[\frac{1}{2}(e + f x)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(e + f x)\right]^2\right] \cos[e + f x] \left(\sec\left[\frac{1}{2}(e + f x)\right]\right)^n \right. \\
 & \quad \left. \left(\cos\left[\frac{1}{2}(e + f x)\right]^2 \sec[e + f x]\right)^{\frac{3}{2}+n} \tan\left[\frac{1}{2}(e + f x)\right] \left(-1 + \tan\left[\frac{1}{2}(e + f x)\right]\right)^2 \right)^2
 \end{aligned}$$

$$\begin{aligned}
 & \left( \left( 2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{3}{2}+n, 2-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. (-3+2n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 1-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \right. \\
 & \quad \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] + 3 \left( -\frac{1}{3}(1-n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{3}{2}+n, 2-n, \right. \right. \\
 & \quad \left. \left. \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] + \right. \\
 & \quad \left. \frac{1}{3} \left( -\frac{3}{2}+n \right) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 1-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \quad \left. \left. \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \right) + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right. \\
 & \quad \left( 2(-1+n) \left( -\frac{3}{5}(2-n) \operatorname{AppellF1}\left[\frac{5}{2}, -\frac{3}{2}+n, 3-n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] + \frac{3}{5} \left( -\frac{3}{2}+n \right) \right. \\
 & \quad \left. \operatorname{AppellF1}\left[\frac{5}{2}, -\frac{1}{2}+n, 2-n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \right) + (-3+2n) \left( -\frac{3}{5}(1-n) \operatorname{AppellF1}\left[\frac{5}{2}, \right. \right. \\
 & \quad \left. \left. -\frac{1}{2}+n, 2-n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \right. \\
 & \quad \left. \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] + \frac{3}{5} \left( -\frac{1}{2}+n \right) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{2}+n, 1-n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \right) \right) \Big/ \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2}+n, 1-n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left( 2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{3}{2}+n, 2-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left. (-3+2n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 1-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right) + \\
 & \left( 6 \left( \frac{3}{2}+n \right) \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2}+n, 1-n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \quad \operatorname{Cos}[e+fx] \left( \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \right)^n \left( \operatorname{Cos}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Sec}[e+fx] \right)^{\frac{1}{2}+n} \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \\
 & \quad \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right)^2 \left( -\operatorname{Cos}\left[\frac{1}{2}(e+fx)\right] \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right] + \right. \\
 & \quad \left. \operatorname{Cos}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Sec}[e+fx] \operatorname{Tan}[e+fx] \right) \Big/ \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2}+n, 1-n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right.
 \end{aligned}$$

$$\left( 2 (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{3}{2}+n, 2-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\ \left. (-3+2n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 1-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \Bigg)$$

**Problem 299: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int (-\operatorname{Sec}[e+fx])^n (1+\operatorname{Sec}[e+fx])^{3/2} dx$$

Optimal (type 5, 117 leaves, 4 steps):

$$\frac{2 (-\operatorname{Sec}[e+fx])^n \operatorname{Tan}[e+fx]}{f (1+2n) \sqrt{1+\operatorname{Sec}[e+fx]}} - \\ \left( \frac{(1+4n) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, n, 1+n, \operatorname{Sec}[e+fx]\right] (-\operatorname{Sec}[e+fx])^n \operatorname{Tan}[e+fx]}{f n (1+2n) \sqrt{1-\operatorname{Sec}[e+fx]} \sqrt{1+\operatorname{Sec}[e+fx]}} \right) /$$

Result (type 5, 6381 leaves):

$$\left( 14 \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^3 \left( \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \right)^n \right. \\ \left. (-\operatorname{Sec}[e+fx])^n \operatorname{Sec}[e+fx]^{-\frac{3}{2}n} \left( \operatorname{Cos}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Sec}[e+fx] \right)^{-\frac{3}{2}n} \right. \\ \left. (1+\operatorname{Sec}[e+fx])^{3/2} \left( \operatorname{Cos}\left[\frac{3}{2}(e+fx)\right] \left( \frac{1}{8} \operatorname{Sec}[e+fx]^{-\frac{3}{2}n} + \frac{3}{8} \operatorname{Sec}[e+fx]^{\frac{1}{2}n} + \right. \right. \right. \\ \left. \left. \frac{3}{4} i \operatorname{Sec}[e+fx]^{\frac{1}{2}n} \operatorname{Sin}[e+fx] - \frac{3}{8} \operatorname{Sec}[e+fx]^{\frac{1}{2}n} \operatorname{Sin}[e+fx]^2 + \right. \right. \\ \left. \left. \operatorname{Cos}[e+fx] \left( \frac{3}{8} \operatorname{Sec}[e+fx]^{\frac{1}{2}n} + \frac{3}{8} i \operatorname{Sec}[e+fx]^{\frac{1}{2}n} \operatorname{Sin}[e+fx] \right) + \right. \right. \\ \left. \left. \operatorname{Sec}[e+fx] \left( \frac{1}{8} \operatorname{Sec}[e+fx]^{\frac{1}{2}n} + \frac{3}{8} i \operatorname{Sec}[e+fx]^{\frac{1}{2}n} \operatorname{Sin}[e+fx] - \right. \right. \right. \\ \left. \left. \left. \frac{3}{8} \operatorname{Sec}[e+fx]^{\frac{1}{2}n} \operatorname{Sin}[e+fx]^2 - \frac{1}{8} i \operatorname{Sec}[e+fx]^{\frac{1}{2}n} \operatorname{Sin}[e+fx]^3 \right) \right) - \right. \\ \left. \frac{1}{8} i \operatorname{Sec}[e+fx]^{-\frac{3}{2}n} \operatorname{Sin}\left[\frac{3}{2}(e+fx)\right] - \frac{3}{8} i \operatorname{Sec}[e+fx]^{\frac{1}{2}n} \operatorname{Sin}\left[\frac{3}{2}(e+fx)\right] + \right. \\ \left. \frac{3}{4} \operatorname{Sec}[e+fx]^{\frac{1}{2}n} \operatorname{Sin}[e+fx] \operatorname{Sin}\left[\frac{3}{2}(e+fx)\right] + \right. \\ \left. \frac{3}{8} i \operatorname{Sec}[e+fx]^{\frac{1}{2}n} \operatorname{Sin}[e+fx]^2 \operatorname{Sin}\left[\frac{3}{2}(e+fx)\right] + \operatorname{Cos}[e+fx] \right. \\ \left. \left( -\frac{3}{8} i \operatorname{Sec}[e+fx]^{\frac{1}{2}n} \operatorname{Sin}\left[\frac{3}{2}(e+fx)\right] + \frac{3}{8} \operatorname{Sec}[e+fx]^{\frac{1}{2}n} \operatorname{Sin}[e+fx] \operatorname{Sin}\left[\frac{3}{2}(e+fx)\right] \right) \right) + \\ \left. \operatorname{Sec}[e+fx] \left( -\frac{1}{8} i \operatorname{Sec}[e+fx]^{\frac{1}{2}n} \operatorname{Sin}\left[\frac{3}{2}(e+fx)\right] + \frac{3}{8} \operatorname{Sec}[e+fx]^{\frac{1}{2}n} \operatorname{Sin}[e+fx] \right) \right)$$

$$\begin{aligned}
 & \left( \sin\left[\frac{3}{2}(e+fx)\right] + \frac{3}{8} \operatorname{Sec}[e+fx]^{\frac{1}{2}+n} \sin[e+fx]^2 \sin\left[\frac{3}{2}(e+fx)\right] - \right. \\
 & \left. \frac{1}{8} \operatorname{Sec}[e+fx]^{\frac{1}{2}+n} \sin[e+fx]^3 \sin\left[\frac{3}{2}(e+fx)\right] \right) \tan\left[\frac{1}{2}(e+fx)\right] \\
 & \left( 8 \operatorname{Gamma}\left[\frac{5}{2}+n\right] \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2 \operatorname{Sec}[e+fx] \sin\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right]^2 + \right. \\
 & \left. 5 \operatorname{Gamma}\left[\frac{3}{2}+n\right] \operatorname{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2}, -2 \operatorname{Sec}[e+fx] \sin\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \left. \left(-3 + \tan\left[\frac{1}{2}(e+fx)\right]^2 + 2 \tan\left[\frac{1}{2}(e+fx)\right]^4\right) \right) \Big/ \\
 & \left( f \left(-1 + \tan\left[\frac{1}{2}(e+fx)\right]^2\right) \left( 8 \operatorname{Gamma}\left[\frac{5}{2}+n\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^4 \tan\left[\frac{1}{2}(e+fx)\right]^2 \right. \right. \\
 & \left. \left( 7 \cos[e+fx] (-5 - 2n + 2(1+n) \cos[e+fx]) \right. \right. \\
 & \left. \left. \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2 \operatorname{Sec}[e+fx] \sin\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 + \right. \right. \\
 & \left. \left. 8(5+2n) \operatorname{Hypergeometric2F1}\left[3, \frac{7}{2}+n, \frac{9}{2}, -2 \operatorname{Sec}[e+fx] \sin\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) + 7 \operatorname{Gamma}\left[\frac{3}{2}+n\right] \left(-1 + \tan\left[\frac{1}{2}(e+fx)\right]^2\right) \right. \\
 & \left. \left(\frac{5}{2} \cos[e+fx] (-15 - 9n + (9+8n) \cos[e+fx] + n \cos[2(e+fx)]) \right) \right. \\
 & \left. \operatorname{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2}, -2 \operatorname{Sec}[e+fx] \sin\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^6 + \right. \\
 & \left. \left. 2(3+2n)(5 + \cos[e+fx]) \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, \right. \right. \right. \\
 & \left. \left. \left. -2 \operatorname{Sec}[e+fx] \sin\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^4 \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \right) \Big/ \\
 & \left( - \left( \left( 14 \left( \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \right)^{1+n} \left( \cos\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Sec}[e+fx] \right)^{-\frac{3}{2}+n} \tan\left[\frac{1}{2}(e+fx)\right]^2 \right. \right. \right. \\
 & \left. \left( 8 \operatorname{Gamma}\left[\frac{5}{2}+n\right] \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2 \operatorname{Sec}[e+fx] \sin\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \\
 & \left. \left. \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right]^2 + \right. \right. \\
 & \left. \left. 5 \operatorname{Gamma}\left[\frac{3}{2}+n\right] \operatorname{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2}, -2 \operatorname{Sec}[e+fx] \sin\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \\
 & \left. \left. \left(-3 + \tan\left[\frac{1}{2}(e+fx)\right]^2 + 2 \tan\left[\frac{1}{2}(e+fx)\right]^4\right) \right) \right) \Big/ \\
 & \left( \left( -1 + \tan\left[\frac{1}{2}(e+fx)\right]^2 \right)^2 \left( 8 \operatorname{Gamma}\left[\frac{5}{2}+n\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^4 \tan\left[\frac{1}{2}(e+fx)\right]^2 \right. \right. \\
 & \left. \left( 7 \cos[e+fx] (-5 - 2n + 2(1+n) \cos[e+fx]) \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \begin{aligned}
 & \frac{7}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 + 8(5+2n) \\
 & \operatorname{Hypergeometric2F1}\left[3, \frac{7}{2}+n, \frac{9}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \\
 & \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 + 7 \operatorname{Gamma}\left[\frac{3}{2}+n\right] \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right) \\
 & \left(\frac{5}{2} \operatorname{Cos}[e+fx] (-15-9n+(9+8n) \operatorname{Cos}[e+fx] + n \operatorname{Cos}[2(e+fx)])\right) \\
 & \operatorname{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \\
 & \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^6 + 2(3+2n)(5+\operatorname{Cos}[e+fx]) \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, \right. \\
 & \left. -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^4 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right) \right) \Bigg) + \\
 & \left(7 \left(\operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2\right)^{1+n} \left(\operatorname{Cos}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Sec}[e+fx]\right)^{-\frac{3}{2}+n} \right. \\
 & \left. \left(8 \operatorname{Gamma}\left[\frac{5}{2}+n\right] \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \\
 & \left. \left. \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 + 5 \operatorname{Gamma}\left[\frac{3}{2}+n\right] \operatorname{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2}, \right. \right. \right. \\
 & \left. \left. \left. -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \left(-3 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 + 2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^4\right)\right)\right) \right) \Bigg) / \\
 & \left( \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right) \left(8 \operatorname{Gamma}\left[\frac{5}{2}+n\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^4 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right. \right. \\
 & \left. \left. \left(7 \operatorname{Cos}[e+fx] (-5-2n+2(1+n) \operatorname{Cos}[e+fx]) \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+ \right. \right. \right. \right. \\
 & \left. \left. \left. n, \frac{7}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 + \right. \right. \right. \\
 & \left. \left. \left. 8(5+2n) \operatorname{Hypergeometric2F1}\left[3, \frac{7}{2}+n, \frac{9}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \right. \\
 & \left. \left. \left. \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 + 7 \operatorname{Gamma}\left[\frac{3}{2}+n\right] \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right) \right. \right. \right. \\
 & \left. \left. \left. \left(\frac{5}{2} \operatorname{Cos}[e+fx] (-15-9n+(9+8n) \operatorname{Cos}[e+fx] + n \operatorname{Cos}[2(e+fx)])\right) \right. \right. \right. \\
 & \left. \left. \left. \operatorname{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \right. \\
 & \left. \left. \left. \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^6 + 2(3+2n)(5+\operatorname{Cos}[e+fx]) \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \right. \right. \right. \\
 & \left. \left. \left. \frac{7}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^4 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right)\right) \right) \right) \Bigg) + \\
 & \left(14n \left(\operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2\right)^n \left(\operatorname{Cos}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Sec}[e+fx]\right)^{-\frac{3}{2}+n} \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right. \right. \\
 & \left. \left. \left(8 \operatorname{Gamma}\left[\frac{5}{2}+n\right] \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \right. \right.
 \end{aligned}
 \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( \left( \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2 + 5 \text{Gamma}\left[\frac{3}{2}+n\right] \text{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2}, \right. \right. \right. \\
 & \quad \left. \left. -2 \text{Sec}[e+fx] \text{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \left(-3 + \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2 + 2 \text{Tan}\left[\frac{1}{2}(e+fx)\right]^4\right)\right)\right) / \\
 & \left( \left( -1 + \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right) \left( 8 \text{Gamma}\left[\frac{5}{2}+n\right] \text{Sec}\left[\frac{1}{2}(e+fx)\right]^4 \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right. \right. \\
 & \quad \left( 7 \text{Cos}[e+fx] (-5 - 2n + 2(1+n) \text{Cos}[e+fx]) \text{Hypergeometric2F1}\left[2, \frac{5}{2}+ \right. \right. \\
 & \quad \quad \left. \left. n, \frac{7}{2}, -2 \text{Sec}[e+fx] \text{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 + \right. \right. \\
 & \quad \left. 8(5+2n) \text{Hypergeometric2F1}\left[3, \frac{7}{2}+n, \frac{9}{2}, -2 \text{Sec}[e+fx] \text{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \quad \left. \left. \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right) + 7 \text{Gamma}\left[\frac{3}{2}+n\right] \left(-1 + \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right) \right. \\
 & \quad \left( \frac{5}{2} \text{Cos}[e+fx] (-15 - 9n + (9+8n) \text{Cos}[e+fx] + n \text{Cos}[2(e+fx)]) \right) \\
 & \quad \left. \text{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2}, -2 \text{Sec}[e+fx] \text{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \quad \left. \left. \text{Sec}\left[\frac{1}{2}(e+fx)\right]^6 + 2(3+2n)(5 + \text{Cos}[e+fx]) \text{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \right. \right. \right. \\
 & \quad \left. \left. \frac{7}{2}, -2 \text{Sec}[e+fx] \text{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(e+fx)\right]^4 \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right)\right) \right) + \\
 & \left( 14 \left(-\frac{3}{2}+n\right) \left(\text{Sec}\left[\frac{1}{2}(e+fx)\right]^2\right)^n \left(\text{Cos}\left[\frac{1}{2}(e+fx)\right]^2 \text{Sec}[e+fx]\right)^{-\frac{5}{2}+n} \text{Tan}\left[\frac{1}{2}(e+fx)\right] \right. \\
 & \quad \left( 8 \text{Gamma}\left[\frac{5}{2}+n\right] \text{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2 \text{Sec}[e+fx] \text{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \quad \left. \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2 + 5 \text{Gamma}\left[\frac{3}{2}+n\right] \text{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2}, \right. \right. \\
 & \quad \left. \left. -2 \text{Sec}[e+fx] \text{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \left(-3 + \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2 + 2 \text{Tan}\left[\frac{1}{2}(e+fx)\right]^4\right)\right) \right) \\
 & \left( -\text{Cos}\left[\frac{1}{2}(e+fx)\right] \text{Sec}[e+fx] \text{Sin}\left[\frac{1}{2}(e+fx)\right] + \right. \\
 & \quad \left. \text{Cos}\left[\frac{1}{2}(e+fx)\right]^2 \text{Sec}[e+fx] \text{Tan}[e+fx] \right) \right) / \\
 & \left( \left( -1 + \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right) \left( 8 \text{Gamma}\left[\frac{5}{2}+n\right] \text{Sec}\left[\frac{1}{2}(e+fx)\right]^4 \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right. \right. \\
 & \quad \left( 7 \text{Cos}[e+fx] (-5 - 2n + 2(1+n) \text{Cos}[e+fx]) \text{Hypergeometric2F1}\left[2, \frac{5}{2}+ \right. \right. \\
 & \quad \quad \left. \left. n, \frac{7}{2}, -2 \text{Sec}[e+fx] \text{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 + \right. \right. \\
 & \quad \left. 8(5+2n) \text{Hypergeometric2F1}\left[3, \frac{7}{2}+n, \frac{9}{2}, -2 \text{Sec}[e+fx] \text{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \quad \left. \left. \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right) + 7 \text{Gamma}\left[\frac{3}{2}+n\right] \left(-1 + \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right) \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( \frac{5}{2} \cos[e+fx] (-15-9n+(9+8n)\cos[e+fx]+n\cos[2(e+fx)]) \right. \\
 & \quad \text{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2}, -2\sec[e+fx]\sin\left[\frac{1}{2}(e+fx)\right]^2\right] \\
 & \quad \left. \sec\left[\frac{1}{2}(e+fx)\right]^6 + 2(3+2n)(5+\cos[e+fx]) \text{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2\sec[e+fx]\sin\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^4 \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \right) + \\
 & \left( 14 \left( \sec\left[\frac{1}{2}(e+fx)\right]^2 \right)^n \left( \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \right)^{-\frac{3}{2}+n} \tan\left[\frac{1}{2}(e+fx)\right] \right. \\
 & \quad \left( 8 \Gamma\left[\frac{5}{2}+n\right] \text{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2\sec[e+fx]\sin\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \quad \left. \sec\left[\frac{1}{2}(e+fx)\right]^4 \tan\left[\frac{1}{2}(e+fx)\right] + 8 \Gamma\left[\frac{5}{2}+n\right] \text{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2\sec[e+fx]\sin\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right]^3 + \right. \\
 & \quad \left. 5 \Gamma\left[\frac{3}{2}+n\right] \text{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2}, -2\sec[e+fx]\sin\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \quad \left. \left( \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + 4 \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right]^3 \right) + \right. \\
 & \quad \left. \frac{32}{7} \left(\frac{5}{2}+n\right) \Gamma\left[\frac{5}{2}+n\right] \text{Hypergeometric2F1}\left[3, \frac{7}{2}+n, \frac{9}{2}, -2\sec[e+fx]\sin\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \right. \\
 & \quad \left. \tan\left[\frac{1}{2}(e+fx)\right]^2 \left( -2\cos\left[\frac{1}{2}(e+fx)\right] \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right] - \right. \right. \\
 & \quad \left. \left. 2\sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right]^2 \tan[e+fx] \right) + 2 \left(\frac{3}{2}+n\right) \Gamma\left[\frac{3}{2}+n\right] \right. \\
 & \quad \left. \text{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2\sec[e+fx]\sin\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \quad \left. \left( -3 + \tan\left[\frac{1}{2}(e+fx)\right]^2 + 2 \tan\left[\frac{1}{2}(e+fx)\right]^4 \right) \left( -2\cos\left[\frac{1}{2}(e+fx)\right] \sec[e+fx] \right. \right. \\
 & \quad \left. \left. \sin\left[\frac{1}{2}(e+fx)\right] - 2\sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right]^2 \tan[e+fx] \right) \right) \right) \Big/ \\
 & \left( \left( -1 + \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \left( 8 \Gamma\left[\frac{5}{2}+n\right] \sec\left[\frac{1}{2}(e+fx)\right]^4 \tan\left[\frac{1}{2}(e+fx)\right]^2 \right. \right. \\
 & \quad \left. \left( 7 \cos[e+fx] (-5-2n+2(1+n)\cos[e+fx]) \text{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2\sec[e+fx]\sin\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 + \right. \right. \\
 & \quad \left. \left. 8(5+2n) \text{Hypergeometric2F1}\left[3, \frac{7}{2}+n, \frac{9}{2}, -2\sec[e+fx]\sin\left[\frac{1}{2}(e+fx)\right]^2\right] \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) + 7 \Gamma\left[\frac{3}{2}+n\right] \left( -1 + \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \right. \\
 & \quad \left. \left( \frac{5}{2} \cos[e+fx] (-15-9n+(9+8n)\cos[e+fx]+n\cos[2(e+fx)]) \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \text{Hypergeometric2F1}\left[1, \frac{3}{2} + n, \frac{5}{2}, -2 \text{Sec}[e + f x] \text{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \\
 & \text{Sec}\left[\frac{1}{2}(e + f x)\right]^6 + 2(3 + 2n)(5 + \text{Cos}[e + f x]) \text{Hypergeometric2F1}\left[2, \frac{5}{2} + n, \frac{7}{2}, -2 \text{Sec}[e + f x] \text{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \text{Sec}\left[\frac{1}{2}(e + f x)\right]^4 \text{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right) - \\
 & \left(14 \left(\text{Sec}\left[\frac{1}{2}(e + f x)\right]^2\right)^n \left(\text{Cos}\left[\frac{1}{2}(e + f x)\right]^2 \text{Sec}[e + f x]\right)^{-\frac{3}{2}+n} \text{Tan}\left[\frac{1}{2}(e + f x)\right]\right. \\
 & \left. \left(8 \text{Gamma}\left[\frac{5}{2} + n\right] \text{Hypergeometric2F1}\left[2, \frac{5}{2} + n, \frac{7}{2}, -2 \text{Sec}[e + f x] \text{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \right. \right. \\
 & \left. \left. \text{Sec}\left[\frac{1}{2}(e + f x)\right]^2 \text{Tan}\left[\frac{1}{2}(e + f x)\right]^2 + 5 \text{Gamma}\left[\frac{3}{2} + n\right] \text{Hypergeometric2F1}\left[1, \frac{3}{2} + n, \frac{5}{2}, -2 \text{Sec}[e + f x] \text{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \right. \right. \\
 & \left. \left. \left(-3 + \text{Tan}\left[\frac{1}{2}(e + f x)\right]^2 + 2 \text{Tan}\left[\frac{1}{2}(e + f x)\right]^4\right)\right)\right) \\
 & \left(8 \text{Gamma}\left[\frac{5}{2} + n\right] \text{Sec}\left[\frac{1}{2}(e + f x)\right]^6 \text{Tan}\left[\frac{1}{2}(e + f x)\right]\right. \\
 & \left. \left(7 \text{Cos}[e + f x](-5 - 2n + 2(1 + n) \text{Cos}[e + f x]) \text{Hypergeometric2F1}\left[2, \frac{5}{2} + n, \frac{7}{2}, -2 \text{Sec}[e + f x] \text{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \text{Sec}\left[\frac{1}{2}(e + f x)\right]^2 + \right. \right. \\
 & \left. \left. 8(5 + 2n) \text{Hypergeometric2F1}\left[3, \frac{7}{2} + n, \frac{9}{2}, -2 \text{Sec}[e + f x] \text{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \text{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right) + 16 \text{Gamma}\left[\frac{5}{2} + n\right] \text{Sec}\left[\frac{1}{2}(e + f x)\right]^4 \text{Tan}\left[\frac{1}{2}(e + f x)\right]^3 \right. \right. \\
 & \left. \left. \left(7 \text{Cos}[e + f x](-5 - 2n + 2(1 + n) \text{Cos}[e + f x]) \text{Hypergeometric2F1}\left[2, \frac{5}{2} + n, \frac{7}{2}, -2 \text{Sec}[e + f x] \text{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \text{Sec}\left[\frac{1}{2}(e + f x)\right]^2 + \right. \right. \right. \\
 & \left. \left. 8(5 + 2n) \text{Hypergeometric2F1}\left[3, \frac{7}{2} + n, \frac{9}{2}, -2 \text{Sec}[e + f x] \text{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \text{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right) + 7 \text{Gamma}\left[\frac{3}{2} + n\right] \text{Sec}\left[\frac{1}{2}(e + f x)\right]^2 \text{Tan}\left[\frac{1}{2}(e + f x)\right] \right. \right. \\
 & \left. \left. \left(\frac{5}{2} \text{Cos}[e + f x](-15 - 9n + (9 + 8n) \text{Cos}[e + f x] + n \text{Cos}[2(e + f x)])\right)\right) \right. \\
 & \left. \text{Hypergeometric2F1}\left[1, \frac{3}{2} + n, \frac{5}{2}, -2 \text{Sec}[e + f x] \text{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \right. \\
 & \left. \text{Sec}\left[\frac{1}{2}(e + f x)\right]^6 + 2(3 + 2n)(5 + \text{Cos}[e + f x]) \text{Hypergeometric2F1}\left[2, \frac{5}{2} + n, \frac{7}{2}, -2 \text{Sec}[e + f x] \text{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \text{Sec}\left[\frac{1}{2}(e + f x)\right]^4 \text{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right) + \\
 & 8 \text{Gamma}\left[\frac{5}{2} + n\right] \text{Sec}\left[\frac{1}{2}(e + f x)\right]^4 \text{Tan}\left[\frac{1}{2}(e + f x)\right]^2 \left(-14(1 + n) \text{Cos}[e + f x] \right. \\
 & \left. \text{Hypergeometric2F1}\left[2, \frac{5}{2} + n, \frac{7}{2}, -2 \text{Sec}[e + f x] \text{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \right. \\
 & \left. \left. \text{Sec}\left[\frac{1}{2}(e + f x)\right]^2 \text{Sin}[e + f x] - 7(-5 - 2n + 2(1 + n) \text{Cos}[e + f x])\right)\right)
 \end{aligned}$$



$$\begin{aligned}
 & \text{Hypergeometric2F1}\left[2, \frac{5}{2} + n, \frac{7}{2}, -2 \operatorname{Sec}[e + f x] \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \\
 & \operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^2 \operatorname{Sin}[e + f x] + 7 \operatorname{Cos}[e + f x] (-5 - 2n + 2(1 + n) \operatorname{Cos}[e + f x]) \\
 & \text{Hypergeometric2F1}\left[2, \frac{5}{2} + n, \frac{7}{2}, -2 \operatorname{Sec}[e + f x] \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \\
 & \operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right] + 8(5 + 2n) \text{Hypergeometric2F1}\left[3, \frac{7}{2} + \right. \\
 & \quad \left. n, \frac{9}{2}, -2 \operatorname{Sec}[e + f x] \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right] + \\
 & 4\left(\frac{5}{2} + n\right) \operatorname{Cos}[e + f x] (-5 - 2n + 2(1 + n) \operatorname{Cos}[e + f x]) \text{Hypergeometric2F1}\left[3, \frac{7}{2} + \right. \\
 & \quad \left. n, \frac{9}{2}, -2 \operatorname{Sec}[e + f x] \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^2 \left(-2 \operatorname{Cos}\left[\frac{1}{2}(e + f x)\right] \right. \\
 & \quad \left. \operatorname{Sec}[e + f x] \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right] - 2 \operatorname{Sec}[e + f x] \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right]^2 \operatorname{Tan}[e + f x]\right) + \\
 & \frac{16}{3}\left(\frac{7}{2} + n\right)(5 + 2n) \text{Hypergeometric2F1}\left[4, \frac{9}{2} + n, \frac{11}{2}, -2 \operatorname{Sec}[e + f x] \right. \\
 & \quad \left. \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2 \left(-2 \operatorname{Cos}\left[\frac{1}{2}(e + f x)\right] \operatorname{Sec}[e + f x] \right. \\
 & \quad \left. \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right] - 2 \operatorname{Sec}[e + f x] \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right]^2 \operatorname{Tan}[e + f x]\right) + \\
 & 7 \operatorname{Gamma}\left[\frac{3}{2} + n\right] \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right) \left(-\frac{5}{2}(-15 - 9n + (9 + 8n) \operatorname{Cos}[e + f x] + \right. \\
 & \quad \left. n \operatorname{Cos}[2(e + f x)])\right) \text{Hypergeometric2F1}\left[1, \frac{3}{2} + n, \frac{5}{2}, -2 \right. \\
 & \quad \left. \operatorname{Sec}[e + f x] \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^6 \operatorname{Sin}[e + f x] + \\
 & \frac{5}{2} \operatorname{Cos}[e + f x] \text{Hypergeometric2F1}\left[1, \frac{3}{2} + n, \frac{5}{2}, -2 \operatorname{Sec}[e + f x] \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \\
 & \quad \operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^6 (-9 + 8n) \operatorname{Sin}[e + f x] - 2n \operatorname{Sin}[2(e + f x)] + \\
 & \frac{15}{2} \operatorname{Cos}[e + f x] (-15 - 9n + (9 + 8n) \operatorname{Cos}[e + f x] + n \operatorname{Cos}[2(e + f x)]) \\
 & \text{Hypergeometric2F1}\left[1, \frac{3}{2} + n, \frac{5}{2}, -2 \operatorname{Sec}[e + f x] \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \\
 & \operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^6 \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right] + 2(3 + 2n)(5 + \operatorname{Cos}[e + f x]) \\
 & \text{Hypergeometric2F1}\left[2, \frac{5}{2} + n, \frac{7}{2}, -2 \operatorname{Sec}[e + f x] \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \\
 & \operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^6 \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right] - 2(3 + 2n) \text{Hypergeometric2F1}\left[2, \frac{5}{2} + n, \frac{7}{2}, -2 \right. \\
 & \quad \left. \operatorname{Sec}[e + f x] \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^4 \operatorname{Sin}[e + f x] \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2 + \\
 & 4(3 + 2n)(5 + \operatorname{Cos}[e + f x]) \text{Hypergeometric2F1}\left[2, \frac{5}{2} + n, \frac{7}{2}, -2 \right.
 \end{aligned}$$

$$\begin{aligned}
 & \text{Sec}[e + f x] \text{Sin}\left[\frac{1}{2}(e + f x)\right]^2 \text{Sec}\left[\frac{1}{2}(e + f x)\right]^4 \text{Tan}\left[\frac{1}{2}(e + f x)\right]^3 + \\
 & \left(\frac{3}{2} + n\right) \text{Cos}[e + f x] \left(-15 - 9n + (9 + 8n) \text{Cos}[e + f x] + n \text{Cos}[2(e + f x)]\right) \\
 & \text{Hypergeometric2F1}\left[2, \frac{5}{2} + n, \frac{7}{2}, -2 \text{Sec}[e + f x] \text{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \\
 & \text{Sec}\left[\frac{1}{2}(e + f x)\right]^6 \left(-2 \text{Cos}\left[\frac{1}{2}(e + f x)\right] \text{Sec}[e + f x] \text{Sin}\left[\frac{1}{2}(e + f x)\right] - 2 \text{Sec}[e + f x] \text{Sin}\left[\frac{1}{2}(e + f x)\right]^2 \text{Tan}[e + f x]\right) + \frac{8}{7} \left(\frac{5}{2} + n\right) (3 + 2n) (5 + \text{Cos}[e + f x]) \\
 & \text{Hypergeometric2F1}\left[3, \frac{7}{2} + n, \frac{9}{2}, -2 \text{Sec}[e + f x] \text{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \\
 & \text{Sec}\left[\frac{1}{2}(e + f x)\right]^4 \text{Tan}\left[\frac{1}{2}(e + f x)\right]^2 \left(-2 \text{Cos}\left[\frac{1}{2}(e + f x)\right] \text{Sec}[e + f x] \text{Sin}\left[\frac{1}{2}(e + f x)\right] - 2 \text{Sec}[e + f x] \text{Sin}\left[\frac{1}{2}(e + f x)\right]^2 \text{Tan}[e + f x]\right) \right) \right) \Big/ \\
 & \left( \left(-1 + \text{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right) \left(8 \text{Gamma}\left[\frac{5}{2} + n\right] \text{Sec}\left[\frac{1}{2}(e + f x)\right]^4 \text{Tan}\left[\frac{1}{2}(e + f x)\right]^2 \right. \right. \\
 & \left. \left(7 \text{Cos}[e + f x] (-5 - 2n + 2(1 + n) \text{Cos}[e + f x]) \text{Hypergeometric2F1}\left[2, \frac{5}{2} + n, \frac{7}{2}, -2 \text{Sec}[e + f x] \text{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \text{Sec}\left[\frac{1}{2}(e + f x)\right]^2 + 8(5 + 2n) \right. \right. \\
 & \left. \left. \text{Hypergeometric2F1}\left[3, \frac{7}{2} + n, \frac{9}{2}, -2 \text{Sec}[e + f x] \text{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \right. \right. \\
 & \left. \left. \text{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right) + 7 \text{Gamma}\left[\frac{3}{2} + n\right] \left(-1 + \text{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right) \right. \right. \\
 & \left. \left(\frac{5}{2} \text{Cos}[e + f x] (-15 - 9n + (9 + 8n) \text{Cos}[e + f x] + n \text{Cos}[2(e + f x)]) \right. \right. \\
 & \left. \left. \text{Hypergeometric2F1}\left[1, \frac{3}{2} + n, \frac{5}{2}, -2 \text{Sec}[e + f x] \text{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \right. \right. \\
 & \left. \left. \text{Sec}\left[\frac{1}{2}(e + f x)\right]^6 + 2(3 + 2n)(5 + \text{Cos}[e + f x]) \text{Hypergeometric2F1}\left[2, \frac{5}{2} + n, \frac{7}{2}, -2 \text{Sec}[e + f x] \text{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \text{Sec}\left[\frac{1}{2}(e + f x)\right]^4 \text{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right) \right) \right) \Big/
 \end{aligned}$$

**Problem 300: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int (-\text{Sec}[e + f x])^n \sqrt{1 + \text{Sec}[e + f x]} \, dx$$

Optimal (type 5, 64 leaves, 2 steps):

$$- \left( \left( \text{Hypergeometric2F1}\left[\frac{1}{2}, n, 1 + n, \text{Sec}[e + f x]\right] (-\text{Sec}[e + f x])^n \text{Tan}[e + f x] \right) \Big/ \left( f n \sqrt{1 - \text{Sec}[e + f x]} \sqrt{1 + \text{Sec}[e + f x]} \right) \right)$$

Result (type 5, 213 leaves):

$$\begin{aligned}
 & -\frac{1}{f n (1+n)} i^{\frac{1}{2}+n} e^{\frac{1}{2} i (e+f x)} \left(1+e^{2 i (e+f x)}\right)^{-\frac{1}{2}+n} \left(e^{-i (e+f x)} \left(1+e^{2 i (e+f x)}\right)\right)^{\frac{1}{2}-n} \\
 & \cos [e+f x]^{\frac{1}{2}+n} \left( (1+n) \operatorname{Hypergeometric2F1}\left[\frac{n}{2}, \frac{1}{2}+n, \frac{2+n}{2}, -e^{2 i (e+f x)}\right] + \right. \\
 & \quad \left. e^{i (e+f x)} n \operatorname{Hypergeometric2F1}\left[\frac{1}{2}+n, \frac{1+n}{2}, \frac{3+n}{2}, -e^{2 i (e+f x)}\right] \right) \\
 & \operatorname{Sec}\left[\frac{1}{2}(e+f x)\right] \left(-\operatorname{Sec}[e+f x]\right)^n \sqrt{1+\operatorname{Sec}[e+f x]}
 \end{aligned}$$

**Problem 301: Result more than twice size of optimal antiderivative.**

$$\int \frac{(-\operatorname{Sec}[e+f x])^n}{\sqrt{1+\operatorname{Sec}[e+f x]}} dx$$

Optimal (type 6, 73 leaves, 2 steps):

$$\begin{aligned}
 & -\left( \operatorname{AppellF1}\left[n, \frac{1}{2}, 1, 1+n, \operatorname{Sec}[e+f x], -\operatorname{Sec}[e+f x]\right] (-\operatorname{Sec}[e+f x])^n \operatorname{Tan}[e+f x] \right) / \\
 & \quad \left( f n \sqrt{1-\operatorname{Sec}[e+f x]} \sqrt{1+\operatorname{Sec}[e+f x]} \right)
 \end{aligned}$$

Result (type 6, 2951 leaves):

$$\begin{aligned}
 & \left( 3 \sqrt{2} \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, 1-n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^2\right] \left(\operatorname{Sec}\left[\frac{1}{2}(e+f x)\right]^2\right)^n \right. \\
 & \quad \left. (-\operatorname{Sec}[e+f x])^n \operatorname{Sec}[e+f x]^{-\frac{1}{2}-n+\frac{1}{2}(-1+2n)} \left(\cos\left[\frac{1}{2}(e+f x)\right]^2 \operatorname{Sec}[e+f x]\right)^n \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right] \right) / \\
 & \left( f \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, 1-n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^2\right] + \right. \right. \\
 & \quad \left( 2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 2-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^2\right] + \right. \\
 & \quad \left. (-1+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+n, 1-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^2\right] \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^2 \right) \right. \\
 & \left. \left( \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, 1-n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^2\right] \cos[e+f x] \right. \right. \right. \\
 & \quad \left. \left. \left(\operatorname{Sec}\left[\frac{1}{2}(e+f x)\right]^2\right)^{1+n} \left(\cos\left[\frac{1}{2}(e+f x)\right]^2 \operatorname{Sec}[e+f x]\right)^n \sqrt{1+\operatorname{Sec}[e+f x]} \right) \right) / \\
 & \left( \sqrt{2} \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, 1-n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^2\right] + \right. \right. \\
 & \quad \left( 2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 2-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^2\right] + \right. \\
 & \quad \left. (-1+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+n, 1-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^2\right] \right) \right. \\
 & \quad \left. \left. \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^2 \right) \right) - \left( 3 \sqrt{2} \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, 1-n, \frac{3}{2}, \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \left( \sec\left[\frac{1}{2}(e+fx)\right]^2 \right)^n \\
 & \left( \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \right)^n \sqrt{1+\sec[e+fx]} \sin[e+fx] \tan\left[\frac{1}{2}(e+fx)\right] \Big/ \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \left( 2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \left. (-1+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \\
 & \tan\left[\frac{1}{2}(e+fx)\right]^2 \Big) + \left( 3\sqrt{2} n \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \cos[e+fx] \left( \sec\left[\frac{1}{2}(e+fx)\right]^2 \right)^n \right. \\
 & \left. \left( \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \right)^n \sqrt{1+\sec[e+fx]} \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \Big/ \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \left( 2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \left. (-1+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \\
 & \tan\left[\frac{1}{2}(e+fx)\right]^2 \Big) + \left( 3\sqrt{2} \cos[e+fx] \left( \sec\left[\frac{1}{2}(e+fx)\right]^2 \right)^n \right. \\
 & \left. \left( \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \right)^n \sqrt{1+\sec[e+fx]} \tan\left[\frac{1}{2}(e+fx)\right] \right. \\
 & \left. \left( -\frac{1}{3}(1-n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \\
 & \left. \left. \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \frac{1}{3}\left(-\frac{1}{2}+n\right) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+n, 1-n, \frac{5}{2}, \right. \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) \right) \Big/ \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \left( 2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \left. (-1+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \\
 & \tan\left[\frac{1}{2}(e+fx)\right]^2 \Big) - \left( 3\sqrt{2} \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \cos[e+fx] \left( \sec\left[\frac{1}{2}(e+fx)\right]^2 \right)^n \right. \\
 & \left. \left( \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \right)^n \sqrt{1+\sec[e+fx]} \tan\left[\frac{1}{2}(e+fx)\right] \right. \\
 & \left. \left( \left( 2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & (-1+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+n, 1-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \\
 & \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] + \\
 & 3\left(-\frac{1}{3}(1-n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 2-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \quad \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] + \frac{1}{3}\left(-\frac{1}{2}+n\right) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+n, 1-n, \frac{5}{2}, \right. \\
 & \quad \left. \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\left. \right) + \\
 & \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \left(2(-1+n)\left(-\frac{3}{5}(2-n) \operatorname{AppellF1}\left[\frac{5}{2}, -\frac{1}{2}+n, 3-n, \frac{7}{2}, \right. \right. \right. \\
 & \quad \left. \left. \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] + \frac{3}{5} \right. \\
 & \quad \left. \left(-\frac{1}{2}+n\right) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{2}+n, 2-n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right) + (-1+2n)\left(-\frac{3}{5}(1-n) \operatorname{AppellF1}\left[\frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \frac{1}{2}+n, 2-n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \right. \\
 & \quad \left. \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] + \frac{3}{5}\left(\frac{1}{2}+n\right) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{3}{2}+n, 1-n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)\right)\right) / \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, 1-n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left(2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 2-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left. (-1+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+n, 1-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right)^2 + \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, 1-n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \quad \left. \left(\operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2\right)^n \left(\operatorname{Cos}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Sec}[e+fx]\right)^n \right. \\
 & \quad \left. \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \operatorname{Tan}[e+fx]\right) / \left(\sqrt{2} \sqrt{1+\operatorname{Sec}[e+fx]}\right) \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, 1-n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left(2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 2-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left. (-1+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+n, 1-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right)^2 +
 \end{aligned}$$

$$\begin{aligned} & \left( 3 \sqrt{2} n \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2} + n, 1 - n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right] \right. \\ & \quad \left. \operatorname{Cos}[e + f x] \left(\operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^2\right)^n \left(\operatorname{Cos}\left[\frac{1}{2}(e + f x)\right]^2 \operatorname{Sec}[e + f x]\right)^{-1+n} \right. \\ & \quad \left. \sqrt{1 + \operatorname{Sec}[e + f x]} \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right] \left(-\operatorname{Cos}\left[\frac{1}{2}(e + f x)\right] \operatorname{Sec}[e + f x] \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right] + \right. \right. \\ & \quad \left. \left. \operatorname{Cos}\left[\frac{1}{2}(e + f x)\right]^2 \operatorname{Sec}[e + f x] \operatorname{Tan}[e + f x]\right)\right) \right) / \\ & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2} + n, 1 - n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right] + \right. \\ & \quad \left( 2(-1 + n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2} + n, 2 - n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right] + \right. \\ & \quad \left. (-1 + 2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2} + n, 1 - n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2, \right. \right. \\ & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right] \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2 \right) \right) \end{aligned}$$

**Problem 302: Result more than twice size of optimal antiderivative.**

$$\int \frac{(-\operatorname{Sec}[e + f x])^n}{(1 + \operatorname{Sec}[e + f x])^{3/2}} dx$$

Optimal (type 6, 73 leaves, 2 steps):

$$\begin{aligned} & - \left( \left( \operatorname{AppellF1}\left[n, \frac{1}{2}, 2, 1 + n, \operatorname{Sec}[e + f x], -\operatorname{Sec}[e + f x]\right] (-\operatorname{Sec}[e + f x])^n \operatorname{Tan}[e + f x] \right) / \right. \\ & \quad \left. \left( f n \sqrt{1 - \operatorname{Sec}[e + f x]} \sqrt{1 + \operatorname{Sec}[e + f x]} \right) \right) \end{aligned}$$

Result (type 6, 3003 leaves):

$$\begin{aligned} & \left( 6 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2} + n, 1 - n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right] \right. \\ & \quad \left. \left(\operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^2\right)^n (-\operatorname{Sec}[e + f x])^n \operatorname{Sec}[e + f x]^{\frac{1}{2} - n + \frac{1}{2}(-3 + 2n)} \right. \\ & \quad \left. \left(\operatorname{Cos}\left[\frac{1}{2}(e + f x)\right]^2 \operatorname{Sec}[e + f x]\right)^{\frac{3}{2} + n} \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right] \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right)^2 \right) / \\ & \left( f (1 + \operatorname{Sec}[e + f x])^{3/2} \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2} + n, 1 - n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right] + \right. \right. \\ & \quad \left( 2(-1 + n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{3}{2} + n, 2 - n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right] + \right. \\ & \quad \left. (-3 + 2n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2} + n, 1 - n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right] \right) \right. \\ & \quad \left. \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2 \right) \left( \left( 12 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2} + n, 1 - n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2, \right. \right. \right. \end{aligned}$$

$$\begin{aligned}
 & -\tan\left[\frac{1}{2}(e+fx)\right]^2 \cos[e+fx] \left(\sec\left[\frac{1}{2}(e+fx)\right]^2\right)^{1+n} \\
 & \left(\cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx]\right)^{\frac{3+n}{2}} \tan\left[\frac{1}{2}(e+fx)\right]^2 \left(-1+\tan\left[\frac{1}{2}(e+fx)\right]^2\right)\right) / \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \left(2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{3}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \left. (-3+2n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right]\right) \tan\left[\frac{1}{2}(e+fx)\right]^2\right) + \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \cos[e+fx] \right. \\
 & \left. \left(\sec\left[\frac{1}{2}(e+fx)\right]^2\right)^{1+n} \left(\cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx]\right)^{\frac{3+n}{2}} \left(-1+\tan\left[\frac{1}{2}(e+fx)\right]^2\right)^2\right) / \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \left(2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{3}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \left. (-3+2n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right]\right) \\
 & \tan\left[\frac{1}{2}(e+fx)\right]^2\right) - \left(6 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \left(\sec\left[\frac{1}{2}(e+fx)\right]^2\right)^n \left(\cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx]\right)^{\frac{3+n}{2}} \right. \\
 & \left. \sin[e+fx] \tan\left[\frac{1}{2}(e+fx)\right] \left(-1+\tan\left[\frac{1}{2}(e+fx)\right]^2\right)^2\right) / \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \left(2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{3}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \left. (-3+2n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right]\right) \\
 & \tan\left[\frac{1}{2}(e+fx)\right]^2\right) + \left(6n \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \cos[e+fx] \left(\sec\left[\frac{1}{2}(e+fx)\right]^2\right)^n \right. \\
 & \left. \left(\cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx]\right)^{\frac{3+n}{2}} \tan\left[\frac{1}{2}(e+fx)\right]^2 \left(-1+\tan\left[\frac{1}{2}(e+fx)\right]^2\right)^2\right) / \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( 2 (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{3}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left. (-3+2n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \\
 & \tan\left[\frac{1}{2}(e+fx)\right]^2 \Bigg) + \left( 6 \cos[e+fx] \left( \sec\left[\frac{1}{2}(e+fx)\right]^2 \right)^n \right. \\
 & \quad \left( \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \right)^{\frac{3+n}{2}} \tan\left[\frac{1}{2}(e+fx)\right] \left( -\frac{1}{3}(1-n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{3}{2}+n, \right. \right. \\
 & \quad \left. \left. 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \right. \right. \\
 & \quad \left. \left. \frac{1}{3}\left(-\frac{3}{2}+n\right) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \\
 & \quad \left. \left. \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) \left( -1 + \tan\left[\frac{1}{2}(e+fx)\right]^2 \right)^2 \right) / \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left( 2 (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{3}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left. \left. (-3+2n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \right) \\
 & \tan\left[\frac{1}{2}(e+fx)\right]^2 \Bigg) - \left( 6 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \cos[e+fx] \left( \sec\left[\frac{1}{2}(e+fx)\right]^2 \right)^n \right. \\
 & \quad \left( \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \right)^{\frac{3+n}{2}} \tan\left[\frac{1}{2}(e+fx)\right] \left( -1 + \tan\left[\frac{1}{2}(e+fx)\right]^2 \right)^2 \right. \\
 & \quad \left( \left( 2 (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{3}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. (-3+2n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \right) \\
 & \quad \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + 3 \left( -\frac{1}{3}(1-n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{3}{2}+n, 2-n, \right. \right. \\
 & \quad \left. \left. \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \right. \right. \\
 & \quad \left. \left. \frac{1}{3}\left(-\frac{3}{2}+n\right) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \\
 & \quad \left. \left. \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) + \tan\left[\frac{1}{2}(e+fx)\right]^2 \right. \\
 & \quad \left( 2 (-1+n) \left( -\frac{3}{5}(2-n) \operatorname{AppellF1}\left[\frac{5}{2}, -\frac{3}{2}+n, 3-n, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \frac{3}{5}\left(-\frac{3}{2}+n\right) \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1}\left[\frac{5}{2}, -\frac{1}{2}+n, 2-n, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \right)
 \end{aligned}$$



$$\begin{aligned}
 & \left( \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) + (-3+2n) \left( -\frac{3}{5}(1-n) \operatorname{AppellF1}\left[\frac{5}{2}, \right. \right. \\
 & \quad \left. \left. -\frac{1}{2}+n, 2-n, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \right. \\
 & \quad \left. \tan\left[\frac{1}{2}(e+fx)\right] + \frac{3}{5}\left(-\frac{1}{2}+n\right) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{2}+n, 1-n, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) \right) \Big/ \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left( 2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{3}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left. (-3+2n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) + \right. \\
 & \left. \left( 6\left(\frac{3}{2}+n\right) \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \\
 & \quad \left. \cos[e+fx] \left( \sec\left[\frac{1}{2}(e+fx)\right]^2 \right)^n \left( \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \right)^{\frac{1}{2}+n} \tan\left[\frac{1}{2}(e+fx)\right] \right. \\
 & \quad \left. \left( -1 + \tan\left[\frac{1}{2}(e+fx)\right]^2 \right)^2 \left( -\cos\left[\frac{1}{2}(e+fx)\right] \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right] + \right. \right. \\
 & \quad \left. \left. \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \tan[e+fx] \right) \right) \right) \Big/ \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left( 2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{3}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left. (-3+2n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \right) \Big/
 \end{aligned}$$

**Problem 303: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int (d \operatorname{Sec}[e+fx])^n (1 + \operatorname{Sec}[e+fx])^{3/2} dx$$

Optimal (type 5, 117 leaves, 4 steps):

$$\frac{2 (d \operatorname{Sec}[e + f x])^n \operatorname{Tan}[e + f x]}{f (1 + 2 n) \sqrt{1 + \operatorname{Sec}[e + f x]}} - \frac{\left( (1 + 4 n) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, n, 1 + n, \operatorname{Sec}[e + f x]\right] (d \operatorname{Sec}[e + f x])^n \operatorname{Tan}[e + f x] \right)}{\left( f n (1 + 2 n) \sqrt{1 - \operatorname{Sec}[e + f x]} \sqrt{1 + \operatorname{Sec}[e + f x]} \right)}$$

Result (type 5, 6381 leaves):

$$\left( 14 \operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^3 \left(\operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^2\right)^n \operatorname{Sec}[e + f x]^{-\frac{3}{2}-n} (d \operatorname{Sec}[e + f x])^n \left(\operatorname{Cos}\left[\frac{1}{2}(e + f x)\right]^2 \operatorname{Sec}[e + f x]\right)^{-\frac{3}{2}+n} \right. \\ \left. (1 + \operatorname{Sec}[e + f x])^{3/2} \left(\operatorname{Cos}\left[\frac{3}{2}(e + f x)\right] \left(\frac{1}{8} \operatorname{Sec}[e + f x]^{-\frac{3}{2}+n} + \frac{3}{8} \operatorname{Sec}[e + f x]^{\frac{1}{2}+n} + \frac{3}{4} \operatorname{Sec}[e + f x]^{\frac{1}{2}+n} \operatorname{Sin}[e + f x] - \frac{3}{8} \operatorname{Sec}[e + f x]^{\frac{1}{2}+n} \operatorname{Sin}[e + f x]^2 + \operatorname{Cos}[e + f x] \left(\frac{3}{8} \operatorname{Sec}[e + f x]^{\frac{1}{2}+n} + \frac{3}{8} \operatorname{Sec}[e + f x]^{\frac{1}{2}+n} \operatorname{Sin}[e + f x]\right) + \operatorname{Sec}[e + f x] \left(\frac{1}{8} \operatorname{Sec}[e + f x]^{\frac{1}{2}+n} + \frac{3}{8} \operatorname{Sec}[e + f x]^{\frac{1}{2}+n} \operatorname{Sin}[e + f x] - \frac{3}{8} \operatorname{Sec}[e + f x]^{\frac{1}{2}+n} \operatorname{Sin}[e + f x]^2 - \frac{1}{8} \operatorname{Sec}[e + f x]^{\frac{1}{2}+n} \operatorname{Sin}[e + f x]^3\right)\right) - \frac{1}{8} \operatorname{Sec}[e + f x]^{-\frac{3}{2}+n} \operatorname{Sin}\left[\frac{3}{2}(e + f x)\right] - \frac{3}{8} \operatorname{Sec}[e + f x]^{\frac{1}{2}+n} \operatorname{Sin}\left[\frac{3}{2}(e + f x)\right] + \frac{3}{4} \operatorname{Sec}[e + f x]^{\frac{1}{2}+n} \operatorname{Sin}[e + f x] \operatorname{Sin}\left[\frac{3}{2}(e + f x)\right] + \frac{3}{8} \operatorname{Sec}[e + f x]^{\frac{1}{2}+n} \operatorname{Sin}[e + f x]^2 \operatorname{Sin}\left[\frac{3}{2}(e + f x)\right] + \operatorname{Cos}[e + f x] \left(-\frac{3}{8} \operatorname{Sec}[e + f x]^{\frac{1}{2}+n} \operatorname{Sin}\left[\frac{3}{2}(e + f x)\right] + \frac{3}{8} \operatorname{Sec}[e + f x]^{\frac{1}{2}+n} \operatorname{Sin}[e + f x] \operatorname{Sin}\left[\frac{3}{2}(e + f x)\right]\right) + \operatorname{Sec}[e + f x] \left(-\frac{1}{8} \operatorname{Sec}[e + f x]^{\frac{1}{2}+n} \operatorname{Sin}\left[\frac{3}{2}(e + f x)\right] + \frac{3}{8} \operatorname{Sec}[e + f x]^{\frac{1}{2}+n} \operatorname{Sin}[e + f x] \operatorname{Sin}\left[\frac{3}{2}(e + f x)\right] - \operatorname{Sin}\left[\frac{3}{2}(e + f x)\right] + \frac{3}{8} \operatorname{Sec}[e + f x]^{\frac{1}{2}+n} \operatorname{Sin}[e + f x]^2 \operatorname{Sin}\left[\frac{3}{2}(e + f x)\right] - \frac{1}{8} \operatorname{Sec}[e + f x]^{\frac{1}{2}+n} \operatorname{Sin}[e + f x]^3 \operatorname{Sin}\left[\frac{3}{2}(e + f x)\right]\right)\right) \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right] \right. \\ \left. \left( 8 \operatorname{Gamma}\left[\frac{5}{2} + n\right] \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2} + n, \frac{7}{2}, -2 \operatorname{Sec}[e + f x] \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2 + 5 \operatorname{Gamma}\left[\frac{3}{2} + n\right] \operatorname{Hypergeometric2F1}\left[1, \frac{3}{2} + n, \frac{5}{2}, -2 \operatorname{Sec}[e + f x] \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \left(-3 + \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2 + 2 \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^4\right) \right) \right) /$$

$$\begin{aligned}
 & \left( f \left( -1 + \tan \left[ \frac{1}{2} (e + f x) \right] \right)^2 \right) \left( 8 \Gamma \left[ \frac{5}{2} + n \right] \sec \left[ \frac{1}{2} (e + f x) \right]^4 \tan \left[ \frac{1}{2} (e + f x) \right]^2 \right. \\
 & \quad \left( 7 \cos [e + f x] (-5 - 2n + 2(1+n) \cos [e + f x]) \right. \\
 & \quad \quad \text{Hypergeometric2F1} \left[ 2, \frac{5}{2} + n, \frac{7}{2}, -2 \sec [e + f x] \sin \left[ \frac{1}{2} (e + f x) \right]^2 \right] \sec \left[ \frac{1}{2} (e + f x) \right]^2 + \\
 & \quad \quad 8(5 + 2n) \text{Hypergeometric2F1} \left[ 3, \frac{7}{2} + n, \frac{9}{2}, -2 \sec [e + f x] \sin \left[ \frac{1}{2} (e + f x) \right]^2 \right] \\
 & \quad \quad \tan \left[ \frac{1}{2} (e + f x) \right]^2 \right) + 7 \Gamma \left[ \frac{3}{2} + n \right] \left( -1 + \tan \left[ \frac{1}{2} (e + f x) \right] \right)^2 \\
 & \quad \left( \frac{5}{2} \cos [e + f x] (-15 - 9n + (9 + 8n) \cos [e + f x] + n \cos [2(e + f x)]) \right) \\
 & \quad \quad \text{Hypergeometric2F1} \left[ 1, \frac{3}{2} + n, \frac{5}{2}, -2 \sec [e + f x] \sin \left[ \frac{1}{2} (e + f x) \right]^2 \right] \sec \left[ \frac{1}{2} (e + f x) \right]^6 + \\
 & \quad \quad 2(3 + 2n)(5 + \cos [e + f x]) \text{Hypergeometric2F1} \left[ 2, \frac{5}{2} + n, \frac{7}{2}, \right. \\
 & \quad \quad \left. -2 \sec [e + f x] \sin \left[ \frac{1}{2} (e + f x) \right]^2 \right] \sec \left[ \frac{1}{2} (e + f x) \right]^4 \tan \left[ \frac{1}{2} (e + f x) \right]^2 \right) \\
 & \quad \left( - \left( \left( 14 \left( \sec \left[ \frac{1}{2} (e + f x) \right]^2 \right)^{1+n} \left( \cos \left[ \frac{1}{2} (e + f x) \right]^2 \sec [e + f x] \right)^{-\frac{3}{2}+n} \tan \left[ \frac{1}{2} (e + f x) \right]^2 \right. \right. \right. \\
 & \quad \left( 8 \Gamma \left[ \frac{5}{2} + n \right] \text{Hypergeometric2F1} \left[ 2, \frac{5}{2} + n, \frac{7}{2}, -2 \sec [e + f x] \sin \left[ \frac{1}{2} (e + f x) \right]^2 \right] \right. \\
 & \quad \quad \left. \sec \left[ \frac{1}{2} (e + f x) \right]^2 \tan \left[ \frac{1}{2} (e + f x) \right]^2 + \right. \\
 & \quad \quad \left. 5 \Gamma \left[ \frac{3}{2} + n \right] \text{Hypergeometric2F1} \left[ 1, \frac{3}{2} + n, \frac{5}{2}, -2 \sec [e + f x] \sin \left[ \frac{1}{2} (e + f x) \right]^2 \right] \right. \\
 & \quad \quad \left. \left. \left. \left( -3 + \tan \left[ \frac{1}{2} (e + f x) \right]^2 + 2 \tan \left[ \frac{1}{2} (e + f x) \right]^4 \right) \right) \right) \right) / \\
 & \quad \left( \left( -1 + \tan \left[ \frac{1}{2} (e + f x) \right] \right)^2 \right)^2 \left( 8 \Gamma \left[ \frac{5}{2} + n \right] \sec \left[ \frac{1}{2} (e + f x) \right]^4 \tan \left[ \frac{1}{2} (e + f x) \right]^2 \right. \\
 & \quad \left( 7 \cos [e + f x] (-5 - 2n + 2(1+n) \cos [e + f x]) \text{Hypergeometric2F1} \left[ 2, \frac{5}{2} + n, \right. \right. \\
 & \quad \quad \left. \frac{7}{2}, -2 \sec [e + f x] \sin \left[ \frac{1}{2} (e + f x) \right]^2 \right] \sec \left[ \frac{1}{2} (e + f x) \right]^2 + 8(5 + 2n) \right. \\
 & \quad \quad \text{Hypergeometric2F1} \left[ 3, \frac{7}{2} + n, \frac{9}{2}, -2 \sec [e + f x] \sin \left[ \frac{1}{2} (e + f x) \right]^2 \right] \\
 & \quad \quad \tan \left[ \frac{1}{2} (e + f x) \right]^2 \right) + 7 \Gamma \left[ \frac{3}{2} + n \right] \left( -1 + \tan \left[ \frac{1}{2} (e + f x) \right] \right)^2 \\
 & \quad \left( \frac{5}{2} \cos [e + f x] (-15 - 9n + (9 + 8n) \cos [e + f x] + n \cos [2(e + f x)]) \right) \\
 & \quad \quad \text{Hypergeometric2F1} \left[ 1, \frac{3}{2} + n, \frac{5}{2}, -2 \sec [e + f x] \sin \left[ \frac{1}{2} (e + f x) \right]^2 \right] \\
 & \quad \quad \left. \sec \left[ \frac{1}{2} (e + f x) \right]^6 + 2(3 + 2n)(5 + \cos [e + f x]) \text{Hypergeometric2F1} \left[ 2, \frac{5}{2} + n, \frac{7}{2}, \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^4 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \Big) \Big) \Big) + \\
 & \left( 7 \left( \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \right)^{1+n} \left( \operatorname{Cos}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Sec}[e+fx] \right)^{-\frac{3}{2}+n} \right. \\
 & \quad \left( 8 \operatorname{Gamma}\left[\frac{5}{2}+n\right] \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \quad \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 + 5 \operatorname{Gamma}\left[\frac{3}{2}+n\right] \operatorname{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2}, \right. \\
 & \quad \left. \left. -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \left(-3 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 + 2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^4\right)\right] \Big) \Big) \Big) / \\
 & \left( \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right) \left( 8 \operatorname{Gamma}\left[\frac{5}{2}+n\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^4 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right. \right. \\
 & \quad \left( 7 \operatorname{Cos}[e+fx] (-5 - 2n + 2(1+n) \operatorname{Cos}[e+fx]) \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+ \right. \right. \\
 & \quad \left. \left. n, \frac{7}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 + \right. \right. \\
 & \quad \left. \left. 8(5+2n) \operatorname{Hypergeometric2F1}\left[3, \frac{7}{2}+n, \frac{9}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \\
 & \quad \left. \left. \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right) + 7 \operatorname{Gamma}\left[\frac{3}{2}+n\right] \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right) \right. \right. \\
 & \quad \left. \left. \left(\frac{5}{2} \operatorname{Cos}[e+fx] (-15 - 9n + (9+8n) \operatorname{Cos}[e+fx] + n \operatorname{Cos}[2(e+fx)])\right) \right. \right. \\
 & \quad \left. \left. \operatorname{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \\
 & \quad \left. \left. \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^6 + 2(3+2n)(5 + \operatorname{Cos}[e+fx]) \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \right. \right. \\
 & \quad \left. \left. \frac{7}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^4 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right) \Big) \Big) \Big) + \\
 & \left( 14n \left( \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \right)^n \left( \operatorname{Cos}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Sec}[e+fx] \right)^{-\frac{3}{2}+n} \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right. \right. \\
 & \quad \left( 8 \operatorname{Gamma}\left[\frac{5}{2}+n\right] \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \quad \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 + 5 \operatorname{Gamma}\left[\frac{3}{2}+n\right] \operatorname{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2}, \right. \\
 & \quad \left. \left. -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \left(-3 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 + 2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^4\right)\right] \Big) \Big) \Big) / \\
 & \left( \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right) \left( 8 \operatorname{Gamma}\left[\frac{5}{2}+n\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^4 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right. \right. \\
 & \quad \left( 7 \operatorname{Cos}[e+fx] (-5 - 2n + 2(1+n) \operatorname{Cos}[e+fx]) \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+ \right. \right. \\
 & \quad \left. \left. n, \frac{7}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 + \right. \right. \\
 & \quad \left. \left. 8(5+2n) \operatorname{Hypergeometric2F1}\left[3, \frac{7}{2}+n, \frac{9}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( \tan\left[\frac{1}{2}(e+fx)\right]^2 + 7 \operatorname{Gamma}\left[\frac{3}{2}+n\right] \left(-1 + \tan\left[\frac{1}{2}(e+fx)\right]^2\right) \right. \\
 & \left. \left(\frac{5}{2} \cos[e+fx] (-15-9n+(9+8n)\cos[e+fx]+n\cos[2(e+fx)])\right) \right. \\
 & \operatorname{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2}, -2 \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right]^2\right] \\
 & \left. \sec\left[\frac{1}{2}(e+fx)\right]^6 + 2(3+2n)(5+\cos[e+fx]) \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \right. \right. \\
 & \left. \left. \frac{7}{2}, -2 \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^4 \tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) + \\
 & \left( 14 \left(-\frac{3}{2}+n\right) \left(\sec\left[\frac{1}{2}(e+fx)\right]^2\right)^n \left(\cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx]\right)^{-\frac{5}{2}+n} \tan\left[\frac{1}{2}(e+fx)\right] \right. \\
 & \left( 8 \operatorname{Gamma}\left[\frac{5}{2}+n\right] \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2 \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \left. \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right]^2 + 5 \operatorname{Gamma}\left[\frac{3}{2}+n\right] \operatorname{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2}, \right. \right. \\
 & \left. \left. -2 \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right]^2\right] \left(-3 + \tan\left[\frac{1}{2}(e+fx)\right]^2 + 2 \tan\left[\frac{1}{2}(e+fx)\right]^4\right) \right) \\
 & \left(-\cos\left[\frac{1}{2}(e+fx)\right] \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right] + \right. \\
 & \left. \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \tan[e+fx] \right) \Big/ \\
 & \left( \left(-1 + \tan\left[\frac{1}{2}(e+fx)\right]^2\right) \left( 8 \operatorname{Gamma}\left[\frac{5}{2}+n\right] \sec\left[\frac{1}{2}(e+fx)\right]^4 \tan\left[\frac{1}{2}(e+fx)\right]^2 \right. \right. \\
 & \left. \left( 7 \cos[e+fx] (-5-2n+2(1+n)\cos[e+fx]) \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+ \right. \right. \right. \\
 & \left. \left. n, \frac{7}{2}, -2 \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 + \right. \right. \\
 & \left. 8(5+2n) \operatorname{Hypergeometric2F1}\left[3, \frac{7}{2}+n, \frac{9}{2}, -2 \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \left. \tan\left[\frac{1}{2}(e+fx)\right]^2 + 7 \operatorname{Gamma}\left[\frac{3}{2}+n\right] \left(-1 + \tan\left[\frac{1}{2}(e+fx)\right]^2\right) \right. \\
 & \left. \left(\frac{5}{2} \cos[e+fx] (-15-9n+(9+8n)\cos[e+fx]+n\cos[2(e+fx)])\right) \right. \\
 & \operatorname{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2}, -2 \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right]^2\right] \\
 & \left. \sec\left[\frac{1}{2}(e+fx)\right]^6 + 2(3+2n)(5+\cos[e+fx]) \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \right. \right. \\
 & \left. \left. \frac{7}{2}, -2 \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^4 \tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \Big) + \\
 & \left( 14 \left(\sec\left[\frac{1}{2}(e+fx)\right]^2\right)^n \left(\cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx]\right)^{-\frac{3}{2}+n} \tan\left[\frac{1}{2}(e+fx)\right] \right. \\
 & \left( 8 \operatorname{Gamma}\left[\frac{5}{2}+n\right] \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2 \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right]^2\right] \right.
 \end{aligned}$$

$$\begin{aligned}
& \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^4 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] + 8 \operatorname{Gamma}\left[\frac{5}{2}+n\right] \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^3 + \\
& 5 \operatorname{Gamma}\left[\frac{3}{2}+n\right] \operatorname{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \\
& \left(\operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] + 4 \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^3\right) + \\
& \frac{32}{7} \left(\frac{5}{2}+n\right) \operatorname{Gamma}\left[\frac{5}{2}+n\right] \operatorname{Hypergeometric2F1}\left[3, \frac{7}{2}+n, \frac{9}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \\
& \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \left(-2 \operatorname{Cos}\left[\frac{1}{2}(e+fx)\right] \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right] - \right. \\
& \left. 2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}[e+fx]\right) + 2 \left(\frac{3}{2}+n\right) \operatorname{Gamma}\left[\frac{3}{2}+n\right] \\
& \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \\
& \left(-3 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 + 2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^4\right) \left(-2 \operatorname{Cos}\left[\frac{1}{2}(e+fx)\right] \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right] - 2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}[e+fx]\right) \Bigg) / \\
& \left(\left(-1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right) \left(8 \operatorname{Gamma}\left[\frac{5}{2}+n\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^4 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right. \right. \\
& \left. \left(7 \operatorname{Cos}[e+fx] (-5 - 2n + 2(1+n) \operatorname{Cos}[e+fx]) \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 + \right. \right. \\
& \left. \left. 8(5+2n) \operatorname{Hypergeometric2F1}\left[3, \frac{7}{2}+n, \frac{9}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right) + 7 \operatorname{Gamma}\left[\frac{3}{2}+n\right] \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right) \right. \\
& \left. \left(\frac{5}{2} \operatorname{Cos}[e+fx] (-15 - 9n + (9+8n) \operatorname{Cos}[e+fx] + n \operatorname{Cos}[2(e+fx)])\right) \right. \\
& \left. \operatorname{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^6 + 2(3+2n)(5 + \operatorname{Cos}[e+fx]) \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^4 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right) \Bigg) - \\
& \left(14 \left(\operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2\right)^n \left(\operatorname{Cos}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Sec}[e+fx]\right)^{-\frac{3}{2}+n} \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \right. \\
& \left. \left(8 \operatorname{Gamma}\left[\frac{5}{2}+n\right] \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 + 5 \operatorname{Gamma}\left[\frac{3}{2}+n\right] \operatorname{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2}, \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
 & -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2 \left(-3 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 + 2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^4\right) \\
 & \left(8 \operatorname{Gamma}\left[\frac{5}{2}+n\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^6 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right. \\
 & \left(7 \operatorname{Cos}[e+fx] (-5-2n+2(1+n) \operatorname{Cos}[e+fx]) \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+\right.\right. \\
 & \left.\left.n, \frac{7}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 + \right. \\
 & \left.8(5+2n) \operatorname{Hypergeometric2F1}\left[3, \frac{7}{2}+n, \frac{9}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \left. \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right) + 16 \operatorname{Gamma}\left[\frac{5}{2}+n\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^4 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^3 \\
 & \left(7 \operatorname{Cos}[e+fx] (-5-2n+2(1+n) \operatorname{Cos}[e+fx]) \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+\right.\right. \\
 & \left.\left.n, \frac{7}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 + \right. \\
 & \left.8(5+2n) \operatorname{Hypergeometric2F1}\left[3, \frac{7}{2}+n, \frac{9}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \left. \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right) + 7 \operatorname{Gamma}\left[\frac{3}{2}+n\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \\
 & \left(\frac{5}{2} \operatorname{Cos}[e+fx] (-15-9n+(9+8n) \operatorname{Cos}[e+fx]+n \operatorname{Cos}[2(e+fx)])\right) \\
 & \operatorname{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \\
 & \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^6 + 2(3+2n)(5+\operatorname{Cos}[e+fx]) \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+\right. \\
 & \left.\left.n, \frac{7}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^4 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right) + \\
 & 8 \operatorname{Gamma}\left[\frac{5}{2}+n\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^4 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \left(-14(1+n) \operatorname{Cos}[e+fx]\right. \\
 & \left.\operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \left.\operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Sin}[e+fx] - 7(-5-2n+2(1+n) \operatorname{Cos}[e+fx])\right) \\
 & \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \\
 & \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Sin}[e+fx] + 7 \operatorname{Cos}[e+fx] (-5-2n+2(1+n) \operatorname{Cos}[e+fx]) \\
 & \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \\
 & \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] + 8(5+2n) \operatorname{Hypergeometric2F1}\left[3, \frac{7}{2}+\right. \\
 & \left.\left.n, \frac{9}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] + \right. \\
 & \left.4\left(\frac{5}{2}+n\right) \operatorname{Cos}[e+fx] (-5-2n+2(1+n) \operatorname{Cos}[e+fx]) \operatorname{Hypergeometric2F1}\left[3, \frac{7}{2}+\right.\right.
 \end{aligned}$$

$$\begin{aligned}
 & n, \frac{9}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \left(-2 \operatorname{Cos}\left[\frac{1}{2}(e+fx)\right]\right. \\
 & \left. \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right] - 2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}[e+fx]\right) + \\
 & \frac{16}{3} \left(\frac{7}{2}+n\right) (5+2n) \operatorname{Hypergeometric2F1}\left[4, \frac{9}{2}+n, \frac{11}{2}, -2 \operatorname{Sec}[e+fx] \right. \\
 & \left. \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \left(-2 \operatorname{Cos}\left[\frac{1}{2}(e+fx)\right] \operatorname{Sec}[e+fx] \right. \right. \\
 & \left. \left. \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right] - 2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}[e+fx]\right)\right] + \\
 & 7 \operatorname{Gamma}\left[\frac{3}{2}+n\right] \left(-1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right) \left(-\frac{5}{2}(-15-9n+(9+8n) \operatorname{Cos}[e+fx] + \right. \\
 & \left. n \operatorname{Cos}[2(e+fx)])\right) \operatorname{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2}, -2 \right. \\
 & \left. \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^6 \operatorname{Sin}[e+fx] + \\
 & \frac{5}{2} \operatorname{Cos}[e+fx] \operatorname{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \\
 & \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^6 \left(- (9+8n) \operatorname{Sin}[e+fx] - 2n \operatorname{Sin}[2(e+fx)]\right) + \\
 & \frac{15}{2} \operatorname{Cos}[e+fx] \left(-15-9n+(9+8n) \operatorname{Cos}[e+fx] + n \operatorname{Cos}[2(e+fx)]\right) \\
 & \operatorname{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \\
 & \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^6 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] + 2(3+2n)(5+\operatorname{Cos}[e+fx]) \\
 & \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \\
 & \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^6 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] - 2(3+2n) \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2 \right. \\
 & \left. \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^4 \operatorname{Sin}[e+fx] \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 + \\
 & 4(3+2n)(5+\operatorname{Cos}[e+fx]) \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2 \right. \\
 & \left. \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^4 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^3 + \\
 & \left(\frac{3}{2}+n\right) \operatorname{Cos}[e+fx] \left(-15-9n+(9+8n) \operatorname{Cos}[e+fx] + n \operatorname{Cos}[2(e+fx)]\right) \\
 & \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \\
 & \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^6 \left(-2 \operatorname{Cos}\left[\frac{1}{2}(e+fx)\right] \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right] - 2 \operatorname{Sec}[ \right. \\
 & \left. e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}[e+fx]\right) + \frac{8}{7} \left(\frac{5}{2}+n\right) (3+2n)(5+\operatorname{Cos}[e+fx]) \\
 & \operatorname{Hypergeometric2F1}\left[3, \frac{7}{2}+n, \frac{9}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right]
 \end{aligned}$$



$$\begin{aligned}
& \text{Sec}\left[\frac{1}{2}(e+fx)\right]^4 \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \left( -2 \text{Cos}\left[\frac{1}{2}(e+fx)\right] \text{Sec}[e+fx] \right. \\
& \quad \left. \text{Sin}\left[\frac{1}{2}(e+fx)\right] - 2 \text{Sec}[e+fx] \text{Sin}\left[\frac{1}{2}(e+fx)\right]^2 \text{Tan}[e+fx] \right) \Bigg) \Bigg) \Bigg) \Bigg) \Bigg) \Bigg) / \\
& \left( \left( -1 + \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right) \left( 8 \text{Gamma}\left[\frac{5}{2} + n\right] \text{Sec}\left[\frac{1}{2}(e+fx)\right]^4 \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right. \right. \\
& \quad \left. \left( 7 \text{Cos}[e+fx] (-5 - 2n + 2(1+n) \text{Cos}[e+fx]) \text{Hypergeometric2F1}\left[2, \frac{5}{2} + n, \right. \right. \right. \\
& \quad \left. \left. \left. \frac{7}{2}, -2 \text{Sec}[e+fx] \text{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 + 8(5+2n) \right. \right. \right. \\
& \quad \left. \left. \text{Hypergeometric2F1}\left[3, \frac{7}{2} + n, \frac{9}{2}, -2 \text{Sec}[e+fx] \text{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \right. \\
& \quad \left. \left. \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right) + 7 \text{Gamma}\left[\frac{3}{2} + n\right] \left( -1 + \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right) \right. \right. \\
& \quad \left. \left. \left. \left( \frac{5}{2} \text{Cos}[e+fx] (-15 - 9n + (9+8n) \text{Cos}[e+fx] + n \text{Cos}[2(e+fx)]) \right) \right. \right. \right. \\
& \quad \left. \left. \text{Hypergeometric2F1}\left[1, \frac{3}{2} + n, \frac{5}{2}, -2 \text{Sec}[e+fx] \text{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \right. \\
& \quad \left. \left. \text{Sec}\left[\frac{1}{2}(e+fx)\right]^6 + 2(3+2n)(5 + \text{Cos}[e+fx]) \text{Hypergeometric2F1}\left[2, \frac{5}{2} + n, \frac{7}{2}, \right. \right. \right. \\
& \quad \left. \left. \left. - 2 \text{Sec}[e+fx] \text{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(e+fx)\right]^4 \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right) \right) \right) \Bigg) \Bigg) \Bigg) \Bigg) \Bigg) \Bigg) \Bigg)
\end{aligned}$$

**Problem 304: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int (d \text{Sec}[e+fx])^n \sqrt{1 + \text{Sec}[e+fx]} \, dx$$

Optimal (type 5, 64 leaves, 2 steps):

$$- \left( \left( \text{Hypergeometric2F1}\left[\frac{1}{2}, n, 1+n, \text{Sec}[e+fx]\right] (d \text{Sec}[e+fx])^n \text{Tan}[e+fx] \right) / \right. \\
\left. \left( fn \sqrt{1 - \text{Sec}[e+fx]} \sqrt{1 + \text{Sec}[e+fx]} \right) \right)$$

Result (type 5, 213 leaves):

$$- \frac{1}{fn(1+n)} i^{2^{-\frac{1}{2}+n}} e^{\frac{1}{2}i(e+fx)} \left( 1 + e^{2i(e+fx)} \right)^{-\frac{1}{2}+n} \left( e^{-i(e+fx)} \left( 1 + e^{2i(e+fx)} \right) \right)^{\frac{1}{2}-n} \\
\text{Cos}[e+fx]^{\frac{1}{2}+n} \left( (1+n) \text{Hypergeometric2F1}\left[\frac{n}{2}, \frac{1}{2} + n, \frac{2+n}{2}, -e^{2i(e+fx)}\right] + \right. \\
\left. e^{i(e+fx)} n \text{Hypergeometric2F1}\left[\frac{1}{2} + n, \frac{1+n}{2}, \frac{3+n}{2}, -e^{2i(e+fx)}\right] \right) \\
\text{Sec}\left[\frac{1}{2}(e+fx)\right] (d \text{Sec}[e+fx])^n \sqrt{1 + \text{Sec}[e+fx]}$$

### Problem 305: Result more than twice size of optimal antiderivative.

$$\int \frac{(d \operatorname{Sec}[e + f x])^n}{\sqrt{1 + \operatorname{Sec}[e + f x]}} dx$$

Optimal (type 6, 73 leaves, 2 steps):

$$- \left( \operatorname{AppellF1}\left[n, \frac{1}{2}, 1, 1+n, \operatorname{Sec}[e + f x], -\operatorname{Sec}[e + f x]\right] (d \operatorname{Sec}[e + f x])^n \operatorname{Tan}[e + f x] \right) / \left( f n \sqrt{1 - \operatorname{Sec}[e + f x]} \sqrt{1 + \operatorname{Sec}[e + f x]} \right)$$

Result (type 6, 2951 leaves):

$$\begin{aligned} & \left( 3 \sqrt{2} \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2} + n, 1 - n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right] \left(\operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^2\right)^n \right. \\ & \quad \left. \operatorname{Sec}[e + f x]^{-\frac{1}{2} - n + \frac{1}{2}(-1 + 2n)} (d \operatorname{Sec}[e + f x])^n \left(\operatorname{Cos}\left[\frac{1}{2}(e + f x)\right]^2 \operatorname{Sec}[e + f x]\right)^n \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right] \right) / \\ & \left( f \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2} + n, 1 - n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right] + \right. \right. \\ & \quad \left( 2(-1 + n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2} + n, 2 - n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right] + \right. \\ & \quad \left. \left. (-1 + 2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2} + n, 1 - n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2, \right. \right. \right. \\ & \quad \left. \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right] \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2 \right) \right) \right) \\ & \left( \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2} + n, 1 - n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right] \operatorname{Cos}[e + f x] \right. \right. \\ & \quad \left. \left. \left(\operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^2\right)^{1+n} \left(\operatorname{Cos}\left[\frac{1}{2}(e + f x)\right]^2 \operatorname{Sec}[e + f x]\right)^n \sqrt{1 + \operatorname{Sec}[e + f x]} \right) \right) / \\ & \left( \sqrt{2} \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2} + n, 1 - n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right] + \right. \right. \\ & \quad \left( 2(-1 + n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2} + n, 2 - n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right] + \right. \\ & \quad \left. \left. (-1 + 2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2} + n, 1 - n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right] \right) \right) \\ & \quad \left. \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2 \right) - \left( 3 \sqrt{2} \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2} + n, 1 - n, \frac{3}{2}, \right. \right. \\ & \quad \left. \left. \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right] \left(\operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^2\right)^n \right. \\ & \quad \left. \left(\operatorname{Cos}\left[\frac{1}{2}(e + f x)\right]^2 \operatorname{Sec}[e + f x]\right)^n \sqrt{1 + \operatorname{Sec}[e + f x]} \operatorname{Sin}[e + f x] \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right] \right) / \\ & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2} + n, 1 - n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right] + \right. \\ & \quad \left( 2(-1 + n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2} + n, 2 - n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right] + \right. \\ & \quad \left. \left. (-1 + 2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2} + n, 1 - n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right] \right) \right) \end{aligned}$$

$$\begin{aligned}
 & \tan\left[\frac{1}{2}(e+fx)\right]^2 + \left(3\sqrt{2} n \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right.\right. \\
 & \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \cos[e+fx] \left(\sec\left[\frac{1}{2}(e+fx)\right]^2\right)^n \right. \\
 & \left. \left(\cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx]\right)^n \sqrt{1+\sec[e+fx]} \tan\left[\frac{1}{2}(e+fx)\right]^2\right) / \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \left(2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \left. \left. (-1+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right]\right) \right. \\
 & \left. \tan\left[\frac{1}{2}(e+fx)\right]^2 + \left(3\sqrt{2} \cos[e+fx] \left(\sec\left[\frac{1}{2}(e+fx)\right]^2\right)^n \right. \right. \\
 & \left. \left(\cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx]\right)^n \sqrt{1+\sec[e+fx]} \tan\left[\frac{1}{2}(e+fx)\right] \right. \\
 & \left. \left(-\frac{1}{3}(1-n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \\
 & \left. \left. \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \frac{1}{3}\left(-\frac{1}{2}+n\right) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+n, 1-n, \frac{5}{2}, \right.\right. \right. \\
 & \left. \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right]\right)\right) / \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \left(2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \left. \left. (-1+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right]\right) \right. \\
 & \left. \tan\left[\frac{1}{2}(e+fx)\right]^2 - \left(3\sqrt{2} \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right.\right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \cos[e+fx] \left(\sec\left[\frac{1}{2}(e+fx)\right]^2\right)^n \right. \right. \\
 & \left. \left(\cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx]\right)^n \sqrt{1+\sec[e+fx]} \tan\left[\frac{1}{2}(e+fx)\right] \right. \\
 & \left. \left(\left(2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right.\right. \right. \\
 & \left. \left. \left. (-1+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right]\right)\right) \right. \\
 & \left. \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \right. \\
 & \left. 3\left(-\frac{1}{3}(1-n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \\
 & \left. \left. \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \frac{1}{3}\left(-\frac{1}{2}+n\right) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+n, 1-n, \frac{5}{2}, \right.\right. \right. \\
 & \left. \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right]\right)\right) +
 \end{aligned}$$

$$\begin{aligned}
 & \left( \tan\left[\frac{1}{2}(e+fx)\right]^2 \left( 2(-1+n) \left( -\frac{3}{5}(2-n) \operatorname{AppellF1}\left[\frac{5}{2}, -\frac{1}{2}+n, 3-n, \frac{7}{2}, \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \frac{3}{5} \right. \right. \right. \\
 & \quad \left. \left. \left. \left( -\frac{1}{2}+n \right) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{2}+n, 2-n, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right] \right. \right. \right. \\
 & \quad \left. \left. \left. \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) + (-1+2n) \left( -\frac{3}{5}(1-n) \operatorname{AppellF1}\left[\frac{5}{2}, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{1}{2}+n, 2-n, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \sec\left[\frac{1}{2}(e+fx)\right]^2 \right. \right. \right. \\
 & \quad \left. \left. \left. \tan\left[\frac{1}{2}(e+fx)\right] + \frac{3}{5} \left( \frac{1}{2}+n \right) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{3}{2}+n, 1-n, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) \right) \right) / \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right] + \right. \\
 & \quad \left( 2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right] + \right. \\
 & \quad \left. (-1+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right] \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) + \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right] \right. \\
 & \quad \left. \left( \sec\left[\frac{1}{2}(e+fx)\right]^2 \right)^n \left( \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \right)^n \right. \\
 & \quad \left. \tan\left[\frac{1}{2}(e+fx)\right] \tan[e+fx] \right) / \left( \sqrt{2} \sqrt{1+\sec[e+fx]} \right) \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right] + \right. \\
 & \quad \left( 2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right] + \right. \\
 & \quad \left. (-1+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right] \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) + \\
 & \left( 3 \sqrt{2} n \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right] \right. \\
 & \quad \left. \cos[e+fx] \left( \sec\left[\frac{1}{2}(e+fx)\right]^2 \right)^n \left( \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \right)^{-1+n} \right. \\
 & \quad \left. \sqrt{1+\sec[e+fx]} \tan\left[\frac{1}{2}(e+fx)\right] \left( -\cos\left[\frac{1}{2}(e+fx)\right] \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right] + \right. \right. \\
 & \quad \left. \left. \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \tan[e+fx] \right) \right) \right) / \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right] + \right.
 \end{aligned}$$

$$\begin{aligned} & \left( 2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\ & \quad \left. (-1+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\ & \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \end{aligned}$$

### Problem 306: Result more than twice size of optimal antiderivative.

$$\int \frac{(d \operatorname{Sec}[e+fx])^n}{(1+\operatorname{Sec}[e+fx])^{3/2}} dx$$

Optimal (type 6, 73 leaves, 2 steps):

$$\begin{aligned} & - \left( \left( \operatorname{AppellF1}\left[n, \frac{1}{2}, 2, 1+n, \operatorname{Sec}[e+fx], -\operatorname{Sec}[e+fx]\right] (d \operatorname{Sec}[e+fx])^n \tan[e+fx] \right) / \right. \\ & \quad \left. (fn \sqrt{1-\operatorname{Sec}[e+fx]} \sqrt{1+\operatorname{Sec}[e+fx]}) \right) \end{aligned}$$

Result (type 6, 3003 leaves):

$$\begin{aligned} & \left( 6 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\ & \quad \left( \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \right)^n \operatorname{Sec}[e+fx]^{\frac{1}{2}-n+\frac{1}{2}(-3+2n)} (d \operatorname{Sec}[e+fx])^n \\ & \quad \left( \cos\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Sec}[e+fx] \right)^{\frac{3}{2}+n} \tan\left[\frac{1}{2}(e+fx)\right] \left( -1 + \tan\left[\frac{1}{2}(e+fx)\right]^2 \right)^2 \right) / \\ & \left( f (1+\operatorname{Sec}[e+fx])^{3/2} \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \\ & \quad \left( 2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{3}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\ & \quad \left. \left. (-3+2n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \right. \\ & \quad \left. \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \left( \left( 12 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \\ & \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \cos[e+fx] \left( \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \right)^{1+n} \right. \right. \\ & \quad \left. \left. \left( \cos\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Sec}[e+fx] \right)^{\frac{3}{2}+n} \tan\left[\frac{1}{2}(e+fx)\right]^2 \left( -1 + \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \right) \right) / \\ & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\ & \quad \left( 2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{3}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\ & \quad \left. \left. (-3+2n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \end{aligned}$$

$$\begin{aligned}
 & -\tan\left[\frac{1}{2}(e+fx)\right]^2 \Big) \tan\left[\frac{1}{2}(e+fx)\right]^2 \Big) + \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \cos[e+fx] \right. \\
 & \quad \left. \left( \sec\left[\frac{1}{2}(e+fx)\right]^2 \right)^{1+n} \left( \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \right)^{\frac{3}{2}+n} \left( -1 + \tan\left[\frac{1}{2}(e+fx)\right]^2 \right)^2 \right) \right] / \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left( 2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{3}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left. \left. (-3+2n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \right) \\
 & \quad \tan\left[\frac{1}{2}(e+fx)\right]^2 \Big) - \left( 6 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \left( \sec\left[\frac{1}{2}(e+fx)\right]^2 \right)^n \left( \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \right)^{\frac{3}{2}+n} \right. \right. \\
 & \quad \left. \left. \sin[e+fx] \tan\left[\frac{1}{2}(e+fx)\right] \left( -1 + \tan\left[\frac{1}{2}(e+fx)\right]^2 \right)^2 \right) \right) \right] / \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left( 2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{3}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left. \left. (-3+2n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \right) \\
 & \quad \tan\left[\frac{1}{2}(e+fx)\right]^2 \Big) + \left( 6n \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \cos[e+fx] \left( \sec\left[\frac{1}{2}(e+fx)\right]^2 \right)^n \right. \right. \\
 & \quad \left. \left. \left( \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \right)^{\frac{3}{2}+n} \tan\left[\frac{1}{2}(e+fx)\right]^2 \left( -1 + \tan\left[\frac{1}{2}(e+fx)\right]^2 \right)^2 \right) \right) \right] / \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left( 2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{3}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left. \left. (-3+2n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \right) \\
 & \quad \tan\left[\frac{1}{2}(e+fx)\right]^2 \Big) + \left( 6 \cos[e+fx] \left( \sec\left[\frac{1}{2}(e+fx)\right]^2 \right)^n \right. \right. \\
 & \quad \left. \left. \left( \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \right)^{\frac{3}{2}+n} \tan\left[\frac{1}{2}(e+fx)\right] \left( -\frac{1}{3}(1-n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{3}{2}+n, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) \right) \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{3} \left( -\frac{3}{2} + n \right) \text{AppellF1} \left[ \frac{3}{2}, -\frac{1}{2} + n, 1 - n, \frac{5}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] \\
 & \quad \text{Sec} \left[ \frac{1}{2} (e + f x) \right]^2 \tan \left[ \frac{1}{2} (e + f x) \right] \left( -1 + \tan \left[ \frac{1}{2} (e + f x) \right]^2 \right)^2 \Big/ \\
 & \left( 3 \text{AppellF1} \left[ \frac{1}{2}, -\frac{3}{2} + n, 1 - n, \frac{3}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] + \right. \\
 & \quad \left( 2 (-1 + n) \text{AppellF1} \left[ \frac{3}{2}, -\frac{3}{2} + n, 2 - n, \frac{5}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] + \right. \\
 & \quad \left. (-3 + 2 n) \text{AppellF1} \left[ \frac{3}{2}, -\frac{1}{2} + n, 1 - n, \frac{5}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] \right) \\
 & \quad \tan \left[ \frac{1}{2} (e + f x) \right]^2 \Big) - \left( 6 \text{AppellF1} \left[ \frac{1}{2}, -\frac{3}{2} + n, 1 - n, \frac{3}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] \cos [e + f x] \left( \text{Sec} \left[ \frac{1}{2} (e + f x) \right]^2 \right)^n \right. \\
 & \quad \left. \left( \cos \left[ \frac{1}{2} (e + f x) \right]^2 \text{Sec} [e + f x] \right)^{\frac{3}{2} + n} \tan \left[ \frac{1}{2} (e + f x) \right] \left( -1 + \tan \left[ \frac{1}{2} (e + f x) \right]^2 \right)^2 \right. \\
 & \quad \left. \left( \left( 2 (-1 + n) \text{AppellF1} \left[ \frac{3}{2}, -\frac{3}{2} + n, 2 - n, \frac{5}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] + \right. \right. \right. \\
 & \quad \left. \left. (-3 + 2 n) \text{AppellF1} \left[ \frac{3}{2}, -\frac{1}{2} + n, 1 - n, \frac{5}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] \right) \right. \\
 & \quad \left. \text{Sec} \left[ \frac{1}{2} (e + f x) \right]^2 \tan \left[ \frac{1}{2} (e + f x) \right] + 3 \left( -\frac{1}{3} (1 - n) \text{AppellF1} \left[ \frac{3}{2}, -\frac{3}{2} + n, 2 - n, \right. \right. \right. \\
 & \quad \left. \left. \frac{5}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] \text{Sec} \left[ \frac{1}{2} (e + f x) \right]^2 \tan \left[ \frac{1}{2} (e + f x) \right] + \right. \\
 & \quad \left. \frac{1}{3} \left( -\frac{3}{2} + n \right) \text{AppellF1} \left[ \frac{3}{2}, -\frac{1}{2} + n, 1 - n, \frac{5}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] \right. \\
 & \quad \left. \left. \text{Sec} \left[ \frac{1}{2} (e + f x) \right]^2 \tan \left[ \frac{1}{2} (e + f x) \right] \right) + \tan \left[ \frac{1}{2} (e + f x) \right]^2 \right. \\
 & \quad \left. \left( 2 (-1 + n) \left( -\frac{3}{5} (2 - n) \text{AppellF1} \left[ \frac{5}{2}, -\frac{3}{2} + n, 3 - n, \frac{7}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] \text{Sec} \left[ \frac{1}{2} (e + f x) \right]^2 \tan \left[ \frac{1}{2} (e + f x) \right] + \frac{3}{5} \left( -\frac{3}{2} + n \right) \right. \right. \right. \\
 & \quad \left. \left. \text{AppellF1} \left[ \frac{5}{2}, -\frac{1}{2} + n, 2 - n, \frac{7}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] \right. \right. \\
 & \quad \left. \left. \text{Sec} \left[ \frac{1}{2} (e + f x) \right]^2 \tan \left[ \frac{1}{2} (e + f x) \right] \right) + (-3 + 2 n) \left( -\frac{3}{5} (1 - n) \text{AppellF1} \left[ \frac{5}{2}, \right. \right. \right. \\
 & \quad \left. \left. -\frac{1}{2} + n, 2 - n, \frac{7}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] \text{Sec} \left[ \frac{1}{2} (e + f x) \right]^2 \right. \\
 & \quad \left. \tan \left[ \frac{1}{2} (e + f x) \right] + \frac{3}{5} \left( -\frac{1}{2} + n \right) \text{AppellF1} \left[ \frac{5}{2}, \frac{1}{2} + n, 1 - n, \frac{7}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] \text{Sec} \left[ \frac{1}{2} (e + f x) \right]^2 \tan \left[ \frac{1}{2} (e + f x) \right] \right) \Big) \Big/ \\
 & \left( 3 \text{AppellF1} \left[ \frac{1}{2}, -\frac{3}{2} + n, 1 - n, \frac{3}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] + \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( 2 (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{3}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left. (-3+2n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right]\right) \tan\left[\frac{1}{2}(e+fx)\right]^2 + \\
 & \left( 6 \left(\frac{3}{2}+n\right) \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \quad \cos[e+fx] \left(\sec\left[\frac{1}{2}(e+fx)\right]^2\right)^n \left(\cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx]\right)^{\frac{1}{2}+n} \tan\left[\frac{1}{2}(e+fx)\right] \\
 & \quad \left(-1+\tan\left[\frac{1}{2}(e+fx)\right]^2\right)^2 \left(-\cos\left[\frac{1}{2}(e+fx)\right] \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right] + \right. \\
 & \quad \quad \left. \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \tan[e+fx]\right) \Bigg) / \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left( 2 (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{3}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \quad \left. (-3+2n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \quad \quad \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right]\right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \Bigg) \Bigg)
 \end{aligned}$$

**Problem 307: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \sec[e+fx]^n (a+a \sec[e+fx])^{5/2} dx$$

Optimal (type 5, 177 leaves, 4 steps):

$$\begin{aligned}
 & \frac{2 a^3 (7+4 n) \sec [e+f x]^{1+n} \sin [e+f x]}{f (1+2 n) (3+2 n) \sqrt{a+a \sec [e+f x]}} + \frac{2 a^2 \sec [e+f x]^{1+n} \sqrt{a+a \sec [e+f x]} \sin [e+f x]}{f (3+2 n)} + \\
 & \left( \frac{2 a^3 (3+24 n+16 n^2) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, 1-n, \frac{3}{2}, 1-\sec [e+f x]\right] \tan [e+f x]}{f (1+2 n) (3+2 n) \sqrt{a+a \sec [e+f x]}} \right) /
 \end{aligned}$$

Result (type 5, 435 leaves):



$$\begin{aligned}
 & -\frac{1}{f \operatorname{Sec}[e+f x]^{5/2}} \int 2^{-\frac{5}{2}+n} e^{-i\left(\frac{1}{2}+n\right)(e+f x)} \left( \frac{e^{i(e+f x)}}{1+e^{2i(e+f x)}} \right)^{\frac{1}{2}+n} \left( 1+e^{2i(e+f x)} \right)^{\frac{1}{2}+n} \\
 & \left( \frac{1}{2+n} 10 e^{i(2+n)(e+f x)} \operatorname{Hypergeometric2F1}\left[1+\frac{n}{2}, \frac{5}{2}+n, 2+\frac{n}{2}, -e^{2i(e+f x)}\right] + \right. \\
 & \frac{1}{4+n} 5 e^{i(4+n)(e+f x)} \operatorname{Hypergeometric2F1}\left[2+\frac{n}{2}, \frac{5}{2}+n, 3+\frac{n}{2}, -e^{2i(e+f x)}\right] + \\
 & \frac{e^{in(e+f x)} \operatorname{Hypergeometric2F1}\left[\frac{n}{2}, \frac{5}{2}+n, 1+\frac{n}{2}, -e^{2i(e+f x)}\right]}{n} + \\
 & \frac{5 e^{i(1+n)(e+f x)} \operatorname{Hypergeometric2F1}\left[\frac{1+n}{2}, \frac{5}{2}+n, \frac{3+n}{2}, -e^{2i(e+f x)}\right]}{1+n} + \\
 & \frac{10 e^{i(3+n)(e+f x)} \operatorname{Hypergeometric2F1}\left[\frac{5}{2}+n, \frac{3+n}{2}, \frac{5+n}{2}, -e^{2i(e+f x)}\right]}{3+n} + \\
 & \left. \frac{e^{i(5+n)(e+f x)} \operatorname{Hypergeometric2F1}\left[\frac{5}{2}+n, \frac{5+n}{2}, \frac{7+n}{2}, -e^{2i(e+f x)}\right]}{5+n} \right) \\
 & \operatorname{Sec}\left[\frac{1}{2}(e+f x)\right]^5 (a(1+\operatorname{Sec}[e+f x]))^{5/2}
 \end{aligned}$$

**Problem 308: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \operatorname{Sec}[e+f x]^n (a+a \operatorname{Sec}[e+f x])^{3/2} dx$$

Optimal (type 5, 108 leaves, 4 steps):

$$\begin{aligned}
 & \frac{2 a^2 \operatorname{Sec}[e+f x]^{1+n} \operatorname{Sin}[e+f x]}{f(1+2 n) \sqrt{a+a \operatorname{Sec}[e+f x]}} + \\
 & \left( \frac{2 a^2(1+4 n) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, 1-n, \frac{3}{2}, 1-\operatorname{Sec}[e+f x]\right] \operatorname{Tan}[e+f x]}{f(1+2 n) \sqrt{a+a \operatorname{Sec}[e+f x]}} \right)
 \end{aligned}$$

Result (type 5, 6369 leaves):

$$\begin{aligned}
 & \left( 14 \operatorname{Sec}\left[\frac{1}{2}(e+f x)\right]^3 \left( \operatorname{Sec}\left[\frac{1}{2}(e+f x)\right]^2 \right)^n \right. \\
 & \left( \operatorname{Cos}\left[\frac{1}{2}(e+f x)\right]^2 \operatorname{Sec}[e+f x] \right)^{-\frac{3}{2}+n} (a(1+\operatorname{Sec}[e+f x]))^{3/2} \\
 & \left( \operatorname{Cos}\left[\frac{3}{2}(e+f x)\right] \right) \left( \frac{1}{8} \operatorname{Sec}[e+f x]^{-\frac{3}{2}+n} + \frac{3}{8} \operatorname{Sec}[e+f x]^{\frac{1}{2}+n} + \frac{3}{4} \int \operatorname{Sec}[e+f x]^{\frac{1}{2}+n} \operatorname{Sin}[e+f x] - \right. \\
 & \frac{3}{8} \operatorname{Sec}[e+f x]^{\frac{1}{2}+n} \operatorname{Sin}[e+f x]^2 + \operatorname{Cos}[e+f x] \left( \frac{3}{8} \operatorname{Sec}[e+f x]^{\frac{1}{2}+n} + \frac{3}{8} \int \operatorname{Sec}[e+f x]^{\frac{1}{2}+n} \right. \\
 & \left. \left. \operatorname{Sin}[e+f x] \right) + \operatorname{Sec}[e+f x] \left( \frac{1}{8} \operatorname{Sec}[e+f x]^{\frac{1}{2}+n} + \frac{3}{8} \int \operatorname{Sec}[e+f x]^{\frac{1}{2}+n} \operatorname{Sin}[e+f x] - \right. \right.
 \end{aligned}$$

$$\begin{aligned}
& \left. \frac{3}{8} \operatorname{Sec}[e+fx]^{\frac{1}{2}+n} \operatorname{Sin}[e+fx]^2 - \frac{1}{8} \operatorname{Sec}[e+fx]^{\frac{1}{2}+n} \operatorname{Sin}[e+fx]^3 \right) - \\
& \frac{1}{8} \operatorname{Sec}[e+fx]^{\frac{3}{2}+n} \operatorname{Sin}\left[\frac{3}{2}(e+fx)\right] - \frac{3}{8} \operatorname{Sec}[e+fx]^{\frac{1}{2}+n} \operatorname{Sin}\left[\frac{3}{2}(e+fx)\right] + \\
& \frac{3}{4} \operatorname{Sec}[e+fx]^{\frac{1}{2}+n} \operatorname{Sin}[e+fx] \operatorname{Sin}\left[\frac{3}{2}(e+fx)\right] + \\
& \frac{3}{8} \operatorname{Sec}[e+fx]^{\frac{1}{2}+n} \operatorname{Sin}[e+fx]^2 \operatorname{Sin}\left[\frac{3}{2}(e+fx)\right] + \operatorname{Cos}[e+fx] \\
& \left( -\frac{3}{8} \operatorname{Sec}[e+fx]^{\frac{1}{2}+n} \operatorname{Sin}\left[\frac{3}{2}(e+fx)\right] + \frac{3}{8} \operatorname{Sec}[e+fx]^{\frac{1}{2}+n} \operatorname{Sin}[e+fx] \operatorname{Sin}\left[\frac{3}{2}(e+fx)\right] \right) + \\
& \operatorname{Sec}[e+fx] \left( -\frac{1}{8} \operatorname{Sec}[e+fx]^{\frac{1}{2}+n} \operatorname{Sin}\left[\frac{3}{2}(e+fx)\right] + \frac{3}{8} \operatorname{Sec}[e+fx]^{\frac{1}{2}+n} \operatorname{Sin}[e+fx] \right. \\
& \left. \operatorname{Sin}\left[\frac{3}{2}(e+fx)\right] + \frac{3}{8} \operatorname{Sec}[e+fx]^{\frac{1}{2}+n} \operatorname{Sin}[e+fx]^2 \operatorname{Sin}\left[\frac{3}{2}(e+fx)\right] - \right. \\
& \left. \frac{1}{8} \operatorname{Sec}[e+fx]^{\frac{1}{2}+n} \operatorname{Sin}[e+fx]^3 \operatorname{Sin}\left[\frac{3}{2}(e+fx)\right] \right) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \\
& \left( 8 \operatorname{Gamma}\left[\frac{5}{2}+n\right] \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
& \left. \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 + \right. \\
& \left. 5 \operatorname{Gamma}\left[\frac{3}{2}+n\right] \operatorname{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
& \left. \left( -3 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 + 2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^4 \right) \right) \Big/ \\
& \left( f \operatorname{Sec}[e+fx]^{3/2} \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right) \left( 8 \operatorname{Gamma}\left[\frac{5}{2}+n\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^4 \right. \right. \\
& \left. \left. \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \left( 7 \operatorname{Cos}[e+fx] (-5-2n+2(1+n) \operatorname{Cos}[e+fx]) \right. \right. \right. \\
& \left. \left. \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 + \right. \right. \\
& \left. \left. 8(5+2n) \operatorname{Hypergeometric2F1}\left[3, \frac{7}{2}+n, \frac{9}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \\
& \left. \left. \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right) + 7 \operatorname{Gamma}\left[\frac{3}{2}+n\right] \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right) \right. \\
& \left. \left( \frac{5}{2} \operatorname{Cos}[e+fx] (-15-9n+(9+8n) \operatorname{Cos}[e+fx] + n \operatorname{Cos}[2(e+fx)]) \right. \right. \\
& \left. \left. \operatorname{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^6 + \right. \right. \\
& \left. \left. 2(3+2n)(5+\operatorname{Cos}[e+fx]) \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, \right. \right. \right. \\
& \left. \left. \left. -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2 \right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^4 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right) \right) \right) \\
& \left( - \left( \left( 14 \left( \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \right)^{1+n} \left( \operatorname{Cos}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Sec}[e+fx] \right)^{-\frac{3}{2}+n} \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right. \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
 & \left( 8 \Gamma\left[\frac{5}{2} + n\right] \text{Hypergeometric2F1}\left[2, \frac{5}{2} + n, \frac{7}{2}, -2 \sec[e + f x] \sin\left[\frac{1}{2}(e + f x)\right]^2\right] \right. \\
 & \quad \left. \sec\left[\frac{1}{2}(e + f x)\right]^2 \tan\left[\frac{1}{2}(e + f x)\right]^2 + 5 \Gamma\left[\frac{3}{2} + n\right] \text{Hypergeometric2F1}\left[1, \frac{3}{2} + n, \frac{5}{2}, -2 \sec[e + f x] \sin\left[\frac{1}{2}(e + f x)\right]^2\right] \right. \\
 & \quad \left. \left(-3 + \tan\left[\frac{1}{2}(e + f x)\right]^2 + 2 \tan\left[\frac{1}{2}(e + f x)\right]^4\right)\right) \Big/ \\
 & \left( \left(-1 + \tan\left[\frac{1}{2}(e + f x)\right]^2\right)^2 \left(8 \Gamma\left[\frac{5}{2} + n\right] \sec\left[\frac{1}{2}(e + f x)\right]^4 \tan\left[\frac{1}{2}(e + f x)\right]^2 \right. \right. \\
 & \quad \left(7 \cos[e + f x] (-5 - 2n + 2(1 + n) \cos[e + f x]) \text{Hypergeometric2F1}\left[2, \frac{5}{2} + n, \right. \right. \\
 & \quad \left. \left. \frac{7}{2}, -2 \sec[e + f x] \sin\left[\frac{1}{2}(e + f x)\right]^2\right] \sec\left[\frac{1}{2}(e + f x)\right]^2 + 8(5 + 2n) \right. \right. \\
 & \quad \left. \left. \text{Hypergeometric2F1}\left[3, \frac{7}{2} + n, \frac{9}{2}, -2 \sec[e + f x] \sin\left[\frac{1}{2}(e + f x)\right]^2\right] \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(e + f x)\right]^2\right) + 7 \Gamma\left[\frac{3}{2} + n\right] \left(-1 + \tan\left[\frac{1}{2}(e + f x)\right]^2\right) \right. \right. \\
 & \quad \left( \frac{5}{2} \cos[e + f x] (-15 - 9n + (9 + 8n) \cos[e + f x] + n \cos[2(e + f x)]) \right. \\
 & \quad \left. \text{Hypergeometric2F1}\left[1, \frac{3}{2} + n, \frac{5}{2}, -2 \sec[e + f x] \sin\left[\frac{1}{2}(e + f x)\right]^2\right] \right. \\
 & \quad \left. \left. \sec\left[\frac{1}{2}(e + f x)\right]^6 + 2(3 + 2n)(5 + \cos[e + f x]) \text{Hypergeometric2F1}\left[2, \frac{5}{2} + n, \frac{7}{2}, \right. \right. \right. \\
 & \quad \left. \left. \left. -2 \sec[e + f x] \sin\left[\frac{1}{2}(e + f x)\right]^2\right] \sec\left[\frac{1}{2}(e + f x)\right]^4 \tan\left[\frac{1}{2}(e + f x)\right]^2\right)\right) \Big) + \\
 & \left( 7 \left(\sec\left[\frac{1}{2}(e + f x)\right]^2\right)^{1+n} \left(\cos\left[\frac{1}{2}(e + f x)\right]^2 \sec[e + f x]\right)^{-\frac{3}{2}+n} \right. \\
 & \quad \left( 8 \Gamma\left[\frac{5}{2} + n\right] \text{Hypergeometric2F1}\left[2, \frac{5}{2} + n, \frac{7}{2}, -2 \sec[e + f x] \sin\left[\frac{1}{2}(e + f x)\right]^2\right] \right. \\
 & \quad \left. \sec\left[\frac{1}{2}(e + f x)\right]^2 \tan\left[\frac{1}{2}(e + f x)\right]^2 + 5 \Gamma\left[\frac{3}{2} + n\right] \text{Hypergeometric2F1}\left[1, \frac{3}{2} + n, \frac{5}{2}, \right. \right. \\
 & \quad \left. \left. -2 \sec[e + f x] \sin\left[\frac{1}{2}(e + f x)\right]^2\right] \left(-3 + \tan\left[\frac{1}{2}(e + f x)\right]^2 + 2 \tan\left[\frac{1}{2}(e + f x)\right]^4\right)\right) \Big) \Big/ \\
 & \left( \left(-1 + \tan\left[\frac{1}{2}(e + f x)\right]^2\right)^2 \left(8 \Gamma\left[\frac{5}{2} + n\right] \sec\left[\frac{1}{2}(e + f x)\right]^4 \tan\left[\frac{1}{2}(e + f x)\right]^2 \right. \right. \\
 & \quad \left(7 \cos[e + f x] (-5 - 2n + 2(1 + n) \cos[e + f x]) \text{Hypergeometric2F1}\left[2, \frac{5}{2} + \right. \right. \\
 & \quad \left. \left. n, \frac{7}{2}, -2 \sec[e + f x] \sin\left[\frac{1}{2}(e + f x)\right]^2\right] \sec\left[\frac{1}{2}(e + f x)\right]^2 + \right. \right. \\
 & \quad \left. \left. 8(5 + 2n) \text{Hypergeometric2F1}\left[3, \frac{7}{2} + n, \frac{9}{2}, -2 \sec[e + f x] \sin\left[\frac{1}{2}(e + f x)\right]^2\right] \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(e + f x)\right]^2\right) + 7 \Gamma\left[\frac{3}{2} + n\right] \left(-1 + \tan\left[\frac{1}{2}(e + f x)\right]^2\right) \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( \frac{5}{2} \cos [e+f x] \left( -15-9 n+(9+8 n) \cos [e+f x]+n \cos [2(e+f x)] \right) \right. \\
 & \quad \text{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2}, -2 \sec [e+f x] \sin \left[\frac{1}{2}(e+f x)\right]^2\right] \\
 & \quad \left. \sec \left[\frac{1}{2}(e+f x)\right]^6+2(3+2 n)(5+\cos [e+f x]) \text{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2 \sec [e+f x] \sin \left[\frac{1}{2}(e+f x)\right]^2\right] \sec \left[\frac{1}{2}(e+f x)\right]^4 \tan \left[\frac{1}{2}(e+f x)\right]^2\right] \right) + \\
 & \left( 14 n \left( \sec \left[\frac{1}{2}(e+f x)\right]^2\right)^n \left( \cos \left[\frac{1}{2}(e+f x)\right]^2 \sec [e+f x] \right)^{-\frac{3}{2}+n} \tan \left[\frac{1}{2}(e+f x)\right]^2 \right. \\
 & \quad \left( 8 \Gamma\left[\frac{5}{2}+n\right] \text{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2 \sec [e+f x] \sin \left[\frac{1}{2}(e+f x)\right]^2\right] \right. \\
 & \quad \left. \sec \left[\frac{1}{2}(e+f x)\right]^2 \tan \left[\frac{1}{2}(e+f x)\right]^2+5 \Gamma\left[\frac{3}{2}+n\right] \text{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2}, -2 \sec [e+f x] \sin \left[\frac{1}{2}(e+f x)\right]^2\right] \left(-3+\tan \left[\frac{1}{2}(e+f x)\right]^2+2 \tan \left[\frac{1}{2}(e+f x)\right]^4\right) \right) \right) / \\
 & \left( \left(-1+\tan \left[\frac{1}{2}(e+f x)\right]^2\right) \left( 8 \Gamma\left[\frac{5}{2}+n\right] \sec \left[\frac{1}{2}(e+f x)\right]^4 \tan \left[\frac{1}{2}(e+f x)\right]^2 \right. \right. \\
 & \quad \left. \left( 7 \cos [e+f x] \left(-5-2 n+2(1+n) \cos [e+f x]\right) \text{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2 \sec [e+f x] \sin \left[\frac{1}{2}(e+f x)\right]^2\right] \sec \left[\frac{1}{2}(e+f x)\right]^2+ \right. \right. \\
 & \quad \left. \left. 8(5+2 n) \text{Hypergeometric2F1}\left[3, \frac{7}{2}+n, \frac{9}{2}, -2 \sec [e+f x] \sin \left[\frac{1}{2}(e+f x)\right]^2\right] \tan \left[\frac{1}{2}(e+f x)\right]^2\right)+7 \Gamma\left[\frac{3}{2}+n\right] \left(-1+\tan \left[\frac{1}{2}(e+f x)\right]^2\right) \right) \right) \\
 & \left( \frac{5}{2} \cos [e+f x] \left( -15-9 n+(9+8 n) \cos [e+f x]+n \cos [2(e+f x)] \right) \right. \\
 & \quad \text{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2}, -2 \sec [e+f x] \sin \left[\frac{1}{2}(e+f x)\right]^2\right] \\
 & \quad \left. \sec \left[\frac{1}{2}(e+f x)\right]^6+2(3+2 n)(5+\cos [e+f x]) \text{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2 \sec [e+f x] \sin \left[\frac{1}{2}(e+f x)\right]^2\right] \sec \left[\frac{1}{2}(e+f x)\right]^4 \tan \left[\frac{1}{2}(e+f x)\right]^2\right] \right) + \\
 & \left( 14 \left(-\frac{3}{2}+n\right) \left( \sec \left[\frac{1}{2}(e+f x)\right]^2\right)^n \left( \cos \left[\frac{1}{2}(e+f x)\right]^2 \sec [e+f x] \right)^{-\frac{5}{2}+n} \tan \left[\frac{1}{2}(e+f x)\right] \right. \\
 & \quad \left( 8 \Gamma\left[\frac{5}{2}+n\right] \text{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2 \sec [e+f x] \sin \left[\frac{1}{2}(e+f x)\right]^2\right] \right. \\
 & \quad \left. \sec \left[\frac{1}{2}(e+f x)\right]^2 \tan \left[\frac{1}{2}(e+f x)\right]^2+5 \Gamma\left[\frac{3}{2}+n\right] \text{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2}, -2 \sec [e+f x] \sin \left[\frac{1}{2}(e+f x)\right]^2\right] \left(-3+\tan \left[\frac{1}{2}(e+f x)\right]^2+2 \tan \left[\frac{1}{2}(e+f x)\right]^4\right) \right) \right) \\
 & \quad \left(-\cos \left[\frac{1}{2}(e+f x)\right] \sec [e+f x] \sin \left[\frac{1}{2}(e+f x)\right]+ \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left. \left. \cos \left[ \frac{1}{2} (e + f x) \right]^2 \sec [e + f x] \tan [e + f x] \right) \right) \right) / \\
 & \left( \left( -1 + \tan \left[ \frac{1}{2} (e + f x) \right]^2 \right) \left( 8 \Gamma \left[ \frac{5}{2} + n \right] \sec \left[ \frac{1}{2} (e + f x) \right]^4 \tan \left[ \frac{1}{2} (e + f x) \right]^2 \right. \right. \right. \\
 & \quad \left( 7 \cos [e + f x] (-5 - 2n + 2(1 + n) \cos [e + f x]) \operatorname{Hypergeometric2F1} \left[ 2, \frac{5}{2} + \right. \right. \\
 & \quad \quad \left. \left. n, \frac{7}{2}, -2 \sec [e + f x] \sin \left[ \frac{1}{2} (e + f x) \right]^2 \right] \sec \left[ \frac{1}{2} (e + f x) \right]^2 + \right. \\
 & \quad \left. 8(5 + 2n) \operatorname{Hypergeometric2F1} \left[ 3, \frac{7}{2} + n, \frac{9}{2}, -2 \sec [e + f x] \sin \left[ \frac{1}{2} (e + f x) \right]^2 \right] \right. \\
 & \quad \left. \tan \left[ \frac{1}{2} (e + f x) \right]^2 \right) + 7 \Gamma \left[ \frac{3}{2} + n \right] \left( -1 + \tan \left[ \frac{1}{2} (e + f x) \right]^2 \right) \right. \\
 & \quad \left( \frac{5}{2} \cos [e + f x] (-15 - 9n + (9 + 8n) \cos [e + f x] + n \cos [2(e + f x)]) \right) \\
 & \quad \operatorname{Hypergeometric2F1} \left[ 1, \frac{3}{2} + n, \frac{5}{2}, -2 \sec [e + f x] \sin \left[ \frac{1}{2} (e + f x) \right]^2 \right] \\
 & \quad \left. \sec \left[ \frac{1}{2} (e + f x) \right]^6 + 2(3 + 2n)(5 + \cos [e + f x]) \operatorname{Hypergeometric2F1} \left[ 2, \frac{5}{2} + n, \right. \right. \\
 & \quad \left. \left. \frac{7}{2}, -2 \sec [e + f x] \sin \left[ \frac{1}{2} (e + f x) \right]^2 \right] \sec \left[ \frac{1}{2} (e + f x) \right]^4 \tan \left[ \frac{1}{2} (e + f x) \right]^2 \right) \right) \right) + \\
 & \left( 14 \left( \sec \left[ \frac{1}{2} (e + f x) \right]^2 \right)^n \left( \cos \left[ \frac{1}{2} (e + f x) \right]^2 \sec [e + f x] \right)^{-\frac{3}{2} + n} \tan \left[ \frac{1}{2} (e + f x) \right] \right. \\
 & \quad \left( 8 \Gamma \left[ \frac{5}{2} + n \right] \operatorname{Hypergeometric2F1} \left[ 2, \frac{5}{2} + n, \frac{7}{2}, -2 \sec [e + f x] \sin \left[ \frac{1}{2} (e + f x) \right]^2 \right] \right. \\
 & \quad \left. \sec \left[ \frac{1}{2} (e + f x) \right]^4 \tan \left[ \frac{1}{2} (e + f x) \right] + 8 \Gamma \left[ \frac{5}{2} + n \right] \operatorname{Hypergeometric2F1} \left[ 2, \frac{5}{2} + n, \right. \right. \\
 & \quad \left. \left. \frac{7}{2}, -2 \sec [e + f x] \sin \left[ \frac{1}{2} (e + f x) \right]^2 \right] \sec \left[ \frac{1}{2} (e + f x) \right]^2 \tan \left[ \frac{1}{2} (e + f x) \right]^3 + \right. \\
 & \quad \left. 5 \Gamma \left[ \frac{3}{2} + n \right] \operatorname{Hypergeometric2F1} \left[ 1, \frac{3}{2} + n, \frac{5}{2}, -2 \sec [e + f x] \sin \left[ \frac{1}{2} (e + f x) \right]^2 \right] \right. \\
 & \quad \left. \left( \sec \left[ \frac{1}{2} (e + f x) \right]^2 \tan \left[ \frac{1}{2} (e + f x) \right] + 4 \sec \left[ \frac{1}{2} (e + f x) \right]^2 \tan \left[ \frac{1}{2} (e + f x) \right]^3 \right) + \right. \\
 & \quad \left. \frac{32}{7} \left( \frac{5}{2} + n \right) \Gamma \left[ \frac{5}{2} + n \right] \operatorname{Hypergeometric2F1} \left[ 3, \frac{7}{2} + n, \frac{9}{2}, \right. \right. \\
 & \quad \left. \left. -2 \sec [e + f x] \sin \left[ \frac{1}{2} (e + f x) \right]^2 \right] \sec \left[ \frac{1}{2} (e + f x) \right]^2 \right. \\
 & \quad \left. \tan \left[ \frac{1}{2} (e + f x) \right]^2 \left( -2 \cos \left[ \frac{1}{2} (e + f x) \right] \sec [e + f x] \sin \left[ \frac{1}{2} (e + f x) \right] - \right. \right. \\
 & \quad \left. \left. 2 \sec [e + f x] \sin \left[ \frac{1}{2} (e + f x) \right]^2 \tan [e + f x] \right) + 2 \left( \frac{3}{2} + n \right) \Gamma \left[ \frac{3}{2} + n \right] \right. \\
 & \quad \left. \operatorname{Hypergeometric2F1} \left[ 2, \frac{5}{2} + n, \frac{7}{2}, -2 \sec [e + f x] \sin \left[ \frac{1}{2} (e + f x) \right]^2 \right] \right. \\
 & \quad \left. \left( -3 + \tan \left[ \frac{1}{2} (e + f x) \right]^2 + 2 \tan \left[ \frac{1}{2} (e + f x) \right]^4 \right) \left( -2 \cos \left[ \frac{1}{2} (e + f x) \right] \sec [e + f x] \right. \right.
 \end{aligned}$$

$$\begin{aligned} & \left. \left( \sin\left[\frac{1}{2}(e+fx)\right] - 2 \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right]^2 \tan[e+fx] \right) \right) / \\ & \left( \left( -1 + \tan\left[\frac{1}{2}(e+fx)\right] \right)^2 \right) \left( 8 \Gamma\left[\frac{5}{2}+n\right] \sec\left[\frac{1}{2}(e+fx)\right]^4 \tan\left[\frac{1}{2}(e+fx)\right]^2 \right. \\ & \quad \left. \left( 7 \cos[e+fx] (-5-2n+2(1+n) \cos[e+fx]) \text{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2 \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 + \right. \right. \\ & \quad \left. \left. 8(5+2n) \text{Hypergeometric2F1}\left[3, \frac{7}{2}+n, \frac{9}{2}, -2 \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right]^2\right] \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) + 7 \Gamma\left[\frac{3}{2}+n\right] \left( -1 + \tan\left[\frac{1}{2}(e+fx)\right] \right)^2 \right) \\ & \quad \left( \frac{5}{2} \cos[e+fx] (-15-9n+(9+8n) \cos[e+fx]+n \cos[2(e+fx)]) \right) \\ & \quad \text{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2}, -2 \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right]^2\right] \\ & \quad \left. \sec\left[\frac{1}{2}(e+fx)\right]^6 + 2(3+2n)(5+\cos[e+fx]) \text{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2 \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^4 \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \right) - \\ & \left( 14 \left( \sec\left[\frac{1}{2}(e+fx)\right]^2 \right)^n \left( \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \right)^{-\frac{3}{2}+n} \tan\left[\frac{1}{2}(e+fx)\right] \right. \\ & \quad \left( 8 \Gamma\left[\frac{5}{2}+n\right] \text{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2 \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right]^2 + 5 \Gamma\left[\frac{3}{2}+n\right] \text{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2}, \right. \right. \\ & \quad \left. \left. -2 \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right]^2\right] \left( -3 + \tan\left[\frac{1}{2}(e+fx)\right]^2 + 2 \tan\left[\frac{1}{2}(e+fx)\right]^4 \right) \right) \right) \\ & \quad \left( 8 \Gamma\left[\frac{5}{2}+n\right] \sec\left[\frac{1}{2}(e+fx)\right]^6 \tan\left[\frac{1}{2}(e+fx)\right] \right) \\ & \quad \left( 7 \cos[e+fx] (-5-2n+2(1+n) \cos[e+fx]) \text{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2 \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 + \right. \\ & \quad \left. 8(5+2n) \text{Hypergeometric2F1}\left[3, \frac{7}{2}+n, \frac{9}{2}, -2 \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right]^2\right] \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) + 16 \Gamma\left[\frac{5}{2}+n\right] \sec\left[\frac{1}{2}(e+fx)\right]^4 \tan\left[\frac{1}{2}(e+fx)\right]^3 \\ & \quad \left( 7 \cos[e+fx] (-5-2n+2(1+n) \cos[e+fx]) \text{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2 \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 + \right. \\ & \quad \left. 8(5+2n) \text{Hypergeometric2F1}\left[3, \frac{7}{2}+n, \frac{9}{2}, -2 \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right]^2\right] \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) + 7 \Gamma\left[\frac{3}{2}+n\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \end{aligned}$$

$$\begin{aligned}
 & \left( \frac{5}{2} \cos[e+fx] (-15-9n + (9+8n) \cos[e+fx] + n \cos[2(e+fx)]) \right. \\
 & \quad \text{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2}, -2 \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right]^2\right] \\
 & \quad \sec\left[\frac{1}{2}(e+fx)\right]^6 + 2(3+2n)(5+\cos[e+fx]) \text{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2 \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^4 \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) + \\
 & 8 \Gamma\left[\frac{5}{2}+n\right] \sec\left[\frac{1}{2}(e+fx)\right]^4 \tan\left[\frac{1}{2}(e+fx)\right]^2 \left(-14(1+n) \cos[e+fx] \right. \\
 & \quad \text{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2 \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right]^2\right] \\
 & \quad \sec\left[\frac{1}{2}(e+fx)\right]^2 \sin[e+fx] - 7(-5-2n+2(1+n) \cos[e+fx]) \\
 & \quad \text{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2 \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right]^2\right] \\
 & \quad \sec\left[\frac{1}{2}(e+fx)\right]^2 \sin[e+fx] + 7 \cos[e+fx](-5-2n+2(1+n) \cos[e+fx]) \\
 & \quad \text{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2 \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right]^2\right] \\
 & \quad \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + 8(5+2n) \text{Hypergeometric2F1}\left[3, \frac{7}{2}+n, \frac{9}{2}, -2 \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \\
 & 4 \left(\frac{5}{2}+n\right) \cos[e+fx](-5-2n+2(1+n) \cos[e+fx]) \text{Hypergeometric2F1}\left[3, \frac{7}{2}+n, \frac{9}{2}, -2 \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \left(-2 \cos\left[\frac{1}{2}(e+fx)\right] \right. \\
 & \quad \left. \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right] - 2 \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right]^2 \tan[e+fx]\right) + \\
 & \frac{16}{3} \left(\frac{7}{2}+n\right)(5+2n) \text{Hypergeometric2F1}\left[4, \frac{9}{2}+n, \frac{11}{2}, -2 \sec[e+fx] \right. \\
 & \quad \left. \sin\left[\frac{1}{2}(e+fx)\right]^2\right] \tan\left[\frac{1}{2}(e+fx)\right]^2 \left(-2 \cos\left[\frac{1}{2}(e+fx)\right] \sec[e+fx] \right. \\
 & \quad \left. \sin\left[\frac{1}{2}(e+fx)\right] - 2 \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right]^2 \tan[e+fx]\right) \right) + \\
 & 7 \Gamma\left[\frac{3}{2}+n\right] \left(-1 + \tan\left[\frac{1}{2}(e+fx)\right]^2\right) \left(-\frac{5}{2}(-15-9n + (9+8n) \cos[e+fx] + \right. \\
 & \quad \left. n \cos[2(e+fx)]) \text{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2}, -2 \right. \right. \\
 & \quad \left. \left. \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^6 \sin[e+fx] + \right. \\
 & \quad \left. \frac{5}{2} \cos[e+fx] \text{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2}, -2 \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \quad \left. \left. \sec\left[\frac{1}{2}(e+fx)\right]^6(- (9+8n) \sin[e+fx] - 2n \sin[2(e+fx)])\right) + \right.
 \end{aligned}$$

$$\begin{aligned}
& \frac{15}{2} \cos [e+f x] \left(-15-9 n+(9+8 n) \cos [e+f x]+n \cos [2(e+f x)]\right) \\
& \operatorname{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2}, -2 \operatorname{Sec}[e+f x] \sin \left[\frac{1}{2}(e+f x)\right]^2\right] \\
& \operatorname{Sec}\left[\frac{1}{2}(e+f x)\right]^6 \tan \left[\frac{1}{2}(e+f x)\right]+2(3+2 n)\left(5+\cos [e+f x]\right) \\
& \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2 \operatorname{Sec}[e+f x] \sin \left[\frac{1}{2}(e+f x)\right]^2\right] \\
& \operatorname{Sec}\left[\frac{1}{2}(e+f x)\right]^6 \tan \left[\frac{1}{2}(e+f x)\right]-2(3+2 n) \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2\right. \\
& \quad \left.\operatorname{Sec}[e+f x] \sin \left[\frac{1}{2}(e+f x)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+f x)\right]^4 \sin [e+f x] \tan \left[\frac{1}{2}(e+f x)\right]^2+\right. \\
& \quad \left.4(3+2 n)\left(5+\cos [e+f x]\right) \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2\right.\right. \\
& \quad \left.\left.\operatorname{Sec}[e+f x] \sin \left[\frac{1}{2}(e+f x)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+f x)\right]^4 \tan \left[\frac{1}{2}(e+f x)\right]^3+\right.\right. \\
& \quad \left.\left.\left(\frac{3}{2}+n\right) \cos [e+f x] \left(-15-9 n+(9+8 n) \cos [e+f x]+n \cos [2(e+f x)]\right)\right.\right. \\
& \quad \left.\left.\operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2 \operatorname{Sec}[e+f x] \sin \left[\frac{1}{2}(e+f x)\right]^2\right]\right.\right. \\
& \quad \left.\left.\operatorname{Sec}\left[\frac{1}{2}(e+f x)\right]^6\left(-2 \cos \left[\frac{1}{2}(e+f x)\right] \operatorname{Sec}[e+f x] \sin \left[\frac{1}{2}(e+f x)\right]-2 \operatorname{Sec}\left[\frac{1}{2}\right.\right.\right.\right. \\
& \quad \left.\left.\left.\left[e+f x\right] \sin \left[\frac{1}{2}(e+f x)\right]^2 \tan [e+f x]\right)+\frac{8}{7}\left(\frac{5}{2}+n\right)(3+2 n)\left(5+\cos [e+f x]\right)\right.\right.\right. \\
& \quad \left.\left.\operatorname{Hypergeometric2F1}\left[3, \frac{7}{2}+n, \frac{9}{2}, -2 \operatorname{Sec}[e+f x] \sin \left[\frac{1}{2}(e+f x)\right]^2\right]\right.\right. \\
& \quad \left.\left.\operatorname{Sec}\left[\frac{1}{2}(e+f x)\right]^4 \tan \left[\frac{1}{2}(e+f x)\right]^2\left(-2 \cos \left[\frac{1}{2}(e+f x)\right] \operatorname{Sec}[e+f x]\right.\right.\right. \\
& \quad \left.\left.\left.\sin \left[\frac{1}{2}(e+f x)\right]-2 \operatorname{Sec}[e+f x] \sin \left[\frac{1}{2}(e+f x)\right]^2 \tan [e+f x]\right)\right]\right)\right) \Big/ \\
& \left(\left(-1+\tan \left[\frac{1}{2}(e+f x)\right]^2\right)\left(8 \operatorname{Gamma}\left[\frac{5}{2}+n\right] \operatorname{Sec}\left[\frac{1}{2}(e+f x)\right]^4 \tan \left[\frac{1}{2}(e+f x)\right]^2\right.\right. \\
& \quad \left.\left.(7 \cos [e+f x] \left(-5-2 n+2(1+n) \cos [e+f x]\right) \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2},\right.\right.\right. \\
& \quad \left.\left.-2 \operatorname{Sec}[e+f x] \sin \left[\frac{1}{2}(e+f x)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+f x)\right]^2+8(5+2 n)\right.\right. \\
& \quad \left.\left.\operatorname{Hypergeometric2F1}\left[3, \frac{7}{2}+n, \frac{9}{2}, -2 \operatorname{Sec}[e+f x] \sin \left[\frac{1}{2}(e+f x)\right]^2\right]\right.\right. \\
& \quad \left.\left.\tan \left[\frac{1}{2}(e+f x)\right]^2\right)+7 \operatorname{Gamma}\left[\frac{3}{2}+n\right]\left(-1+\tan \left[\frac{1}{2}(e+f x)\right]^2\right)\right)\right) \\
& \left(\frac{5}{2} \cos [e+f x] \left(-15-9 n+(9+8 n) \cos [e+f x]+n \cos [2(e+f x)]\right)\right) \\
& \operatorname{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2}, -2 \operatorname{Sec}[e+f x] \sin \left[\frac{1}{2}(e+f x)\right]^2\right] \\
& \operatorname{Sec}\left[\frac{1}{2}(e+f x)\right]^6+2(3+2 n)\left(5+\cos [e+f x]\right) \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2},\right.
\end{aligned}$$



$$-2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^4 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right)^2 \right)^2 \right)^2 \right)^2 \right)$$

**Problem 309: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \operatorname{Sec}[e+fx]^n \sqrt{a+a \operatorname{Sec}[e+fx]} dx$$

Optimal (type 5, 48 leaves, 2 steps):

$$\frac{2 a \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, 1-n, \frac{3}{2}, 1-\operatorname{Sec}[e+fx]\right] \operatorname{Tan}[e+fx]}{f \sqrt{a+a \operatorname{Sec}[e+fx]}}$$

Result (type 5, 213 leaves):

$$\begin{aligned} & -\frac{1}{f n (1+n)} i^{2^{-\frac{1}{2}+n}} e^{\frac{1}{2} i (e+fx)} \left(1+e^{2 i (e+fx)}\right)^{-\frac{1}{2}+n} \left(e^{-i (e+fx)}\left(1+e^{2 i (e+fx)}\right)\right)^{\frac{1}{2}-n} \\ & \operatorname{Cos}[e+fx]^{\frac{1}{2}+n} \left( (1+n) \operatorname{Hypergeometric2F1}\left[\frac{n}{2}, \frac{1}{2}+n, \frac{2+n}{2}, -e^{2 i (e+fx)}\right] + \right. \\ & \quad \left. e^{i (e+fx)} n \operatorname{Hypergeometric2F1}\left[\frac{1}{2}+n, \frac{1+n}{2}, \frac{3+n}{2}, -e^{2 i (e+fx)}\right] \right) \\ & \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right] \operatorname{Sec}[e+fx]^n \sqrt{a(1+\operatorname{Sec}[e+fx])} \end{aligned}$$

**Problem 310: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec}[e+fx]^n}{\sqrt{a+a \operatorname{Sec}[e+fx]}} dx$$

Optimal (type 6, 61 leaves, 4 steps):

$$\frac{\left(\operatorname{AppellF1}\left[\frac{1}{2}, 1-n, 1, \frac{3}{2}, 1-\operatorname{Sec}[e+fx], \frac{1}{2}(1-\operatorname{Sec}[e+fx])\right] \operatorname{Tan}[e+fx]\right)}{\left(f \sqrt{a+a \operatorname{Sec}[e+fx]}\right)}$$

Result (type 6, 2964 leaves):

$$\begin{aligned} & \left(3 \sqrt{2} \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, 1-n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\ & \quad \left. \left(\operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2\right)^n \operatorname{Sec}[e+fx]^{-\frac{1}{2}+\frac{1}{2}(-1+2n)} \left(\operatorname{Cos}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Sec}[e+fx]\right)^n \right. \\ & \quad \left. \sqrt{1+\operatorname{Sec}[e+fx]} \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right) / \left(f \sqrt{a(1+\operatorname{Sec}[e+fx])}\right) \\ & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, 1-n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\ & \quad \left. \left(2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 2-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \end{aligned}$$



$$\begin{aligned}
& \left. \left( \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) \Big/ \\
& \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
& \quad \left( 2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
& \quad \quad \left. (-1+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \\
& \quad \tan\left[\frac{1}{2}(e+fx)\right]^2 \Big) - \left( 3\sqrt{2} \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \cos[e+fx] \left( \sec\left[\frac{1}{2}(e+fx)\right]^2 \right)^n \right. \\
& \quad \left. \left( \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \right)^n \sqrt{1+\sec[e+fx]} \tan\left[\frac{1}{2}(e+fx)\right] \right. \\
& \quad \left. \left( 2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \\
& \quad \quad \left. \left. (-1+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \right) \\
& \quad \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \\
& \quad 3 \left( -\frac{1}{3}(1-n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
& \quad \quad \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \frac{1}{3} \left( -\frac{1}{2}+n \right) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+n, 1-n, \frac{5}{2}, \right. \\
& \quad \quad \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \Big) + \\
& \quad \tan\left[\frac{1}{2}(e+fx)\right]^2 \left( 2(-1+n) \left( -\frac{3}{5}(2-n) \operatorname{AppellF1}\left[\frac{5}{2}, -\frac{1}{2}+n, 3-n, \frac{7}{2}, \right. \right. \right. \\
& \quad \quad \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \frac{3}{5} \right. \right. \\
& \quad \quad \left. \left. \left( -\frac{1}{2}+n \right) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{2}+n, 2-n, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \right. \\
& \quad \quad \left. \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) + (-1+2n) \left( -\frac{3}{5}(1-n) \operatorname{AppellF1}\left[\frac{5}{2}, \right. \right. \\
& \quad \quad \left. \left. \frac{1}{2}+n, 2-n, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \right. \\
& \quad \quad \left. \tan\left[\frac{1}{2}(e+fx)\right] + \frac{3}{5} \left( \frac{1}{2}+n \right) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{3}{2}+n, 1-n, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
& \quad \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) \right) \Big/ \\
& \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
& \quad \left( 2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
& \quad \quad \left. (-1+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right.
\end{aligned}$$

$$\begin{aligned}
 & -\tan\left[\frac{1}{2}(e+fx)\right]^2 \Big) \tan\left[\frac{1}{2}(e+fx)\right]^2 + \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \quad \left. \left( \sec\left[\frac{1}{2}(e+fx)\right]^2 \right)^n \left( \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \right)^n \right. \\
 & \quad \left. \tan\left[\frac{1}{2}(e+fx)\right] \tan[e+fx] \right) / \left( \sqrt{2} \sqrt{1+\sec[e+fx]} \right. \\
 & \quad \left. \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \\
 & \quad \left. \left( 2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. (-1+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \right) + \right. \\
 & \quad \left. \left( 3\sqrt{2} n \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \\
 & \quad \left. \left. \cos[e+fx] \left( \sec\left[\frac{1}{2}(e+fx)\right]^2 \right)^n \left( \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \right)^{-1+n} \right. \right. \\
 & \quad \left. \left. \sqrt{1+\sec[e+fx]} \tan\left[\frac{1}{2}(e+fx)\right] \left( -\cos\left[\frac{1}{2}(e+fx)\right] \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right] + \right. \right. \right. \\
 & \quad \left. \left. \left. \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \tan[e+fx] \right) \right) \right) / \right. \\
 & \quad \left. \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \\
 & \quad \left. \left( 2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. (-1+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \right) \right)
 \end{aligned}$$

**Problem 311: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sec[e+fx]^n}{(a+a \sec[e+fx])^{3/2}} dx$$

Optimal (type 6, 67 leaves, 4 steps):

$$\left( \operatorname{AppellF1}\left[\frac{1}{2}, 1-n, 2, \frac{3}{2}, 1-\sec[e+fx], \frac{1}{2}(1-\sec[e+fx])\right] \tan[e+fx] \right) / \left( 2af \sqrt{a+a \sec[e+fx]} \right)$$

Result (type 6, 2992 leaves):

$$\left( 6 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right)$$

$$\begin{aligned}
 & \left( \sec \left[ \frac{1}{2} (e + f x) \right]^2 \right)^n \sec [e + f x]^{\frac{1}{2} + \frac{1}{2} (-3+2n)} \left( \cos \left[ \frac{1}{2} (e + f x) \right]^2 \sec [e + f x] \right)^{\frac{3}{2}+n} \\
 & \tan \left[ \frac{1}{2} (e + f x) \right] \left( -1 + \tan \left[ \frac{1}{2} (e + f x) \right]^2 \right)^2 \Big/ \left( f (a (1 + \sec [e + f x])) \right)^{3/2} \\
 & \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{3}{2} + n, 1 - n, \frac{3}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] + \right. \\
 & \quad \left( 2 (-1 + n) \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{3}{2} + n, 2 - n, \frac{5}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] + \right. \\
 & \quad \left. \left. (-3 + 2n) \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{1}{2} + n, 1 - n, \frac{5}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] \right) \right) \\
 & \tan \left[ \frac{1}{2} (e + f x) \right]^2 \left( \left( 12 \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{3}{2} + n, 1 - n, \frac{3}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] \cos [e + f x] \left( \sec \left[ \frac{1}{2} (e + f x) \right]^2 \right)^{1+n} \right. \right. \\
 & \quad \left. \left. \left( \cos \left[ \frac{1}{2} (e + f x) \right]^2 \sec [e + f x] \right)^{\frac{3}{2}+n} \tan \left[ \frac{1}{2} (e + f x) \right]^2 \left( -1 + \tan \left[ \frac{1}{2} (e + f x) \right]^2 \right) \right) \right) \Big/ \\
 & \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{3}{2} + n, 1 - n, \frac{3}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] + \right. \\
 & \quad \left( 2 (-1 + n) \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{3}{2} + n, 2 - n, \frac{5}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] + \right. \\
 & \quad \left. \left. (-3 + 2n) \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{1}{2} + n, 1 - n, \frac{5}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (e + f x) \right]^2 \right) + \\
 & \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{3}{2} + n, 1 - n, \frac{3}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] \cos [e + f x] \right. \\
 & \quad \left. \left( \sec \left[ \frac{1}{2} (e + f x) \right]^2 \right)^{1+n} \left( \cos \left[ \frac{1}{2} (e + f x) \right]^2 \sec [e + f x] \right)^{\frac{3}{2}+n} \left( -1 + \tan \left[ \frac{1}{2} (e + f x) \right]^2 \right)^2 \right) \Big/ \\
 & \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{3}{2} + n, 1 - n, \frac{3}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] + \right. \\
 & \quad \left( 2 (-1 + n) \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{3}{2} + n, 2 - n, \frac{5}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] + \right. \\
 & \quad \left. \left. (-3 + 2n) \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{1}{2} + n, 1 - n, \frac{5}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] \right) \right) \\
 & \tan \left[ \frac{1}{2} (e + f x) \right]^2 \left( 6 \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{3}{2} + n, 1 - n, \frac{3}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] \left( \sec \left[ \frac{1}{2} (e + f x) \right]^2 \right)^n \left( \cos \left[ \frac{1}{2} (e + f x) \right]^2 \sec [e + f x] \right)^{\frac{3}{2}+n} \right. \\
 & \quad \left. \sin [e + f x] \tan \left[ \frac{1}{2} (e + f x) \right] \left( -1 + \tan \left[ \frac{1}{2} (e + f x) \right]^2 \right)^2 \right) \Big/ \\
 & \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{3}{2} + n, 1 - n, \frac{3}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] + \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( 2 (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{3}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left. (-3+2n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \\
 & \tan\left[\frac{1}{2}(e+fx)\right]^2 + \left( 6n \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \cos[e+fx] \left(\sec\left[\frac{1}{2}(e+fx)\right]^2\right)^n \right. \\
 & \quad \left. \left(\cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx]\right)^{\frac{3}{2}+n} \tan\left[\frac{1}{2}(e+fx)\right]^2 \left(-1+\tan\left[\frac{1}{2}(e+fx)\right]^2\right)^2 \right) \right) / \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left( 2 (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{3}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left. (-3+2n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \\
 & \quad \left. \tan\left[\frac{1}{2}(e+fx)\right]^2 + \left( 6 \cos[e+fx] \left(\sec\left[\frac{1}{2}(e+fx)\right]^2\right)^n \right. \right. \\
 & \quad \left. \left(\cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx]\right)^{\frac{3}{2}+n} \tan\left[\frac{1}{2}(e+fx)\right] \left(-\frac{1}{3}(1-n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{3}{2}+n, \right. \right. \right. \\
 & \quad \left. \left. 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \right. \right. \\
 & \quad \left. \left. \frac{1}{3} \left(-\frac{3}{2}+n\right) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \\
 & \quad \left. \left. \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) \left(-1+\tan\left[\frac{1}{2}(e+fx)\right]^2\right)^2 \right) \right) / \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left( 2 (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{3}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left. (-3+2n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \\
 & \quad \left. \tan\left[\frac{1}{2}(e+fx)\right]^2 - \left( 6 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \cos[e+fx] \left(\sec\left[\frac{1}{2}(e+fx)\right]^2\right)^n \right. \right. \\
 & \quad \left. \left(\cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx]\right)^{\frac{3}{2}+n} \tan\left[\frac{1}{2}(e+fx)\right] \left(-1+\tan\left[\frac{1}{2}(e+fx)\right]^2\right)^2 \right) \right) \\
 & \left( \left( 2 (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{3}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. (-3+2n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \text{Tan}\left[\frac{1}{2}(e+fx)\right] + 3\left(-\frac{1}{3}(1-n) \text{AppellF1}\left[\frac{3}{2}, -\frac{3}{2}+n, 2-n, \right. \right. \\
 & \quad \left. \left. \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \text{Tan}\left[\frac{1}{2}(e+fx)\right] + \right. \\
 & \quad \left. \frac{1}{3}\left(-\frac{3}{2}+n\right) \text{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 1-n, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \quad \left. \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \text{Tan}\left[\frac{1}{2}(e+fx)\right]\right) + \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \\
 & \left(2(-1+n)\left(-\frac{3}{5}(2-n) \text{AppellF1}\left[\frac{5}{2}, -\frac{3}{2}+n, 3-n, \frac{7}{2}, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \text{Tan}\left[\frac{1}{2}(e+fx)\right] + \frac{3}{5}\left(-\frac{3}{2}+n\right) \right. \\
 & \quad \left. \text{AppellF1}\left[\frac{5}{2}, -\frac{1}{2}+n, 2-n, \frac{7}{2}, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \quad \left. \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \text{Tan}\left[\frac{1}{2}(e+fx)\right]\right) + (-3+2n)\left(-\frac{3}{5}(1-n) \text{AppellF1}\left[\frac{5}{2}, \right. \right. \\
 & \quad \left. \left. -\frac{1}{2}+n, 2-n, \frac{7}{2}, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \right. \\
 & \quad \left. \text{Tan}\left[\frac{1}{2}(e+fx)\right] + \frac{3}{5}\left(-\frac{1}{2}+n\right) \text{AppellF1}\left[\frac{5}{2}, \frac{1}{2}+n, 1-n, \frac{7}{2}, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \text{Tan}\left[\frac{1}{2}(e+fx)\right]\right)\right) \Big/ \\
 & \left(3 \text{AppellF1}\left[\frac{1}{2}, -\frac{3}{2}+n, 1-n, \frac{3}{2}, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left(2(-1+n) \text{AppellF1}\left[\frac{3}{2}, -\frac{3}{2}+n, 2-n, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left. (-3+2n) \text{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 1-n, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \Big) + \\
 & \left(6\left(\frac{3}{2}+n\right) \text{AppellF1}\left[\frac{1}{2}, -\frac{3}{2}+n, 1-n, \frac{3}{2}, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \quad \left. \text{Cos}[e+fx] \left(\text{Sec}\left[\frac{1}{2}(e+fx)\right]^2\right)^n \left(\text{Cos}\left[\frac{1}{2}(e+fx)\right]^2 \text{Sec}[e+fx]\right)^{\frac{1}{2}+n} \text{Tan}\left[\frac{1}{2}(e+fx)\right] \right. \\
 & \quad \left. \left(-1+\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right)^2 \left(-\text{Cos}\left[\frac{1}{2}(e+fx)\right] \text{Sec}[e+fx] \text{Sin}\left[\frac{1}{2}(e+fx)\right] + \right. \right. \\
 & \quad \left. \left. \text{Cos}\left[\frac{1}{2}(e+fx)\right]^2 \text{Sec}[e+fx] \text{Tan}[e+fx]\right)\right) \Big/ \\
 & \left(3 \text{AppellF1}\left[\frac{1}{2}, -\frac{3}{2}+n, 1-n, \frac{3}{2}, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left(2(-1+n) \text{AppellF1}\left[\frac{3}{2}, -\frac{3}{2}+n, 2-n, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left. (-3+2n) \text{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 1-n, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right. \right.
 \end{aligned}$$

$$-\tan\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right]^2 \right)$$

**Problem 312: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int (-\sec[e+fx])^n (a+a\sec[e+fx])^{3/2} dx$$

Optimal (type 5, 130 leaves, 5 steps):

$$\left(2a^2(1+4n) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, 1-n, \frac{3}{2}, 1-\sec[e+fx]\right] (-\sec[e+fx])^n \sec[e+fx]^{1-n} \sin[e+fx]\right) / \left(f(1+2n) \sqrt{a+a\sec[e+fx]}\right) + \frac{2a^2(-\sec[e+fx])^n \tan[e+fx]}{f(1+2n) \sqrt{a+a\sec[e+fx]}}$$

Result (type 5, 6383 leaves):

$$\left(14 \sec\left[\frac{1}{2}(e+fx)\right]^3 \left(\sec\left[\frac{1}{2}(e+fx)\right]^2\right)^n (-\sec[e+fx])^n \sec[e+fx]^{-\frac{3}{2}-n} \left(\cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx]\right)^{-\frac{3}{2}+n} (a(1+\sec[e+fx]))^{3/2} \left(\cos\left[\frac{3}{2}(e+fx)\right] \left(\frac{1}{8} \sec[e+fx]^{-\frac{3}{2}+n} + \frac{3}{8} \sec[e+fx]^{\frac{1}{2}+n} + \frac{3}{4} \sec[e+fx]^{\frac{1}{2}+n} \sin[e+fx] - \frac{3}{8} \sec[e+fx]^{\frac{1}{2}+n} \sin[e+fx]^2 + \cos[e+fx] \left(\frac{3}{8} \sec[e+fx]^{\frac{1}{2}+n} + \frac{3}{8} \sec[e+fx]^{\frac{1}{2}+n} \sin[e+fx]\right) + \sec[e+fx] \left(\frac{1}{8} \sec[e+fx]^{\frac{1}{2}+n} + \frac{3}{8} \sec[e+fx]^{\frac{1}{2}+n} \sin[e+fx] - \frac{3}{8} \sec[e+fx]^{\frac{1}{2}+n} \sin[e+fx]^2 - \frac{1}{8} \sec[e+fx]^{\frac{1}{2}+n} \sin[e+fx]^3\right) - \frac{1}{8} \sec[e+fx]^{-\frac{3}{2}+n} \sin\left[\frac{3}{2}(e+fx)\right] - \frac{3}{8} \sec[e+fx]^{\frac{1}{2}+n} \sin\left[\frac{3}{2}(e+fx)\right] + \frac{3}{4} \sec[e+fx]^{\frac{1}{2}+n} \sin[e+fx] \sin\left[\frac{3}{2}(e+fx)\right] + \frac{3}{8} \sec[e+fx]^{\frac{1}{2}+n} \sin[e+fx]^2 \sin\left[\frac{3}{2}(e+fx)\right] + \cos[e+fx] \left(-\frac{3}{8} \sec[e+fx]^{\frac{1}{2}+n} \sin\left[\frac{3}{2}(e+fx)\right] + \frac{3}{8} \sec[e+fx]^{\frac{1}{2}+n} \sin[e+fx] \sin\left[\frac{3}{2}(e+fx)\right]\right) + \sec[e+fx] \left(-\frac{1}{8} \sec[e+fx]^{\frac{1}{2}+n} \sin\left[\frac{3}{2}(e+fx)\right] + \frac{3}{8} \sec[e+fx]^{\frac{1}{2}+n} \sin[e+fx] \sin\left[\frac{3}{2}(e+fx)\right] + \sin\left[\frac{3}{2}(e+fx)\right] + \frac{3}{8} \sec[e+fx]^{\frac{1}{2}+n} \sin[e+fx]^2 \sin\left[\frac{3}{2}(e+fx)\right] - \frac{1}{8} \sec[e+fx]^{\frac{1}{2}+n} \sin[e+fx]^3 \sin\left[\frac{3}{2}(e+fx)\right])\right) \tan\left[\frac{1}{2}(e+fx)\right]$$



$$\begin{aligned}
 & \left( 8 \Gamma\left[\frac{5}{2} + n\right] \text{Hypergeometric2F1}\left[2, \frac{5}{2} + n, \frac{7}{2}, -2 \sec[e + f x] \sin\left[\frac{1}{2}(e + f x)\right]^2\right] \right. \\
 & \quad \left. \sec\left[\frac{1}{2}(e + f x)\right]^2 \tan\left[\frac{1}{2}(e + f x)\right]^2 + \right. \\
 & \quad \left. 5 \Gamma\left[\frac{3}{2} + n\right] \text{Hypergeometric2F1}\left[1, \frac{3}{2} + n, \frac{5}{2}, -2 \sec[e + f x] \sin\left[\frac{1}{2}(e + f x)\right]^2\right] \right. \\
 & \quad \left. \left(-3 + \tan\left[\frac{1}{2}(e + f x)\right]^2 + 2 \tan\left[\frac{1}{2}(e + f x)\right]^4\right)\right) \Big/ \\
 & \left( f \left(-1 + \tan\left[\frac{1}{2}(e + f x)\right]^2\right) \left(8 \Gamma\left[\frac{5}{2} + n\right] \sec\left[\frac{1}{2}(e + f x)\right]^4 \tan\left[\frac{1}{2}(e + f x)\right]^2 \right. \right. \\
 & \quad \left. \left(7 \cos[e + f x] (-5 - 2n + 2(1 + n) \cos[e + f x]) \right. \right. \\
 & \quad \left. \left. \text{Hypergeometric2F1}\left[2, \frac{5}{2} + n, \frac{7}{2}, -2 \sec[e + f x] \sin\left[\frac{1}{2}(e + f x)\right]^2\right] \sec\left[\frac{1}{2}(e + f x)\right]^2 + \right. \right. \\
 & \quad \left. \left. 8(5 + 2n) \text{Hypergeometric2F1}\left[3, \frac{7}{2} + n, \frac{9}{2}, -2 \sec[e + f x] \sin\left[\frac{1}{2}(e + f x)\right]^2\right] \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(e + f x)\right]^2\right) + 7 \Gamma\left[\frac{3}{2} + n\right] \left(-1 + \tan\left[\frac{1}{2}(e + f x)\right]^2\right) \right. \\
 & \quad \left. \left(\frac{5}{2} \cos[e + f x] (-15 - 9n + (9 + 8n) \cos[e + f x] + n \cos[2(e + f x)]) \right. \right. \\
 & \quad \left. \left. \text{Hypergeometric2F1}\left[1, \frac{3}{2} + n, \frac{5}{2}, -2 \sec[e + f x] \sin\left[\frac{1}{2}(e + f x)\right]^2\right] \sec\left[\frac{1}{2}(e + f x)\right]^6 + \right. \right. \\
 & \quad \left. \left. 2(3 + 2n)(5 + \cos[e + f x]) \text{Hypergeometric2F1}\left[2, \frac{5}{2} + n, \frac{7}{2}, \right. \right. \\
 & \quad \left. \left. -2 \sec[e + f x] \sin\left[\frac{1}{2}(e + f x)\right]^2\right] \sec\left[\frac{1}{2}(e + f x)\right]^4 \tan\left[\frac{1}{2}(e + f x)\right]^2\right) \right) \\
 & \left( - \left( \left( 14 \left( \sec\left[\frac{1}{2}(e + f x)\right]^2 \right)^{1+n} \left( \cos\left[\frac{1}{2}(e + f x)\right]^2 \sec[e + f x] \right)^{-\frac{3}{2}+n} \tan\left[\frac{1}{2}(e + f x)\right]^2 \right. \right. \right. \\
 & \quad \left. \left( 8 \Gamma\left[\frac{5}{2} + n\right] \text{Hypergeometric2F1}\left[2, \frac{5}{2} + n, \frac{7}{2}, -2 \sec[e + f x] \sin\left[\frac{1}{2}(e + f x)\right]^2\right] \right. \right. \\
 & \quad \left. \left. \sec\left[\frac{1}{2}(e + f x)\right]^2 \tan\left[\frac{1}{2}(e + f x)\right]^2 + \right. \right. \\
 & \quad \left. \left. 5 \Gamma\left[\frac{3}{2} + n\right] \text{Hypergeometric2F1}\left[1, \frac{3}{2} + n, \frac{5}{2}, -2 \sec[e + f x] \sin\left[\frac{1}{2}(e + f x)\right]^2\right] \right. \right. \\
 & \quad \left. \left. \left(-3 + \tan\left[\frac{1}{2}(e + f x)\right]^2 + 2 \tan\left[\frac{1}{2}(e + f x)\right]^4\right)\right) \right) \Big/ \\
 & \left( \left( -1 + \tan\left[\frac{1}{2}(e + f x)\right]^2 \right)^2 \left( 8 \Gamma\left[\frac{5}{2} + n\right] \sec\left[\frac{1}{2}(e + f x)\right]^4 \tan\left[\frac{1}{2}(e + f x)\right]^2 \right. \right. \\
 & \quad \left. \left( 7 \cos[e + f x] (-5 - 2n + 2(1 + n) \cos[e + f x]) \text{Hypergeometric2F1}\left[2, \frac{5}{2} + n, \right. \right. \\
 & \quad \left. \left. \frac{7}{2}, -2 \sec[e + f x] \sin\left[\frac{1}{2}(e + f x)\right]^2\right] \sec\left[\frac{1}{2}(e + f x)\right]^2 + 8(5 + 2n) \right. \right. \\
 & \quad \left. \left. \text{Hypergeometric2F1}\left[3, \frac{7}{2} + n, \frac{9}{2}, -2 \sec[e + f x] \sin\left[\frac{1}{2}(e + f x)\right]^2\right] \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( \tan\left[\frac{1}{2}(e+fx)\right]^2 + 7 \Gamma\left[\frac{3}{2}+n\right] \left(-1 + \tan\left[\frac{1}{2}(e+fx)\right]\right)^2 \right. \\
 & \left. \left(\frac{5}{2} \cos[e+fx] (-15 - 9n + (9+8n) \cos[e+fx] + n \cos[2(e+fx)]) \right) \right. \\
 & \text{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2}, -2 \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right]^2\right] \\
 & \left. \sec\left[\frac{1}{2}(e+fx)\right]^6 + 2(3+2n)(5 + \cos[e+fx]) \text{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, \right. \right. \\
 & \left. \left. -2 \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^4 \tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \Bigg) + \\
 & \left( 7 \left( \sec\left[\frac{1}{2}(e+fx)\right]^2 \right)^{1+n} \left( \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \right)^{-\frac{3}{2}+n} \right. \\
 & \left( 8 \Gamma\left[\frac{5}{2}+n\right] \text{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2 \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \left. \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right]^2 + 5 \Gamma\left[\frac{3}{2}+n\right] \text{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2}, \right. \right. \\
 & \left. \left. -2 \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right]^2\right] \left(-3 + \tan\left[\frac{1}{2}(e+fx)\right]^2 + 2 \tan\left[\frac{1}{2}(e+fx)\right]^4\right) \right) \right) \Bigg) / \\
 & \left( \left(-1 + \tan\left[\frac{1}{2}(e+fx)\right]^2\right) \left( 8 \Gamma\left[\frac{5}{2}+n\right] \sec\left[\frac{1}{2}(e+fx)\right]^4 \tan\left[\frac{1}{2}(e+fx)\right]^2 \right. \right. \\
 & \left. \left( 7 \cos[e+fx] (-5 - 2n + 2(1+n) \cos[e+fx]) \text{Hypergeometric2F1}\left[2, \frac{5}{2}+ \right. \right. \right. \\
 & \left. \left. \left. n, \frac{7}{2}, -2 \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 + \right. \right. \right. \\
 & \left. \left. 8(5+2n) \text{Hypergeometric2F1}\left[3, \frac{7}{2}+n, \frac{9}{2}, -2 \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2 + 7 \Gamma\left[\frac{3}{2}+n\right] \left(-1 + \tan\left[\frac{1}{2}(e+fx)\right]\right)^2 \right) \right. \\
 & \left. \left(\frac{5}{2} \cos[e+fx] (-15 - 9n + (9+8n) \cos[e+fx] + n \cos[2(e+fx)]) \right) \right. \\
 & \text{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2}, -2 \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right]^2\right] \\
 & \left. \sec\left[\frac{1}{2}(e+fx)\right]^6 + 2(3+2n)(5 + \cos[e+fx]) \text{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \right. \right. \\
 & \left. \left. \frac{7}{2}, -2 \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^4 \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \right) \Bigg) + \\
 & \left( 14n \left( \sec\left[\frac{1}{2}(e+fx)\right]^2 \right)^n \left( \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \right)^{-\frac{3}{2}+n} \tan\left[\frac{1}{2}(e+fx)\right]^2 \right. \right. \\
 & \left( 8 \Gamma\left[\frac{5}{2}+n\right] \text{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2 \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \left. \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right]^2 + 5 \Gamma\left[\frac{3}{2}+n\right] \text{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2}, \right. \right. \\
 & \left. \left. -2 \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right]^2\right] \left(-3 + \tan\left[\frac{1}{2}(e+fx)\right]^2 + 2 \tan\left[\frac{1}{2}(e+fx)\right]^4\right) \right) \right) \Bigg) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( \left( -1 + \tan\left[\frac{1}{2}(e+fx)\right] \right)^2 \left( 8 \Gamma\left[\frac{5}{2}+n\right] \sec\left[\frac{1}{2}(e+fx)\right]^4 \tan\left[\frac{1}{2}(e+fx)\right]^2 \right. \right. \\
 & \quad \left. \left( 7 \cos[e+fx] (-5-2n+2(1+n) \cos[e+fx]) \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2 \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 + \right. \right. \\
 & \quad \left. \left. 8(5+2n) \operatorname{Hypergeometric2F1}\left[3, \frac{7}{2}+n, \frac{9}{2}, -2 \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right]^2\right] \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) + 7 \Gamma\left[\frac{3}{2}+n\right] \left( -1 + \tan\left[\frac{1}{2}(e+fx)\right] \right)^2 \right) \\
 & \quad \left( \frac{5}{2} \cos[e+fx] (-15-9n+(9+8n) \cos[e+fx] + n \cos[2(e+fx)]) \right) \\
 & \quad \operatorname{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2}, -2 \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right]^2\right] \\
 & \quad \left. \left. \sec\left[\frac{1}{2}(e+fx)\right]^6 + 2(3+2n)(5+\cos[e+fx]) \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2 \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^4 \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \right) \right) + \\
 & \left( 14 \left( -\frac{3}{2}+n \right) \left( \sec\left[\frac{1}{2}(e+fx)\right]^2 \right)^n \left( \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \right)^{-\frac{5}{2}+n} \tan\left[\frac{1}{2}(e+fx)\right] \right. \\
 & \quad \left( 8 \Gamma\left[\frac{5}{2}+n\right] \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2 \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \quad \left. \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right]^2 + 5 \Gamma\left[\frac{3}{2}+n\right] \operatorname{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2}, -2 \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \quad \left. \left. -3 + \tan\left[\frac{1}{2}(e+fx)\right]^2 + 2 \tan\left[\frac{1}{2}(e+fx)\right]^4 \right) \right) \\
 & \quad \left( -\cos\left[\frac{1}{2}(e+fx)\right] \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right] + \right. \\
 & \quad \left. \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \tan[e+fx] \right) \Big/ \\
 & \left( \left( -1 + \tan\left[\frac{1}{2}(e+fx)\right] \right)^2 \left( 8 \Gamma\left[\frac{5}{2}+n\right] \sec\left[\frac{1}{2}(e+fx)\right]^4 \tan\left[\frac{1}{2}(e+fx)\right]^2 \right. \right. \\
 & \quad \left. \left( 7 \cos[e+fx] (-5-2n+2(1+n) \cos[e+fx]) \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2 \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 + \right. \right. \\
 & \quad \left. \left. 8(5+2n) \operatorname{Hypergeometric2F1}\left[3, \frac{7}{2}+n, \frac{9}{2}, -2 \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right]^2\right] \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) + 7 \Gamma\left[\frac{3}{2}+n\right] \left( -1 + \tan\left[\frac{1}{2}(e+fx)\right] \right)^2 \right) \\
 & \quad \left( \frac{5}{2} \cos[e+fx] (-15-9n+(9+8n) \cos[e+fx] + n \cos[2(e+fx)]) \right) \\
 & \quad \operatorname{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2}, -2 \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right]^2\right] \\
 & \quad \left. \left. \sec\left[\frac{1}{2}(e+fx)\right]^6 + 2(3+2n)(5+\cos[e+fx]) \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2 \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^4 \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left. \left. \left. \left. \frac{7}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^4 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right)\right)\right) + \right. \\
 & \left( 14 \left( \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \right)^n \left( \operatorname{Cos}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Sec}[e+fx] \right)^{-\frac{3}{2}+n} \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \right. \right. \\
 & \left. \left( 8 \operatorname{Gamma}\left[\frac{5}{2}+n\right] \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \\
 & \left. \left. \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^4 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] + 8 \operatorname{Gamma}\left[\frac{5}{2}+n\right] \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \right. \right. \right. \\
 & \left. \left. \left. \frac{7}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^3 + \right. \right. \right. \\
 & \left. \left. 5 \operatorname{Gamma}\left[\frac{3}{2}+n\right] \operatorname{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \\
 & \left. \left. \left( \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] + 4 \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^3 \right) + \right. \right. \\
 & \left. \left. \frac{32}{7} \left(\frac{5}{2}+n\right) \operatorname{Gamma}\left[\frac{5}{2}+n\right] \operatorname{Hypergeometric2F1}\left[3, \frac{7}{2}+n, \frac{9}{2}, \right. \right. \right. \\
 & \left. \left. \left. -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \right. \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \left(-2 \operatorname{Cos}\left[\frac{1}{2}(e+fx)\right] \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right] - \right. \right. \right. \\
 & \left. \left. \left. 2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}[e+fx] \right) + 2 \left(\frac{3}{2}+n\right) \operatorname{Gamma}\left[\frac{3}{2}+n\right] \right. \right. \\
 & \left. \left. \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \\
 & \left. \left. \left(-3 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 + 2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^4\right) \left(-2 \operatorname{Cos}\left[\frac{1}{2}(e+fx)\right] \operatorname{Sec}[e+fx] \right. \right. \right. \\
 & \left. \left. \left. \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right] - 2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}[e+fx] \right)\right)\right)\right)\right) / \\
 & \left( \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right) \left( 8 \operatorname{Gamma}\left[\frac{5}{2}+n\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^4 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right. \right. \right. \\
 & \left. \left. \left( 7 \operatorname{Cos}[e+fx] (-5 - 2n + 2(1+n) \operatorname{Cos}[e+fx]) \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+ \right. \right. \right. \right. \\
 & \left. \left. \left. n, \frac{7}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 + \right. \right. \right. \\
 & \left. \left. 8(5+2n) \operatorname{Hypergeometric2F1}\left[3, \frac{7}{2}+n, \frac{9}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right) + 7 \operatorname{Gamma}\left[\frac{3}{2}+n\right] \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right) \right. \right. \\
 & \left. \left. \left(\frac{5}{2} \operatorname{Cos}[e+fx] (-15 - 9n + (9+8n) \operatorname{Cos}[e+fx] + n \operatorname{Cos}[2(e+fx)]) \right) \right. \right. \\
 & \left. \left. \operatorname{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \\
 & \left. \left. \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^6 + 2(3+2n)(5 + \operatorname{Cos}[e+fx]) \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \right. \right. \right. \\
 & \left. \left. \left. \frac{7}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^4 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right)\right)\right)\right) -
 \end{aligned}$$

$$\begin{aligned}
 & \left( 14 \left( \operatorname{Sec} \left[ \frac{1}{2} (e + f x) \right]^2 \right)^n \left( \operatorname{Cos} \left[ \frac{1}{2} (e + f x) \right]^2 \operatorname{Sec} [e + f x] \right)^{-\frac{3}{2}+n} \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right. \\
 & \quad \left( 8 \operatorname{Gamma} \left[ \frac{5}{2} + n \right] \operatorname{Hypergeometric2F1} \left[ 2, \frac{5}{2} + n, \frac{7}{2}, -2 \operatorname{Sec} [e + f x] \operatorname{Sin} \left[ \frac{1}{2} (e + f x) \right]^2 \right] \right. \\
 & \quad \quad \operatorname{Sec} \left[ \frac{1}{2} (e + f x) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]^2 + 5 \operatorname{Gamma} \left[ \frac{3}{2} + n \right] \operatorname{Hypergeometric2F1} \left[ 1, \frac{3}{2} + n, \frac{5}{2}, \right. \\
 & \quad \quad \left. -2 \operatorname{Sec} [e + f x] \operatorname{Sin} \left[ \frac{1}{2} (e + f x) \right]^2 \right] \left( -3 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]^2 + 2 \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]^4 \right) \left. \right) \\
 & \quad \left( 8 \operatorname{Gamma} \left[ \frac{5}{2} + n \right] \operatorname{Sec} \left[ \frac{1}{2} (e + f x) \right]^6 \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right. \\
 & \quad \left( 7 \operatorname{Cos} [e + f x] (-5 - 2n + 2(1+n) \operatorname{Cos} [e + f x]) \operatorname{Hypergeometric2F1} \left[ 2, \frac{5}{2} + \right. \right. \\
 & \quad \quad \left. \left. n, \frac{7}{2}, -2 \operatorname{Sec} [e + f x] \operatorname{Sin} \left[ \frac{1}{2} (e + f x) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (e + f x) \right]^2 + \right. \\
 & \quad \quad 8 (5 + 2n) \operatorname{Hypergeometric2F1} \left[ 3, \frac{7}{2} + n, \frac{9}{2}, -2 \operatorname{Sec} [e + f x] \operatorname{Sin} \left[ \frac{1}{2} (e + f x) \right]^2 \right] \right. \\
 & \quad \quad \left. \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]^2 \right) + 16 \operatorname{Gamma} \left[ \frac{5}{2} + n \right] \operatorname{Sec} \left[ \frac{1}{2} (e + f x) \right]^4 \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]^3 \\
 & \quad \left( 7 \operatorname{Cos} [e + f x] (-5 - 2n + 2(1+n) \operatorname{Cos} [e + f x]) \operatorname{Hypergeometric2F1} \left[ 2, \frac{5}{2} + \right. \right. \\
 & \quad \quad \left. \left. n, \frac{7}{2}, -2 \operatorname{Sec} [e + f x] \operatorname{Sin} \left[ \frac{1}{2} (e + f x) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (e + f x) \right]^2 + \right. \\
 & \quad \quad 8 (5 + 2n) \operatorname{Hypergeometric2F1} \left[ 3, \frac{7}{2} + n, \frac{9}{2}, -2 \operatorname{Sec} [e + f x] \operatorname{Sin} \left[ \frac{1}{2} (e + f x) \right]^2 \right] \right. \\
 & \quad \quad \left. \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]^2 \right) + 7 \operatorname{Gamma} \left[ \frac{3}{2} + n \right] \operatorname{Sec} \left[ \frac{1}{2} (e + f x) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \\
 & \quad \left( \frac{5}{2} \operatorname{Cos} [e + f x] (-15 - 9n + (9 + 8n) \operatorname{Cos} [e + f x] + n \operatorname{Cos} [2(e + f x)]) \right) \\
 & \quad \quad \operatorname{Hypergeometric2F1} \left[ 1, \frac{3}{2} + n, \frac{5}{2}, -2 \operatorname{Sec} [e + f x] \operatorname{Sin} \left[ \frac{1}{2} (e + f x) \right]^2 \right] \\
 & \quad \quad \operatorname{Sec} \left[ \frac{1}{2} (e + f x) \right]^6 + 2 (3 + 2n) (5 + \operatorname{Cos} [e + f x]) \operatorname{Hypergeometric2F1} \left[ 2, \frac{5}{2} + \right. \\
 & \quad \quad \left. n, \frac{7}{2}, -2 \operatorname{Sec} [e + f x] \operatorname{Sin} \left[ \frac{1}{2} (e + f x) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (e + f x) \right]^4 \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]^2 \right) + \\
 & \quad 8 \operatorname{Gamma} \left[ \frac{5}{2} + n \right] \operatorname{Sec} \left[ \frac{1}{2} (e + f x) \right]^4 \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]^2 \left( -14 (1+n) \operatorname{Cos} [e + f x] \right. \\
 & \quad \quad \operatorname{Hypergeometric2F1} \left[ 2, \frac{5}{2} + n, \frac{7}{2}, -2 \operatorname{Sec} [e + f x] \operatorname{Sin} \left[ \frac{1}{2} (e + f x) \right]^2 \right] \\
 & \quad \quad \operatorname{Sec} \left[ \frac{1}{2} (e + f x) \right]^2 \operatorname{Sin} [e + f x] - 7 (-5 - 2n + 2(1+n) \operatorname{Cos} [e + f x]) \\
 & \quad \quad \operatorname{Hypergeometric2F1} \left[ 2, \frac{5}{2} + n, \frac{7}{2}, -2 \operatorname{Sec} [e + f x] \operatorname{Sin} \left[ \frac{1}{2} (e + f x) \right]^2 \right] \\
 & \quad \quad \operatorname{Sec} \left[ \frac{1}{2} (e + f x) \right]^2 \operatorname{Sin} [e + f x] + 7 \operatorname{Cos} [e + f x] (-5 - 2n + 2(1+n) \operatorname{Cos} [e + f x]) \\
 & \quad \quad \left. \operatorname{Hypergeometric2F1} \left[ 2, \frac{5}{2} + n, \frac{7}{2}, -2 \operatorname{Sec} [e + f x] \operatorname{Sin} \left[ \frac{1}{2} (e + f x) \right]^2 \right] \right)
 \end{aligned}$$

$$\begin{aligned}
& \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \text{Tan}\left[\frac{1}{2}(e+fx)\right] + 8(5+2n) \text{Hypergeometric2F1}\left[3, \frac{7}{2} + \right. \\
& \quad \left. n, \frac{9}{2}, -2 \text{Sec}[e+fx] \text{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \text{Tan}\left[\frac{1}{2}(e+fx)\right] + \\
& 4\left(\frac{5}{2} + n\right) \text{Cos}[e+fx] (-5 - 2n + 2(1+n) \text{Cos}[e+fx]) \text{Hypergeometric2F1}\left[3, \frac{7}{2} + \right. \\
& \quad \left. n, \frac{9}{2}, -2 \text{Sec}[e+fx] \text{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \left(-2 \text{Cos}\left[\frac{1}{2}(e+fx)\right] \right. \\
& \quad \left. \text{Sec}[e+fx] \text{Sin}\left[\frac{1}{2}(e+fx)\right] - 2 \text{Sec}[e+fx] \text{Sin}\left[\frac{1}{2}(e+fx)\right]^2 \text{Tan}[e+fx]\right) + \\
& \frac{16}{3}\left(\frac{7}{2} + n\right) (5+2n) \text{Hypergeometric2F1}\left[4, \frac{9}{2} + n, \frac{11}{2}, -2 \text{Sec}[e+fx] \right. \\
& \quad \left. \text{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \left(-2 \text{Cos}\left[\frac{1}{2}(e+fx)\right] \text{Sec}[e+fx] \right. \\
& \quad \left. \text{Sin}\left[\frac{1}{2}(e+fx)\right] - 2 \text{Sec}[e+fx] \text{Sin}\left[\frac{1}{2}(e+fx)\right]^2 \text{Tan}[e+fx]\right) + \\
& 7 \text{Gamma}\left[\frac{3}{2} + n\right] \left(-1 + \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right) \left(-\frac{5}{2}(-15 - 9n + (9+8n) \text{Cos}[e+fx] + \right. \\
& \quad \left. n \text{Cos}[2(e+fx)])\right) \text{Hypergeometric2F1}\left[1, \frac{3}{2} + n, \frac{5}{2}, -2 \right. \\
& \quad \left. \text{Sec}[e+fx] \text{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(e+fx)\right]^6 \text{Sin}[e+fx] + \\
& \frac{5}{2} \text{Cos}[e+fx] \text{Hypergeometric2F1}\left[1, \frac{3}{2} + n, \frac{5}{2}, -2 \text{Sec}[e+fx] \text{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \\
& \quad \text{Sec}\left[\frac{1}{2}(e+fx)\right]^6 (- (9+8n) \text{Sin}[e+fx] - 2n \text{Sin}[2(e+fx)]) + \\
& \frac{15}{2} \text{Cos}[e+fx] (-15 - 9n + (9+8n) \text{Cos}[e+fx] + n \text{Cos}[2(e+fx)]) \\
& \quad \text{Hypergeometric2F1}\left[1, \frac{3}{2} + n, \frac{5}{2}, -2 \text{Sec}[e+fx] \text{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \\
& \quad \text{Sec}\left[\frac{1}{2}(e+fx)\right]^6 \text{Tan}\left[\frac{1}{2}(e+fx)\right] + 2(3+2n)(5 + \text{Cos}[e+fx]) \\
& \quad \text{Hypergeometric2F1}\left[2, \frac{5}{2} + n, \frac{7}{2}, -2 \text{Sec}[e+fx] \text{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \\
& \quad \text{Sec}\left[\frac{1}{2}(e+fx)\right]^6 \text{Tan}\left[\frac{1}{2}(e+fx)\right] - 2(3+2n) \text{Hypergeometric2F1}\left[2, \frac{5}{2} + n, \frac{7}{2}, -2 \right. \\
& \quad \left. \text{Sec}[e+fx] \text{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(e+fx)\right]^4 \text{Sin}[e+fx] \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2 + \\
& 4(3+2n)(5 + \text{Cos}[e+fx]) \text{Hypergeometric2F1}\left[2, \frac{5}{2} + n, \frac{7}{2}, -2 \right. \\
& \quad \left. \text{Sec}[e+fx] \text{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(e+fx)\right]^4 \text{Tan}\left[\frac{1}{2}(e+fx)\right]^3 + \\
& \left(\frac{3}{2} + n\right) \text{Cos}[e+fx] (-15 - 9n + (9+8n) \text{Cos}[e+fx] + n \text{Cos}[2(e+fx)]) \\
& \quad \text{Hypergeometric2F1}\left[2, \frac{5}{2} + n, \frac{7}{2}, -2 \text{Sec}[e+fx] \text{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right]
\end{aligned}$$

$$\begin{aligned}
 & \left( \sec \left[ \frac{1}{2} (e+fx) \right]^6 \left( -2 \cos \left[ \frac{1}{2} (e+fx) \right] \sec [e+fx] \sin \left[ \frac{1}{2} (e+fx) \right] - 2 \sec [e+fx] \sin \left[ \frac{1}{2} (e+fx) \right]^2 \tan [e+fx] \right) + \frac{8}{7} \left( \frac{5}{2} + n \right) (3+2n) (5+\cos [e+fx]) \right. \\
 & \left. \text{Hypergeometric2F1} \left[ 3, \frac{7}{2} + n, \frac{9}{2}, -2 \sec [e+fx] \sin \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right. \\
 & \left. \sec \left[ \frac{1}{2} (e+fx) \right]^4 \tan \left[ \frac{1}{2} (e+fx) \right]^2 \left( -2 \cos \left[ \frac{1}{2} (e+fx) \right] \sec [e+fx] \sin \left[ \frac{1}{2} (e+fx) \right] - 2 \sec [e+fx] \sin \left[ \frac{1}{2} (e+fx) \right]^2 \tan [e+fx] \right) \right) \Bigg) / \\
 & \left( \left( -1 + \tan \left[ \frac{1}{2} (e+fx) \right]^2 \right) \left( 8 \text{Gamma} \left[ \frac{5}{2} + n \right] \sec \left[ \frac{1}{2} (e+fx) \right]^4 \tan \left[ \frac{1}{2} (e+fx) \right]^2 \right. \right. \\
 & \left. \left( 7 \cos [e+fx] (-5-2n+2(1+n) \cos [e+fx]) \text{Hypergeometric2F1} \left[ 2, \frac{5}{2} + n, \frac{7}{2}, -2 \sec [e+fx] \sin \left[ \frac{1}{2} (e+fx) \right]^2 \right] \sec \left[ \frac{1}{2} (e+fx) \right]^2 + 8(5+2n) \right. \right. \\
 & \left. \left. \text{Hypergeometric2F1} \left[ 3, \frac{7}{2} + n, \frac{9}{2}, -2 \sec [e+fx] \sin \left[ \frac{1}{2} (e+fx) \right]^2 \right] \tan \left[ \frac{1}{2} (e+fx) \right]^2 \right) + 7 \text{Gamma} \left[ \frac{3}{2} + n \right] \left( -1 + \tan \left[ \frac{1}{2} (e+fx) \right]^2 \right) \right) \right. \\
 & \left. \left( \frac{5}{2} \cos [e+fx] (-15-9n+(9+8n) \cos [e+fx] + n \cos [2(e+fx)]) \right) \right. \\
 & \left. \text{Hypergeometric2F1} \left[ 1, \frac{3}{2} + n, \frac{5}{2}, -2 \sec [e+fx] \sin \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right. \\
 & \left. \sec \left[ \frac{1}{2} (e+fx) \right]^6 + 2(3+2n)(5+\cos [e+fx]) \text{Hypergeometric2F1} \left[ 2, \frac{5}{2} + n, \frac{7}{2}, -2 \sec [e+fx] \sin \left[ \frac{1}{2} (e+fx) \right]^2 \right] \sec \left[ \frac{1}{2} (e+fx) \right]^4 \tan \left[ \frac{1}{2} (e+fx) \right]^2 \right) \Bigg) \Bigg)
 \end{aligned}$$

**Problem 313: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int (-\sec [e+fx])^n \sqrt{a+a \sec [e+fx]} dx$$

Optimal (type 5, 70 leaves, 3 steps):

$$\left( 2 a \text{Hypergeometric2F1} \left[ \frac{1}{2}, 1-n, \frac{3}{2}, 1-\sec [e+fx] \right] \right. \\
 \left. (-\sec [e+fx])^n \sec [e+fx]^{1-n} \sin [e+fx] \right) / \left( f \sqrt{a+a \sec [e+fx]} \right)$$

Result (type 5, 215 leaves):

$$\begin{aligned}
 & -\frac{1}{f n (1+n)} i^{2^{-\frac{1}{2}+n}} e^{\frac{1}{2} i (e+fx)} (1 + e^{2 i (e+fx)})^{-\frac{1}{2}+n} (e^{-i (e+fx)} (1 + e^{2 i (e+fx)}))^{\frac{1}{2}-n} \\
 & \cos [e + f x]^{\frac{1}{2}+n} \left( (1+n) \operatorname{Hypergeometric2F1}\left[\frac{n}{2}, \frac{1}{2} + n, \frac{2+n}{2}, -e^{2 i (e+fx)}\right] + \right. \\
 & \quad \left. e^{i (e+fx)} n \operatorname{Hypergeometric2F1}\left[\frac{1}{2} + n, \frac{1+n}{2}, \frac{3+n}{2}, -e^{2 i (e+fx)}\right] \right) \\
 & \operatorname{Sec}\left[\frac{1}{2} (e + f x)\right] (-\operatorname{Sec}[e + f x])^n \sqrt{a (1 + \operatorname{Sec}[e + f x])}
 \end{aligned}$$

**Problem 314: Result more than twice size of optimal antiderivative.**

$$\int \frac{(-\operatorname{Sec}[e + f x])^n}{\sqrt{a + a \operatorname{Sec}[e + f x]}} dx$$

Optimal (type 6, 75 leaves, 3 steps):

$$\begin{aligned}
 & -\left( \left( \operatorname{AppellF1}\left[n, \frac{1}{2}, 1, 1+n, \operatorname{Sec}[e + f x], -\operatorname{Sec}[e + f x]\right] (-\operatorname{Sec}[e + f x])^n \operatorname{Tan}[e + f x] \right) / \right. \\
 & \quad \left. (f n \sqrt{1 - \operatorname{Sec}[e + f x]} \sqrt{a + a \operatorname{Sec}[e + f x]}) \right)
 \end{aligned}$$

Result (type 6, 2977 leaves):

$$\begin{aligned}
 & \left( 3 \sqrt{2} \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2} + n, 1 - n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]^2\right] \left(\operatorname{Sec}\left[\frac{1}{2} (e + f x)\right]^2\right)^n \right. \\
 & \quad \left. (-\operatorname{Sec}[e + f x])^n \operatorname{Sec}[e + f x]^{-\frac{1}{2}-n+\frac{1}{2}(-1+2n)} \left(\cos\left[\frac{1}{2} (e + f x)\right]^2 \operatorname{Sec}[e + f x]\right)^n \right. \\
 & \quad \left. \sqrt{1 + \operatorname{Sec}[e + f x]} \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right] \right) / \left( f \sqrt{a (1 + \operatorname{Sec}[e + f x])} \right) \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2} + n, 1 - n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]^2\right] + \right. \\
 & \quad \left( 2 (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2} + n, 2 - n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]^2\right] + \right. \\
 & \quad \left. (-1+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2} + n, 1 - n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]^2\right] \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]^2 \right) \\
 & \left( \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2} + n, 1 - n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]^2\right] \cos[e + f x] \right. \right. \\
 & \quad \left. \left. \left(\operatorname{Sec}\left[\frac{1}{2} (e + f x)\right]^2\right)^{1+n} \left(\cos\left[\frac{1}{2} (e + f x)\right]^2 \operatorname{Sec}[e + f x]\right)^n \sqrt{1 + \operatorname{Sec}[e + f x]} \right) / \right. \\
 & \quad \left( \sqrt{2} \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2} + n, 1 - n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]^2\right] + \right. \right. \\
 & \quad \left( 2 (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2} + n, 2 - n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]^2\right] + \right. \\
 & \quad \left. \left. (-1+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2} + n, 1 - n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]^2\right] \right) \right)
 \end{aligned}$$



$$\begin{aligned}
& \left. \tan\left[\frac{1}{2}(e+fx)\right]^2\right) - \left(3\sqrt{2} \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, 1-n, \frac{3}{2}, \right.\right. \\
& \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \left(\sec\left[\frac{1}{2}(e+fx)\right]^2\right)^n \right. \\
& \left. \left(\cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx]\right)^n \sqrt{1+\sec[e+fx]} \sin[e+fx] \tan\left[\frac{1}{2}(e+fx)\right]\right) / \\
& \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
& \left. \left(2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right.\right. \\
& \left. \left. (-1+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right]\right) \right. \\
& \left. \tan\left[\frac{1}{2}(e+fx)\right]^2\right) + \left(3\sqrt{2} n \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right.\right. \\
& \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \cos[e+fx] \left(\sec\left[\frac{1}{2}(e+fx)\right]^2\right)^n \right. \\
& \left. \left(\cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx]\right)^n \sqrt{1+\sec[e+fx]} \tan\left[\frac{1}{2}(e+fx)\right]^2\right) / \\
& \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
& \left. \left(2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right.\right. \\
& \left. \left. (-1+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right]\right) \right. \\
& \left. \tan\left[\frac{1}{2}(e+fx)\right]^2\right) + \left(3\sqrt{2} \cos[e+fx] \left(\sec\left[\frac{1}{2}(e+fx)\right]^2\right)^n \right. \\
& \left. \left(\cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx]\right)^n \sqrt{1+\sec[e+fx]} \tan\left[\frac{1}{2}(e+fx)\right]\right) \\
& \left(-\frac{1}{3}(1-n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
& \left. \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \frac{1}{3}\left(-\frac{1}{2}+n\right) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+n, 1-n, \frac{5}{2}, \right.\right. \\
& \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right]\right) / \\
& \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
& \left. \left(2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right.\right. \\
& \left. \left. (-1+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right]\right) \right. \\
& \left. \tan\left[\frac{1}{2}(e+fx)\right]^2\right) - \left(3\sqrt{2} \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right.\right. \\
& \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \cos[e+fx] \left(\sec\left[\frac{1}{2}(e+fx)\right]^2\right)^n \right. \\
& \left. \left(\cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx]\right)^n \sqrt{1+\sec[e+fx]} \tan\left[\frac{1}{2}(e+fx)\right]\right)
\end{aligned}$$

$$\begin{aligned}
 & \left( \left( 2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 2-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. (-1+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+n, 1-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] + \right. \\
 & \quad 3 \left( -\frac{1}{3}(1-n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 2-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \quad \quad \left. \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] + \frac{1}{3}\left(-\frac{1}{2}+n\right) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+n, 1-n, \frac{5}{2}, \right. \right. \\
 & \quad \quad \left. \left. \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \right) + \right. \\
 & \quad \left. \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \left( 2(-1+n) \left( -\frac{3}{5}(2-n) \operatorname{AppellF1}\left[\frac{5}{2}, -\frac{1}{2}+n, 3-n, \frac{7}{2}, \right. \right. \right. \right. \\
 & \quad \quad \left. \left. \left. \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] + \frac{3}{5} \right. \right. \right. \\
 & \quad \quad \left. \left. \left( -\frac{1}{2}+n \right) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{2}+n, 2-n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \\
 & \quad \quad \left. \left. \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \right) + (-1+2n) \left( -\frac{3}{5}(1-n) \operatorname{AppellF1}\left[\frac{5}{2}, \right. \right. \right. \\
 & \quad \quad \left. \left. \frac{1}{2}+n, 2-n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \right. \right. \\
 & \quad \quad \left. \left. \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] + \frac{3}{5}\left(\frac{1}{2}+n\right) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{3}{2}+n, 1-n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \\
 & \quad \quad \left. \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \right) \right) \right) \Big/ \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, 1-n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left( 2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 2-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \quad \left. (-1+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+n, 1-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \Big) + \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, 1-n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \quad \left. \left( \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \right)^n \left( \operatorname{Cos}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Sec}[e+fx] \right)^n \right. \\
 & \quad \left. \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \operatorname{Tan}[e+fx] \right) \Big/ \left( \sqrt{2} \sqrt{1+\operatorname{Sec}[e+fx]} \right) \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, 1-n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left( 2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 2-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \quad \left. (-1+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+n, 1-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \right) \Big/ \left( \sqrt{2} \sqrt{1+\operatorname{Sec}[e+fx]} \right)
 \end{aligned}$$

$$\begin{aligned}
 & -\tan\left[\frac{1}{2}(e+fx)\right]^2\right)\tan\left[\frac{1}{2}(e+fx)\right]^2\right)\Bigg)+ \\
 & \left(3\sqrt{2}n\operatorname{AppellF1}\left[\frac{1}{2},-\frac{1}{2}+n,1-n,\frac{3}{2},\tan\left[\frac{1}{2}(e+fx)\right]^2,-\tan\left[\frac{1}{2}(e+fx)\right]^2\right]\right. \right. \\
 & \left.\left.\cos[e+fx]\left(\sec\left[\frac{1}{2}(e+fx)\right]^2\right)^n\left(\cos\left[\frac{1}{2}(e+fx)\right]^2\sec[e+fx]\right)^{-1+n}\right.\right. \right. \\
 & \left.\left.\sqrt{1+\sec[e+fx]}\tan\left[\frac{1}{2}(e+fx)\right]\left(-\cos\left[\frac{1}{2}(e+fx)\right]\sec[e+fx]\sin\left[\frac{1}{2}(e+fx)\right]+ \right.\right. \right. \\
 & \left.\left.\left.\cos\left[\frac{1}{2}(e+fx)\right]^2\sec[e+fx]\tan[e+fx]\right)\right]\right)\Bigg)/ \\
 & \left(3\operatorname{AppellF1}\left[\frac{1}{2},-\frac{1}{2}+n,1-n,\frac{3}{2},\tan\left[\frac{1}{2}(e+fx)\right]^2,-\tan\left[\frac{1}{2}(e+fx)\right]^2\right]+ \right. \\
 & \left(2(-1+n)\operatorname{AppellF1}\left[\frac{3}{2},-\frac{1}{2}+n,2-n,\frac{5}{2},\tan\left[\frac{1}{2}(e+fx)\right]^2,-\tan\left[\frac{1}{2}(e+fx)\right]^2\right]+ \right. \\
 & \left.(-1+2n)\operatorname{AppellF1}\left[\frac{3}{2},\frac{1}{2}+n,1-n,\frac{5}{2},\tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \left.\left.-\tan\left[\frac{1}{2}(e+fx)\right]^2\right)\tan\left[\frac{1}{2}(e+fx)\right]^2\right)\right)\Bigg)
 \end{aligned}$$

### Problem 315: Result more than twice size of optimal antiderivative.

$$\int \frac{(-\sec[e+fx])^n}{(a+a\sec[e+fx])^{3/2}} dx$$

Optimal (type 6, 78 leaves, 3 steps):

$$-\left(\left(\operatorname{AppellF1}\left[n,\frac{1}{2},2,1+n,\sec[e+fx],-\sec[e+fx]\right](-\sec[e+fx])^n\tan[e+fx]\right)\Bigg)/\left(afn\sqrt{1-\sec[e+fx]}\sqrt{a+a\sec[e+fx]}\right)$$

Result (type 6, 3005 leaves):

$$\begin{aligned}
 & \left(6\operatorname{AppellF1}\left[\frac{1}{2},-\frac{3}{2}+n,1-n,\frac{3}{2},\tan\left[\frac{1}{2}(e+fx)\right]^2,-\tan\left[\frac{1}{2}(e+fx)\right]^2\right]\left(\sec\left[\frac{1}{2}(e+fx)\right]^2\right)^n \right. \\
 & \left.(-\sec[e+fx])^n\sec[e+fx]^{\frac{1}{2}-n+\frac{1}{2}(-3+2n)}\left(\cos\left[\frac{1}{2}(e+fx)\right]^2\sec[e+fx]\right)^{\frac{3}{2}+n}\right. \\
 & \left.\tan\left[\frac{1}{2}(e+fx)\right]\left(-1+\tan\left[\frac{1}{2}(e+fx)\right]^2\right)^2\right)\Bigg)/\left(f(a(1+\sec[e+fx]))^{3/2}\right) \\
 & \left(3\operatorname{AppellF1}\left[\frac{1}{2},-\frac{3}{2}+n,1-n,\frac{3}{2},\tan\left[\frac{1}{2}(e+fx)\right]^2,-\tan\left[\frac{1}{2}(e+fx)\right]^2\right]+ \right. \\
 & \left(2(-1+n)\operatorname{AppellF1}\left[\frac{3}{2},-\frac{3}{2}+n,2-n,\frac{5}{2},\tan\left[\frac{1}{2}(e+fx)\right]^2,-\tan\left[\frac{1}{2}(e+fx)\right]^2\right]+ \right. \\
 & \left.(-3+2n)\operatorname{AppellF1}\left[\frac{3}{2},-\frac{1}{2}+n,1-n,\frac{5}{2},\tan\left[\frac{1}{2}(e+fx)\right]^2,-\tan\left[\frac{1}{2}(e+fx)\right]^2\right]\right) \\
 & \left.\tan\left[\frac{1}{2}(e+fx)\right]^2\right)\Bigg)\left(\left(12\operatorname{AppellF1}\left[\frac{1}{2},-\frac{3}{2}+n,1-n,\frac{3}{2},\tan\left[\frac{1}{2}(e+fx)\right]^2, \right.\right.\right.
 \end{aligned}$$

$$\begin{aligned}
 & -\tan\left[\frac{1}{2}(e+fx)\right]^2 \cos[e+fx] \left(\sec\left[\frac{1}{2}(e+fx)\right]^2\right)^{1+n} \\
 & \left(\cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx]\right)^{\frac{3+n}{2}} \tan\left[\frac{1}{2}(e+fx)\right]^2 \left(-1+\tan\left[\frac{1}{2}(e+fx)\right]^2\right) \Big/ \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \left(2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{3}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \left. (-3+2n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right]\right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \Big) + \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \cos[e+fx] \right. \\
 & \left. \left(\sec\left[\frac{1}{2}(e+fx)\right]^2\right)^{1+n} \left(\cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx]\right)^{\frac{3+n}{2}} \left(-1+\tan\left[\frac{1}{2}(e+fx)\right]^2\right)^2\right) \Big/ \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \left(2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{3}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \left. (-3+2n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right]\right) \\
 & \tan\left[\frac{1}{2}(e+fx)\right]^2 \Big) - \left(6 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \left(\sec\left[\frac{1}{2}(e+fx)\right]^2\right)^n \left(\cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx]\right)^{\frac{3+n}{2}} \right. \\
 & \left. \sin[e+fx] \tan\left[\frac{1}{2}(e+fx)\right] \left(-1+\tan\left[\frac{1}{2}(e+fx)\right]^2\right)^2\right) \Big/ \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \left(2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{3}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \left. (-3+2n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right]\right) \\
 & \tan\left[\frac{1}{2}(e+fx)\right]^2 \Big) + \left(6n \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \cos[e+fx] \left(\sec\left[\frac{1}{2}(e+fx)\right]^2\right)^n \right. \\
 & \left. \left(\cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx]\right)^{\frac{3+n}{2}} \tan\left[\frac{1}{2}(e+fx)\right]^2 \left(-1+\tan\left[\frac{1}{2}(e+fx)\right]^2\right)^2\right) \Big/ \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( 2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{3}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left. (-3+2n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \\
 & \tan\left[\frac{1}{2}(e+fx)\right]^2 \left( 6 \cos[e+fx] \left( \sec\left[\frac{1}{2}(e+fx)\right]^2 \right)^n \right. \\
 & \quad \left( \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \right)^{\frac{3}{2}+n} \tan\left[\frac{1}{2}(e+fx)\right] \left( -\frac{1}{3}(1-n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{3}{2}+n, \right. \right. \\
 & \quad \left. \left. 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \right. \\
 & \quad \left. \frac{1}{3}\left(-\frac{3}{2}+n\right) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \quad \left. \left. \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) \left( -1 + \tan\left[\frac{1}{2}(e+fx)\right]^2 \right)^2 \right) / \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left( 2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{3}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left. (-3+2n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \\
 & \tan\left[\frac{1}{2}(e+fx)\right]^2 \left( 6 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \cos[e+fx] \left( \sec\left[\frac{1}{2}(e+fx)\right]^2 \right)^n \right. \\
 & \quad \left( \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \right)^{\frac{3}{2}+n} \tan\left[\frac{1}{2}(e+fx)\right] \left( -1 + \tan\left[\frac{1}{2}(e+fx)\right]^2 \right)^2 \right) \\
 & \left( \left( 2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{3}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. (-3+2n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \right. \\
 & \quad \left. \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + 3 \left( -\frac{1}{3}(1-n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{3}{2}+n, 2-n, \right. \right. \right. \\
 & \quad \left. \left. \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \right. \right. \\
 & \quad \left. \left. \frac{1}{3}\left(-\frac{3}{2}+n\right) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \right. \\
 & \quad \left. \left. \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) + \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \\
 & \left( 2(-1+n) \left( -\frac{3}{5}(2-n) \operatorname{AppellF1}\left[\frac{5}{2}, -\frac{3}{2}+n, 3-n, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \frac{3}{5}\left(-\frac{3}{2}+n\right) \right. \\
 & \quad \left. \left. \operatorname{AppellF1}\left[\frac{5}{2}, -\frac{1}{2}+n, 2-n, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) + (-3+2n) \left( -\frac{3}{5}(1-n) \operatorname{AppellF1}\left[\frac{5}{2}, \right. \right. \\
 & \quad \left. \left. -\frac{1}{2}+n, 2-n, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \right. \\
 & \quad \left. \tan\left[\frac{1}{2}(e+fx)\right] + \frac{3}{5}\left(-\frac{1}{2}+n\right) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{2}+n, 1-n, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) \right) \Big/ \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left( 2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{3}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left. (-3+2n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) + \right. \\
 & \left. \left( 6\left(\frac{3}{2}+n\right) \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \\
 & \quad \left. \left. \cos[e+fx] \left( \sec\left[\frac{1}{2}(e+fx)\right]^2 \right)^n \left( \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \right)^{\frac{1}{2}+n} \tan\left[\frac{1}{2}(e+fx)\right] \right. \right. \\
 & \quad \left. \left. \left( -1 + \tan\left[\frac{1}{2}(e+fx)\right]^2 \right)^2 \left( -\cos\left[\frac{1}{2}(e+fx)\right] \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right] + \right. \right. \right. \\
 & \quad \left. \left. \left. \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \tan[e+fx] \right) \right) \right) \Big/ \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left( 2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{3}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left. (-3+2n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \right) \Big)
 \end{aligned}$$

**Problem 316: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int (d \operatorname{Sec}[e+fx])^n (a+a \operatorname{Sec}[e+fx])^{3/2} dx$$

Optimal (type 5, 130 leaves, 5 steps):

$$\left( 2 a^2 (1+4 n) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, 1-n, \frac{3}{2}, 1-\operatorname{Sec}[e+f x]\right] \operatorname{Sec}[e+f x]^{1-n} (d \operatorname{Sec}[e+f x])^n \right. \\ \left. \operatorname{Sin}[e+f x] \right) / \left( f (1+2 n) \sqrt{a+a \operatorname{Sec}[e+f x]} \right) + \frac{2 a^2 (d \operatorname{Sec}[e+f x])^n \operatorname{Tan}[e+f x]}{f (1+2 n) \sqrt{a+a \operatorname{Sec}[e+f x]}}$$

Result (type 5, 6383 leaves):

$$\left( 14 \operatorname{Sec}\left[\frac{1}{2}(e+f x)\right]^3 \left(\operatorname{Sec}\left[\frac{1}{2}(e+f x)\right]^2\right)^n \right. \\ \operatorname{Sec}[e+f x]^{-\frac{3}{2}-n} (d \operatorname{Sec}[e+f x])^n \left(\operatorname{Cos}\left[\frac{1}{2}(e+f x)\right]^2 \operatorname{Sec}[e+f x]\right)^{-\frac{3}{2}+n} \\ (a(1+\operatorname{Sec}[e+f x]))^{3/2} \left(\operatorname{Cos}\left[\frac{3}{2}(e+f x)\right] \left(\frac{1}{8} \operatorname{Sec}[e+f x]^{-\frac{3}{2}+n} + \frac{3}{8} \operatorname{Sec}[e+f x]^{\frac{1}{2}+n} + \right. \right. \\ \left. \frac{3}{4} i \operatorname{Sec}[e+f x]^{\frac{1}{2}+n} \operatorname{Sin}[e+f x] - \frac{3}{8} \operatorname{Sec}[e+f x]^{\frac{1}{2}+n} \operatorname{Sin}[e+f x]^2 + \right. \\ \left. \operatorname{Cos}[e+f x] \left(\frac{3}{8} \operatorname{Sec}[e+f x]^{\frac{1}{2}+n} + \frac{3}{8} i \operatorname{Sec}[e+f x]^{\frac{1}{2}+n} \operatorname{Sin}[e+f x]\right) + \right. \\ \left. \operatorname{Sec}[e+f x] \left(\frac{1}{8} \operatorname{Sec}[e+f x]^{\frac{1}{2}+n} + \frac{3}{8} i \operatorname{Sec}[e+f x]^{\frac{1}{2}+n} \operatorname{Sin}[e+f x] - \right. \right. \\ \left. \left. \frac{3}{8} \operatorname{Sec}[e+f x]^{\frac{1}{2}+n} \operatorname{Sin}[e+f x]^2 - \frac{1}{8} i \operatorname{Sec}[e+f x]^{\frac{1}{2}+n} \operatorname{Sin}[e+f x]^3\right)\right) - \\ \frac{1}{8} i \operatorname{Sec}[e+f x]^{-\frac{3}{2}+n} \operatorname{Sin}\left[\frac{3}{2}(e+f x)\right] - \frac{3}{8} i \operatorname{Sec}[e+f x]^{\frac{1}{2}+n} \operatorname{Sin}\left[\frac{3}{2}(e+f x)\right] + \\ \frac{3}{4} \operatorname{Sec}[e+f x]^{\frac{1}{2}+n} \operatorname{Sin}[e+f x] \operatorname{Sin}\left[\frac{3}{2}(e+f x)\right] + \\ \left. \frac{3}{8} i \operatorname{Sec}[e+f x]^{\frac{1}{2}+n} \operatorname{Sin}[e+f x]^2 \operatorname{Sin}\left[\frac{3}{2}(e+f x)\right] + \operatorname{Cos}[e+f x] \right) \\ \left(-\frac{3}{8} i \operatorname{Sec}[e+f x]^{\frac{1}{2}+n} \operatorname{Sin}\left[\frac{3}{2}(e+f x)\right] + \frac{3}{8} \operatorname{Sec}[e+f x]^{\frac{1}{2}+n} \operatorname{Sin}[e+f x] \operatorname{Sin}\left[\frac{3}{2}(e+f x)\right]\right) + \\ \operatorname{Sec}[e+f x] \left(-\frac{1}{8} i \operatorname{Sec}[e+f x]^{\frac{1}{2}+n} \operatorname{Sin}\left[\frac{3}{2}(e+f x)\right] + \frac{3}{8} \operatorname{Sec}[e+f x]^{\frac{1}{2}+n} \operatorname{Sin}[e+f x] \right. \\ \left. \operatorname{Sin}\left[\frac{3}{2}(e+f x)\right] + \frac{3}{8} i \operatorname{Sec}[e+f x]^{\frac{1}{2}+n} \operatorname{Sin}[e+f x]^2 \operatorname{Sin}\left[\frac{3}{2}(e+f x)\right] - \right. \\ \left. \frac{1}{8} \operatorname{Sec}[e+f x]^{\frac{1}{2}+n} \operatorname{Sin}[e+f x]^3 \operatorname{Sin}\left[\frac{3}{2}(e+f x)\right]\right) \left. \right) \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right] \\ \left( 8 \operatorname{Gamma}\left[\frac{5}{2}+n\right] \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2 \operatorname{Sec}[e+f x] \operatorname{Sin}\left[\frac{1}{2}(e+f x)\right]^2\right] \right. \\ \operatorname{Sec}\left[\frac{1}{2}(e+f x)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^2 + \\ 5 \operatorname{Gamma}\left[\frac{3}{2}+n\right] \operatorname{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2}, -2 \operatorname{Sec}[e+f x] \operatorname{Sin}\left[\frac{1}{2}(e+f x)\right]^2\right] \\ \left. \left(-3 + \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^2 + 2 \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^4\right) \right) \right) / \\ \left( f \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^2\right) \left( 8 \operatorname{Gamma}\left[\frac{5}{2}+n\right] \operatorname{Sec}\left[\frac{1}{2}(e+f x)\right]^4 \operatorname{Tan}\left[\frac{1}{2}(e+f x)\right]^2 \right. \right.$$

$$\begin{aligned}
 & \left( 7 \cos [e+f x] (-5-2 n+2(1+n) \cos [e+f x]) \right. \\
 & \quad \text{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2 \sec [e+f x] \sin \left[\frac{1}{2}(e+f x)\right]^2\right] \sec \left[\frac{1}{2}(e+f x)\right]^2 + \\
 & \quad 8(5+2 n) \text{Hypergeometric2F1}\left[3, \frac{7}{2}+n, \frac{9}{2}, -2 \sec [e+f x] \sin \left[\frac{1}{2}(e+f x)\right]^2\right] \\
 & \quad \tan \left[\frac{1}{2}(e+f x)\right]^2\right) + 7 \Gamma\left[\frac{3}{2}+n\right] \left(-1+\tan \left[\frac{1}{2}(e+f x)\right]^2\right) \\
 & \left(\frac{5}{2} \cos [e+f x] (-15-9 n+(9+8 n) \cos [e+f x]+n \cos [2(e+f x)])\right) \\
 & \quad \text{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2}, -2 \sec [e+f x] \sin \left[\frac{1}{2}(e+f x)\right]^2\right] \sec \left[\frac{1}{2}(e+f x)\right]^6 + \\
 & \quad 2(3+2 n)(5+\cos [e+f x]) \text{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, \right. \\
 & \quad \left. -2 \sec [e+f x] \sin \left[\frac{1}{2}(e+f x)\right]^2\right] \sec \left[\frac{1}{2}(e+f x)\right]^4 \tan \left[\frac{1}{2}(e+f x)\right]^2\right) \\
 & \left(-\left(\left(14\left(\sec \left[\frac{1}{2}(e+f x)\right]^2\right)^{1+n}\left(\cos \left[\frac{1}{2}(e+f x)\right]^2 \sec [e+f x]\right)^{-\frac{3}{2}+n} \tan \left[\frac{1}{2}(e+f x)\right]^2\right.\right.\right. \\
 & \quad \left.\left.\left(8 \Gamma\left[\frac{5}{2}+n\right] \text{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2 \sec [e+f x] \sin \left[\frac{1}{2}(e+f x)\right]^2\right] \right.\right.\right. \\
 & \quad \left.\left.\sec \left[\frac{1}{2}(e+f x)\right]^2 \tan \left[\frac{1}{2}(e+f x)\right]^2 +\right.\right. \\
 & \quad \left.\left.5 \Gamma\left[\frac{3}{2}+n\right] \text{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2}, -2 \sec [e+f x] \sin \left[\frac{1}{2}(e+f x)\right]^2\right] \right.\right. \\
 & \quad \left.\left.\left(-3+\tan \left[\frac{1}{2}(e+f x)\right]^2+2 \tan \left[\frac{1}{2}(e+f x)\right]^4\right)\right)\right)\right) / \\
 & \left(\left(-1+\tan \left[\frac{1}{2}(e+f x)\right]^2\right)^2\left(8 \Gamma\left[\frac{5}{2}+n\right] \sec \left[\frac{1}{2}(e+f x)\right]^4 \tan \left[\frac{1}{2}(e+f x)\right]^2\right.\right. \\
 & \quad \left.\left(7 \cos [e+f x] (-5-2 n+2(1+n) \cos [e+f x]) \text{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \right.\right. \\
 & \quad \left.\left.\frac{7}{2}, -2 \sec [e+f x] \sin \left[\frac{1}{2}(e+f x)\right]^2\right] \sec \left[\frac{1}{2}(e+f x)\right]^2 + 8(5+2 n) \right.\right. \\
 & \quad \left.\left.\text{Hypergeometric2F1}\left[3, \frac{7}{2}+n, \frac{9}{2}, -2 \sec [e+f x] \sin \left[\frac{1}{2}(e+f x)\right]^2\right] \right.\right. \\
 & \quad \left.\left.\tan \left[\frac{1}{2}(e+f x)\right]^2\right) + 7 \Gamma\left[\frac{3}{2}+n\right] \left(-1+\tan \left[\frac{1}{2}(e+f x)\right]^2\right)\right.\right. \\
 & \quad \left.\left(\frac{5}{2} \cos [e+f x] (-15-9 n+(9+8 n) \cos [e+f x]+n \cos [2(e+f x)])\right)\right. \\
 & \quad \left.\text{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2}, -2 \sec [e+f x] \sin \left[\frac{1}{2}(e+f x)\right]^2\right] \right.\right. \\
 & \quad \left.\left.\sec \left[\frac{1}{2}(e+f x)\right]^6 + 2(3+2 n)(5+\cos [e+f x]) \text{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, \right.\right. \\
 & \quad \left.\left.-2 \sec [e+f x] \sin \left[\frac{1}{2}(e+f x)\right]^2\right] \sec \left[\frac{1}{2}(e+f x)\right]^4 \tan \left[\frac{1}{2}(e+f x)\right]^2\right)\right)\right) +
 \end{aligned}$$



$$\begin{aligned}
 & \left( 7 \left( \sec \left[ \frac{1}{2} (e + f x) \right] \right)^{1+n} \left( \cos \left[ \frac{1}{2} (e + f x) \right] \right)^2 \sec [e + f x] \right)^{-\frac{3}{2}+n} \\
 & \left( 8 \operatorname{Gamma} \left[ \frac{5}{2} + n \right] \operatorname{Hypergeometric2F1} \left[ 2, \frac{5}{2} + n, \frac{7}{2}, -2 \sec [e + f x] \sin \left[ \frac{1}{2} (e + f x) \right] \right]^2 \right. \\
 & \quad \sec \left[ \frac{1}{2} (e + f x) \right]^2 \tan \left[ \frac{1}{2} (e + f x) \right]^2 + 5 \operatorname{Gamma} \left[ \frac{3}{2} + n \right] \operatorname{Hypergeometric2F1} \left[ 1, \frac{3}{2} + n, \frac{5}{2}, \right. \\
 & \quad \left. \left. -2 \sec [e + f x] \sin \left[ \frac{1}{2} (e + f x) \right] \right]^2 \left( -3 + \tan \left[ \frac{1}{2} (e + f x) \right]^2 + 2 \tan \left[ \frac{1}{2} (e + f x) \right]^4 \right) \right) \Bigg) / \\
 & \left( \left( -1 + \tan \left[ \frac{1}{2} (e + f x) \right] \right)^2 \right) \left( 8 \operatorname{Gamma} \left[ \frac{5}{2} + n \right] \sec \left[ \frac{1}{2} (e + f x) \right]^4 \tan \left[ \frac{1}{2} (e + f x) \right]^2 \right. \\
 & \quad \left( 7 \cos [e + f x] (-5 - 2n + 2(1+n) \cos [e + f x]) \operatorname{Hypergeometric2F1} \left[ 2, \frac{5}{2} + \right. \right. \\
 & \quad \left. \left. n, \frac{7}{2}, -2 \sec [e + f x] \sin \left[ \frac{1}{2} (e + f x) \right] \right]^2 \right) \sec \left[ \frac{1}{2} (e + f x) \right]^2 + \right. \\
 & \quad \left. 8(5+2n) \operatorname{Hypergeometric2F1} \left[ 3, \frac{7}{2} + n, \frac{9}{2}, -2 \sec [e + f x] \sin \left[ \frac{1}{2} (e + f x) \right] \right]^2 \right. \\
 & \quad \left. \tan \left[ \frac{1}{2} (e + f x) \right]^2 \right) + 7 \operatorname{Gamma} \left[ \frac{3}{2} + n \right] \left( -1 + \tan \left[ \frac{1}{2} (e + f x) \right] \right)^2 \\
 & \quad \left( \frac{5}{2} \cos [e + f x] (-15 - 9n + (9+8n) \cos [e + f x] + n \cos [2(e + f x)]) \right) \\
 & \quad \operatorname{Hypergeometric2F1} \left[ 1, \frac{3}{2} + n, \frac{5}{2}, -2 \sec [e + f x] \sin \left[ \frac{1}{2} (e + f x) \right] \right]^2 \\
 & \quad \left. \sec \left[ \frac{1}{2} (e + f x) \right]^6 + 2(3+2n)(5 + \cos [e + f x]) \operatorname{Hypergeometric2F1} \left[ 2, \frac{5}{2} + n, \right. \right. \\
 & \quad \left. \left. \frac{7}{2}, -2 \sec [e + f x] \sin \left[ \frac{1}{2} (e + f x) \right] \right]^2 \right) \sec \left[ \frac{1}{2} (e + f x) \right]^4 \tan \left[ \frac{1}{2} (e + f x) \right]^2 \right) \Bigg) + \\
 & \left( 14n \left( \sec \left[ \frac{1}{2} (e + f x) \right] \right)^n \left( \cos \left[ \frac{1}{2} (e + f x) \right] \right)^2 \sec [e + f x] \right)^{-\frac{3}{2}+n} \tan \left[ \frac{1}{2} (e + f x) \right]^2 \\
 & \left( 8 \operatorname{Gamma} \left[ \frac{5}{2} + n \right] \operatorname{Hypergeometric2F1} \left[ 2, \frac{5}{2} + n, \frac{7}{2}, -2 \sec [e + f x] \sin \left[ \frac{1}{2} (e + f x) \right] \right]^2 \right. \\
 & \quad \sec \left[ \frac{1}{2} (e + f x) \right]^2 \tan \left[ \frac{1}{2} (e + f x) \right]^2 + 5 \operatorname{Gamma} \left[ \frac{3}{2} + n \right] \operatorname{Hypergeometric2F1} \left[ 1, \frac{3}{2} + n, \frac{5}{2}, \right. \\
 & \quad \left. \left. -2 \sec [e + f x] \sin \left[ \frac{1}{2} (e + f x) \right] \right]^2 \left( -3 + \tan \left[ \frac{1}{2} (e + f x) \right]^2 + 2 \tan \left[ \frac{1}{2} (e + f x) \right]^4 \right) \right) \Bigg) / \\
 & \left( \left( -1 + \tan \left[ \frac{1}{2} (e + f x) \right] \right)^2 \right) \left( 8 \operatorname{Gamma} \left[ \frac{5}{2} + n \right] \sec \left[ \frac{1}{2} (e + f x) \right]^4 \tan \left[ \frac{1}{2} (e + f x) \right]^2 \right. \\
 & \quad \left( 7 \cos [e + f x] (-5 - 2n + 2(1+n) \cos [e + f x]) \operatorname{Hypergeometric2F1} \left[ 2, \frac{5}{2} + \right. \right. \\
 & \quad \left. \left. n, \frac{7}{2}, -2 \sec [e + f x] \sin \left[ \frac{1}{2} (e + f x) \right] \right]^2 \right) \sec \left[ \frac{1}{2} (e + f x) \right]^2 + \right. \\
 & \quad \left. 8(5+2n) \operatorname{Hypergeometric2F1} \left[ 3, \frac{7}{2} + n, \frac{9}{2}, -2 \sec [e + f x] \sin \left[ \frac{1}{2} (e + f x) \right] \right]^2 \right. \\
 & \quad \left. \tan \left[ \frac{1}{2} (e + f x) \right]^2 \right) + 7 \operatorname{Gamma} \left[ \frac{3}{2} + n \right] \left( -1 + \tan \left[ \frac{1}{2} (e + f x) \right] \right)^2 \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( \frac{5}{2} \cos[e+fx] (-15-9n+(9+8n)\cos[e+fx]+n\cos[2(e+fx)]) \right. \\
 & \quad \text{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2}, -2\sec[e+fx]\sin\left[\frac{1}{2}(e+fx)\right]^2\right] \\
 & \quad \left. \sec\left[\frac{1}{2}(e+fx)\right]^6 + 2(3+2n)(5+\cos[e+fx]) \text{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \right. \right. \\
 & \quad \left. \left. \frac{7}{2}, -2\sec[e+fx]\sin\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^4 \tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) + \\
 & \left( 14 \left( -\frac{3}{2}+n \right) \left( \sec\left[\frac{1}{2}(e+fx)\right]^2 \right)^n \left( \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \right)^{-\frac{5}{2}+n} \tan\left[\frac{1}{2}(e+fx)\right] \right. \\
 & \quad \left( 8 \Gamma\left[\frac{5}{2}+n\right] \text{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2\sec[e+fx]\sin\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \quad \left. \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right]^2 + 5 \Gamma\left[\frac{3}{2}+n\right] \text{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2}, \right. \right. \\
 & \quad \left. \left. -2\sec[e+fx]\sin\left[\frac{1}{2}(e+fx)\right]^2\right] \left( -3 + \tan\left[\frac{1}{2}(e+fx)\right]^2 + 2 \tan\left[\frac{1}{2}(e+fx)\right]^4 \right) \right) \\
 & \quad \left( -\cos\left[\frac{1}{2}(e+fx)\right] \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right] + \right. \\
 & \quad \left. \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \tan[e+fx] \right) \Big/ \\
 & \left( \left( -1 + \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \left( 8 \Gamma\left[\frac{5}{2}+n\right] \sec\left[\frac{1}{2}(e+fx)\right]^4 \tan\left[\frac{1}{2}(e+fx)\right]^2 \right. \right. \\
 & \quad \left. \left( 7 \cos[e+fx] (-5-2n+2(1+n)\cos[e+fx]) \text{Hypergeometric2F1}\left[2, \frac{5}{2}+ \right. \right. \right. \\
 & \quad \left. \left. \left. n, \frac{7}{2}, -2\sec[e+fx]\sin\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 + \right. \right. \\
 & \quad \left. \left. 8(5+2n) \text{Hypergeometric2F1}\left[3, \frac{7}{2}+n, \frac{9}{2}, -2\sec[e+fx]\sin\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) + 7 \Gamma\left[\frac{3}{2}+n\right] \left( -1 + \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \right) \\
 & \left( \frac{5}{2} \cos[e+fx] (-15-9n+(9+8n)\cos[e+fx]+n\cos[2(e+fx)]) \right. \\
 & \quad \text{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2}, -2\sec[e+fx]\sin\left[\frac{1}{2}(e+fx)\right]^2\right] \\
 & \quad \left. \sec\left[\frac{1}{2}(e+fx)\right]^6 + 2(3+2n)(5+\cos[e+fx]) \text{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \right. \right. \\
 & \quad \left. \left. \frac{7}{2}, -2\sec[e+fx]\sin\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^4 \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \right) + \\
 & \left( 14 \left( \sec\left[\frac{1}{2}(e+fx)\right]^2 \right)^n \left( \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \right)^{-\frac{3}{2}+n} \tan\left[\frac{1}{2}(e+fx)\right] \right. \\
 & \quad \left( 8 \Gamma\left[\frac{5}{2}+n\right] \text{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2\sec[e+fx]\sin\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \quad \left. \sec\left[\frac{1}{2}(e+fx)\right]^4 \tan\left[\frac{1}{2}(e+fx)\right] + 8 \Gamma\left[\frac{5}{2}+n\right] \text{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \frac{7}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^3 + \\
 & 5 \operatorname{Gamma}\left[\frac{3}{2}+n\right] \operatorname{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \\
 & \left(\operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] + 4 \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^3\right) + \\
 & \frac{32}{7} \left(\frac{5}{2}+n\right) \operatorname{Gamma}\left[\frac{5}{2}+n\right] \operatorname{Hypergeometric2F1}\left[3, \frac{7}{2}+n, \frac{9}{2}, \right. \\
 & \quad \left.-2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \\
 & \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \left(-2 \operatorname{Cos}\left[\frac{1}{2}(e+fx)\right] \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right] - \right. \\
 & \quad \left. 2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}[e+fx]\right) + 2 \left(\frac{3}{2}+n\right) \operatorname{Gamma}\left[\frac{3}{2}+n\right] \\
 & \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \\
 & \left(-3 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 + 2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^4\right) \left(-2 \operatorname{Cos}\left[\frac{1}{2}(e+fx)\right] \operatorname{Sec}[e+fx] \right. \\
 & \quad \left. \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right] - 2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}[e+fx]\right) \Bigg) \Bigg) / \\
 & \left(\left(-1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right) \left(8 \operatorname{Gamma}\left[\frac{5}{2}+n\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^4 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right. \right. \\
 & \quad \left. \left. \left(7 \operatorname{Cos}[e+fx] (-5 - 2n + 2(1+n) \operatorname{Cos}[e+fx]) \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+ \right. \right. \right. \right. \\
 & \quad \quad \left. \left. \left. n, \frac{7}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 + \right. \right. \right. \\
 & \quad \left. \left. 8(5+2n) \operatorname{Hypergeometric2F1}\left[3, \frac{7}{2}+n, \frac{9}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \\
 & \quad \left. \left. \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right) + 7 \operatorname{Gamma}\left[\frac{3}{2}+n\right] \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right) \right. \right. \\
 & \quad \left. \left. \left(\frac{5}{2} \operatorname{Cos}[e+fx] (-15 - 9n + (9+8n) \operatorname{Cos}[e+fx] + n \operatorname{Cos}[2(e+fx)])\right) \right. \right. \\
 & \quad \left. \left. \operatorname{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \\
 & \quad \left. \left. \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^6 + 2(3+2n)(5 + \operatorname{Cos}[e+fx]) \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \right. \right. \\
 & \quad \left. \left. \left. \frac{7}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^4 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right)\right)\right) - \\
 & \left(14 \left(\operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2\right)^n \left(\operatorname{Cos}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Sec}[e+fx]\right)^{-\frac{3}{2}+n} \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \right. \\
 & \quad \left. \left(8 \operatorname{Gamma}\left[\frac{5}{2}+n\right] \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2}, -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \\
 & \quad \left. \left. \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 + 5 \operatorname{Gamma}\left[\frac{3}{2}+n\right] \operatorname{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2}, \right. \right. \right. \\
 & \quad \left. \left. \left. -2 \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right]^2\right] \left(-3 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 + 2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^4\right)\right)\right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( 8 \Gamma\left[\frac{5}{2} + n\right] \operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^6 \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right] \right. \\
 & \quad \left( 7 \operatorname{Cos}[e + f x] (-5 - 2n + 2(1 + n) \operatorname{Cos}[e + f x]) \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2} + \right. \right. \\
 & \quad \quad \left. \left. n, \frac{7}{2}, -2 \operatorname{Sec}[e + f x] \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^2 + \right. \\
 & \quad \left. 8(5 + 2n) \operatorname{Hypergeometric2F1}\left[3, \frac{7}{2} + n, \frac{9}{2}, -2 \operatorname{Sec}[e + f x] \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \right. \\
 & \quad \left. \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right) + 16 \Gamma\left[\frac{5}{2} + n\right] \operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^4 \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^3 \\
 & \quad \left( 7 \operatorname{Cos}[e + f x] (-5 - 2n + 2(1 + n) \operatorname{Cos}[e + f x]) \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2} + \right. \right. \\
 & \quad \quad \left. \left. n, \frac{7}{2}, -2 \operatorname{Sec}[e + f x] \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^2 + \right. \\
 & \quad \left. 8(5 + 2n) \operatorname{Hypergeometric2F1}\left[3, \frac{7}{2} + n, \frac{9}{2}, -2 \operatorname{Sec}[e + f x] \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \right. \\
 & \quad \left. \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right) + 7 \Gamma\left[\frac{3}{2} + n\right] \operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right] \\
 & \quad \left( \frac{5}{2} \operatorname{Cos}[e + f x] (-15 - 9n + (9 + 8n) \operatorname{Cos}[e + f x] + n \operatorname{Cos}[2(e + f x)]) \right) \\
 & \quad \operatorname{Hypergeometric2F1}\left[1, \frac{3}{2} + n, \frac{5}{2}, -2 \operatorname{Sec}[e + f x] \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \\
 & \quad \operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^6 + 2(3 + 2n)(5 + \operatorname{Cos}[e + f x]) \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2} + \right. \\
 & \quad \quad \left. n, \frac{7}{2}, -2 \operatorname{Sec}[e + f x] \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^4 \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2 \right) + \\
 & \quad 8 \Gamma\left[\frac{5}{2} + n\right] \operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^4 \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2 \left( -14(1 + n) \operatorname{Cos}[e + f x] \right. \\
 & \quad \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2} + n, \frac{7}{2}, -2 \operatorname{Sec}[e + f x] \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \\
 & \quad \operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^2 \operatorname{Sin}[e + f x] - 7(-5 - 2n + 2(1 + n) \operatorname{Cos}[e + f x]) \\
 & \quad \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2} + n, \frac{7}{2}, -2 \operatorname{Sec}[e + f x] \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \\
 & \quad \operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^2 \operatorname{Sin}[e + f x] + 7 \operatorname{Cos}[e + f x] (-5 - 2n + 2(1 + n) \operatorname{Cos}[e + f x]) \right) \\
 & \quad \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2} + n, \frac{7}{2}, -2 \operatorname{Sec}[e + f x] \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \\
 & \quad \operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right] + 8(5 + 2n) \operatorname{Hypergeometric2F1}\left[3, \frac{7}{2} + \right. \\
 & \quad \quad \left. n, \frac{9}{2}, -2 \operatorname{Sec}[e + f x] \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right] + \\
 & \quad 4 \left( \frac{5}{2} + n \right) \operatorname{Cos}[e + f x] (-5 - 2n + 2(1 + n) \operatorname{Cos}[e + f x]) \operatorname{Hypergeometric2F1}\left[3, \frac{7}{2} + \right. \\
 & \quad \quad \left. n, \frac{9}{2}, -2 \operatorname{Sec}[e + f x] \operatorname{Sin}\left[\frac{1}{2}(e + f x)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^2 \left( -2 \operatorname{Cos}\left[\frac{1}{2}(e + f x)\right] \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \sec [e+f x] \sin \left[ \frac{1}{2}(e+f x)\right]-2 \sec [e+f x] \sin \left[ \frac{1}{2}(e+f x)\right]^2 \tan [e+f x]\right) + \\
 & \frac{16}{3}\left(\frac{7}{2}+n\right)(5+2 n) \operatorname{Hypergeometric2F1}\left[4, \frac{9}{2}+n, \frac{11}{2},-2 \sec [e+f x] \right. \\
 & \left. \sin \left[ \frac{1}{2}(e+f x)\right]^2\right] \tan \left[ \frac{1}{2}(e+f x)\right]^2\left(-2 \cos \left[ \frac{1}{2}(e+f x)\right] \sec [e+f x] \right. \\
 & \left. \sin \left[ \frac{1}{2}(e+f x)\right]-2 \sec [e+f x] \sin \left[ \frac{1}{2}(e+f x)\right]^2 \tan [e+f x]\right)\right) + \\
 & 7 \operatorname{Gamma}\left[\frac{3}{2}+n\right]\left(-1+\tan \left[ \frac{1}{2}(e+f x)\right]^2\right)\left(-\frac{5}{2}(-15-9 n+(9+8 n) \cos [e+f x]+ \right. \\
 & \left. n \cos [2(e+f x)])\right) \operatorname{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2},-2 \right. \\
 & \left. \sec [e+f x] \sin \left[ \frac{1}{2}(e+f x)\right]^2\right] \sec \left[ \frac{1}{2}(e+f x)\right]^6 \sin [e+f x]+ \\
 & \left. \frac{5}{2} \cos [e+f x] \operatorname{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2},-2 \sec [e+f x] \sin \left[ \frac{1}{2}(e+f x)\right]^2\right] \right. \\
 & \left. \sec \left[ \frac{1}{2}(e+f x)\right]^6(-9+8 n) \sin [e+f x]-2 n \sin [2(e+f x)]\right)+ \\
 & \frac{15}{2} \cos [e+f x](-15-9 n+(9+8 n) \cos [e+f x]+n \cos [2(e+f x)]) \\
 & \operatorname{Hypergeometric2F1}\left[1, \frac{3}{2}+n, \frac{5}{2},-2 \sec [e+f x] \sin \left[ \frac{1}{2}(e+f x)\right]^2\right] \\
 & \sec \left[ \frac{1}{2}(e+f x)\right]^6 \tan \left[ \frac{1}{2}(e+f x)\right]+2(3+2 n)(5+\cos [e+f x]) \\
 & \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2},-2 \sec [e+f x] \sin \left[ \frac{1}{2}(e+f x)\right]^2\right] \\
 & \sec \left[ \frac{1}{2}(e+f x)\right]^6 \tan \left[ \frac{1}{2}(e+f x)\right]-2(3+2 n) \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2},-2 \right. \\
 & \left. \sec [e+f x] \sin \left[ \frac{1}{2}(e+f x)\right]^2\right] \sec \left[ \frac{1}{2}(e+f x)\right]^4 \sin [e+f x] \tan \left[ \frac{1}{2}(e+f x)\right]^2+ \\
 & 4(3+2 n)(5+\cos [e+f x]) \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2},-2 \right. \\
 & \left. \sec [e+f x] \sin \left[ \frac{1}{2}(e+f x)\right]^2\right] \sec \left[ \frac{1}{2}(e+f x)\right]^4 \tan \left[ \frac{1}{2}(e+f x)\right]^3+ \\
 & \left(\frac{3}{2}+n\right) \cos [e+f x](-15-9 n+(9+8 n) \cos [e+f x]+n \cos [2(e+f x)]) \\
 & \operatorname{Hypergeometric2F1}\left[2, \frac{5}{2}+n, \frac{7}{2},-2 \sec [e+f x] \sin \left[ \frac{1}{2}(e+f x)\right]^2\right] \\
 & \sec \left[ \frac{1}{2}(e+f x)\right]^6\left(-2 \cos \left[ \frac{1}{2}(e+f x)\right] \sec [e+f x] \sin \left[ \frac{1}{2}(e+f x)\right]-2 \sec [ \right. \\
 & \left. e+f x] \sin \left[ \frac{1}{2}(e+f x)\right]^2 \tan [e+f x]\right)+\frac{8}{7}\left(\frac{5}{2}+n\right)(3+2 n)(5+\cos [e+f x]) \\
 & \operatorname{Hypergeometric2F1}\left[3, \frac{7}{2}+n, \frac{9}{2},-2 \sec [e+f x] \sin \left[ \frac{1}{2}(e+f x)\right]^2\right] \\
 & \sec \left[ \frac{1}{2}(e+f x)\right]^4 \tan \left[ \frac{1}{2}(e+f x)\right]^2\left(-2 \cos \left[ \frac{1}{2}(e+f x)\right] \sec [e+f x] \right.
 \end{aligned}$$



### Problem 318: Result more than twice size of optimal antiderivative.

$$\int \frac{(d \operatorname{Sec}[e + f x])^n}{\sqrt{a + a \operatorname{Sec}[e + f x]}} dx$$

Optimal (type 6, 75 leaves, 3 steps):

$$- \left( \operatorname{AppellF1}\left[n, \frac{1}{2}, 1, 1+n, \operatorname{Sec}[e + f x], -\operatorname{Sec}[e + f x]\right] (d \operatorname{Sec}[e + f x])^n \operatorname{Tan}[e + f x] \right) / \left( f n \sqrt{1 - \operatorname{Sec}[e + f x]} \sqrt{a + a \operatorname{Sec}[e + f x]} \right)$$

Result (type 6, 2977 leaves):

$$\begin{aligned} & \left( 3 \sqrt{2} \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2} + n, 1 - n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right] \left(\operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^2\right)^n \right. \\ & \quad \left. \operatorname{Sec}[e + f x]^{-\frac{1}{2} - n + \frac{1}{2}(-1 + 2n)} (d \operatorname{Sec}[e + f x])^n \left(\operatorname{Cos}\left[\frac{1}{2}(e + f x)\right]^2 \operatorname{Sec}[e + f x]\right)^n \right. \\ & \quad \left. \sqrt{1 + \operatorname{Sec}[e + f x]} \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right] \right) / \left( f \sqrt{a(1 + \operatorname{Sec}[e + f x])} \right) \\ & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2} + n, 1 - n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right] + \right. \\ & \quad \left( 2(-1 + n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2} + n, 2 - n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right] + \right. \\ & \quad \left. (-1 + 2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2} + n, 1 - n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2, \right. \right. \\ & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right] \right) \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2 \left. \right) \\ & \left( \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2} + n, 1 - n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right] \operatorname{Cos}[e + f x] \right. \right. \\ & \quad \left. \left. \left(\operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^2\right)^{1+n} \left(\operatorname{Cos}\left[\frac{1}{2}(e + f x)\right]^2 \operatorname{Sec}[e + f x]\right)^n \sqrt{1 + \operatorname{Sec}[e + f x]} \right) \right) / \right. \\ & \quad \left( \sqrt{2} \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2} + n, 1 - n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right] + \right. \right. \\ & \quad \left( 2(-1 + n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2} + n, 2 - n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right] + \right. \\ & \quad \left. (-1 + 2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2} + n, 1 - n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right] \right) \right. \\ & \quad \left. \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2 \right) - \left( 3 \sqrt{2} \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2} + n, 1 - n, \frac{3}{2}, \right. \right. \\ & \quad \left. \left. \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right] \left(\operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^2\right)^n \right. \\ & \quad \left. \left(\operatorname{Cos}\left[\frac{1}{2}(e + f x)\right]^2 \operatorname{Sec}[e + f x]\right)^n \sqrt{1 + \operatorname{Sec}[e + f x]} \operatorname{Sin}[e + f x] \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right] \right) \right) / \right. \\ & \quad \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2} + n, 1 - n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right] + \right. \\ & \quad \left. \left( 2(-1 + n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2} + n, 2 - n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right] + \right. \right. \end{aligned}$$

$$\begin{aligned}
 & (-1+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \\
 & \tan\left[\frac{1}{2}(e+fx)\right]^2 + \left(3\sqrt{2}n \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \cos[e+fx] \left(\sec\left[\frac{1}{2}(e+fx)\right]^2\right)^n \right. \\
 & \left. \left(\cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx]\right)^n \sqrt{1+\sec[e+fx]} \tan\left[\frac{1}{2}(e+fx)\right]^2\right) / \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \left. \left(2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \\
 & \left. \left. (-1+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \right. \\
 & \left. \tan\left[\frac{1}{2}(e+fx)\right]^2 + \left(3\sqrt{2} \cos[e+fx] \left(\sec\left[\frac{1}{2}(e+fx)\right]^2\right)^n \right. \right. \\
 & \left. \left(\cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx]\right)^n \sqrt{1+\sec[e+fx]} \tan\left[\frac{1}{2}(e+fx)\right] \right. \\
 & \left. \left(-\frac{1}{3}(1-n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \right. \\
 & \left. \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \frac{1}{3}\left(-\frac{1}{2}+n\right) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+n, 1-n, \frac{5}{2}, \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right]\right) \right) / \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \left. \left(2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \\
 & \left. \left. (-1+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \right. \\
 & \left. \tan\left[\frac{1}{2}(e+fx)\right]^2 - \left(3\sqrt{2} \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \cos[e+fx] \left(\sec\left[\frac{1}{2}(e+fx)\right]^2\right)^n \right. \right. \\
 & \left. \left(\cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx]\right)^n \sqrt{1+\sec[e+fx]} \tan\left[\frac{1}{2}(e+fx)\right] \right. \\
 & \left. \left(\left(2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \right. \\
 & \left. \left. (-1+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \right) \right. \\
 & \left. \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \right. \\
 & \left. 3\left(-\frac{1}{3}(1-n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \right. \\
 & \left. \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \frac{1}{3}\left(-\frac{1}{2}+n\right) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+n, 1-n, \frac{5}{2}, \right. \right.
 \end{aligned}$$



$$\begin{aligned}
& \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) + \\
& \tan\left[\frac{1}{2}(e+fx)\right]^2 \left( 2(-1+n) \left( -\frac{3}{5}(2-n) \operatorname{AppellF1}\left[\frac{5}{2}, -\frac{1}{2}+n, 3-n, \frac{7}{2}, \right. \right. \right. \\
& \quad \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \frac{3}{5} \right. \\
& \quad \left. \left( -\frac{1}{2}+n \right) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{2}+n, 2-n, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
& \quad \left. \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) + (-1+2n) \left( -\frac{3}{5}(1-n) \operatorname{AppellF1}\left[\frac{5}{2}, \right. \right. \\
& \quad \left. \frac{1}{2}+n, 2-n, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \right. \\
& \quad \left. \tan\left[\frac{1}{2}(e+fx)\right] + \frac{3}{5}\left(\frac{1}{2}+n\right) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{3}{2}+n, 1-n, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) \right) \right) \Big/ \\
& \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
& \quad \left. \left( 2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \\
& \quad \left. \left. (-1+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \\
& \quad \left. \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \right)^2 + \right. \\
& \left. \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \right. \\
& \quad \left. \left( \sec\left[\frac{1}{2}(e+fx)\right]^2 \right)^n \left( \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \right)^n \right. \\
& \quad \left. \tan\left[\frac{1}{2}(e+fx)\right] \tan[e+fx] \right) \Big/ \left( \sqrt{2} \sqrt{1+\sec[e+fx]} \right. \\
& \quad \left. \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \\
& \quad \left. \left( 2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \\
& \quad \left. \left. (-1+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \\
& \quad \left. \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \right) + \\
& \left. \left( 3 \sqrt{2} n \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \right. \\
& \quad \left. \cos[e+fx] \left( \sec\left[\frac{1}{2}(e+fx)\right]^2 \right)^n \left( \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \right)^{-1+n} \right. \\
& \quad \left. \sqrt{1+\sec[e+fx]} \tan\left[\frac{1}{2}(e+fx)\right] \left( -\cos\left[\frac{1}{2}(e+fx)\right] \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right] + \right. \right. \\
& \quad \left. \left. \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \tan[e+fx] \right) \right) \Big/
\end{aligned}$$

$$\left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2} + n, 1 - n, \frac{3}{2}, \tan\left[\frac{1}{2}(e + fx)\right]^2, -\tan\left[\frac{1}{2}(e + fx)\right]^2\right] + \right. \\ \left. \left( 2(-1 + n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2} + n, 2 - n, \frac{5}{2}, \tan\left[\frac{1}{2}(e + fx)\right]^2, -\tan\left[\frac{1}{2}(e + fx)\right]^2\right] + \right. \right. \\ \left. \left. (-1 + 2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2} + n, 1 - n, \frac{5}{2}, \tan\left[\frac{1}{2}(e + fx)\right]^2, \right. \right. \right. \\ \left. \left. \left. -\tan\left[\frac{1}{2}(e + fx)\right]^2\right] \right) \tan\left[\frac{1}{2}(e + fx)\right]^2 \right) \right)$$

**Problem 319: Result more than twice size of optimal antiderivative.**

$$\int \frac{(d \operatorname{Sec}[e + fx])^n}{(a + a \operatorname{Sec}[e + fx])^{3/2}} dx$$

Optimal (type 6, 78 leaves, 3 steps):

$$- \left( \left( \operatorname{AppellF1}\left[n, \frac{1}{2}, 2, 1 + n, \operatorname{Sec}[e + fx], -\operatorname{Sec}[e + fx]\right] (d \operatorname{Sec}[e + fx])^n \tan[e + fx] \right) / \right. \\ \left. \left( a f n \sqrt{1 - \operatorname{Sec}[e + fx]} \sqrt{a + a \operatorname{Sec}[e + fx]} \right) \right)$$

Result (type 6, 3005 leaves):

$$\left( 6 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2} + n, 1 - n, \frac{3}{2}, \tan\left[\frac{1}{2}(e + fx)\right]^2, -\tan\left[\frac{1}{2}(e + fx)\right]^2\right] \left( \operatorname{Sec}\left[\frac{1}{2}(e + fx)\right]^2 \right)^n \right. \\ \left. \operatorname{Sec}[e + fx]^{\frac{1}{2} - n + \frac{1}{2}(-3 + 2n)} (d \operatorname{Sec}[e + fx])^n \left( \cos\left[\frac{1}{2}(e + fx)\right]^2 \operatorname{Sec}[e + fx] \right)^{\frac{3}{2} + n} \right. \\ \left. \tan\left[\frac{1}{2}(e + fx)\right] \left( -1 + \tan\left[\frac{1}{2}(e + fx)\right]^2 \right)^2 \right) / \left( f (a (1 + \operatorname{Sec}[e + fx]))^{3/2} \right. \\ \left. \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2} + n, 1 - n, \frac{3}{2}, \tan\left[\frac{1}{2}(e + fx)\right]^2, -\tan\left[\frac{1}{2}(e + fx)\right]^2\right] + \right. \right. \\ \left. \left. \left( 2(-1 + n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{3}{2} + n, 2 - n, \frac{5}{2}, \tan\left[\frac{1}{2}(e + fx)\right]^2, -\tan\left[\frac{1}{2}(e + fx)\right]^2\right] + \right. \right. \right. \\ \left. \left. \left. (-3 + 2n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2} + n, 1 - n, \frac{5}{2}, \tan\left[\frac{1}{2}(e + fx)\right]^2, -\tan\left[\frac{1}{2}(e + fx)\right]^2\right] \right) \right) \right. \\ \left. \tan\left[\frac{1}{2}(e + fx)\right]^2 \right) \left( \left( 12 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2} + n, 1 - n, \frac{3}{2}, \tan\left[\frac{1}{2}(e + fx)\right]^2, \right. \right. \right. \right. \\ \left. \left. \left. -\tan\left[\frac{1}{2}(e + fx)\right]^2\right] \cos[e + fx] \left( \operatorname{Sec}\left[\frac{1}{2}(e + fx)\right]^2 \right)^{1+n} \right. \right. \right. \\ \left. \left. \left. \left( \cos\left[\frac{1}{2}(e + fx)\right]^2 \operatorname{Sec}[e + fx] \right)^{\frac{3}{2} + n} \tan\left[\frac{1}{2}(e + fx)\right]^2 \left( -1 + \tan\left[\frac{1}{2}(e + fx)\right]^2 \right) \right) \right) \right) / \right. \\ \left. \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2} + n, 1 - n, \frac{3}{2}, \tan\left[\frac{1}{2}(e + fx)\right]^2, -\tan\left[\frac{1}{2}(e + fx)\right]^2\right] + \right. \right. \\ \left. \left. \left( 2(-1 + n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{3}{2} + n, 2 - n, \frac{5}{2}, \tan\left[\frac{1}{2}(e + fx)\right]^2, -\tan\left[\frac{1}{2}(e + fx)\right]^2\right] + \right. \right. \right. \right.$$

$$\begin{aligned}
 & (-3+2n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \\
 & \quad \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \tan\left[\frac{1}{2}(e+fx)\right]^2 + \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \cos[e+fx] \right. \\
 & \quad \left. \left(\sec\left[\frac{1}{2}(e+fx)\right]^2\right)^{1+n} \left(\cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx]\right)^{\frac{3}{2}+n} \left(-1+\tan\left[\frac{1}{2}(e+fx)\right]^2\right)^2\right) / \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left(2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{3}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left. (-3+2n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right]\right) \\
 & \quad \tan\left[\frac{1}{2}(e+fx)\right]^2 - \left(6 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \left(\sec\left[\frac{1}{2}(e+fx)\right]^2\right)^n \left(\cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx]\right)^{\frac{3}{2}+n} \right. \\
 & \quad \left. \sin[e+fx] \tan\left[\frac{1}{2}(e+fx)\right] \left(-1+\tan\left[\frac{1}{2}(e+fx)\right]^2\right)^2\right) / \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left(2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{3}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left. (-3+2n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right]\right) \\
 & \quad \tan\left[\frac{1}{2}(e+fx)\right]^2 + \left(6n \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \cos[e+fx] \left(\sec\left[\frac{1}{2}(e+fx)\right]^2\right)^n \right. \\
 & \quad \left. \left(\cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx]\right)^{\frac{3}{2}+n} \tan\left[\frac{1}{2}(e+fx)\right]^2 \left(-1+\tan\left[\frac{1}{2}(e+fx)\right]^2\right)^2\right) / \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left(2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{3}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left. (-3+2n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right]\right) \\
 & \quad \tan\left[\frac{1}{2}(e+fx)\right]^2 + \left(6 \cos[e+fx] \left(\sec\left[\frac{1}{2}(e+fx)\right]^2\right)^n \right. \\
 & \quad \left. \left(\cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx]\right)^{\frac{3}{2}+n} \tan\left[\frac{1}{2}(e+fx)\right] \left(-\frac{1}{3}(1-n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{3}{2}+n, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
& 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \\
& \frac{1}{3}\left(-\frac{3}{2}+n\right) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \\
& \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \left(-1+\tan\left[\frac{1}{2}(e+fx)\right]^2\right)^2 \Big/ \\
& \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
& \left(2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{3}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
& \left. (-3+2n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right]\right) \\
& \tan\left[\frac{1}{2}(e+fx)\right]^2 \Big) - \left(6 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{3}{2}+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \cos[e+fx] \left(\operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2\right)^n \right. \\
& \left. \left(\cos\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Sec}[e+fx]\right)^{\frac{3}{2}+n} \tan\left[\frac{1}{2}(e+fx)\right] \left(-1+\tan\left[\frac{1}{2}(e+fx)\right]^2\right)^2 \right. \\
& \left. \left(\left(2(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{3}{2}+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \right. \\
& \left. \left. (-3+2n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right]\right) \right. \\
& \left. \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + 3\left(-\frac{1}{3}(1-n) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{3}{2}+n, 2-n, \right. \right. \right. \\
& \left. \left. \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \right. \\
& \left. \frac{1}{3}\left(-\frac{3}{2}+n\right) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
& \left. \left. \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right]\right) + \tan\left[\frac{1}{2}(e+fx)\right]^2 \right. \\
& \left. \left(2(-1+n)\left(-\frac{3}{5}(2-n) \operatorname{AppellF1}\left[\frac{5}{2}, -\frac{3}{2}+n, 3-n, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \right. \\
& \left. \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \frac{3}{5}\left(-\frac{3}{2}+n\right) \right. \right. \\
& \left. \left. \operatorname{AppellF1}\left[\frac{5}{2}, -\frac{1}{2}+n, 2-n, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \\
& \left. \left. \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right]\right) + (-3+2n)\left(-\frac{3}{5}(1-n) \operatorname{AppellF1}\left[\frac{5}{2}, \right. \right. \right. \\
& \left. \left. -\frac{1}{2}+n, 2-n, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \right. \\
& \left. \tan\left[\frac{1}{2}(e+fx)\right] + \frac{3}{5}\left(-\frac{1}{2}+n\right) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{2}+n, 1-n, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
& \left. \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right]\right)\right)\right)\Big/
\end{aligned}$$

$$\begin{aligned}
 & \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{3}{2} + n, 1 - n, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]^2 \right] + \right. \\
 & \quad \left( 2 (-1 + n) \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{3}{2} + n, 2 - n, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]^2 \right] + \right. \\
 & \quad \quad \left. (-3 + 2 n) \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{1}{2} + n, 1 - n, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]^2, \right. \right. \\
 & \quad \quad \quad \left. \left. -\operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]^2 \right] \right) \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]^2 \right) + \\
 & \left( 6 \left( \frac{3}{2} + n \right) \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{3}{2} + n, 1 - n, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]^2 \right] \right. \\
 & \quad \left. \operatorname{Cos} [e + f x] \left( \operatorname{Sec} \left[ \frac{1}{2} (e + f x) \right]^2 \right)^n \left( \operatorname{Cos} \left[ \frac{1}{2} (e + f x) \right]^2 \operatorname{Sec} [e + f x] \right)^{\frac{1}{2} + n} \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \right. \\
 & \quad \left. \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]^2 \right)^2 \left( -\operatorname{Cos} \left[ \frac{1}{2} (e + f x) \right] \operatorname{Sec} [e + f x] \operatorname{Sin} \left[ \frac{1}{2} (e + f x) \right] + \right. \right. \\
 & \quad \quad \left. \left. \operatorname{Cos} \left[ \frac{1}{2} (e + f x) \right]^2 \operatorname{Sec} [e + f x] \operatorname{Tan} [e + f x] \right) \right) \right) / \\
 & \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{3}{2} + n, 1 - n, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]^2 \right] + \right. \\
 & \quad \left( 2 (-1 + n) \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{3}{2} + n, 2 - n, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]^2 \right] + \right. \\
 & \quad \quad \left. (-3 + 2 n) \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{1}{2} + n, 1 - n, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]^2, \right. \right. \\
 & \quad \quad \quad \left. \left. -\operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]^2 \right] \right) \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]^2 \right) \right)
 \end{aligned}$$

**Problem 320: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int (-\operatorname{Sec} [e + f x])^n (a - a \operatorname{Sec} [e + f x])^{5/2} dx$$

Optimal (type 5, 178 leaves, 4 steps):

$$\begin{aligned}
 & \left( 2 a^3 (3 + 24 n + 16 n^2) \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, 1 - n, \frac{3}{2}, 1 + \operatorname{Sec} [e + f x] \right] \operatorname{Tan} [e + f x] \right) / \\
 & \quad \left( f (1 + 2 n) (3 + 2 n) \sqrt{a - a \operatorname{Sec} [e + f x]} \right) + \frac{2 a^3 (7 + 4 n) (-\operatorname{Sec} [e + f x])^n \operatorname{Tan} [e + f x]}{f (1 + 2 n) (3 + 2 n) \sqrt{a - a \operatorname{Sec} [e + f x]}} + \\
 & \quad \frac{2 a^2 (-\operatorname{Sec} [e + f x])^n \sqrt{a - a \operatorname{Sec} [e + f x]} \operatorname{Tan} [e + f x]}{f (3 + 2 n)}
 \end{aligned}$$

Result (type 5, 455 leaves):

$$\frac{1}{f} 2^{-\frac{5}{2}+n} e^{\frac{1}{2}i(e+f(1-2n)x)} \left( \frac{e^{i(e+fx)}}{1+e^{2i(e+fx)}} \right)^{-\frac{1}{2}+n} (1+e^{2i(e+fx)})^{-\frac{1}{2}+n}$$

$$\text{Csc}\left[\frac{1}{2}(e+fx)\right]^5 \left( \frac{e^{ifnx} \text{Hypergeometric2F1}\left[\frac{n}{2}, \frac{5}{2}+n, \frac{2+n}{2}, -e^{2i(e+fx)}\right]}{n} - \frac{5 e^{i(e+f(1+n)x)} \text{Hypergeometric2F1}\left[\frac{1+n}{2}, \frac{5}{2}+n, \frac{3+n}{2}, -e^{2i(e+fx)}\right]}{1+n} + \frac{10 e^{i(2e+f(2+n)x)} \text{Hypergeometric2F1}\left[\frac{2+n}{2}, \frac{5}{2}+n, \frac{4+n}{2}, -e^{2i(e+fx)}\right]}{2+n} - \frac{10 e^{i(3e+f(3+n)x)} \text{Hypergeometric2F1}\left[\frac{5}{2}+n, \frac{3+n}{2}, \frac{5+n}{2}, -e^{2i(e+fx)}\right]}{3+n} + \frac{5 e^{i(4e+f(4+n)x)} \text{Hypergeometric2F1}\left[\frac{5}{2}+n, \frac{4+n}{2}, \frac{6+n}{2}, -e^{2i(e+fx)}\right]}{4+n} - \frac{e^{i(5e+f(5+n)x)} \text{Hypergeometric2F1}\left[\frac{5}{2}+n, \frac{5+n}{2}, \frac{7+n}{2}, -e^{2i(e+fx)}\right]}{5+n} \right)$$

$$(-\text{Sec}[e+fx])^n \text{Sec}[e+fx]^{-\frac{5}{2}-n} (a-a\text{Sec}[e+fx])^{5/2}$$

**Problem 321: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int (-\text{Sec}[e+fx])^n (a-a\text{Sec}[e+fx])^{3/2} dx$$

Optimal (type 5, 108 leaves, 4 steps):

$$\left( 2a^2(1+4n) \text{Hypergeometric2F1}\left[\frac{1}{2}, 1-n, \frac{3}{2}, 1+\text{Sec}[e+fx]\right] \text{Tan}[e+fx] \right) /$$

$$\left( f(1+2n) \sqrt{a-a\text{Sec}[e+fx]} \right) + \frac{2a^2(-\text{Sec}[e+fx])^n \text{Tan}[e+fx]}{f(1+2n) \sqrt{a-a\text{Sec}[e+fx]}}$$

Result (type 5, 377 leaves):

$$\frac{1}{fn(1+n)(2+n)(3+n)} 2^{-\frac{3}{2}+n} e^{\frac{1}{2}i(e+f(1-2n)x)} \left( \frac{e^{i(e+fx)}}{1+e^{2i(e+fx)}} \right)^{-\frac{1}{2}+n} (1+e^{2i(e+fx)})^{-\frac{1}{2}+n}$$

$$\text{Csc}\left[\frac{1}{2}(e+fx)\right]^3 \left( -e^{ifnx} (6+11n+6n^2+n^3) \text{Hypergeometric2F1}\left[\frac{n}{2}, \frac{3}{2}+n, \frac{2+n}{2}, -e^{2i(e+fx)}\right] + \frac{3 e^{i(e+f(1+n)x}} n (6+5n+n^2) \text{Hypergeometric2F1}\left[\frac{1+n}{2}, \frac{3}{2}+n, \frac{3+n}{2}, -e^{2i(e+fx)}\right] + e^{2ie} n (1+n) \left( -3 e^{if(2+n)x} (3+n) \text{Hypergeometric2F1}\left[\frac{3}{2}+n, \frac{2+n}{2}, \frac{4+n}{2}, -e^{2i(e+fx)}\right] + e^{i(e+f(3+n)x} (2+n) \text{Hypergeometric2F1}\left[\frac{3}{2}+n, \frac{3+n}{2}, \frac{5+n}{2}, -e^{2i(e+fx)}\right] \right) \right)$$

$$(-\text{Sec}[e+fx])^n \text{Sec}[e+fx]^{-\frac{3}{2}-n} (a-a\text{Sec}[e+fx])^{3/2}$$

**Problem 322: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int (-\operatorname{Sec}[e + f x])^n \sqrt{a - a \operatorname{Sec}[e + f x]} \, dx$$

Optimal (type 5, 47 leaves, 2 steps):

$$\frac{2 a \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, 1 - n, \frac{3}{2}, 1 + \operatorname{Sec}[e + f x]\right] \operatorname{Tan}[e + f x]}{f \sqrt{a - a \operatorname{Sec}[e + f x]}}$$

Result (type 5, 236 leaves):

$$\frac{1}{f n (1 + n)} 2^{\frac{1}{2} + n} e^{-\frac{1}{2} i (e + f (1 + 2n) x)} \left( \frac{e^{i (e + f x)}}{1 + e^{2 i (e + f x)}} \right)^{\frac{1}{2} + n} (1 + e^{2 i (e + f x)})^{\frac{1}{2} + n} \\ \operatorname{Csc}\left[\frac{e}{2} + \frac{f x}{2}\right] \left( e^{i f n x} (1 + n) \operatorname{Hypergeometric2F1}\left[\frac{n}{2}, \frac{1}{2} + n, \frac{2 + n}{2}, -e^{2 i (e + f x)}\right] - \right. \\ \left. e^{i (e + f (1 + n) x)} n \operatorname{Hypergeometric2F1}\left[\frac{1}{2} + n, \frac{1 + n}{2}, \frac{3 + n}{2}, -e^{2 i (e + f x)}\right] \right) \\ (-\operatorname{Sec}[e + f x])^n \operatorname{Sec}[e + f x]^{\frac{1}{2} - n} \sqrt{a - a \operatorname{Sec}[e + f x]}$$

**Problem 323: Unable to integrate problem.**

$$\int \frac{(-\operatorname{Sec}[e + f x])^n}{\sqrt{a - a \operatorname{Sec}[e + f x]}} \, dx$$

Optimal (type 6, 58 leaves, 4 steps):

$$\left( \operatorname{AppellF1}\left[\frac{1}{2}, 1 - n, 1, \frac{3}{2}, 1 + \operatorname{Sec}[e + f x], \frac{1}{2} (1 + \operatorname{Sec}[e + f x])\right] \operatorname{Tan}[e + f x] \right) / \\ (f \sqrt{a - a \operatorname{Sec}[e + f x]})$$

Result (type 8, 28 leaves):

$$\int \frac{(-\operatorname{Sec}[e + f x])^n}{\sqrt{a - a \operatorname{Sec}[e + f x]}} \, dx$$

**Problem 324: Unable to integrate problem.**

$$\int \frac{(-\operatorname{Sec}[e + f x])^n}{(a - a \operatorname{Sec}[e + f x])^{3/2}} \, dx$$

Optimal (type 6, 64 leaves, 4 steps):

$$\left( \operatorname{AppellF1}\left[\frac{1}{2}, 1 - n, 2, \frac{3}{2}, 1 + \operatorname{Sec}[e + f x], \frac{1}{2} (1 + \operatorname{Sec}[e + f x])\right] \operatorname{Tan}[e + f x] \right) / \\ (2 a f \sqrt{a - a \operatorname{Sec}[e + f x]})$$

Result (type 8, 28 leaves):

$$\int \frac{(-\operatorname{Sec}[e+fx])^n}{(a-a\operatorname{Sec}[e+fx])^{3/2}} dx$$

**Problem 325: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \operatorname{Sec}[e+fx]^n (a-a\operatorname{Sec}[e+fx])^{3/2} dx$$

Optimal (type 5, 130 leaves, 5 steps):

$$\frac{2a^2 \operatorname{Sec}[e+fx]^{1+n} \operatorname{Sin}[e+fx]}{f(1+2n)\sqrt{a-a\operatorname{Sec}[e+fx]}} + \left( 2a^2(1+4n) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, 1-n, \frac{3}{2}, 1+\operatorname{Sec}[e+fx]\right] (-\operatorname{Sec}[e+fx])^{-n} \operatorname{Sec}[e+fx]^{1+n} \operatorname{Sin}[e+fx] \right) / \left( f(1+2n)\sqrt{a-a\operatorname{Sec}[e+fx]} \right)$$

Result (type 5, 366 leaves):

$$\frac{1}{fn(1+n)(2+n)(3+n)\operatorname{Sec}[e+fx]^{3/2}} 2^{-\frac{3}{2}+n} e^{\frac{1}{2}i(e+f(1-2n)x)} \left( \frac{e^{i(e+fx)}}{1+e^{2i(e+fx)}} \right)^{-\frac{1}{2}+n} (1+e^{2i(e+fx)})^{-\frac{1}{2}+n} \operatorname{Csc}\left[\frac{e}{2} + \frac{fx}{2}\right]^3 \left( -e^{ifnx} (6+11n+6n^2+n^3) \operatorname{Hypergeometric2F1}\left[\frac{n}{2}, \frac{3}{2}+n, \frac{2+n}{2}, -e^{2i(e+fx)}\right] + 3e^{i(e+f(1+n)x)} n(6+5n+n^2) \operatorname{Hypergeometric2F1}\left[\frac{1+n}{2}, \frac{3}{2}+n, \frac{3+n}{2}, -e^{2i(e+fx)}\right] + e^{2ie} n(1+n) \left( -3e^{i f(2+n)x} (3+n) \operatorname{Hypergeometric2F1}\left[\frac{3}{2}+n, \frac{2+n}{2}, \frac{4+n}{2}, -e^{2i(e+fx)}\right] + e^{i(e+f(3+n)x)} (2+n) \operatorname{Hypergeometric2F1}\left[\frac{3}{2}+n, \frac{3+n}{2}, \frac{5+n}{2}, -e^{2i(e+fx)}\right] \right) \right) (a-a\operatorname{Sec}[e+fx])^{3/2}$$

**Problem 326: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \operatorname{Sec}[e+fx]^n \sqrt{a-a\operatorname{Sec}[e+fx]} dx$$

Optimal (type 5, 69 leaves, 3 steps):

$$\left( 2a \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, 1-n, \frac{3}{2}, 1+\operatorname{Sec}[e+fx]\right] (-\operatorname{Sec}[e+fx])^{-n} \operatorname{Sec}[e+fx]^{1+n} \operatorname{Sin}[e+fx] \right) / \left( f\sqrt{a-a\operatorname{Sec}[e+fx]} \right)$$

Result (type 5, 222 leaves):



$$\left( 2^{-\frac{1}{2}+n} e^{-\frac{1}{2}i(e+f(1+2n)x)} \left( \frac{e^{i(e+fx)}}{1+e^{2i(e+fx)}} \right)^{\frac{1}{2}+n} (1+e^{2i(e+fx)})^{\frac{1}{2}+n} \right. \\ \left. \operatorname{Csc}\left[\frac{e}{2} + \frac{fx}{2}\right] \left( e^{ifnx} (1+n) \operatorname{Hypergeometric2F1}\left[\frac{n}{2}, \frac{1}{2}+n, \frac{2+n}{2}, -e^{2i(e+fx)}\right] - \right. \right. \\ \left. \left. e^{i(e+f(1+n)x)} n \operatorname{Hypergeometric2F1}\left[\frac{1}{2}+n, \frac{1+n}{2}, \frac{3+n}{2}, -e^{2i(e+fx)}\right] \right) \right. \\ \left. \sqrt{a-a \operatorname{Sec}[e+fx]} \right) / \left( f n (1+n) \sqrt{\operatorname{Sec}[e+fx]} \right)$$

**Problem 327: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int (d \operatorname{Sec}[e+fx])^n (a-a \operatorname{Sec}[e+fx])^{3/2} dx$$

Optimal (type 5, 130 leaves, 5 steps):

$$\frac{2 a^2 (d \operatorname{Sec}[e+fx])^n \operatorname{Tan}[e+fx]}{f (1+2n) \sqrt{a-a \operatorname{Sec}[e+fx]}} + \\ \left( 2 a^2 (1+4n) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, 1-n, \frac{3}{2}, 1+\operatorname{Sec}[e+fx]\right] (-\operatorname{Sec}[e+fx])^{-n} \right. \\ \left. (d \operatorname{Sec}[e+fx])^n \operatorname{Tan}[e+fx] \right) / \left( f (1+2n) \sqrt{a-a \operatorname{Sec}[e+fx]} \right)$$

Result (type 5, 377 leaves):

$$\frac{1}{f n (1+n) (2+n) (3+n)} 2^{-\frac{3}{2}+n} e^{\frac{1}{2}i(e+f(1-2n)x)} \left( \frac{e^{i(e+fx)}}{1+e^{2i(e+fx)}} \right)^{-\frac{1}{2}+n} (1+e^{2i(e+fx)})^{-\frac{1}{2}+n} \\ \operatorname{Csc}\left[\frac{1}{2}(e+fx)\right]^3 \left( -e^{ifnx} (6+11n+6n^2+n^3) \operatorname{Hypergeometric2F1}\left[\frac{n}{2}, \frac{3}{2}+n, \frac{2+n}{2}, -e^{2i(e+fx)}\right] + \right. \\ \left. 3 e^{i(e+f(1+n)x)} n (6+5n+n^2) \operatorname{Hypergeometric2F1}\left[\frac{1+n}{2}, \frac{3}{2}+n, \frac{3+n}{2}, -e^{2i(e+fx)}\right] + \right. \\ \left. e^{2ie} n (1+n) \left( -3 e^{if(2+n)x} (3+n) \operatorname{Hypergeometric2F1}\left[\frac{3}{2}+n, \frac{2+n}{2}, \frac{4+n}{2}, -e^{2i(e+fx)}\right] + \right. \right. \\ \left. \left. e^{i(e+f(3+n)x)} (2+n) \operatorname{Hypergeometric2F1}\left[\frac{3}{2}+n, \frac{3+n}{2}, \frac{5+n}{2}, -e^{2i(e+fx)}\right] \right) \right) \\ \operatorname{Sec}[e+fx]^{-\frac{3}{2}-n} (d \operatorname{Sec}[e+fx])^n (a-a \operatorname{Sec}[e+fx])^{3/2}$$

**Problem 328: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int (d \operatorname{Sec}[e+fx])^n \sqrt{a-a \operatorname{Sec}[e+fx]} dx$$

Optimal (type 5, 69 leaves, 3 steps):

$$\left( 2 a \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, 1-n, \frac{3}{2}, 1+\operatorname{Sec}[e+f x]\right] \right. \\ \left. (-\operatorname{Sec}[e+f x])^{-n} (d \operatorname{Sec}[e+f x])^n \operatorname{Tan}[e+f x] \right) / \left( f \sqrt{a-a \operatorname{Sec}[e+f x]} \right)$$

Result (type 5, 236 leaves):

$$\frac{1}{f n (1+n)} 2^{-\frac{1}{2}+n} e^{-\frac{1}{2} i (e+f (1+2 n) x)} \left( \frac{e^{i (e+f x)}}{1+e^{2 i (e+f x)}} \right)^{\frac{1}{2}+n} \left( 1+e^{2 i (e+f x)} \right)^{\frac{1}{2}+n} \\ \operatorname{Csc}\left[\frac{e}{2}+\frac{f x}{2}\right] \left( e^{i f n x} (1+n) \operatorname{Hypergeometric2F1}\left[\frac{n}{2}, \frac{1}{2}+n, \frac{2+n}{2}, -e^{2 i (e+f x)}\right] - \right. \\ \left. e^{i (e+f (1+n) x)} n \operatorname{Hypergeometric2F1}\left[\frac{1}{2}+n, \frac{1+n}{2}, \frac{3+n}{2}, -e^{2 i (e+f x)}\right] \right) \\ \operatorname{Sec}[e+f x]^{-\frac{1}{2}-n} (d \operatorname{Sec}[e+f x])^n \sqrt{a-a \operatorname{Sec}[e+f x]}$$

### Problem 329: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Sec}[e+f x]^n (1+\operatorname{Sec}[e+f x])^m dx$$

Optimal (type 6, 72 leaves, 2 steps):

$$\left( 2^{\frac{1}{2}+m} \operatorname{AppellF1}\left[\frac{1}{2}, 1-n, \frac{1}{2}-m, \frac{3}{2}, 1-\operatorname{Sec}[e+f x], \frac{1}{2} (1-\operatorname{Sec}[e+f x])\right] \operatorname{Tan}[e+f x] \right) / \\ \left( f \sqrt{1+\operatorname{Sec}[e+f x]} \right)$$

Result (type 6, 2246 leaves):

$$\left( 3 \times 2^{1+m} \operatorname{AppellF1}\left[\frac{1}{2}, m+n, 1-n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2} (e+f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2} (e+f x)\right]^2\right] \right. \\ \left. \left( \operatorname{Sec}\left[\frac{1}{2} (e+f x)\right]^2 \right)^{-1+n} \operatorname{Sec}[e+f x]^n \left( \operatorname{Cos}\left[\frac{1}{2} (e+f x)\right]^2 \operatorname{Sec}[e+f x] \right)^{m+n} \right. \\ \left. (1+\operatorname{Sec}[e+f x])^m \operatorname{Tan}\left[\frac{1}{2} (e+f x)\right] \right) / \\ \left( f \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, m+n, 1-n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2} (e+f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2} (e+f x)\right]^2\right] + \right. \right. \\ \left. \left. 2 \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, m+n, 2-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2} (e+f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2} (e+f x)\right]^2\right] + \right. \right. \right. \\ \left. \left. (m+n) \operatorname{AppellF1}\left[\frac{3}{2}, 1+m+n, 1-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2} (e+f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2} (e+f x)\right]^2\right] \right) \right. \\ \left. \operatorname{Tan}\left[\frac{1}{2} (e+f x)\right]^2 \right) \left( \left( 3 \times 2^m \operatorname{AppellF1}\left[\frac{1}{2}, m+n, 1-n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2} (e+f x)\right]^2, \right. \right. \right. \\ \left. \left. -\operatorname{Tan}\left[\frac{1}{2} (e+f x)\right]^2 \right) \left( \operatorname{Sec}\left[\frac{1}{2} (e+f x)\right]^2 \right)^n \left( \operatorname{Cos}\left[\frac{1}{2} (e+f x)\right]^2 \operatorname{Sec}[e+f x] \right)^{m+n} \right) / \\ \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, m+n, 1-n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2} (e+f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2} (e+f x)\right]^2\right] + \right. \\ \left. \left. 2 \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, m+n, 2-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2} (e+f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2} (e+f x)\right]^2\right] + \right. \right. \right.$$



$$\begin{aligned}
 & \left( \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \Bigg) + \\
 & 2 \tan\left[\frac{1}{2}(e+fx)\right]^2 \left( (-1+n) \left( -\frac{3}{5}(2-n) \operatorname{AppellF1}\left[\frac{5}{2}, m+n, 3-n, \frac{7}{2}, \right. \right. \right. \\
 & \quad \left. \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \frac{3}{5} \right. \right. \\
 & \quad \left. \left. (m+n) \operatorname{AppellF1}\left[\frac{5}{2}, 1+m+n, 2-n, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right] \right. \right. \\
 & \quad \left. \left. \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) + (m+n) \left( -\frac{3}{5}(1-n) \operatorname{AppellF1}\left[\frac{5}{2}, 1+m+n, \right. \right. \right. \\
 & \quad \left. \left. \left. 2-n, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[ \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{1}{2}(e+fx)\right] + \frac{3}{5}(1+m+n) \operatorname{AppellF1}\left[\frac{5}{2}, 2+m+n, 1-n, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) \right) \Bigg) \Bigg) / \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, m+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right] + \right. \\
 & \quad 2 \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, m+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right] + \right. \\
 & \quad \left. (m+n) \operatorname{AppellF1}\left[\frac{3}{2}, 1+m+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \right)^2 + \\
 & \left. \left( 3 \times 2^{1+m} (m+n) \operatorname{AppellF1}\left[\frac{1}{2}, m+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right] \right. \right. \\
 & \quad \left. \left. \left( \sec\left[\frac{1}{2}(e+fx)\right]^2 \right)^{-1+n} \left( \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \right)^{-1+m+n} \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(e+fx)\right] \left( -\cos\left[\frac{1}{2}(e+fx)\right] \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right] + \right. \right. \right. \\
 & \quad \left. \left. \left. \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \tan[e+fx] \right) \right) \right) \Bigg) / \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, m+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right] + \right. \\
 & \quad 2 \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, m+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right] + \right. \\
 & \quad \left. (m+n) \operatorname{AppellF1}\left[\frac{3}{2}, 1+m+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \Bigg) \Bigg)
 \end{aligned}$$

**Problem 330: Result more than twice size of optimal antiderivative.**

$$\int (1 - \sec[e+fx])^m \sec[e+fx]^n dx$$

Optimal (type 6, 89 leaves, 2 steps):

$$\left( \sqrt{2} \operatorname{AppellF1} \left[ \frac{1}{2} + m, 1 - n, \frac{1}{2}, \frac{3}{2} + m, 1 - \operatorname{Sec}[e + f x], \frac{1}{2} (1 - \operatorname{Sec}[e + f x]) \right] \right. \\ \left. (1 - \operatorname{Sec}[e + f x])^m \operatorname{Tan}[e + f x] \right) / \left( f (1 + 2m) \sqrt{1 + \operatorname{Sec}[e + f x]} \right)$$

Result (type 6, 2751 leaves):

$$\left( 2 (3 + 2m) \operatorname{AppellF1} \left[ \frac{1}{2} + m, m + n, 1 - n, \frac{3}{2} + m, \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]^2 \right] \right. \\ \left. \left( \operatorname{Sec} \left[ \frac{1}{2} (e + f x) \right]^2 \right)^{-\frac{1}{2} + m + n} (1 - \operatorname{Sec}[e + f x])^m \operatorname{Sec}[e + f x]^n \right. \\ \left. \left( \operatorname{Cos} \left[ \frac{1}{2} (e + f x) \right]^2 \operatorname{Sec}[e + f x] \right)^{m+n} \left( \frac{\operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]}{\sqrt{\operatorname{Sec} \left[ \frac{1}{2} (e + f x) \right]^2}} \right)^{1+2m} \right) \right) / \\ \left( f (1 + 2m) \left( (3 + 2m) \operatorname{AppellF1} \left[ \frac{1}{2} + m, m + n, 1 - n, \frac{3}{2} + m, \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]^2 \right] + \right. \right. \\ \left. \left. 2 \left( (-1 + n) \operatorname{AppellF1} \left[ \frac{3}{2} + m, m + n, 2 - n, \frac{5}{2} + m, \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]^2 \right] + \right. \right. \right. \\ \left. \left. (m + n) \operatorname{AppellF1} \left[ \frac{3}{2} + m, 1 + m + n, 1 - n, \frac{5}{2} + m, \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]^2 \right] \right) \right) \right. \\ \left. \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]^2 \right) \left( \left( 2 (3 + 2m) \left( -\frac{1}{2} + m + n \right) \operatorname{AppellF1} \left[ \frac{1}{2} + m, m + n, 1 - n, \right. \right. \right. \\ \left. \left. \left. \frac{3}{2} + m, \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]^2 \right] \left( \operatorname{Sec} \left[ \frac{1}{2} (e + f x) \right]^2 \right)^{-\frac{1}{2} + m + n} \right. \right. \right. \\ \left. \left. \left. \left( \operatorname{Cos} \left[ \frac{1}{2} (e + f x) \right]^2 \operatorname{Sec}[e + f x] \right)^{m+n} \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right] \left( \frac{\operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]}{\sqrt{\operatorname{Sec} \left[ \frac{1}{2} (e + f x) \right]^2}} \right)^{1+2m} \right) \right) \right) / \\ \left( (1 + 2m) \left( (3 + 2m) \operatorname{AppellF1} \left[ \frac{1}{2} + m, m + n, 1 - n, \frac{3}{2} + m, \operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]^2, \right. \right. \right. \\ \left. \left. \left. -\operatorname{Tan} \left[ \frac{1}{2} (e + f x) \right]^2 \right] + 2 \left( (-1 + n) \operatorname{AppellF1} \left[ \frac{3}{2} + m, m + n, 2 - n, \frac{5}{2} + m, \right. \right. \right. \right. \right.$$

$$\begin{aligned}
 & \left( \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right) + (m+n) \operatorname{AppellF1}\left[\frac{3}{2}+m, 1+m+n, 1-n, \frac{5}{2}+m, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) + \\
 & \left( 2(3+2m) \left(\sec\left[\frac{1}{2}(e+fx)\right]^2\right)^{-\frac{1}{2}+m+n} \left(\cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx]\right)^{m+n} \right. \\
 & \left. \left( \frac{\tan\left[\frac{1}{2}(e+fx)\right]}{\sqrt{\sec\left[\frac{1}{2}(e+fx)\right]^2}} \right)^{1+2m} \left( -\frac{1}{\frac{3}{2}+m} \left(\frac{1}{2}+m\right) (1-n) \operatorname{AppellF1}\left[\frac{3}{2}+m, m+n, 2-n, \frac{5}{2}+m, \right. \right. \right. \\
 & \left. \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \frac{1}{\frac{3}{2}+m} \left(\frac{1}{2}+m\right) (m+n) \operatorname{AppellF1}\left[\frac{3}{2}+m, 1+m+n, 1-n, \frac{5}{2}+m, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \\
 & \left. \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) \right) \right) / \left( (1+2m) \right. \\
 & \left. \left( (3+2m) \operatorname{AppellF1}\left[\frac{1}{2}+m, m+n, 1-n, \frac{3}{2}+m, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \\
 & \left. \left. 2 \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}+m, m+n, 2-n, \frac{5}{2}+m, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \right. \\
 & \left. \left. \left. (m+n) \operatorname{AppellF1}\left[\frac{3}{2}+m, 1+m+n, 1-n, \frac{5}{2}+m, \right. \right. \right. \right. \\
 & \left. \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \right) + \\
 & \left( 2(3+2m) \operatorname{AppellF1}\left[\frac{1}{2}+m, m+n, 1-n, \frac{3}{2}+m, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \left. \left( \sec\left[\frac{1}{2}(e+fx)\right]^2 \right)^{-\frac{1}{2}+m+n} \left( \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \right)^{m+n} \right. \\
 & \left. \left( \frac{\tan\left[\frac{1}{2}(e+fx)\right]}{\sqrt{\sec\left[\frac{1}{2}(e+fx)\right]^2}} \right)^{2m} \left( \frac{1}{2} \sqrt{\sec\left[\frac{1}{2}(e+fx)\right]^2} - \frac{\tan\left[\frac{1}{2}(e+fx)\right]^2}{2\sqrt{\sec\left[\frac{1}{2}(e+fx)\right]^2}} \right) \right) \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( (3+2m) \operatorname{AppellF1}\left[\frac{1}{2}+m, m+n, 1-n, \frac{3}{2}+m, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & 2 \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}+m, m+n, 2-n, \frac{5}{2}+m, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad (m+n) \operatorname{AppellF1}\left[\frac{3}{2}+m, 1+m+n, 1-n, \frac{5}{2}+m, \right. \\
 & \quad \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \left. \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \left. \right) - \\
 & \left( 2 (3+2m) \operatorname{AppellF1}\left[\frac{1}{2}+m, m+n, 1-n, \frac{3}{2}+m, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \quad \left. \left( \sec\left[\frac{1}{2}(e+fx)\right]^2 \right)^{-\frac{1}{2}+m+n} \left( \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \right)^{m+n} \left( \frac{\tan\left[\frac{1}{2}(e+fx)\right]}{\sqrt{\sec\left[\frac{1}{2}(e+fx)\right]^2}} \right)^{1+2m} \right. \right. \\
 & \quad \left. \left( 2 \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}+m, m+n, 2-n, \frac{5}{2}+m, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \right. \\
 & \quad \quad (m+n) \operatorname{AppellF1}\left[\frac{3}{2}+m, 1+m+n, 1-n, \frac{5}{2}+m, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \right. \\
 & \quad (3+2m) \left( -\frac{1}{\frac{3}{2}+m} \left(\frac{1}{2}+m\right) (1-n) \operatorname{AppellF1}\left[\frac{3}{2}+m, m+n, 2-n, \frac{5}{2}+m, \right. \right. \\
 & \quad \quad \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \\
 & \quad \left. \frac{1}{\frac{3}{2}+m} \left(\frac{1}{2}+m\right) (m+n) \operatorname{AppellF1}\left[\frac{3}{2}+m, 1+m+n, 1-n, \frac{5}{2}+m, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) \right) + \\
 & 2 \tan\left[\frac{1}{2}(e+fx)\right]^2 \left( (-1+n) \left( -\frac{1}{\frac{5}{2}+m} \left(\frac{3}{2}+m\right) (2-n) \operatorname{AppellF1}\left[\frac{5}{2}+m, m+n, 3-n, \frac{7}{2}+m, \right. \right. \right. \\
 & \quad \quad \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \\
 & \quad \left. \frac{1}{\frac{5}{2}+m} \left(\frac{3}{2}+m\right) (m+n) \operatorname{AppellF1}\left[\frac{5}{2}+m, 1+m+n, 2-n, \frac{7}{2}+m, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) \right) + (m+n)
 \end{aligned}$$

$$\begin{aligned}
 & \left( -\frac{1}{\frac{5}{2}+m} \left( \frac{3}{2}+m \right) (1-n) \operatorname{AppellF1} \left[ \frac{5}{2}+m, 1+m+n, 2-n, \frac{7}{2}+m, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right] + \frac{1}{\frac{5}{2}+m} \right. \\
 & \quad \left. \left( \frac{3}{2}+m \right) (1+m+n) \operatorname{AppellF1} \left[ \frac{5}{2}+m, 2+m+n, 1-n, \frac{7}{2}+m, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right] \right) \right) \Bigg/ \\
 & \left( (1+2m) \left( (3+2m) \operatorname{AppellF1} \left[ \frac{1}{2}+m, m+n, 1-n, \frac{3}{2}+m, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right] + 2 \left( (-1+n) \operatorname{AppellF1} \left[ \frac{3}{2}+m, m+n, 2-n, \frac{5}{2}+m, \right. \right. \right. \right. \\
 & \quad \left. \left. \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right] + (m+n) \operatorname{AppellF1} \left[ \frac{3}{2}+m, 1+m+n, \right. \right. \right. \\
 & \quad \left. \left. \left. 1-n, \frac{5}{2}+m, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right) \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right)^2 \right) + \\
 & \left( 2(3+2m)(m+n) \operatorname{AppellF1} \left[ \frac{1}{2}+m, m+n, 1-n, \frac{3}{2}+m, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right] \left( \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \right)^{-\frac{1}{2}+m+n} \right. \\
 & \quad \left. \left( \operatorname{Cos} \left[ \frac{1}{2} (e+fx) \right]^2 \operatorname{Sec} [e+fx] \right)^{-1+m+n} \left( \frac{\operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]}{\sqrt{\operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2}} \right)^{1+2m} \right. \right. \\
 & \quad \left. \left. \left( -\operatorname{Cos} \left[ \frac{1}{2} (e+fx) \right] \operatorname{Sec} [e+fx] \operatorname{Sin} \left[ \frac{1}{2} (e+fx) \right] + \right. \right. \right. \\
 & \quad \left. \left. \left. \operatorname{Cos} \left[ \frac{1}{2} (e+fx) \right]^2 \operatorname{Sec} [e+fx] \operatorname{Tan} [e+fx] \right) \right) \right) \Bigg/ \left( (1+2m) \right. \\
 & \left( (3+2m) \operatorname{AppellF1} \left[ \frac{1}{2}+m, m+n, 1-n, \frac{3}{2}+m, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right] + \right. \\
 & \quad \left. 2 \left( (-1+n) \operatorname{AppellF1} \left[ \frac{3}{2}+m, m+n, 2-n, \frac{5}{2}+m, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right) + \right.
 \end{aligned}$$



$$(m+n) \operatorname{AppellF1}\left[\frac{3}{2}+m, 1+m+n, 1-n, \frac{5}{2}+m, \right. \\ \left. \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \Bigg) \Bigg)$$

### Problem 331: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Sec}[e+fx]^n (a+a \operatorname{Sec}[e+fx])^m dx$$

Optimal (type 6, 88 leaves, 3 steps):

$$\frac{1}{f} 2^{\frac{1}{2}+m} \operatorname{AppellF1}\left[\frac{1}{2}, 1-n, \frac{1}{2}-m, \frac{3}{2}, 1-\operatorname{Sec}[e+fx], \frac{1}{2}(1-\operatorname{Sec}[e+fx])\right] \\ (1+\operatorname{Sec}[e+fx])^{-\frac{1}{2}-m} (a+a \operatorname{Sec}[e+fx])^m \operatorname{Tan}[e+fx]$$

Result (type 6, 2248 leaves):

$$\left(3 \times 2^{1+m} \operatorname{AppellF1}\left[\frac{1}{2}, m+n, 1-n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\ \left. \left(\operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2\right)^{-1+n} \operatorname{Sec}[e+fx]^n \left(\operatorname{Cos}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Sec}[e+fx]\right)^{m+n} \right. \\ \left. (a(1+\operatorname{Sec}[e+fx]))^m \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right) / \\ \left(f \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, m+n, 1-n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \\ \left. 2 \left((-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, m+n, 2-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \\ \left. \left.(m+n) \operatorname{AppellF1}\left[\frac{3}{2}, 1+m+n, 1-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right]\right) \right. \\ \left. \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right) \left(\left(3 \times 2^m \operatorname{AppellF1}\left[\frac{1}{2}, m+n, 1-n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \\ \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \left(\operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2\right)^n \left(\operatorname{Cos}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Sec}[e+fx]\right)^{m+n}\right) / \right. \\ \left. \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, m+n, 1-n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \\ \left. 2 \left((-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, m+n, 2-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \\ \left. \left.(m+n) \operatorname{AppellF1}\left[\frac{3}{2}, 1+m+n, 1-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \\ \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right) + \\ \left. \left(3 \times 2^{1+m} (-1+n) \operatorname{AppellF1}\left[\frac{1}{2}, m+n, 1-n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right]\right)$$

$$\begin{aligned}
 & \left( \sec\left[\frac{1}{2}(e+fx)\right]^2 \right)^{-1+n} \left( \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \right)^{m+n} \tan\left[\frac{1}{2}(e+fx)\right]^2 \Big/ \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, m+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & 2 \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, m+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & (m+n) \operatorname{AppellF1}\left[\frac{3}{2}, 1+m+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \\
 & \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \Big) + \\
 & \left( 3 \times 2^{1+m} \left( \sec\left[\frac{1}{2}(e+fx)\right]^2 \right)^{-1+n} \left( \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \right)^{m+n} \tan\left[\frac{1}{2}(e+fx)\right] \right. \\
 & \left( -\frac{1}{3}(1-n) \operatorname{AppellF1}\left[\frac{3}{2}, m+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \left. \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \frac{1}{3}(m+n) \operatorname{AppellF1}\left[\frac{3}{2}, 1+m+n, 1-n, \frac{5}{2}, \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) \Big) \Big/ \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, m+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & 2 \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, m+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & (m+n) \operatorname{AppellF1}\left[\frac{3}{2}, 1+m+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \\
 & \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \Big) - \\
 & \left( 3 \times 2^{1+m} \operatorname{AppellF1}\left[\frac{1}{2}, m+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \left( \sec\left[\frac{1}{2}(e+fx)\right]^2 \right)^{-1+n} \left( \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \right)^{m+n} \tan\left[\frac{1}{2}(e+fx)\right] \\
 & \left( 2 \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, m+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \\
 & \left. \left. (m+n) \operatorname{AppellF1}\left[\frac{3}{2}, 1+m+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \right. \\
 & \left. \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \right. \\
 & 3 \left( -\frac{1}{3}(1-n) \operatorname{AppellF1}\left[\frac{3}{2}, m+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \left. \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \frac{1}{3}(m+n) \operatorname{AppellF1}\left[\frac{3}{2}, 1+m+n, 1-n, \frac{5}{2}, \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) \Big) + \\
 & 2 \tan\left[\frac{1}{2}(e+fx)\right]^2 \left( (-1+n) \left( -\frac{3}{5}(2-n) \operatorname{AppellF1}\left[\frac{5}{2}, m+n, 3-n, \frac{7}{2}, \right. \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \frac{3}{5} \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & (m+n) \operatorname{AppellF1}\left[\frac{5}{2}, 1+m+n, 2-n, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \\
 & \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + (m+n) \left(-\frac{3}{5}(1-n) \operatorname{AppellF1}\left[\frac{5}{2}, 1+m+n, \right. \right. \\
 & \left. \left. 2-n, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right. \\
 & \left. + \frac{3}{5}(1+m+n) \operatorname{AppellF1}\left[\frac{5}{2}, 2+m+n, 1-n, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right]\right)\right) \Big/ \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, m+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \left. 2 \left((-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, m+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \\
 & \left. (m+n) \operatorname{AppellF1}\left[\frac{3}{2}, 1+m+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \tan\left[\frac{1}{2}(e+fx)\right]^2\right)\right) \\
 & \left(3 \times 2^{1+m} (m+n) \operatorname{AppellF1}\left[\frac{1}{2}, m+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \left. \left(\operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2\right)^{-1+n} \left(\cos\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Sec}[e+fx]\right)^{-1+m+n} \right. \\
 & \left. \tan\left[\frac{1}{2}(e+fx)\right] \left(-\cos\left[\frac{1}{2}(e+fx)\right] \operatorname{Sec}[e+fx] \sin\left[\frac{1}{2}(e+fx)\right] + \right. \right. \\
 & \left. \left. \cos\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Sec}[e+fx] \tan[e+fx]\right)\right) \Big/ \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, m+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \left. 2 \left((-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, m+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \\
 & \left. (m+n) \operatorname{AppellF1}\left[\frac{3}{2}, 1+m+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \tan\left[\frac{1}{2}(e+fx)\right]^2\right)\right) \Big)
 \end{aligned}$$

### Problem 332: Unable to integrate problem.

$$\int \operatorname{Sec}[e+fx]^n (a - a \operatorname{Sec}[e+fx])^m dx$$

Optimal (type 6, 90 leaves, 3 steps):

$$\begin{aligned}
 & \left(\sqrt{2} \operatorname{AppellF1}\left[\frac{1}{2}, m, 1-n, \frac{1}{2}, \frac{3}{2}, m, 1 - \operatorname{Sec}[e+fx], \frac{1}{2}(1 - \operatorname{Sec}[e+fx])\right] \right. \\
 & \left. (a - a \operatorname{Sec}[e+fx])^m \tan[e+fx]\right) \Big/ \left(f(1+2m) \sqrt{1 + \operatorname{Sec}[e+fx]}\right)
 \end{aligned}$$

Result (type 8, 24 leaves):

$$\int \text{Sec}[e + f x]^n (a - a \text{Sec}[e + f x])^m dx$$

**Problem 333: Result more than twice size of optimal antiderivative.**

$$\int (-\text{Sec}[e + f x])^n (1 + \text{Sec}[e + f x])^m dx$$

Optimal (type 6, 85 leaves, 2 steps):

$$\left( \sqrt{2} \text{AppellF1}\left[\frac{1}{2} + m, 1 - n, \frac{1}{2}, \frac{3}{2} + m, 1 + \text{Sec}[e + f x], \frac{1}{2} (1 + \text{Sec}[e + f x])\right] \right. \\ \left. (1 + \text{Sec}[e + f x])^m \text{Tan}[e + f x] \right) / \left( f (1 + 2m) \sqrt{1 - \text{Sec}[e + f x]} \right)$$

Result (type 6, 2248 leaves):

$$\left( 3 \times 2^{1+m} \text{AppellF1}\left[\frac{1}{2}, m + n, 1 - n, \frac{3}{2}, \text{Tan}\left[\frac{1}{2} (e + f x)\right]^2, -\text{Tan}\left[\frac{1}{2} (e + f x)\right]^2\right] \right. \\ \left( \text{Sec}\left[\frac{1}{2} (e + f x)\right]^2 \right)^{-1+n} (-\text{Sec}[e + f x])^n \\ \left( \text{Cos}\left[\frac{1}{2} (e + f x)\right]^2 \text{Sec}[e + f x] \right)^{m+n} (1 + \text{Sec}[e + f x])^m \text{Tan}\left[\frac{1}{2} (e + f x)\right] \right) / \\ \left( f \left( 3 \text{AppellF1}\left[\frac{1}{2}, m + n, 1 - n, \frac{3}{2}, \text{Tan}\left[\frac{1}{2} (e + f x)\right]^2, -\text{Tan}\left[\frac{1}{2} (e + f x)\right]^2\right] + \right. \right. \\ 2 \left( (-1 + n) \text{AppellF1}\left[\frac{3}{2}, m + n, 2 - n, \frac{5}{2}, \text{Tan}\left[\frac{1}{2} (e + f x)\right]^2, -\text{Tan}\left[\frac{1}{2} (e + f x)\right]^2\right] + \right. \\ \left. (m + n) \text{AppellF1}\left[\frac{3}{2}, 1 + m + n, 1 - n, \frac{5}{2}, \text{Tan}\left[\frac{1}{2} (e + f x)\right]^2, -\text{Tan}\left[\frac{1}{2} (e + f x)\right]^2\right] \right) \\ \left. \text{Tan}\left[\frac{1}{2} (e + f x)\right]^2 \right) \left( \left( 3 \times 2^m \text{AppellF1}\left[\frac{1}{2}, m + n, 1 - n, \frac{3}{2}, \text{Tan}\left[\frac{1}{2} (e + f x)\right]^2, \right. \right. \right. \\ \left. \left. -\text{Tan}\left[\frac{1}{2} (e + f x)\right]^2 \right) \left( \text{Sec}\left[\frac{1}{2} (e + f x)\right]^2 \right)^n \left( \text{Cos}\left[\frac{1}{2} (e + f x)\right]^2 \text{Sec}[e + f x] \right)^{m+n} \right) / \\ \left( 3 \text{AppellF1}\left[\frac{1}{2}, m + n, 1 - n, \frac{3}{2}, \text{Tan}\left[\frac{1}{2} (e + f x)\right]^2, -\text{Tan}\left[\frac{1}{2} (e + f x)\right]^2\right] + \right. \\ 2 \left( (-1 + n) \text{AppellF1}\left[\frac{3}{2}, m + n, 2 - n, \frac{5}{2}, \text{Tan}\left[\frac{1}{2} (e + f x)\right]^2, -\text{Tan}\left[\frac{1}{2} (e + f x)\right]^2\right] + \right. \\ \left. (m + n) \text{AppellF1}\left[\frac{3}{2}, 1 + m + n, 1 - n, \frac{5}{2}, \text{Tan}\left[\frac{1}{2} (e + f x)\right]^2, \right. \right. \\ \left. \left. -\text{Tan}\left[\frac{1}{2} (e + f x)\right]^2 \right) \right) \text{Tan}\left[\frac{1}{2} (e + f x)\right]^2 \right) + \\ \left( 3 \times 2^{1+m} (-1 + n) \text{AppellF1}\left[\frac{1}{2}, m + n, 1 - n, \frac{3}{2}, \text{Tan}\left[\frac{1}{2} (e + f x)\right]^2, -\text{Tan}\left[\frac{1}{2} (e + f x)\right]^2\right] \right. \\ \left( \text{Sec}\left[\frac{1}{2} (e + f x)\right]^2 \right)^{-1+n} \left( \text{Cos}\left[\frac{1}{2} (e + f x)\right]^2 \text{Sec}[e + f x] \right)^{m+n} \text{Tan}\left[\frac{1}{2} (e + f x)\right]^2 \right) / \\ \left( 3 \text{AppellF1}\left[\frac{1}{2}, m + n, 1 - n, \frac{3}{2}, \text{Tan}\left[\frac{1}{2} (e + f x)\right]^2, -\text{Tan}\left[\frac{1}{2} (e + f x)\right]^2\right] + \right. \\ 2 \left( (-1 + n) \text{AppellF1}\left[\frac{3}{2}, m + n, 2 - n, \frac{5}{2}, \text{Tan}\left[\frac{1}{2} (e + f x)\right]^2, -\text{Tan}\left[\frac{1}{2} (e + f x)\right]^2\right] + \right. \\ \left. (m + n) \text{AppellF1}\left[\frac{3}{2}, 1 + m + n, 1 - n, \frac{5}{2}, \text{Tan}\left[\frac{1}{2} (e + f x)\right]^2, -\text{Tan}\left[\frac{1}{2} (e + f x)\right]^2\right] \right) \right)$$

$$\begin{aligned}
 & (m+n) \operatorname{AppellF1}\left[\frac{3}{2}, 1+m+n, 1-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right. \\
 & \quad \left. -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 + \\
 & \left(3 \times 2^{1+m} \left(\operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2\right)^{-1+n} \left(\operatorname{Cos}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Sec}[e+fx]\right)^{m+n} \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \right. \\
 & \quad \left(-\frac{1}{3}(1-n) \operatorname{AppellF1}\left[\frac{3}{2}, m+n, 2-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] + \frac{1}{3}(m+n) \operatorname{AppellF1}\left[\frac{3}{2}, 1+m+n, 1-n, \frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)\right) / \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, m+n, 1-n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad 2 \left(\left(-1+n\right) \operatorname{AppellF1}\left[\frac{3}{2}, m+n, 2-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left.(m+n) \operatorname{AppellF1}\left[\frac{3}{2}, 1+m+n, 1-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right) - \\
 & \left(3 \times 2^{1+m} \operatorname{AppellF1}\left[\frac{1}{2}, m+n, 1-n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \quad \left.\left(\operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2\right)^{-1+n} \left(\operatorname{Cos}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Sec}[e+fx]\right)^{m+n} \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \right. \\
 & \quad \left. 2 \left(\left(-1+n\right) \operatorname{AppellF1}\left[\frac{3}{2}, m+n, 2-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \\
 & \quad \left. \left.(m+n) \operatorname{AppellF1}\left[\frac{3}{2}, 1+m+n, 1-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right)\right) + \\
 & \quad \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] + \\
 & \quad 3 \left(-\frac{1}{3}(1-n) \operatorname{AppellF1}\left[\frac{3}{2}, m+n, 2-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] + \frac{1}{3}(m+n) \operatorname{AppellF1}\left[\frac{3}{2}, 1+m+n, 1-n, \frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right) + \\
 & \quad 2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \left(\left(-1+n\right) \left(-\frac{3}{5}(2-n) \operatorname{AppellF1}\left[\frac{5}{2}, m+n, 3-n, \frac{7}{2}, \right. \right. \right. \\
 & \quad \left. \left. \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] + \frac{3}{5} \right. \right. \\
 & \quad \left. \left.(m+n) \operatorname{AppellF1}\left[\frac{5}{2}, 1+m+n, 2-n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \\
 & \quad \left. \left. \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right) + (m+n) \left(-\frac{3}{5}(1-n) \operatorname{AppellF1}\left[\frac{5}{2}, 1+m+n, \right. \right. \right. \\
 & \quad \left. \left. 2-n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \right.
 \end{aligned}$$

$$\begin{aligned}
& \frac{1}{2} (e + f x) + \frac{3}{5} (1 + m + n) \operatorname{AppellF1}\left[\frac{5}{2}, 2 + m + n, 1 - n, \frac{7}{2}, \tan\left[\frac{1}{2} (e + f x)\right]^2, \right. \\
& \left. -\tan\left[\frac{1}{2} (e + f x)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2} (e + f x)\right]^2 \tan\left[\frac{1}{2} (e + f x)\right]\right] \Big/ \\
& \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, m + n, 1 - n, \frac{3}{2}, \tan\left[\frac{1}{2} (e + f x)\right]^2, -\tan\left[\frac{1}{2} (e + f x)\right]^2\right] + \right. \\
& 2 \left( (-1 + n) \operatorname{AppellF1}\left[\frac{3}{2}, m + n, 2 - n, \frac{5}{2}, \tan\left[\frac{1}{2} (e + f x)\right]^2, -\tan\left[\frac{1}{2} (e + f x)\right]^2\right] + \right. \\
& (m + n) \operatorname{AppellF1}\left[\frac{3}{2}, 1 + m + n, 1 - n, \frac{5}{2}, \tan\left[\frac{1}{2} (e + f x)\right]^2, \right. \\
& \left. \left. -\tan\left[\frac{1}{2} (e + f x)\right]^2\right] \right) \tan\left[\frac{1}{2} (e + f x)\right]^2 \Big/ \\
& \left( 3 \times 2^{1+m} (m + n) \operatorname{AppellF1}\left[\frac{1}{2}, m + n, 1 - n, \frac{3}{2}, \tan\left[\frac{1}{2} (e + f x)\right]^2, -\tan\left[\frac{1}{2} (e + f x)\right]^2\right] \right. \\
& \left. \left( \operatorname{Sec}\left[\frac{1}{2} (e + f x)\right]^2 \right)^{-1+n} \left( \cos\left[\frac{1}{2} (e + f x)\right]^2 \operatorname{Sec}[e + f x] \right)^{-1+m+n} \right. \\
& \tan\left[\frac{1}{2} (e + f x)\right] \left( -\cos\left[\frac{1}{2} (e + f x)\right] \operatorname{Sec}[e + f x] \sin\left[\frac{1}{2} (e + f x)\right] + \right. \\
& \left. \left. \cos\left[\frac{1}{2} (e + f x)\right]^2 \operatorname{Sec}[e + f x] \tan[e + f x] \right) \right) \Big/ \\
& \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, m + n, 1 - n, \frac{3}{2}, \tan\left[\frac{1}{2} (e + f x)\right]^2, -\tan\left[\frac{1}{2} (e + f x)\right]^2\right] + \right. \\
& 2 \left( (-1 + n) \operatorname{AppellF1}\left[\frac{3}{2}, m + n, 2 - n, \frac{5}{2}, \tan\left[\frac{1}{2} (e + f x)\right]^2, -\tan\left[\frac{1}{2} (e + f x)\right]^2\right] + \right. \\
& (m + n) \operatorname{AppellF1}\left[\frac{3}{2}, 1 + m + n, 1 - n, \frac{5}{2}, \tan\left[\frac{1}{2} (e + f x)\right]^2, \right. \\
& \left. \left. -\tan\left[\frac{1}{2} (e + f x)\right]^2\right] \right) \tan\left[\frac{1}{2} (e + f x)\right]^2 \Big/ \right)
\end{aligned}$$

### Problem 334: Result more than twice size of optimal antiderivative.

$$\int (1 - \operatorname{Sec}[e + f x])^m (-\operatorname{Sec}[e + f x])^n dx$$

Optimal (type 6, 70 leaves, 2 steps):

$$\left( 2^{\frac{1}{2}+m} \operatorname{AppellF1}\left[\frac{1}{2}, 1 - n, \frac{1}{2} - m, \frac{3}{2}, 1 + \operatorname{Sec}[e + f x], \frac{1}{2} (1 + \operatorname{Sec}[e + f x])\right] \tan[e + f x] \right) \Big/ \left( f \sqrt{1 - \operatorname{Sec}[e + f x]} \right)$$

Result (type 6, 2753 leaves):

$$\left( 2 (3 + 2m) \operatorname{AppellF1}\left[\frac{1}{2} + m, m + n, 1 - n, \frac{3}{2} + m, \tan\left[\frac{1}{2} (e + f x)\right]^2, -\tan\left[\frac{1}{2} (e + f x)\right]^2\right] \right)$$

$$\begin{aligned}
 & \left( \sec \left[ \frac{1}{2} (e + f x) \right]^2 \right)^{-\frac{1}{2}+m+n} (1 - \sec [e + f x])^m (-\sec [e + f x])^n \\
 & \left( \cos \left[ \frac{1}{2} (e + f x) \right]^2 \sec [e + f x] \right)^{m+n} \left( \frac{\tan \left[ \frac{1}{2} (e + f x) \right]}{\sqrt{\sec \left[ \frac{1}{2} (e + f x) \right]^2}} \right)^{1+2m} \Bigg/ \\
 & \left( f (1+2m) \left( (3+2m) \operatorname{AppellF1} \left[ \frac{1}{2} + m, m+n, 1-n, \frac{3}{2} + m, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] + \right. \right. \\
 & 2 \left( (-1+n) \operatorname{AppellF1} \left[ \frac{3}{2} + m, m+n, 2-n, \frac{5}{2} + m, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] + \right. \\
 & \quad \left. \left. (m+n) \operatorname{AppellF1} \left[ \frac{3}{2} + m, 1+m+n, 1-n, \frac{5}{2} + m, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] \right) \right) \\
 & \tan \left[ \frac{1}{2} (e + f x) \right]^2 \left( \left( 2 (3+2m) \left( -\frac{1}{2} + m+n \right) \operatorname{AppellF1} \left[ \frac{1}{2} + m, m+n, 1-n, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{3}{2} + m, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] \left( \sec \left[ \frac{1}{2} (e + f x) \right]^2 \right)^{-\frac{1}{2}+m+n} \right. \right. \\
 & \quad \left. \left. \left( \cos \left[ \frac{1}{2} (e + f x) \right]^2 \sec [e + f x] \right)^{m+n} \tan \left[ \frac{1}{2} (e + f x) \right] \left( \frac{\tan \left[ \frac{1}{2} (e + f x) \right]}{\sqrt{\sec \left[ \frac{1}{2} (e + f x) \right]^2}} \right)^{1+2m} \right) \right) \Bigg/ \\
 & \left( (1+2m) \left( (3+2m) \operatorname{AppellF1} \left[ \frac{1}{2} + m, m+n, 1-n, \frac{3}{2} + m, \tan \left[ \frac{1}{2} (e + f x) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] + 2 \left( (-1+n) \operatorname{AppellF1} \left[ \frac{3}{2} + m, m+n, 2-n, \frac{5}{2} + m, \right. \right. \right. \\
 & \quad \left. \left. \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] + (m+n) \operatorname{AppellF1} \left[ \frac{3}{2} + m, 1+m+n, 1-n, \right. \right. \\
 & \quad \left. \left. \frac{5}{2} + m, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (e + f x) \right]^2 \right) + \\
 & \left( 2 (3+2m) \left( \sec \left[ \frac{1}{2} (e + f x) \right]^2 \right)^{-\frac{1}{2}+m+n} \left( \cos \left[ \frac{1}{2} (e + f x) \right]^2 \sec [e + f x] \right)^{m+n} \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( \frac{\tan\left[\frac{1}{2}(e+fx)\right]}{\sqrt{\sec\left[\frac{1}{2}(e+fx)\right]^2}} \right)^{1+2m} \left( -\frac{1}{\frac{3}{2}+m} \left(\frac{1}{2}+m\right) (1-n) \operatorname{AppellF1}\left[\frac{3}{2}+m, m+n, 2-n, \frac{5}{2}+m, \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \right. \\
 & \quad \left. \frac{1}{\frac{3}{2}+m} \left(\frac{1}{2}+m\right) (m+n) \operatorname{AppellF1}\left[\frac{3}{2}+m, 1+m+n, 1-n, \frac{5}{2}+m, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) \right) / \left( (1+2m) \right. \\
 & \quad \left. \left( (3+2m) \operatorname{AppellF1}\left[\frac{1}{2}+m, m+n, 1-n, \frac{3}{2}+m, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. 2 \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}+m, m+n, 2-n, \frac{5}{2}+m, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \right. \\
 & \quad \left. \left. (m+n) \operatorname{AppellF1}\left[\frac{3}{2}+m, 1+m+n, 1-n, \frac{5}{2}+m, \right. \right. \right. \\
 & \quad \left. \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \right) \right) + \\
 & \quad \left( 2(3+2m) \operatorname{AppellF1}\left[\frac{1}{2}+m, m+n, 1-n, \frac{3}{2}+m, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \\
 & \quad \left( \sec\left[\frac{1}{2}(e+fx)\right]^2 \right)^{-\frac{1}{2}+m+n} \left( \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \right)^{m+n} \\
 & \quad \left( \frac{\tan\left[\frac{1}{2}(e+fx)\right]}{\sqrt{\sec\left[\frac{1}{2}(e+fx)\right]^2}} \right)^{2m} \left( \frac{1}{2} \sqrt{\sec\left[\frac{1}{2}(e+fx)\right]^2} - \frac{\tan\left[\frac{1}{2}(e+fx)\right]^2}{2\sqrt{\sec\left[\frac{1}{2}(e+fx)\right]^2}} \right) / \\
 & \quad \left( (3+2m) \operatorname{AppellF1}\left[\frac{1}{2}+m, m+n, 1-n, \frac{3}{2}+m, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left. 2 \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}+m, m+n, 2-n, \frac{5}{2}+m, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. (m+n) \operatorname{AppellF1}\left[\frac{3}{2}+m, 1+m+n, 1-n, \frac{5}{2}+m, \right. \right. \right. \\
 & \quad \left. \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \right) -
 \end{aligned}$$



$$\left( 2 (3+2m) \operatorname{AppellF1} \left[ \frac{1}{2} + m, m+n, 1-n, \frac{3}{2} + m, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right.$$

$$\left. \left( \sec \left[ \frac{1}{2} (e+fx) \right]^2 \right)^{-\frac{1}{2}+m+n} \left( \cos \left[ \frac{1}{2} (e+fx) \right]^2 \sec [e+fx] \right)^{m+n} \left( \frac{\tan \left[ \frac{1}{2} (e+fx) \right]}{\sqrt{\sec \left[ \frac{1}{2} (e+fx) \right]^2}} \right)^{1+2m} \right.$$

$$\left. \left( 2 \left( (-1+n) \operatorname{AppellF1} \left[ \frac{3}{2} + m, m+n, 2-n, \frac{5}{2} + m, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] + \right. \right. \right.$$

$$\left. \left. (m+n) \operatorname{AppellF1} \left[ \frac{3}{2} + m, 1+m+n, 1-n, \frac{5}{2} + m, \tan \left[ \frac{1}{2} (e+fx) \right]^2, \right. \right. \right.$$

$$\left. \left. \left. -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right) \sec \left[ \frac{1}{2} (e+fx) \right]^2 \tan \left[ \frac{1}{2} (e+fx) \right] + \right. \right.$$

$$\left. \left. (3+2m) \left( -\frac{1}{\frac{3}{2} + m} \left( \frac{1}{2} + m \right) (1-n) \operatorname{AppellF1} \left[ \frac{3}{2} + m, m+n, 2-n, \frac{5}{2} + m, \right. \right. \right. \right.$$

$$\left. \left. \left. \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \sec \left[ \frac{1}{2} (e+fx) \right]^2 \tan \left[ \frac{1}{2} (e+fx) \right] + \right. \right. \right.$$

$$\left. \left. \left. \frac{1}{\frac{3}{2} + m} \left( \frac{1}{2} + m \right) (m+n) \operatorname{AppellF1} \left[ \frac{3}{2} + m, 1+m+n, 1-n, \frac{5}{2} + m, \tan \left[ \frac{1}{2} (e+fx) \right]^2, \right. \right. \right. \right.$$

$$\left. \left. \left. \left. -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \sec \left[ \frac{1}{2} (e+fx) \right]^2 \tan \left[ \frac{1}{2} (e+fx) \right] \right) \right) + \right. \right.$$

$$2 \tan \left[ \frac{1}{2} (e+fx) \right]^2 \left( (-1+n) \left( -\frac{1}{\frac{5}{2} + m} \left( \frac{3}{2} + m \right) (2-n) \operatorname{AppellF1} \left[ \frac{5}{2} + m, m+n, 3-n, \frac{7}{2} + m, \right. \right. \right. \right.$$

$$\left. \left. \left. \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \sec \left[ \frac{1}{2} (e+fx) \right]^2 \tan \left[ \frac{1}{2} (e+fx) \right] + \right. \right. \right.$$

$$\left. \left. \left. \frac{1}{\frac{5}{2} + m} \left( \frac{3}{2} + m \right) (m+n) \operatorname{AppellF1} \left[ \frac{5}{2} + m, 1+m+n, 2-n, \frac{7}{2} + m, \tan \left[ \frac{1}{2} (e+fx) \right]^2, \right. \right. \right. \right.$$

$$\left. \left. \left. \left. -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \sec \left[ \frac{1}{2} (e+fx) \right]^2 \tan \left[ \frac{1}{2} (e+fx) \right] \right) \right) + (m+n) \right. \right.$$

$$\left( -\frac{1}{\frac{5}{2} + m} \left( \frac{3}{2} + m \right) (1-n) \operatorname{AppellF1} \left[ \frac{5}{2} + m, 1+m+n, 2-n, \frac{7}{2} + m, \tan \left[ \frac{1}{2} (e+fx) \right]^2, \right. \right. \right.$$

$$\left. \left. \left. -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \sec \left[ \frac{1}{2} (e+fx) \right]^2 \tan \left[ \frac{1}{2} (e+fx) \right] + \frac{1}{\frac{5}{2} + m} \right. \right.$$

$$\left. \left. \left. \left( \frac{3}{2} + m \right) (1+m+n) \operatorname{AppellF1} \left[ \frac{5}{2} + m, 2+m+n, 1-n, \frac{7}{2} + m, \tan \left[ \frac{1}{2} (e+fx) \right]^2, \right. \right. \right. \right.$$

$$\left. \begin{aligned}
 & -\tan\left[\frac{1}{2}(e+fx)\right]^2 \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) \Bigg) / \\
 & \left( (1+2m) \left( (3+2m) \operatorname{AppellF1}\left[\frac{1}{2}+m, m+n, 1-n, \frac{3}{2}+m, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + 2 \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}+m, m+n, 2-n, \frac{5}{2}+m, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + (m+n) \operatorname{AppellF1}\left[\frac{3}{2}+m, 1+m+n, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. 1-n, \frac{5}{2}+m, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \right)^2 \right) + \\
 & \left( 2(3+2m)(m+n) \operatorname{AppellF1}\left[\frac{1}{2}+m, m+n, 1-n, \frac{3}{2}+m, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \left( \sec\left[\frac{1}{2}(e+fx)\right]^2 \right)^{-\frac{1}{2}+m+n} \right. \right. \\
 & \quad \left. \left. \left. \left( \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \right)^{-1+m+n} \left( \frac{\tan\left[\frac{1}{2}(e+fx)\right]}{\sqrt{\sec\left[\frac{1}{2}(e+fx)\right]^2}} \right)^{1+2m} \right. \right. \right. \\
 & \quad \left. \left. \left. \left( -\cos\left[\frac{1}{2}(e+fx)\right] \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right] + \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \left. \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \tan[e+fx] \right) \right) \right) / \left( (1+2m) \right. \right. \\
 & \quad \left( (3+2m) \operatorname{AppellF1}\left[\frac{1}{2}+m, m+n, 1-n, \frac{3}{2}+m, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad 2 \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}+m, m+n, 2-n, \frac{5}{2}+m, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left. (m+n) \operatorname{AppellF1}\left[\frac{3}{2}+m, 1+m+n, 1-n, \frac{5}{2}+m, \right. \right. \\
 & \quad \left. \left. \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \right) \right) \Bigg) \Bigg)
 \end{aligned} \right.$$

### Problem 335: Result more than twice size of optimal antiderivative.

$$\int (-\operatorname{Sec}[e + f x])^n (a + a \operatorname{Sec}[e + f x])^m dx$$

Optimal (type 6, 87 leaves, 3 steps):

$$\left( \sqrt{2} \operatorname{AppellF1}\left[\frac{1}{2} + m, 1 - n, \frac{1}{2}, \frac{3}{2} + m, 1 + \operatorname{Sec}[e + f x], \frac{1}{2} (1 + \operatorname{Sec}[e + f x])\right] \right. \\ \left. (a + a \operatorname{Sec}[e + f x])^m \operatorname{Tan}[e + f x] \right) / \left( f (1 + 2m) \sqrt{1 - \operatorname{Sec}[e + f x]} \right)$$

Result (type 6, 2250 leaves):

$$\left( 3 \times 2^{1+m} \operatorname{AppellF1}\left[\frac{1}{2}, m + n, 1 - n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]^2\right] \right. \\ \left. \left( \operatorname{Sec}\left[\frac{1}{2} (e + f x)\right]^2 \right)^{-1+n} (-\operatorname{Sec}[e + f x])^n \left( \operatorname{Cos}\left[\frac{1}{2} (e + f x)\right]^2 \operatorname{Sec}[e + f x] \right)^{m+n} \right. \\ \left. (a (1 + \operatorname{Sec}[e + f x]))^m \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right] \right) / \\ \left( f \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, m + n, 1 - n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]^2\right] + \right. \right. \\ 2 \left( (-1 + n) \operatorname{AppellF1}\left[\frac{3}{2}, m + n, 2 - n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]^2\right] + \right. \\ \left. (m + n) \operatorname{AppellF1}\left[\frac{3}{2}, 1 + m + n, 1 - n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]^2\right] \right) \\ \left. \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]^2 \right) \left( \left( 3 \times 2^m \operatorname{AppellF1}\left[\frac{1}{2}, m + n, 1 - n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]^2, \right. \right. \right. \\ \left. \left. -\operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]^2 \right) \left( \operatorname{Sec}\left[\frac{1}{2} (e + f x)\right]^2 \right)^n \left( \operatorname{Cos}\left[\frac{1}{2} (e + f x)\right]^2 \operatorname{Sec}[e + f x] \right)^{m+n} \right) \right) / \\ \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, m + n, 1 - n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]^2\right] + \right. \\ 2 \left( (-1 + n) \operatorname{AppellF1}\left[\frac{3}{2}, m + n, 2 - n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]^2\right] + \right. \\ \left. (m + n) \operatorname{AppellF1}\left[\frac{3}{2}, 1 + m + n, 1 - n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]^2, \right. \right. \\ \left. \left. -\operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]^2 \right) \right) \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]^2 \right) + \\ \left( 3 \times 2^{1+m} (-1 + n) \operatorname{AppellF1}\left[\frac{1}{2}, m + n, 1 - n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]^2\right] \right. \\ \left. \left( \operatorname{Sec}\left[\frac{1}{2} (e + f x)\right]^2 \right)^{-1+n} \left( \operatorname{Cos}\left[\frac{1}{2} (e + f x)\right]^2 \operatorname{Sec}[e + f x] \right)^{m+n} \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]^2 \right) / \\ \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, m + n, 1 - n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]^2\right] + \right. \\ 2 \left( (-1 + n) \operatorname{AppellF1}\left[\frac{3}{2}, m + n, 2 - n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]^2\right] + \right. \\ \left. (m + n) \operatorname{AppellF1}\left[\frac{3}{2}, 1 + m + n, 1 - n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]^2, \right. \right. \\ \left. \left. -\operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]^2 \right) \right) \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]^2 \right)$$

$$\begin{aligned}
 & -\tan\left[\frac{1}{2}(e+fx)\right]^2\right)\tan\left[\frac{1}{2}(e+fx)\right]^2\right) + \\
 & \left(3 \times 2^{1+m}\left(\sec\left[\frac{1}{2}(e+fx)\right]^2\right)^{-1+n}\left(\cos\left[\frac{1}{2}(e+fx)\right]^2\sec[e+fx]\right)^{m+n}\tan\left[\frac{1}{2}(e+fx)\right]\right. \\
 & \left(-\frac{1}{3}(1-n)\operatorname{AppellF1}\left[\frac{3}{2}, m+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right]\right. \\
 & \left.\sec\left[\frac{1}{2}(e+fx)\right]^2\tan\left[\frac{1}{2}(e+fx)\right]+\frac{1}{3}(m+n)\operatorname{AppellF1}\left[\frac{3}{2}, 1+m+n, 1-n, \frac{5}{2},\right.\right. \\
 & \left.\left.\tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right]\sec\left[\frac{1}{2}(e+fx)\right]^2\tan\left[\frac{1}{2}(e+fx)\right]\right)\right) / \\
 & \left(3\operatorname{AppellF1}\left[\frac{1}{2}, m+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right]+ \right. \\
 & \left.2\left((-1+n)\operatorname{AppellF1}\left[\frac{3}{2}, m+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right]+ \right. \right. \\
 & \left.\left.(m+n)\operatorname{AppellF1}\left[\frac{3}{2}, 1+m+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2,\right.\right. \right. \\
 & \left.\left.\left.-\tan\left[\frac{1}{2}(e+fx)\right]^2\right)\tan\left[\frac{1}{2}(e+fx)\right]^2\right)- \right. \right. \\
 & \left.3 \times 2^{1+m}\operatorname{AppellF1}\left[\frac{1}{2}, m+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right]\right. \\
 & \left.\left(\sec\left[\frac{1}{2}(e+fx)\right]^2\right)^{-1+n}\left(\cos\left[\frac{1}{2}(e+fx)\right]^2\sec[e+fx]\right)^{m+n}\tan\left[\frac{1}{2}(e+fx)\right]\right) \\
 & \left(2\left((-1+n)\operatorname{AppellF1}\left[\frac{3}{2}, m+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right]+ \right. \right. \\
 & \left.\left.(m+n)\operatorname{AppellF1}\left[\frac{3}{2}, 1+m+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right]\right)\right) \\
 & \sec\left[\frac{1}{2}(e+fx)\right]^2\tan\left[\frac{1}{2}(e+fx)\right]+ \\
 & 3\left(-\frac{1}{3}(1-n)\operatorname{AppellF1}\left[\frac{3}{2}, m+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right]\right. \\
 & \left.\sec\left[\frac{1}{2}(e+fx)\right]^2\tan\left[\frac{1}{2}(e+fx)\right]+\frac{1}{3}(m+n)\operatorname{AppellF1}\left[\frac{3}{2}, 1+m+n, 1-n, \frac{5}{2},\right.\right. \\
 & \left.\left.\tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right]\sec\left[\frac{1}{2}(e+fx)\right]^2\tan\left[\frac{1}{2}(e+fx)\right]\right)+ \\
 & 2\tan\left[\frac{1}{2}(e+fx)\right]^2\left((-1+n)\left(-\frac{3}{5}(2-n)\operatorname{AppellF1}\left[\frac{5}{2}, m+n, 3-n, \frac{7}{2},\right.\right. \right. \\
 & \left.\left.\tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right]\sec\left[\frac{1}{2}(e+fx)\right]^2\tan\left[\frac{1}{2}(e+fx)\right]+\frac{3}{5}\right. \\
 & \left.\left.(m+n)\operatorname{AppellF1}\left[\frac{5}{2}, 1+m+n, 2-n, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right]\right)\right) \\
 & \sec\left[\frac{1}{2}(e+fx)\right]^2\tan\left[\frac{1}{2}(e+fx)\right]\right)+ (m+n)\left(-\frac{3}{5}(1-n)\operatorname{AppellF1}\left[\frac{5}{2}, 1+m+n,\right.\right. \\
 & \left.\left.2-n, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right]\sec\left[\frac{1}{2}(e+fx)\right]^2\tan\left[\frac{1}{2}(e+fx)\right]^2\right) \\
 & \left.\frac{1}{2}(e+fx)\right]+\frac{3}{5}(1+m+n)\operatorname{AppellF1}\left[\frac{5}{2}, 2+m+n, 1-n, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2,\right.
 \end{aligned}$$

$$\begin{aligned}
 & -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)\right)\right)\right)\right) / \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, m+n, 1-n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad 2 \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, m+n, 2-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \quad (m+n) \operatorname{AppellF1}\left[\frac{3}{2}, 1+m+n, 1-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right. \\
 & \quad \quad \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right)^2 + \\
 & \left. \left(3 \times 2^{1+m} (m+n) \operatorname{AppellF1}\left[\frac{1}{2}, m+n, 1-n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \\
 & \quad \left. \left. \left(\operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2\right)^{-1+n} \left(\operatorname{Cos}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Sec}[e+fx]\right)^{-1+m+n} \right. \right. \\
 & \quad \left. \left. \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \left(-\operatorname{Cos}\left[\frac{1}{2}(e+fx)\right] \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right] + \right. \right. \right. \\
 & \quad \quad \left. \left. \left. \operatorname{Cos}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Sec}[e+fx] \operatorname{Tan}[e+fx]\right)\right)\right)\right) / \right. \\
 & \left. \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, m+n, 1-n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \\
 & \quad 2 \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, m+n, 2-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \quad (m+n) \operatorname{AppellF1}\left[\frac{3}{2}, 1+m+n, 1-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right. \\
 & \quad \quad \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right)\right)
 \end{aligned}$$

### Problem 336: Unable to integrate problem.

$$\int (-\operatorname{Sec}[e+fx])^n (a - a \operatorname{Sec}[e+fx])^m dx$$

Optimal (type 6, 87 leaves, 3 steps):

$$\begin{aligned}
 & \frac{1}{f} 2^{\frac{1}{2}+m} \operatorname{AppellF1}\left[\frac{1}{2}, 1-n, \frac{1}{2}-m, \frac{3}{2}, 1+\operatorname{Sec}[e+fx], \frac{1}{2}(1+\operatorname{Sec}[e+fx])\right] \\
 & (1-\operatorname{Sec}[e+fx])^{-\frac{1}{2}-m} (a - a \operatorname{Sec}[e+fx])^m \operatorname{Tan}[e+fx]
 \end{aligned}$$

Result (type 8, 26 leaves):

$$\int (-\operatorname{Sec}[e+fx])^n (a - a \operatorname{Sec}[e+fx])^m dx$$

### Problem 337: Result more than twice size of optimal antiderivative.

$$\int (d \operatorname{Sec}[e+fx])^n (1 + \operatorname{Sec}[e+fx])^m dx$$

Optimal (type 6, 79 leaves, 2 steps):

$$-\left(\left(\text{AppellF1}\left[n, \frac{1}{2}, \frac{1}{2}-m, 1+n, \text{Sec}[e+fx], -\text{Sec}[e+fx]\right] (d \text{Sec}[e+fx])^n \text{Tan}[e+fx]\right) / \left(f n \sqrt{1-\text{Sec}[e+fx]} \sqrt{1+\text{Sec}[e+fx]}\right)\right)$$

Result (type 6, 2248 leaves):

$$\begin{aligned} & \left(3 \times 2^{1+m} \text{AppellF1}\left[\frac{1}{2}, m+n, 1-n, \frac{3}{2}, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\ & \quad \left(\text{Sec}\left[\frac{1}{2}(e+fx)\right]^2\right)^{-1+n} (d \text{Sec}[e+fx])^n \\ & \quad \left(\text{Cos}\left[\frac{1}{2}(e+fx)\right]^2 \text{Sec}[e+fx]\right)^{m+n} (1+\text{Sec}[e+fx])^m \text{Tan}\left[\frac{1}{2}(e+fx)\right] \Big/ \\ & \left(f \left(3 \text{AppellF1}\left[\frac{1}{2}, m+n, 1-n, \frac{3}{2}, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \\ & \quad 2 \left(\left(-1+n\right) \text{AppellF1}\left[\frac{3}{2}, m+n, 2-n, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\ & \quad \left.(m+n\right) \text{AppellF1}\left[\frac{3}{2}, 1+m+n, 1-n, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \Big) \\ & \quad \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \Big) \left(\left(3 \times 2^m \text{AppellF1}\left[\frac{1}{2}, m+n, 1-n, \frac{3}{2}, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \\ & \quad \left. \left. -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \left(\text{Sec}\left[\frac{1}{2}(e+fx)\right]^2\right)^n \left(\text{Cos}\left[\frac{1}{2}(e+fx)\right]^2 \text{Sec}[e+fx]\right)^{m+n}\right) \Big/ \\ & \quad \left(3 \text{AppellF1}\left[\frac{1}{2}, m+n, 1-n, \frac{3}{2}, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\ & \quad 2 \left(\left(-1+n\right) \text{AppellF1}\left[\frac{3}{2}, m+n, 2-n, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\ & \quad \left.(m+n\right) \text{AppellF1}\left[\frac{3}{2}, 1+m+n, 1-n, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right. \\ & \quad \left. -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \Big) \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \Big) + \\ & \quad \left(3 \times 2^{1+m} \left(-1+n\right) \text{AppellF1}\left[\frac{1}{2}, m+n, 1-n, \frac{3}{2}, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\ & \quad \left(\text{Sec}\left[\frac{1}{2}(e+fx)\right]^2\right)^{-1+n} \left(\text{Cos}\left[\frac{1}{2}(e+fx)\right]^2 \text{Sec}[e+fx]\right)^{m+n} \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \Big/ \\ & \quad \left(3 \text{AppellF1}\left[\frac{1}{2}, m+n, 1-n, \frac{3}{2}, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\ & \quad 2 \left(\left(-1+n\right) \text{AppellF1}\left[\frac{3}{2}, m+n, 2-n, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\ & \quad \left.(m+n\right) \text{AppellF1}\left[\frac{3}{2}, 1+m+n, 1-n, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right. \\ & \quad \left. -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \Big) \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \Big) + \\ & \quad \left(3 \times 2^{1+m} \left(\text{Sec}\left[\frac{1}{2}(e+fx)\right]^2\right)^{-1+n} \left(\text{Cos}\left[\frac{1}{2}(e+fx)\right]^2 \text{Sec}[e+fx]\right)^{m+n} \text{Tan}\left[\frac{1}{2}(e+fx)\right] \right. \\ & \quad \left(-\frac{1}{3} (1-n) \text{AppellF1}\left[\frac{3}{2}, m+n, 2-n, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \end{aligned}$$

$$\begin{aligned}
 & \left( \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \text{Tan}\left[\frac{1}{2}(e+fx)\right] + \frac{1}{3}(m+n) \text{AppellF1}\left[\frac{3}{2}, 1+m+n, 1-n, \frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \text{Tan}\left[\frac{1}{2}(e+fx)\right] \right) / \\
 & \left( 3 \text{AppellF1}\left[\frac{1}{2}, m+n, 1-n, \frac{3}{2}, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad 2 \left( (-1+n) \text{AppellF1}\left[\frac{3}{2}, m+n, 2-n, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \quad (m+n) \text{AppellF1}\left[\frac{3}{2}, 1+m+n, 1-n, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right. \\
 & \quad \quad \quad \left. \left. -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right) - \right. \\
 & \left. \left( 3 \times 2^{1+m} \text{AppellF1}\left[\frac{1}{2}, m+n, 1-n, \frac{3}{2}, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \\
 & \quad \left. \left. \left( \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \right)^{-1+n} \left( \text{Cos}\left[\frac{1}{2}(e+fx)\right]^2 \text{Sec}[e+fx] \right)^{m+n} \text{Tan}\left[\frac{1}{2}(e+fx)\right] \right) \right. \\
 & \quad \left. \left( 2 \left( (-1+n) \text{AppellF1}\left[\frac{3}{2}, m+n, 2-n, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \right. \\
 & \quad \quad \left. \left. (m+n) \text{AppellF1}\left[\frac{3}{2}, 1+m+n, 1-n, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \right) \right. \\
 & \quad \left. \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \text{Tan}\left[\frac{1}{2}(e+fx)\right] + \right. \\
 & \quad \left. 3 \left( -\frac{1}{3}(1-n) \text{AppellF1}\left[\frac{3}{2}, m+n, 2-n, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \\
 & \quad \quad \left. \left. \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \text{Tan}\left[\frac{1}{2}(e+fx)\right] + \frac{1}{3}(m+n) \text{AppellF1}\left[\frac{3}{2}, 1+m+n, 1-n, \frac{5}{2}, \right. \right. \right. \\
 & \quad \quad \quad \left. \left. \left. \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \text{Tan}\left[\frac{1}{2}(e+fx)\right] \right) \right) + \right. \\
 & \quad \left. 2 \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \left( (-1+n) \left( -\frac{3}{5}(2-n) \text{AppellF1}\left[\frac{5}{2}, m+n, 3-n, \frac{7}{2}, \right. \right. \right. \right. \\
 & \quad \quad \left. \left. \left. \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \text{Tan}\left[\frac{1}{2}(e+fx)\right] + \frac{3}{5} \right. \right. \right. \\
 & \quad \quad \left. \left. (m+n) \text{AppellF1}\left[\frac{5}{2}, 1+m+n, 2-n, \frac{7}{2}, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \right) \right. \\
 & \quad \left. \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \text{Tan}\left[\frac{1}{2}(e+fx)\right] \right) + (m+n) \left( -\frac{3}{5}(1-n) \text{AppellF1}\left[\frac{5}{2}, 1+m+n, \right. \right. \\
 & \quad \quad \left. \left. 2-n, \frac{7}{2}, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \text{Tan}\left[ \right. \right. \\
 & \quad \quad \quad \left. \left. \frac{1}{2}(e+fx)\right] + \frac{3}{5}(1+m+n) \text{AppellF1}\left[\frac{5}{2}, 2+m+n, 1-n, \frac{7}{2}, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \quad \quad \quad \left. \left. \left. -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \text{Tan}\left[\frac{1}{2}(e+fx)\right] \right) \right) \right) / \\
 & \left( 3 \text{AppellF1}\left[\frac{1}{2}, m+n, 1-n, \frac{3}{2}, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left. 2 \left( (-1+n) \text{AppellF1}\left[\frac{3}{2}, m+n, 2-n, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & (m+n) \operatorname{AppellF1}\left[\frac{3}{2}, 1+m+n, 1-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right. \\
 & \quad \left. -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 + \\
 & \left(3 \times 2^{1+m} (m+n) \operatorname{AppellF1}\left[\frac{1}{2}, m+n, 1-n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \quad \left(\operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2\right)^{-1+n} \left(\operatorname{Cos}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Sec}[e+fx]\right)^{-1+m+n} \\
 & \quad \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \left(-\operatorname{Cos}\left[\frac{1}{2}(e+fx)\right] \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right] + \right. \\
 & \quad \left. \operatorname{Cos}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Sec}[e+fx] \operatorname{Tan}[e+fx]\right) \Big/ \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, m+n, 1-n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad 2 \left((-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, m+n, 2-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad (m+n) \operatorname{AppellF1}\left[\frac{3}{2}, 1+m+n, 1-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right) \Big)
 \end{aligned}$$

**Problem 338: Result more than twice size of optimal antiderivative.**

$$\int (1 - \operatorname{Sec}[e+fx])^m (d \operatorname{Sec}[e+fx])^n dx$$

Optimal (type 6, 79 leaves, 2 steps):

$$- \left( \left( \operatorname{AppellF1}\left[n, \frac{1}{2}-m, \frac{1}{2}, 1+n, \operatorname{Sec}[e+fx], -\operatorname{Sec}[e+fx]\right] (d \operatorname{Sec}[e+fx])^n \operatorname{Tan}[e+fx] \right) \Big/ \left( f n \sqrt{1 - \operatorname{Sec}[e+fx]} \sqrt{1 + \operatorname{Sec}[e+fx]} \right) \right)$$

Result (type 6, 2753 leaves):

$$\left( 2(3+2m) \operatorname{AppellF1}\left[\frac{1}{2}+m, m+n, 1-n, \frac{3}{2}+m, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 \left. \left(\operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2\right)^{-\frac{1}{2}+m+n} (1 - \operatorname{Sec}[e+fx])^m (d \operatorname{Sec}[e+fx])^n \right. \\
 \left. \left(\operatorname{Cos}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Sec}[e+fx]\right)^{m+n} \left(\frac{\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{\sqrt{\operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2}}\right)^{1+2m} \right) \Big/$$



$$\begin{aligned}
 & \left( f (1+2m) \left( (3+2m) \operatorname{AppellF1} \left[ \frac{1}{2}+m, m+n, 1-n, \frac{3}{2}+m, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] + \right. \right. \\
 & 2 \left( (-1+n) \operatorname{AppellF1} \left[ \frac{3}{2}+m, m+n, 2-n, \frac{5}{2}+m, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] + \right. \\
 & \quad \left. \left. (m+n) \operatorname{AppellF1} \left[ \frac{3}{2}+m, 1+m+n, 1-n, \frac{5}{2}+m, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right) \right) \\
 & \tan \left[ \frac{1}{2} (e+fx) \right]^2 \left( \left( 2 (3+2m) \left( -\frac{1}{2}+m+n \right) \operatorname{AppellF1} \left[ \frac{1}{2}+m, m+n, 1-n, \right. \right. \right. \\
 & \quad \left. \left. \frac{3}{2}+m, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \left( \sec \left[ \frac{1}{2} (e+fx) \right]^2 \right)^{-\frac{1}{2}+m+n} \right. \right. \\
 & \quad \left. \left. \left( \cos \left[ \frac{1}{2} (e+fx) \right]^2 \sec [e+fx] \right)^{m+n} \tan \left[ \frac{1}{2} (e+fx) \right] \left( \frac{\tan \left[ \frac{1}{2} (e+fx) \right]}{\sqrt{\sec \left[ \frac{1}{2} (e+fx) \right]^2}} \right)^{1+2m} \right) \right) / \\
 & \left( (1+2m) \left( (3+2m) \operatorname{AppellF1} \left[ \frac{1}{2}+m, m+n, 1-n, \frac{3}{2}+m, \tan \left[ \frac{1}{2} (e+fx) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] + 2 \left( (-1+n) \operatorname{AppellF1} \left[ \frac{3}{2}+m, m+n, 2-n, \frac{5}{2}+m, \right. \right. \right. \\
 & \quad \left. \left. \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] + (m+n) \operatorname{AppellF1} \left[ \frac{3}{2}+m, 1+m+n, 1-n, \right. \right. \\
 & \quad \left. \left. \frac{5}{2}+m, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (e+fx) \right]^2 \right) \right) + \\
 & \left( 2 (3+2m) \left( \sec \left[ \frac{1}{2} (e+fx) \right]^2 \right)^{-\frac{1}{2}+m+n} \left( \cos \left[ \frac{1}{2} (e+fx) \right]^2 \sec [e+fx] \right)^{m+n} \right. \\
 & \quad \left. \left( \frac{\tan \left[ \frac{1}{2} (e+fx) \right]}{\sqrt{\sec \left[ \frac{1}{2} (e+fx) \right]^2}} \right)^{1+2m} \right. \\
 & \quad \left. \left( -\frac{1}{\frac{3}{2}+m} \left( \frac{1}{2}+m \right) (1-n) \operatorname{AppellF1} \left[ \frac{3}{2}+m, m+n, 2-n, \frac{5}{2}+m, \right. \right. \right. \\
 & \quad \left. \left. \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \sec \left[ \frac{1}{2} (e+fx) \right]^2 \tan \left[ \frac{1}{2} (e+fx) \right] + \right. \right. \\
 & \quad \left. \left. \frac{1}{\frac{3}{2}+m} \left( \frac{1}{2}+m \right) (m+n) \operatorname{AppellF1} \left[ \frac{3}{2}+m, 1+m+n, 1-n, \frac{5}{2}+m, \tan \left[ \frac{1}{2} (e+fx) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right]\right) \Bigg/ \left((1+2m)\right. \\
 & \left. \left( (3+2m) \operatorname{AppellF1}\left[\frac{1}{2}+m, m+n, 1-n, \frac{3}{2}+m, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \\
 & \quad 2 \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}+m, m+n, 2-n, \frac{5}{2}+m, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \\
 & \quad \quad (m+n) \operatorname{AppellF1}\left[\frac{3}{2}+m, 1+m+n, 1-n, \frac{5}{2}+m, \right. \\
 & \quad \quad \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \Bigg) + \\
 & \left( 2(3+2m) \operatorname{AppellF1}\left[\frac{1}{2}+m, m+n, 1-n, \frac{3}{2}+m, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \quad \left. \left( \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2\right)^{-\frac{1}{2}+m+n} \left( \cos\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Sec}[e+fx] \right)^{m+n} \right. \right. \\
 & \quad \left. \left. \left( \frac{\tan\left[\frac{1}{2}(e+fx)\right]}{\sqrt{\operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2}} \right)^{2m} \left( \frac{1}{2} \sqrt{\operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2} - \frac{\tan\left[\frac{1}{2}(e+fx)\right]^2}{2\sqrt{\operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2}} \right) \right) \right) \Bigg/ \\
 & \left( (3+2m) \operatorname{AppellF1}\left[\frac{1}{2}+m, m+n, 1-n, \frac{3}{2}+m, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad 2 \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}+m, m+n, 2-n, \frac{5}{2}+m, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \quad (m+n) \operatorname{AppellF1}\left[\frac{3}{2}+m, 1+m+n, 1-n, \frac{5}{2}+m, \right. \\
 & \quad \quad \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) - \\
 & \left( 2(3+2m) \operatorname{AppellF1}\left[\frac{1}{2}+m, m+n, 1-n, \frac{3}{2}+m, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \quad \left. \left( \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2\right)^{-\frac{1}{2}+m+n} \left( \cos\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Sec}[e+fx] \right)^{m+n} \left( \frac{\tan\left[\frac{1}{2}(e+fx)\right]}{\sqrt{\operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2}} \right)^{1+2m} \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( 2 \left( (-1+n) \operatorname{AppellF1} \left[ \frac{3}{2}+m, m+n, 2-n, \frac{5}{2}+m, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] + \right. \right. \\
 & \quad (m+n) \operatorname{AppellF1} \left[ \frac{3}{2}+m, 1+m+n, 1-n, \frac{5}{2}+m, \tan \left[ \frac{1}{2} (e+fx) \right]^2, \right. \\
 & \quad \quad \left. \left. -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right) \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \tan \left[ \frac{1}{2} (e+fx) \right] + \right. \\
 & \quad (3+2m) \left( -\frac{1}{\frac{3}{2}+m} \left( \frac{1}{2}+m \right) (1-n) \operatorname{AppellF1} \left[ \frac{3}{2}+m, m+n, 2-n, \frac{5}{2}+m, \right. \right. \\
 & \quad \quad \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right) \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \tan \left[ \frac{1}{2} (e+fx) \right] + \\
 & \quad \quad \frac{1}{\frac{3}{2}+m} \left( \frac{1}{2}+m \right) (m+n) \operatorname{AppellF1} \left[ \frac{3}{2}+m, 1+m+n, 1-n, \frac{5}{2}+m, \tan \left[ \frac{1}{2} (e+fx) \right]^2, \right. \\
 & \quad \quad \left. \left. -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \tan \left[ \frac{1}{2} (e+fx) \right] \right) \left. \right) + \\
 & \quad 2 \tan \left[ \frac{1}{2} (e+fx) \right]^2 \left( (-1+n) \left( -\frac{1}{\frac{5}{2}+m} \left( \frac{3}{2}+m \right) (2-n) \operatorname{AppellF1} \left[ \frac{5}{2}+m, m+n, 3-n, \frac{7}{2}+m, \right. \right. \right. \\
 & \quad \quad \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right) \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \tan \left[ \frac{1}{2} (e+fx) \right] + \\
 & \quad \quad \frac{1}{\frac{5}{2}+m} \left( \frac{3}{2}+m \right) (m+n) \operatorname{AppellF1} \left[ \frac{5}{2}+m, 1+m+n, 2-n, \frac{7}{2}+m, \tan \left[ \frac{1}{2} (e+fx) \right]^2, \right. \\
 & \quad \quad \left. \left. -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \tan \left[ \frac{1}{2} (e+fx) \right] \right) + (m+n) \right. \\
 & \quad \left( -\frac{1}{\frac{5}{2}+m} \left( \frac{3}{2}+m \right) (1-n) \operatorname{AppellF1} \left[ \frac{5}{2}+m, 1+m+n, 2-n, \frac{7}{2}+m, \tan \left[ \frac{1}{2} (e+fx) \right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \tan \left[ \frac{1}{2} (e+fx) \right] + \frac{1}{\frac{5}{2}+m} \right. \\
 & \quad \quad \left( \frac{3}{2}+m \right) (1+m+n) \operatorname{AppellF1} \left[ \frac{5}{2}+m, 2+m+n, 1-n, \frac{7}{2}+m, \tan \left[ \frac{1}{2} (e+fx) \right]^2, \right. \\
 & \quad \quad \left. \left. -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \tan \left[ \frac{1}{2} (e+fx) \right] \right) \left. \right) \left. \right) \left. \right) / \\
 & \quad \left( (1+2m) \left( (3+2m) \operatorname{AppellF1} \left[ \frac{1}{2}+m, m+n, 1-n, \frac{3}{2}+m, \tan \left[ \frac{1}{2} (e+fx) \right]^2, \right. \right. \right. \\
 & \quad \quad \left. \left. -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] + 2 \left( (-1+n) \operatorname{AppellF1} \left[ \frac{3}{2}+m, m+n, 2-n, \frac{5}{2}+m, \right. \right. \right. \\
 & \quad \quad \quad \left. \left. \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] + (m+n) \operatorname{AppellF1} \left[ \frac{3}{2}+m, 1+m+n, \right. \right. \right.
 \end{aligned}$$



$$\begin{aligned}
 & \left( 3 \times 2^{1+m} \operatorname{AppellF1} \left[ \frac{1}{2}, m+n, 1-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right. \\
 & \quad \left( \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \right)^{-1+n} (d \operatorname{Sec} [e+fx])^n \left( \operatorname{Cos} \left[ \frac{1}{2} (e+fx) \right]^2 \operatorname{Sec} [e+fx] \right)^{m+n} \\
 & \quad \left. (a (1 + \operatorname{Sec} [e+fx]))^m \tan \left[ \frac{1}{2} (e+fx) \right] \right) / \\
 & \left( f \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, m+n, 1-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] + \right. \right. \\
 & \quad 2 \left( (-1+n) \operatorname{AppellF1} \left[ \frac{3}{2}, m+n, 2-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] + \right. \\
 & \quad \left. (m+n) \operatorname{AppellF1} \left[ \frac{3}{2}, 1+m+n, 1-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right) \\
 & \quad \tan \left[ \frac{1}{2} (e+fx) \right]^2 \left( \left( 3 \times 2^m \operatorname{AppellF1} \left[ \frac{1}{2}, m+n, 1-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \left( \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \right)^n \left( \operatorname{Cos} \left[ \frac{1}{2} (e+fx) \right]^2 \operatorname{Sec} [e+fx] \right)^{m+n} \right) \right) / \\
 & \quad \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, m+n, 1-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] + \right. \\
 & \quad 2 \left( (-1+n) \operatorname{AppellF1} \left[ \frac{3}{2}, m+n, 2-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] + \right. \\
 & \quad \left. (m+n) \operatorname{AppellF1} \left[ \frac{3}{2}, 1+m+n, 1-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (e+fx) \right]^2 \right) + \\
 & \quad \left( 3 \times 2^{1+m} (-1+n) \operatorname{AppellF1} \left[ \frac{1}{2}, m+n, 1-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right. \\
 & \quad \left. \left( \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \right)^{-1+n} \left( \operatorname{Cos} \left[ \frac{1}{2} (e+fx) \right]^2 \operatorname{Sec} [e+fx] \right)^{m+n} \tan \left[ \frac{1}{2} (e+fx) \right]^2 \right) / \\
 & \quad \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, m+n, 1-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] + \right. \\
 & \quad 2 \left( (-1+n) \operatorname{AppellF1} \left[ \frac{3}{2}, m+n, 2-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] + \right. \\
 & \quad \left. (m+n) \operatorname{AppellF1} \left[ \frac{3}{2}, 1+m+n, 1-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (e+fx) \right]^2 \right) + \\
 & \quad \left( 3 \times 2^{1+m} \left( \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \right)^{-1+n} \left( \operatorname{Cos} \left[ \frac{1}{2} (e+fx) \right]^2 \operatorname{Sec} [e+fx] \right)^{m+n} \tan \left[ \frac{1}{2} (e+fx) \right] \right. \\
 & \quad \left( -\frac{1}{3} (1-n) \operatorname{AppellF1} \left[ \frac{3}{2}, m+n, 2-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right. \\
 & \quad \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \tan \left[ \frac{1}{2} (e+fx) \right] + \frac{1}{3} (m+n) \operatorname{AppellF1} \left[ \frac{3}{2}, 1+m+n, 1-n, \frac{5}{2}, \right. \\
 & \quad \left. \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \tan \left[ \frac{1}{2} (e+fx) \right] \left. \right) \right) / \\
 & \quad \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, m+n, 1-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] + \right.
 \end{aligned}$$

$$\begin{aligned}
 & 2 \left( (-1+n) \operatorname{AppellF1} \left[ \frac{3}{2}, m+n, 2-n, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right] + \right. \\
 & \quad (m+n) \operatorname{AppellF1} \left[ \frac{3}{2}, 1+m+n, 1-n, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, \right. \\
 & \quad \quad \left. \left. -\operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right] \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right) - \\
 & \left( 3 \times 2^{1+m} \operatorname{AppellF1} \left[ \frac{1}{2}, m+n, 1-n, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right. \\
 & \quad \left. \left( \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \right)^{-1+n} \left( \operatorname{Cos} \left[ \frac{1}{2} (e+fx) \right]^2 \operatorname{Sec} [e+fx] \right)^{m+n} \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right] \right. \\
 & \quad \left. \left( 2 \left( (-1+n) \operatorname{AppellF1} \left[ \frac{3}{2}, m+n, 2-n, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right] + \right. \right. \right. \\
 & \quad \quad \left. \left. (m+n) \operatorname{AppellF1} \left[ \frac{3}{2}, 1+m+n, 1-n, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right) \right. \\
 & \quad \left. \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right] + \right. \\
 & \quad \left. 3 \left( -\frac{1}{3} (1-n) \operatorname{AppellF1} \left[ \frac{3}{2}, m+n, 2-n, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right. \right. \\
 & \quad \quad \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right] + \frac{1}{3} (m+n) \operatorname{AppellF1} \left[ \frac{3}{2}, 1+m+n, 1-n, \frac{5}{2}, \right. \\
 & \quad \quad \left. \left. \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right] \right) \right. \\
 & \quad \left. 2 \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \left( (-1+n) \left( -\frac{3}{5} (2-n) \operatorname{AppellF1} \left[ \frac{5}{2}, m+n, 3-n, \frac{7}{2}, \right. \right. \right. \right. \\
 & \quad \quad \left. \left. \left. \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right] + \frac{3}{5} \right. \right. \right. \\
 & \quad \quad \left. \left. (m+n) \operatorname{AppellF1} \left[ \frac{5}{2}, 1+m+n, 2-n, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right. \right. \\
 & \quad \quad \left. \left. \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right] \right) + (m+n) \left( -\frac{3}{5} (1-n) \operatorname{AppellF1} \left[ \frac{5}{2}, 1+m+n, \right. \right. \right. \\
 & \quad \quad \left. \left. 2-n, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \operatorname{Tan} \left[ \right. \right. \\
 & \quad \quad \left. \left. \frac{1}{2} (e+fx) \right] + \frac{3}{5} (1+m+n) \operatorname{AppellF1} \left[ \frac{5}{2}, 2+m+n, 1-n, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right] \right) \right) \right) \Big/ \\
 & \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, m+n, 1-n, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right] + \right. \\
 & \quad 2 \left( (-1+n) \operatorname{AppellF1} \left[ \frac{3}{2}, m+n, 2-n, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right] + \right. \\
 & \quad \quad (m+n) \operatorname{AppellF1} \left[ \frac{3}{2}, 1+m+n, 1-n, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, \right. \\
 & \quad \quad \left. \left. -\operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right) \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right) + \\
 & \left( 3 \times 2^{1+m} (m+n) \operatorname{AppellF1} \left[ \frac{1}{2}, m+n, 1-n, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \right)^{-1+n} \left( \operatorname{Cos}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Sec}[e+fx] \right)^{-1+m+n} \\
 & \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \left( -\operatorname{Cos}\left[\frac{1}{2}(e+fx)\right] \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right] + \right. \\
 & \quad \left. \operatorname{Cos}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Sec}[e+fx] \operatorname{Tan}[e+fx] \right) \Big/ \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, m+n, 1-n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad 2 \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, m+n, 2-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left. (m+n) \operatorname{AppellF1}\left[\frac{3}{2}, 1+m+n, 1-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \Big) \Big)
 \end{aligned}$$

**Problem 340: Unable to integrate problem.**

$$\int (d \operatorname{Sec}[e+fx])^n (a - a \operatorname{Sec}[e+fx])^m dx$$

Optimal (type 6, 96 leaves, 3 steps):

$$\begin{aligned}
 & - \left( \left( \operatorname{AppellF1}\left[n, \frac{1}{2}-m, \frac{1}{2}, 1+n, \operatorname{Sec}[e+fx], -\operatorname{Sec}[e+fx]\right] (1 - \operatorname{Sec}[e+fx])^{-\frac{1}{2}-m} \right. \right. \\
 & \quad \left. \left. (d \operatorname{Sec}[e+fx])^n (a - a \operatorname{Sec}[e+fx])^m \operatorname{Tan}[e+fx] \right) \Big/ \left( f n \sqrt{1 + \operatorname{Sec}[e+fx]} \right) \right)
 \end{aligned}$$

Result (type 8, 26 leaves):

$$\int (d \operatorname{Sec}[e+fx])^n (a - a \operatorname{Sec}[e+fx])^m dx$$

**Problem 345: Result more than twice size of optimal antiderivative.**

$$\int (a + a \operatorname{Sec}[e+fx])^m dx$$

Optimal (type 6, 83 leaves, 3 steps):

$$\begin{aligned}
 & \left( \sqrt{2} \operatorname{AppellF1}\left[\frac{1}{2}+m, \frac{1}{2}, 1, \frac{3}{2}+m, \frac{1}{2}(1 + \operatorname{Sec}[e+fx]), 1 + \operatorname{Sec}[e+fx]\right] \right. \\
 & \quad \left. (a + a \operatorname{Sec}[e+fx])^m \operatorname{Tan}[e+fx] \right) \Big/ \left( f (1 + 2m) \sqrt{1 - \operatorname{Sec}[e+fx]} \right)
 \end{aligned}$$

Result (type 6, 1653 leaves):

$$\begin{aligned}
 & \left( 3 \times 2^m \operatorname{AppellF1}\left[\frac{1}{2}, m, 1, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \quad \left. \left( \operatorname{Cos}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Sec}[e+fx] \right)^m (a (1 + \operatorname{Sec}[e+fx]))^m \operatorname{Sin}[e+fx] \right) \Big/ \\
 & \left( f \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, m, 1, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] - \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & 2 \left( \text{AppellF1} \left[ \frac{3}{2}, m, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] - \right. \\
 & \quad \left. m \text{AppellF1} \left[ \frac{3}{2}, 1 + m, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (e + f x) \right]^2 \\
 & \left( \left( 3 \times 2^m \text{AppellF1} \left[ \frac{1}{2}, m, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] \right. \right. \\
 & \quad \left. \left. \cos [e + f x] \left( \cos \left[ \frac{1}{2} (e + f x) \right]^2 \sec [e + f x] \right)^m \right) \right) / \\
 & \left( 3 \text{AppellF1} \left[ \frac{1}{2}, m, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] - \right. \\
 & \quad 2 \left( \text{AppellF1} \left[ \frac{3}{2}, m, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] - \right. \\
 & \quad \quad \left. m \text{AppellF1} \left[ \frac{3}{2}, 1 + m, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] \right) \\
 & \quad \tan \left[ \frac{1}{2} (e + f x) \right]^2 \right) + \left( 3 \times 2^m \left( \cos \left[ \frac{1}{2} (e + f x) \right]^2 \sec [e + f x] \right)^m \sin [e + f x] \right. \\
 & \quad \left. \left( -\frac{1}{3} \text{AppellF1} \left[ \frac{3}{2}, m, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] \right. \right. \\
 & \quad \quad \left. \left. \sec \left[ \frac{1}{2} (e + f x) \right]^2 \tan \left[ \frac{1}{2} (e + f x) \right] + \frac{1}{3} m \text{AppellF1} \left[ \frac{3}{2}, 1 + m, 1, \frac{5}{2}, \right. \right. \right. \\
 & \quad \quad \quad \left. \left. \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] \sec \left[ \frac{1}{2} (e + f x) \right]^2 \tan \left[ \frac{1}{2} (e + f x) \right] \right) \right) / \\
 & \left( 3 \text{AppellF1} \left[ \frac{1}{2}, m, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] - \right. \\
 & \quad 2 \left( \text{AppellF1} \left[ \frac{3}{2}, m, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] - m \text{AppellF1} \left[ \frac{3}{2}, \right. \right. \\
 & \quad \quad \left. \left. 1 + m, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (e + f x) \right]^2 \right) - \\
 & \left( 3 \times 2^m \text{AppellF1} \left[ \frac{1}{2}, m, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] \right. \\
 & \quad \left. \left( \cos \left[ \frac{1}{2} (e + f x) \right]^2 \sec [e + f x] \right)^m \sin [e + f x] \right) \\
 & \left( -2 \left( \text{AppellF1} \left[ \frac{3}{2}, m, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] - \right. \right. \\
 & \quad \left. \left. m \text{AppellF1} \left[ \frac{3}{2}, 1 + m, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] \right) \right) \\
 & \quad \sec \left[ \frac{1}{2} (e + f x) \right]^2 \tan \left[ \frac{1}{2} (e + f x) \right] + \\
 & \quad 3 \left( -\frac{1}{3} \text{AppellF1} \left[ \frac{3}{2}, m, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] \sec \left[ \frac{1}{2} (e + f x) \right]^2 \right. \\
 & \quad \quad \left. \tan \left[ \frac{1}{2} (e + f x) \right] + \frac{1}{3} m \text{AppellF1} \left[ \frac{3}{2}, 1 + m, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, \right. \right. \\
 & \quad \quad \quad \left. \left. -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] \sec \left[ \frac{1}{2} (e + f x) \right]^2 \tan \left[ \frac{1}{2} (e + f x) \right] \right) - 2 \tan \left[ \frac{1}{2} (e + f x) \right]^2 \\
 & \quad \left( -\frac{6}{5} \text{AppellF1} \left[ \frac{5}{2}, m, 3, \frac{7}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] \sec \left[ \frac{1}{2} (e + f x) \right]^2 \right)
 \end{aligned}$$



$$\begin{aligned}
 & \tan\left[\frac{1}{2}(e+fx)\right] + \frac{3}{5} m \operatorname{AppellF1}\left[\frac{5}{2}, 1+m, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \\
 & \quad \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] - m \left(-\frac{3}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \right. \right. \\
 & \quad \left. \left. 1+m, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(e+fx)\right] + \frac{3}{5}(1+m) \operatorname{AppellF1}\left[\frac{5}{2}, 2+m, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right]\right)\right)\right) / \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, m, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] - \right. \\
 & \quad \left. 2 \left(\operatorname{AppellF1}\left[\frac{3}{2}, m, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] - m \operatorname{AppellF1}\left[\frac{3}{2}, 1+m, \right. \right. \right. \\
 & \quad \left. \left. \left. 1, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right]\right) \tan\left[\frac{1}{2}(e+fx)\right]^2\right)^2 + \right. \\
 & \left. \left(3 \times 2^m m \operatorname{AppellF1}\left[\frac{1}{2}, m, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \\
 & \quad \left. \left. \left(\cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx]\right)^{-1+m} \sin[e+fx] \right. \right. \\
 & \quad \left. \left. \left(-\cos\left[\frac{1}{2}(e+fx)\right] \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right] + \right. \right. \right. \\
 & \quad \left. \left. \left. \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \tan[e+fx]\right)\right)\right) / \right. \\
 & \left. \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, m, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] - \right. \right. \\
 & \quad \left. \left. 2 \left(\operatorname{AppellF1}\left[\frac{3}{2}, m, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] - m \operatorname{AppellF1}\left[\frac{3}{2}, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. 1+m, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right]\right) \tan\left[\frac{1}{2}(e+fx)\right]^2\right)\right) \right)
 \end{aligned}$$

**Problem 346: Result more than twice size of optimal antiderivative.**

$$\int \cos[e+fx] (a + a \sec[e+fx])^m dx$$

Optimal (type 6, 84 leaves, 3 steps):

$$\begin{aligned}
 & - \left( \left( \sqrt{2} \operatorname{AppellF1}\left[\frac{1}{2}+m, \frac{1}{2}, 2, \frac{3}{2}+m, \frac{1}{2}(1+\sec[e+fx])\right], 1+\sec[e+fx] \right) \right. \\
 & \quad \left. (a + a \sec[e+fx])^m \tan[e+fx] \right) / \left( f(1+2m) \sqrt{1-\sec[e+fx]} \right)
 \end{aligned}$$

Result (type 6, 3781 leaves):

$$\begin{aligned}
 & \left( 2^{1+m} \cos\left[\frac{1}{2}(e+fx)\right]^3 \cos[e+fx] \right. \\
 & \quad \left. \left( \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \right)^m (a(1+\sec[e+fx]))^m \sin\left[\frac{1}{2}(e+fx)\right] \right)
 \end{aligned}$$



$$\begin{aligned}
 & \left( \text{AppellF1}\left[\frac{1}{2}, m, 2, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \frac{2}{3} \left( -2 \text{AppellF1}\left[\frac{3}{2}, m, 3, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + m \text{AppellF1}\left[\frac{3}{2}, \right. \right. \\
 & \quad \quad \left. \left. 1+m, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \Big) + \\
 & 2^{1+m} \cos\left[\frac{1}{2}(e+fx)\right]^3 \left( \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \right)^m \sin\left[\frac{1}{2}(e+fx)\right] \\
 & \left( - \left( \left( 3 \text{AppellF1}\left[\frac{1}{2}, m, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) \right) / \right. \\
 & \quad \left( 3 \text{AppellF1}\left[\frac{1}{2}, m, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] - \right. \\
 & \quad \left. 2 \left( \text{AppellF1}\left[\frac{3}{2}, m, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] - m \text{AppellF1}\left[\frac{3}{2}, \right. \right. \right. \\
 & \quad \quad \left. \left. 1+m, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \Big) \right) - \\
 & \left( 3 \sec\left[\frac{1}{2}(e+fx)\right]^2 \left( -\frac{1}{3} \text{AppellF1}\left[\frac{3}{2}, m, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \\
 & \quad \left. \left. \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \frac{1}{3} m \text{AppellF1}\left[\frac{3}{2}, 1+m, 1, \frac{5}{2}, \right. \right. \right. \\
 & \quad \quad \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) \right) / \\
 & \left( 3 \text{AppellF1}\left[\frac{1}{2}, m, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] - \right. \\
 & \quad \left. 2 \left( \text{AppellF1}\left[\frac{3}{2}, m, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] - m \text{AppellF1}\left[\frac{3}{2}, \right. \right. \right. \\
 & \quad \quad \left. \left. 1+m, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \Big) + \\
 & \left( 2 \left( -\frac{2}{3} \text{AppellF1}\left[\frac{3}{2}, m, 3, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \\
 & \quad \left. \left. \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \frac{1}{3} m \text{AppellF1}\left[\frac{3}{2}, 1+m, 2, \frac{5}{2}, \right. \right. \right. \\
 & \quad \quad \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) \right) / \\
 & \left( \text{AppellF1}\left[\frac{1}{2}, m, 2, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \frac{2}{3} \left( -2 \text{AppellF1}\left[\frac{3}{2}, m, 3, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + m \text{AppellF1}\left[\frac{3}{2}, \right. \right. \\
 & \quad \quad \left. \left. 1+m, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \Big) + \\
 & \left( 3 \text{AppellF1}\left[\frac{1}{2}, m, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \right. \\
 & \quad \left. \left( -2 \left( \text{AppellF1}\left[\frac{3}{2}, m, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] - m \text{AppellF1}\left[\frac{3}{2}, \right. \right. \right. \right. \\
 & \quad \quad \left. \left. 1+m, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) \Big)
 \end{aligned}$$

$$\begin{aligned}
& (e+fx) + 3 \left( -\frac{1}{3} \operatorname{AppellF1} \left[ \frac{3}{2}, m, 2, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right. \\
& \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right] + \frac{1}{3} m \operatorname{AppellF1} \left[ \frac{3}{2}, 1+m, 1, \frac{5}{2}, \right. \\
& \left. \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right] \Big) - \\
& 2 \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \left( -\frac{6}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, m, 3, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, \right. \right. \\
& \left. \left. -\operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right] + \right. \\
& \left. \frac{3}{5} m \operatorname{AppellF1} \left[ \frac{5}{2}, 1+m, 2, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right. \\
& \left. \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right] - m \left( -\frac{3}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, 1+m, 2, \right. \right. \right. \\
& \left. \left. \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \right. \right. \\
& \left. \left. \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right] + \frac{3}{5} (1+m) \operatorname{AppellF1} \left[ \frac{5}{2}, 2+m, 1, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, \right. \right. \right. \\
& \left. \left. \left. -\operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right] \right) \right) \Big) / \\
& \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, m, 1, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right] - \right. \\
& \left. 2 \left( \operatorname{AppellF1} \left[ \frac{3}{2}, m, 2, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right] - m \operatorname{AppellF1} \left[ \frac{3}{2}, \right. \right. \right. \\
& \left. \left. \left. 1+m, 1, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right) \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right) - \\
& \left( 2 \operatorname{AppellF1} \left[ \frac{1}{2}, m, 2, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right. \\
& \left. \left( -\frac{2}{3} \operatorname{AppellF1} \left[ \frac{3}{2}, m, 3, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right. \right. \\
& \left. \left. \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right] + \frac{1}{3} m \operatorname{AppellF1} \left[ \frac{3}{2}, 1+m, 2, \frac{5}{2}, \right. \right. \right. \\
& \left. \left. \left. \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right] + \right. \right. \\
& \left. \left. \frac{2}{3} \left( -2 \operatorname{AppellF1} \left[ \frac{3}{2}, m, 3, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right] + m \operatorname{AppellF1} \left[ \right. \right. \right. \right. \\
& \left. \left. \left. \frac{3}{2}, 1+m, 2, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right) \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \right. \\
& \left. \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right] + \frac{2}{3} \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \left( -2 \left( -\frac{9}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, m, 4, \frac{7}{2}, \operatorname{Tan} \left[ \right. \right. \right. \right. \right. \\
& \left. \left. \left. \frac{1}{2} (e+fx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right] + \right. \right. \\
& \left. \left. \frac{3}{5} m \operatorname{AppellF1} \left[ \frac{5}{2}, 1+m, 3, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, -\operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right. \right. \\
& \left. \left. \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right] \right) + m \left( -\frac{6}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, 1+m, \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
 & 3, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2 \sec\left[\frac{1}{2}(e+fx)\right]^2 \\
 & \tan\left[\frac{1}{2}(e+fx)\right] + \frac{3}{5}(1+m) \operatorname{AppellF1}\left[\frac{5}{2}, 2+m, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \\
 & \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2 \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right]\right] \Big/ \\
 & \left( \operatorname{AppellF1}\left[\frac{1}{2}, m, 2, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \frac{2}{3} \right. \\
 & \left. \left( -2 \operatorname{AppellF1}\left[\frac{3}{2}, m, 3, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + m \operatorname{AppellF1}\left[\frac{3}{2}, \right. \right. \right. \\
 & \left. \left. \left. 1+m, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \right)^2 \right) + \\
 & 2^{1+m} m \cos\left[\frac{1}{2}(e+fx)\right]^3 \left( \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \right)^{-1+m} \\
 & \sin\left[ \frac{1}{2}(e+fx) \right] \\
 & \left( - \left( \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, m, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \right) \Big/ \right. \right. \\
 & \left. \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, m, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] - \right. \right. \\
 & \left. \left. 2 \left( \operatorname{AppellF1}\left[\frac{3}{2}, m, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] - m \operatorname{AppellF1}\left[\frac{3}{2}, \right. \right. \right. \right. \\
 & \left. \left. \left. 1+m, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \right) \Big/ \\
 & \left( 2 \operatorname{AppellF1}\left[\frac{1}{2}, m, 2, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \Big/ \\
 & \left( \operatorname{AppellF1}\left[\frac{1}{2}, m, 2, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \left. \frac{2}{3} \left( -2 \operatorname{AppellF1}\left[\frac{3}{2}, m, 3, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + m \operatorname{AppellF1}\left[\frac{3}{2}, \right. \right. \right. \\
 & \left. \left. \left. 1+m, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \right) \\
 & \left( -\cos\left[\frac{1}{2}(e+fx)\right] \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right] + \cos\left[\frac{1}{2}(e+fx)\right]^2 \right. \\
 & \left. \left. \sec[e+fx] \tan[e+fx] \right) \right) \Big) \Big) \Big)
 \end{aligned}$$

**Problem 347: Result more than twice size of optimal antiderivative.**

$$\int (d \operatorname{Sec}[e+fx])^{3/2} (a + a \operatorname{Sec}[e+fx])^m dx$$

Optimal (type 6, 98 leaves, 3 steps):



$$\begin{aligned}
 & \sin[e + f x] \tan\left[\frac{1}{2}(e + f x)\right] \Big/ \left( \left( -1 + \tan\left[\frac{1}{2}(e + f x)\right] \right)^2 \right) \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{3}{2} + m, -\frac{1}{2}, \frac{3}{2}, \tan\left[\frac{1}{2}(e + f x)\right]^2, -\tan\left[\frac{1}{2}(e + f x)\right]^2\right] + \left( \operatorname{AppellF1}\left[\frac{3}{2}, \right. \right. \right. \\
 & \quad \left. \left. \frac{3}{2} + m, \frac{1}{2}, \frac{5}{2}, \tan\left[\frac{1}{2}(e + f x)\right]^2, -\tan\left[\frac{1}{2}(e + f x)\right]^2\right] + (3 + 2m) \operatorname{AppellF1}\left[\frac{3}{2}, \right. \right. \right. \\
 & \quad \left. \left. \frac{5}{2} + m, -\frac{1}{2}, \frac{5}{2}, \tan\left[\frac{1}{2}(e + f x)\right]^2, -\tan\left[\frac{1}{2}(e + f x)\right]^2\right] \right) \tan\left[\frac{1}{2}(e + f x)\right]^2 \right) - \\
 & \left( 3 \times 2^{1+m} \sqrt{\sec[e + f x]} \left( \cos\left[\frac{1}{2}(e + f x)\right]^2 \sec[e + f x] \right)^m \tan\left[\frac{1}{2}(e + f x)\right] \right. \\
 & \quad \left( \frac{1}{6} \operatorname{AppellF1}\left[\frac{3}{2}, \frac{3}{2} + m, \frac{1}{2}, \frac{5}{2}, \tan\left[\frac{1}{2}(e + f x)\right]^2, -\tan\left[\frac{1}{2}(e + f x)\right]^2\right] \right. \\
 & \quad \left. \sec\left[\frac{1}{2}(e + f x)\right]^2 \tan\left[\frac{1}{2}(e + f x)\right] + \frac{1}{3} \left(\frac{3}{2} + m\right) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{2} + m, -\frac{1}{2}, \frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(e + f x)\right]^2, -\tan\left[\frac{1}{2}(e + f x)\right]^2\right] \sec\left[\frac{1}{2}(e + f x)\right]^2 \tan\left[\frac{1}{2}(e + f x)\right] \right) \right) \Big/ \\
 & \left( \left( -1 + \tan\left[\frac{1}{2}(e + f x)\right] \right)^2 \right) \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{3}{2} + m, -\frac{1}{2}, \frac{3}{2}, \tan\left[\frac{1}{2}(e + f x)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(e + f x)\right]^2\right] + \left( \operatorname{AppellF1}\left[\frac{3}{2}, \frac{3}{2} + m, \frac{1}{2}, \frac{5}{2}, \tan\left[\frac{1}{2}(e + f x)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(e + f x)\right]^2\right] + (3 + 2m) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{2} + m, -\frac{1}{2}, \frac{5}{2}, \right. \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(e + f x)\right]^2, -\tan\left[\frac{1}{2}(e + f x)\right]^2\right] \right) \tan\left[\frac{1}{2}(e + f x)\right]^2 \right) + \\
 & \left( 3 \times 2^{1+m} \operatorname{AppellF1}\left[\frac{1}{2}, \frac{3}{2} + m, -\frac{1}{2}, \frac{3}{2}, \tan\left[\frac{1}{2}(e + f x)\right]^2, -\tan\left[\frac{1}{2}(e + f x)\right]^2\right] \right. \\
 & \quad \left. \sqrt{\sec[e + f x]} \left( \cos\left[\frac{1}{2}(e + f x)\right]^2 \sec[e + f x] \right)^m \tan\left[\frac{1}{2}(e + f x)\right] \right. \\
 & \quad \left( \left( \operatorname{AppellF1}\left[\frac{3}{2}, \frac{3}{2} + m, \frac{1}{2}, \frac{5}{2}, \tan\left[\frac{1}{2}(e + f x)\right]^2, -\tan\left[\frac{1}{2}(e + f x)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. (3 + 2m) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{2} + m, -\frac{1}{2}, \frac{5}{2}, \tan\left[\frac{1}{2}(e + f x)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(e + f x)\right]^2\right] \right) \sec\left[\frac{1}{2}(e + f x)\right]^2 \tan\left[\frac{1}{2}(e + f x)\right] + \right. \\
 & \quad \left. 3 \left( \frac{1}{6} \operatorname{AppellF1}\left[\frac{3}{2}, \frac{3}{2} + m, \frac{1}{2}, \frac{5}{2}, \tan\left[\frac{1}{2}(e + f x)\right]^2, -\tan\left[\frac{1}{2}(e + f x)\right]^2\right] \right. \right. \\
 & \quad \left. \left. \sec\left[\frac{1}{2}(e + f x)\right]^2 \tan\left[\frac{1}{2}(e + f x)\right] + \frac{1}{3} \left(\frac{3}{2} + m\right) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{2} + m, -\frac{1}{2}, \frac{5}{2}, \right. \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(e + f x)\right]^2, -\tan\left[\frac{1}{2}(e + f x)\right]^2\right] \sec\left[\frac{1}{2}(e + f x)\right]^2 \tan\left[\frac{1}{2}(e + f x)\right] \right) \right) + \\
 & \tan\left[\frac{1}{2}(e + f x)\right]^2 \left( -\frac{3}{10} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{3}{2} + m, \frac{3}{2}, \frac{7}{2}, \tan\left[\frac{1}{2}(e + f x)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(e + f x)\right]^2\right] \sec\left[\frac{1}{2}(e + f x)\right]^2 \tan\left[\frac{1}{2}(e + f x)\right] + \frac{3}{5} \left(\frac{3}{2} + m\right) \right. \\
 & \quad \left. \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{2} + m, \frac{1}{2}, \frac{7}{2}, \tan\left[\frac{1}{2}(e + f x)\right]^2, -\tan\left[\frac{1}{2}(e + f x)\right]^2\right] \right)
 \end{aligned}$$

$$\begin{aligned}
 & \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \text{Tan}\left[\frac{1}{2}(e+fx)\right] + (3+2m) \left( \frac{3}{10} \text{AppellF1}\left[\frac{5}{2}, \frac{5}{2}+m, \frac{1}{2}, \frac{7}{2}, \right. \right. \\
 & \quad \left. \left. \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \text{Tan}\left[\frac{1}{2}(e+fx)\right] + \right. \\
 & \quad \left. \frac{3}{5} \left(\frac{5}{2}+m\right) \text{AppellF1}\left[\frac{5}{2}, \frac{7}{2}+m, -\frac{1}{2}, \frac{7}{2}, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \text{Tan}\left[\frac{1}{2}(e+fx)\right] \right) \right) \Big/ \\
 & \left( \left( -1 + \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right) \left( 3 \text{AppellF1}\left[\frac{1}{2}, \frac{3}{2}+m, -\frac{1}{2}, \frac{3}{2}, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \left( \text{AppellF1}\left[\frac{3}{2}, \frac{3}{2}+m, \frac{1}{2}, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + (3+2m) \text{AppellF1}\left[\frac{3}{2}, \frac{5}{2}+m, -\frac{1}{2}, \frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right)^2 - \\
 & \left( 3 \times 2^{1+m} m \text{AppellF1}\left[\frac{1}{2}, \frac{3}{2}+m, -\frac{1}{2}, \frac{3}{2}, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \\
 & \sqrt{\text{Sec}[e+fx]} \left( \text{Cos}\left[\frac{1}{2}(e+fx)\right]^2 \text{Sec}[e+fx] \right)^{-1+m} \\
 & \text{Tan}\left[\frac{1}{2}(e+fx)\right] \left( -\text{Cos}\left[\frac{1}{2}(e+fx)\right] \text{Sec}[e+fx] \text{Sin}\left[\frac{1}{2}(e+fx)\right] + \right. \\
 & \quad \left. \text{Cos}\left[\frac{1}{2}(e+fx)\right]^2 \text{Sec}[e+fx] \text{Tan}[e+fx] \right) \Big/ \left( \left( -1 + \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right) \right) \\
 & \left( 3 \text{AppellF1}\left[\frac{1}{2}, \frac{3}{2}+m, -\frac{1}{2}, \frac{3}{2}, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \left( \text{AppellF1}\left[ \right. \right. \right. \\
 & \quad \left. \left. \frac{3}{2}, \frac{3}{2}+m, \frac{1}{2}, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + (3+2m) \text{AppellF1}\left[\frac{3}{2}, \right. \right. \\
 & \quad \left. \left. \frac{5}{2}+m, -\frac{1}{2}, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right) \Big/ \Big)
 \end{aligned}$$

**Problem 348: Result more than twice size of optimal antiderivative.**

$$\int \sqrt{d \text{Sec}[e+fx]} (a + a \text{Sec}[e+fx])^m dx$$

Optimal (type 6, 96 leaves, 3 steps):

$$\begin{aligned}
 & - \left( \left( 2 \text{AppellF1}\left[\frac{1}{2}, \frac{1}{2}, \frac{1}{2}-m, \frac{3}{2}, \text{Sec}[e+fx], -\text{Sec}[e+fx]\right] \sqrt{d \text{Sec}[e+fx]} \right. \right. \\
 & \quad \left. \left. (1 + \text{Sec}[e+fx])^{-\frac{1}{2}-m} (a + a \text{Sec}[e+fx])^m \text{Tan}[e+fx] \right) \Big/ \left( f \sqrt{1 - \text{Sec}[e+fx]} \right) \right)
 \end{aligned}$$

Result (type 6, 2225 leaves):

$$\left( 2^{1+m} \text{AppellF1}\left[\frac{1}{2}, \frac{1}{2}+m, \frac{1}{2}, \frac{3}{2}, \text{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\text{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \sqrt{d \text{Sec}[e+fx]} \right)$$



$$\begin{aligned}
 & \left( \cos \left[ \frac{1}{2} (e + f x) \right]^2 \sec[e + f x] \right)^{\frac{1}{2}+m} (a (1 + \sec[e + f x]))^m \tan \left[ \frac{1}{2} (e + f x) \right] \Big/ \\
 & \left( f \sqrt{\sec \left[ \frac{1}{2} (e + f x) \right]^2} \left( \text{AppellF1} \left[ \frac{1}{2}, \frac{1}{2} + m, \frac{1}{2}, \frac{3}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] - \right. \right. \\
 & \quad \frac{1}{3} \left( \text{AppellF1} \left[ \frac{3}{2}, \frac{1}{2} + m, \frac{3}{2}, \frac{5}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] - (1 + 2m) \right. \\
 & \quad \quad \left. \left. \text{AppellF1} \left[ \frac{3}{2}, \frac{3}{2} + m, \frac{1}{2}, \frac{5}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (e + f x) \right]^2 \right) \\
 & \left( \left( 2^m \text{AppellF1} \left[ \frac{1}{2}, \frac{1}{2} + m, \frac{1}{2}, \frac{3}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] \right. \right. \\
 & \quad \left. \left. \sqrt{\sec \left[ \frac{1}{2} (e + f x) \right]^2} \left( \cos \left[ \frac{1}{2} (e + f x) \right]^2 \sec[e + f x] \right)^{\frac{1}{2}+m} \right) \Big/ \right. \\
 & \quad \left( \text{AppellF1} \left[ \frac{1}{2}, \frac{1}{2} + m, \frac{1}{2}, \frac{3}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] - \frac{1}{3} \right. \\
 & \quad \left( \text{AppellF1} \left[ \frac{3}{2}, \frac{1}{2} + m, \frac{3}{2}, \frac{5}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] - (1 + 2m) \text{AppellF1} \left[ \right. \right. \\
 & \quad \quad \left. \left. \frac{3}{2}, \frac{3}{2} + m, \frac{1}{2}, \frac{5}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (e + f x) \right]^2 \right) - \\
 & \quad \left( 2^m \text{AppellF1} \left[ \frac{1}{2}, \frac{1}{2} + m, \frac{1}{2}, \frac{3}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] \right. \\
 & \quad \left. \left( \cos \left[ \frac{1}{2} (e + f x) \right]^2 \sec[e + f x] \right)^{\frac{1}{2}+m} \tan \left[ \frac{1}{2} (e + f x) \right]^2 \right) \Big/ \\
 & \left( \sqrt{\sec \left[ \frac{1}{2} (e + f x) \right]^2} \left( \text{AppellF1} \left[ \frac{1}{2}, \frac{1}{2} + m, \frac{1}{2}, \frac{3}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] - \right. \right. \\
 & \quad \frac{1}{3} \left( \text{AppellF1} \left[ \frac{3}{2}, \frac{1}{2} + m, \frac{3}{2}, \frac{5}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] - \right. \\
 & \quad \quad \left. \left. (1 + 2m) \text{AppellF1} \left[ \frac{3}{2}, \frac{3}{2} + m, \frac{1}{2}, \frac{5}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] \right) \right. \\
 & \quad \left. \left. \tan \left[ \frac{1}{2} (e + f x) \right]^2 \right) \right) + \left( 2^{1+m} \left( \cos \left[ \frac{1}{2} (e + f x) \right]^2 \sec[e + f x] \right)^{\frac{1}{2}+m} \tan \left[ \frac{1}{2} (e + f x) \right] \right. \\
 & \quad \left( -\frac{1}{6} \text{AppellF1} \left[ \frac{3}{2}, \frac{1}{2} + m, \frac{3}{2}, \frac{5}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] \right. \\
 & \quad \left. \sec \left[ \frac{1}{2} (e + f x) \right]^2 \tan \left[ \frac{1}{2} (e + f x) \right] + \frac{1}{3} \left( \frac{1}{2} + m \right) \text{AppellF1} \left[ \frac{3}{2}, \frac{3}{2} + m, \frac{1}{2}, \frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] \sec \left[ \frac{1}{2} (e + f x) \right]^2 \tan \left[ \frac{1}{2} (e + f x) \right] \right) \Big/
 \end{aligned}$$

$$\begin{aligned}
 & \left( \sqrt{\sec\left[\frac{1}{2}(e+fx)\right]^2} \left( \text{AppellF1}\left[\frac{1}{2}, \frac{1}{2}+m, \frac{1}{2}, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] - \right. \right. \\
 & \quad \frac{1}{3} \left( \text{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+m, \frac{3}{2}, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] - \right. \\
 & \quad \left. \left. (1+2m) \text{AppellF1}\left[\frac{3}{2}, \frac{3}{2}+m, \frac{1}{2}, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \right. \\
 & \quad \left. \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) - \left( 2^{1+m} \text{AppellF1}\left[\frac{1}{2}, \frac{1}{2}+m, \frac{1}{2}, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \left( \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \right)^{\frac{1}{2}+m} \tan\left[\frac{1}{2}(e+fx)\right] \right. \\
 & \quad \left. \left( -\frac{1}{6} \text{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+m, \frac{3}{2}, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \\
 & \quad \left. \left. \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \frac{1}{3} \left(\frac{1}{2}+m\right) \text{AppellF1}\left[\frac{3}{2}, \frac{3}{2}+m, \frac{1}{2}, \frac{5}{2}, \right. \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] - \right. \right. \\
 & \quad \left. \left. \frac{1}{3} \left( \text{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+m, \frac{3}{2}, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] - \right. \right. \right. \\
 & \quad \left. \left. (1+2m) \text{AppellF1}\left[\frac{3}{2}, \frac{3}{2}+m, \frac{1}{2}, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \right. \right. \\
 & \quad \left. \left. \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] - \frac{1}{3} \tan\left[\frac{1}{2}(e+fx)\right]^2 \left( -\frac{9}{10} \text{AppellF1}\left[\frac{5}{2}, \frac{1}{2}+m, \frac{5}{2}, \right. \right. \right. \right. \\
 & \quad \left. \left. \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \right. \right. \\
 & \quad \left. \left. \frac{3}{5} \left(\frac{1}{2}+m\right) \text{AppellF1}\left[\frac{5}{2}, \frac{3}{2}+m, \frac{3}{2}, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \\
 & \quad \left. \left. \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] - (1+2m) \left( -\frac{3}{10} \text{AppellF1}\left[\frac{5}{2}, \frac{3}{2}+m, \frac{3}{2}, \frac{7}{2}, \right. \right. \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \right. \right. \\
 & \quad \left. \left. \frac{3}{5} \left(\frac{3}{2}+m\right) \text{AppellF1}\left[\frac{5}{2}, \frac{5}{2}+m, \frac{1}{2}, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \\
 & \quad \left. \left. \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) \right) \right) \Big/ \left( \sqrt{\sec\left[\frac{1}{2}(e+fx)\right]^2} \right. \\
 & \quad \left. \left( \text{AppellF1}\left[\frac{1}{2}, \frac{1}{2}+m, \frac{1}{2}, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] - \frac{1}{3} \left( \text{AppellF1}\left[\frac{3}{2}, \right. \right. \right. \right. \\
 & \quad \left. \left. \frac{1}{2}+m, \frac{3}{2}, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] - (1+2m) \text{AppellF1}\left[\frac{3}{2}, \right. \right. \right. \\
 & \quad \left. \left. \frac{3}{2}+m, \frac{1}{2}, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \right)^2 \Big) +
 \end{aligned}$$

$$\begin{aligned}
 & \left( 2^{1+m} \left( \frac{1}{2} + m \right) \text{AppellF1} \left[ \frac{1}{2}, \frac{1}{2} + m, \frac{1}{2}, \frac{3}{2}, \text{Tan} \left[ \frac{1}{2} (e + f x) \right]^2, -\text{Tan} \left[ \frac{1}{2} (e + f x) \right]^2 \right] \right. \\
 & \quad \left( \text{Cos} \left[ \frac{1}{2} (e + f x) \right]^2 \text{Sec} [e + f x] \right)^{-\frac{1}{2}+m} \text{Tan} \left[ \frac{1}{2} (e + f x) \right] \\
 & \quad \left( -\text{Cos} \left[ \frac{1}{2} (e + f x) \right] \text{Sec} [e + f x] \text{Sin} \left[ \frac{1}{2} (e + f x) \right] + \right. \\
 & \quad \left. \left. \text{Cos} \left[ \frac{1}{2} (e + f x) \right]^2 \text{Sec} [e + f x] \text{Tan} [e + f x] \right) \right) \Bigg/ \\
 & \left( \sqrt{\text{Sec} \left[ \frac{1}{2} (e + f x) \right]^2} \left( \text{AppellF1} \left[ \frac{1}{2}, \frac{1}{2} + m, \frac{1}{2}, \frac{3}{2}, \text{Tan} \left[ \frac{1}{2} (e + f x) \right]^2, -\text{Tan} \left[ \frac{1}{2} (e + f x) \right]^2 \right] - \right. \right. \\
 & \quad \frac{1}{3} \left( \text{AppellF1} \left[ \frac{3}{2}, \frac{1}{2} + m, \frac{3}{2}, \frac{5}{2}, \text{Tan} \left[ \frac{1}{2} (e + f x) \right]^2, -\text{Tan} \left[ \frac{1}{2} (e + f x) \right]^2 \right] - \right. \\
 & \quad \left. \left. (1 + 2m) \text{AppellF1} \left[ \frac{3}{2}, \frac{3}{2} + m, \frac{1}{2}, \frac{5}{2}, \text{Tan} \left[ \frac{1}{2} (e + f x) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\text{Tan} \left[ \frac{1}{2} (e + f x) \right]^2 \right] \text{Tan} \left[ \frac{1}{2} (e + f x) \right]^2 \right) \right) \right) \Bigg) \Bigg)
 \end{aligned}$$

**Problem 349: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{(a + a \text{Sec} [e + f x])^m}{\sqrt{d \text{Sec} [e + f x]}} dx$$

Optimal (type 6, 96 leaves, 3 steps):

$$\begin{aligned}
 & \left( 2 \text{AppellF1} \left[ -\frac{1}{2}, \frac{1}{2}, \frac{1}{2} - m, \frac{1}{2}, \text{Sec} [e + f x], -\text{Sec} [e + f x] \right] (1 + \text{Sec} [e + f x])^{-\frac{1}{2}-m} \right. \\
 & \quad \left. (a + a \text{Sec} [e + f x])^m \text{Tan} [e + f x] \right) \Bigg/ \left( f \sqrt{1 - \text{Sec} [e + f x]} \sqrt{d \text{Sec} [e + f x]} \right)
 \end{aligned}$$

Result (type 6, 2424 leaves):

$$\begin{aligned}
 & - \left( \left( 3 \times 2^{1+m} \text{AppellF1} \left[ \frac{1}{2}, -\frac{1}{2} + m, \frac{3}{2}, \frac{3}{2}, \text{Tan} \left[ \frac{1}{2} (e + f x) \right]^2, -\text{Tan} \left[ \frac{1}{2} (e + f x) \right]^2 \right] \sqrt{\text{Sec} [e + f x]} \right. \right. \\
 & \quad \left( \text{Cos} \left[ \frac{1}{2} (e + f x) \right]^2 \text{Sec} [e + f x] \right)^{-\frac{1}{2}+m} (1 + \text{Sec} [e + f x])^{-m} (a (1 + \text{Sec} [e + f x]))^m \\
 & \quad \left( \text{Cos} [2 (e + f x)] \left( \frac{(1 + \text{Sec} [e + f x])^m}{2 \sqrt{\text{Sec} [e + f x]}} - \frac{1}{2} i \sqrt{\text{Sec} [e + f x]} (1 + \text{Sec} [e + f x])^m \text{Sin} [e + f x] \right) + \right. \\
 & \quad \left. \frac{1}{2} (1 + \text{Sec} [e + f x])^m + \frac{1}{2} i (1 + \text{Sec} [e + f x])^m \text{Sin} [2 (e + f x)] \right) \Bigg) \Bigg/ \sqrt{\text{Sec} [e + f x]}
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left( \sin[e+fx] \left( -\frac{1}{2} (1 + \sec[e+fx])^m + \frac{1}{2} (1 + \sec[e+fx])^m \sin[2(e+fx)] \right) \right) \right) \\
 & \tan\left[\frac{1}{2}(e+fx)\right] \Bigg/ \left( f \left( \sec\left[\frac{1}{2}(e+fx)\right]^2 \right)^{3/2} \sqrt{d \sec[e+fx]} \right. \\
 & \left( -3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+m, \frac{3}{2}, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+m, \frac{5}{2}, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \left. (1-2m) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+m, \frac{3}{2}, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \\
 & \left( - \left( \left( 3 \times 2^m \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+m, \frac{3}{2}, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \right. \\
 & \left. \left. \left( \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \right)^{-\frac{1}{2}+m} \right) \Bigg/ \left( \sqrt{\sec\left[\frac{1}{2}(e+fx)\right]^2} \left( -3 \operatorname{AppellF1}\left[\frac{1}{2}, \right. \right. \right. \right. \\
 & \left. \left. \left. -\frac{1}{2}+m, \frac{3}{2}, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \left( 3 \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+m, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{5}{2}, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + (1-2m) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+m, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{3}{2}, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \right) \right) \Bigg) + \\
 & \left( 9 \times 2^m \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+m, \frac{3}{2}, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \left. \left( \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \right)^{-\frac{1}{2}+m} \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \Bigg/ \left( \left( \sec\left[\frac{1}{2}(e+fx)\right]^2 \right)^{3/2} \right. \right. \\
 & \left. \left( -3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+m, \frac{3}{2}, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \left( 3 \operatorname{AppellF1}\left[ \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{3}{2}, -\frac{1}{2}+m, \frac{5}{2}, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + (1-2m) \operatorname{AppellF1}\left[ \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{3}{2}, \frac{1}{2}+m, \frac{3}{2}, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \right) \Bigg) - \\
 & \left( 3 \times 2^{1+m} \left( \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \right)^{-\frac{1}{2}+m} \tan\left[\frac{1}{2}(e+fx)\right] \right. \\
 & \left. \left( -\frac{1}{2} \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+m, \frac{5}{2}, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \right. \\
 & \left. \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \frac{1}{3} \left( -\frac{1}{2}+m \right) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+m, \frac{3}{2}, \frac{5}{2}, \right. \right. \right. \\
 & \left. \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( \left( \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) \Bigg/ \\
 & \left( \left( \left( \sec\left[\frac{1}{2}(e+fx)\right]^2 \right)^{3/2} \left( -3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+m, \frac{3}{2}, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right] + \left( 3 \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+m, \frac{5}{2}, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right] + (1-2m) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+m, \frac{3}{2}, \frac{5}{2}, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right] \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \right) \Bigg) + \\
 & \left( 3 \times 2^{1+m} \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+m, \frac{3}{2}, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right] \right. \\
 & \quad \left( \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \right)^{-\frac{1}{2}+m} \tan\left[\frac{1}{2}(e+fx)\right] \\
 & \quad \left( \left( 3 \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+m, \frac{5}{2}, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right] + \right. \right. \\
 & \quad \left. \left( 1-2m \right) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+m, \frac{3}{2}, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right] \right) \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] - \right. \\
 & \quad \left. 3 \left( -\frac{1}{2} \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+m, \frac{5}{2}, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right] \right) \right. \\
 & \quad \left. \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \frac{1}{3} \left( -\frac{1}{2}+m \right) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+m, \frac{3}{2}, \frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) \right) + \\
 & \tan\left[\frac{1}{2}(e+fx)\right]^2 \left( 3 \left( -\frac{3}{2} \operatorname{AppellF1}\left[\frac{5}{2}, -\frac{1}{2}+m, \frac{7}{2}, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \frac{3}{5} \left( -\frac{1}{2}+m \right) \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{2}+m, \frac{5}{2}, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right] \right) \right. \\
 & \quad \left. \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) + (1-2m) \left( -\frac{9}{10} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{2}+m, \right. \right. \\
 & \quad \left. \left. \frac{5}{2}, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \right. \\
 & \quad \left. \tan\left[\frac{1}{2}(e+fx)\right] + \frac{3}{5} \left( \frac{1}{2}+m \right) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{3}{2}+m, \frac{3}{2}, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) \right) \Bigg) \Bigg) \Bigg/ \\
 & \left( \left( \left( \sec\left[\frac{1}{2}(e+fx)\right]^2 \right)^{3/2} \left( -3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+m, \frac{3}{2}, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right] + \left( 3 \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+m, \frac{5}{2}, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right] \right) \right) \right) \Bigg) \Bigg) \Bigg/
 \end{aligned}$$

$$\begin{aligned}
 & -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 + (1-2m) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+m, \frac{3}{2}, \frac{5}{2}, \right. \\
 & \left. \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right) - \\
 & \left(3 \times 2^{1+m} \left(-\frac{1}{2}+m\right) \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+m, \frac{3}{2}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \left. \left(\operatorname{Cos}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Sec}[e+fx]\right)^{\frac{3}{2}+m} \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \right. \\
 & \left. \left(-\operatorname{Cos}\left[\frac{1}{2}(e+fx)\right] \operatorname{Sec}[e+fx] \operatorname{Sin}\left[\frac{1}{2}(e+fx)\right] + \right. \right. \\
 & \left. \left. \operatorname{Cos}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Sec}[e+fx] \operatorname{Tan}[e+fx]\right)\right) \right] / \left(\left(\operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2\right)^{3/2}\right. \right. \\
 & \left. \left(-3 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+m, \frac{3}{2}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \\
 & \left. \left(3 \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+m, \frac{5}{2}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \\
 & \left. \left. (1-2m) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+m, \frac{3}{2}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \\
 & \left. \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right)\right)\right) \right) \right) \right)
 \end{aligned}$$

**Problem 350: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{(a + a \operatorname{Sec}[e + fx])^m}{(d \operatorname{Sec}[e + fx])^{3/2}} dx$$

Optimal (type 6, 98 leaves, 3 steps):

$$\begin{aligned}
 & \left(2 \operatorname{AppellF1}\left[-\frac{3}{2}, \frac{1}{2}, \frac{1}{2}-m, -\frac{1}{2}, \operatorname{Sec}[e+fx], -\operatorname{Sec}[e+fx]\right] (1 + \operatorname{Sec}[e+fx])^{-\frac{1}{2}-m} \right. \\
 & \left. (a + a \operatorname{Sec}[e+fx])^m \operatorname{Tan}[e+fx]\right) / \left(3 f \sqrt{1 - \operatorname{Sec}[e+fx]} (d \operatorname{Sec}[e+fx])^{3/2}\right)
 \end{aligned}$$

Result (type 6, 5127 leaves):

$$\begin{aligned}
 & \left(2^{1+m} \operatorname{Sec}[e+fx]^{3/2} \left(\operatorname{Cos}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Sec}[e+fx]\right)^{\frac{3}{2}+m} (1 + \operatorname{Sec}[e+fx])^{-m} (a (1 + \operatorname{Sec}[e+fx]))^m \right. \\
 & \left. \left(\frac{1}{4} \operatorname{Cos}[2(e+fx)]^3 \sqrt{\operatorname{Sec}[e+fx]} (1 + \operatorname{Sec}[e+fx])^m + \operatorname{Cos}[2(e+fx)]^2 \sqrt{\operatorname{Sec}[e+fx]} \right. \right. \\
 & \left. \left. \left(\frac{1}{2} (1 + \operatorname{Sec}[e+fx])^m + \frac{1}{4} i (1 + \operatorname{Sec}[e+fx])^m \operatorname{Sin}[2(e+fx)]\right) + \operatorname{Cos}[2(e+fx)] \right. \right. \\
 & \left. \left. \sqrt{\operatorname{Sec}[e+fx]} \left(\frac{1}{4} (1 + \operatorname{Sec}[e+fx])^m + \frac{1}{4} (1 + \operatorname{Sec}[e+fx])^m \operatorname{Sin}[2(e+fx)]^2\right) + \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{\text{Sec}[e + f x]} \left( -\frac{1}{4} i (1 + \text{Sec}[e + f x])^m \text{Sin}[2(e + f x)] + \right. \\
 & \quad \left. \frac{1}{2} (1 + \text{Sec}[e + f x])^m \text{Sin}[2(e + f x)]^2 + \frac{1}{4} i (1 + \text{Sec}[e + f x])^m \text{Sin}[2(e + f x)]^3 \right) \\
 & \text{Tan}\left[\frac{1}{2}(e + f x)\right] \left( -1 + \text{Tan}\left[\frac{1}{2}(e + f x)\right]^2 \right)^2 \\
 & \left( \left( 3 \text{AppellF1}\left[\frac{1}{2}, -\frac{1}{2} + m, \frac{5}{2}, \frac{3}{2}, \text{Tan}\left[\frac{1}{2}(e + f x)\right]^2, -\text{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right] \right) / \right. \\
 & \quad \left( \text{AppellF1}\left[\frac{1}{2}, -\frac{1}{2} + m, \frac{5}{2}, \frac{3}{2}, \text{Tan}\left[\frac{1}{2}(e + f x)\right]^2, -\text{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right] - \frac{1}{3} \left( 5 \text{AppellF1}\left[\frac{3}{2}, \right. \right. \right. \\
 & \quad \left. \left. -\frac{1}{2} + m, \frac{7}{2}, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(e + f x)\right]^2, -\text{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right] + (1 - 2m) \text{AppellF1}\left[\frac{3}{2}, \right. \right. \right. \\
 & \quad \left. \left. \frac{1}{2} + m, \frac{5}{2}, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(e + f x)\right]^2, -\text{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right] \right) \text{Tan}\left[\frac{1}{2}(e + f x)\right]^2 \right) + \\
 & \quad \left( 5 \text{AppellF1}\left[\frac{3}{2}, -\frac{1}{2} + m, \frac{5}{2}, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(e + f x)\right]^2, -\text{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right] \text{Tan}\left[\frac{1}{2}(e + f x)\right]^2 \right) / \\
 & \quad \left( -5 \text{AppellF1}\left[\frac{3}{2}, -\frac{1}{2} + m, \frac{5}{2}, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(e + f x)\right]^2, -\text{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right] + \right. \\
 & \quad \left( 5 \text{AppellF1}\left[\frac{5}{2}, -\frac{1}{2} + m, \frac{7}{2}, \frac{7}{2}, \text{Tan}\left[\frac{1}{2}(e + f x)\right]^2, -\text{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right] + \right. \\
 & \quad \left. \left. (1 - 2m) \text{AppellF1}\left[\frac{5}{2}, \frac{1}{2} + m, \frac{5}{2}, \frac{7}{2}, \text{Tan}\left[\frac{1}{2}(e + f x)\right]^2, -\text{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right] \right) \right) \\
 & \quad \left. \text{Tan}\left[\frac{1}{2}(e + f x)\right]^2 \right) \right) / \left( 3 f \left( \text{Sec}\left[\frac{1}{2}(e + f x)\right]^2 \right)^{5/2} (d \text{Sec}[e + f x])^{3/2} \right. \\
 & \quad \left. \left( \frac{1}{3 \left( \text{Sec}\left[\frac{1}{2}(e + f x)\right]^2 \right)^{3/2}} 2^{2+m} \left( \text{Cos}\left[\frac{1}{2}(e + f x)\right]^2 \text{Sec}[e + f x] \right)^{\frac{3}{2}+m} \right. \right. \\
 & \quad \left. \left. \text{Tan}\left[\frac{1}{2}(e + f x)\right]^2 \left( -1 + \text{Tan}\left[\frac{1}{2}(e + f x)\right]^2 \right) \right. \right. \\
 & \quad \left( \left( 3 \text{AppellF1}\left[\frac{1}{2}, -\frac{1}{2} + m, \frac{5}{2}, \frac{3}{2}, \text{Tan}\left[\frac{1}{2}(e + f x)\right]^2, -\text{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right] \right) / \right. \\
 & \quad \left( \text{AppellF1}\left[\frac{1}{2}, -\frac{1}{2} + m, \frac{5}{2}, \frac{3}{2}, \text{Tan}\left[\frac{1}{2}(e + f x)\right]^2, -\text{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right] - \right. \\
 & \quad \left. \frac{1}{3} \left( 5 \text{AppellF1}\left[\frac{3}{2}, -\frac{1}{2} + m, \frac{7}{2}, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(e + f x)\right]^2, -\text{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right] + (1 - 2m) \right. \right. \\
 & \quad \left. \left. \text{AppellF1}\left[\frac{3}{2}, \frac{1}{2} + m, \frac{5}{2}, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(e + f x)\right]^2, -\text{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right] \right) \right) \\
 & \quad \left. \text{Tan}\left[\frac{1}{2}(e + f x)\right]^2 \right) + \left( 5 \text{AppellF1}\left[\frac{3}{2}, -\frac{1}{2} + m, \frac{5}{2}, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(e + f x)\right]^2, \right. \right. \\
 & \quad \left. \left. -\text{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right] \text{Tan}\left[\frac{1}{2}(e + f x)\right]^2 \right) / \\
 & \quad \left( -5 \text{AppellF1}\left[\frac{3}{2}, -\frac{1}{2} + m, \frac{5}{2}, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(e + f x)\right]^2, -\text{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right] + \left( 5 \text{AppellF1}\left[\frac{5}{2}, \right. \right. \right. \\
 & \quad \left. \left. -\frac{1}{2} + m, \frac{7}{2}, \frac{7}{2}, \text{Tan}\left[\frac{1}{2}(e + f x)\right]^2, -\text{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right] + (1 - 2m) \text{AppellF1}\left[\frac{5}{2}, \right. \right. \right. \\
 & \quad \left. \left. \frac{1}{2} + m, \frac{5}{2}, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(e + f x)\right]^2, -\text{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right] \right) \right)
 \end{aligned}$$





$$\begin{aligned}
 & \frac{1}{3 \left( \sec \left[ \frac{1}{2} (e+fx) \right]^2 \right)^{5/2}} 2^{1+m} \left( \cos \left[ \frac{1}{2} (e+fx) \right]^2 \sec [e+fx] \right)^{\frac{3}{2}+m} \tan \left[ \frac{1}{2} (e+fx) \right] \\
 & \left( -1 + \tan \left[ \frac{1}{2} (e+fx) \right]^2 \right)^2 \\
 & \left( \left( 3 \left( -\frac{5}{6} \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{1}{2}+m, \frac{7}{2}, \frac{5}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right. \right. \right. \\
 & \quad \left. \left. \left. \sec \left[ \frac{1}{2} (e+fx) \right]^2 \tan \left[ \frac{1}{2} (e+fx) \right] + \frac{1}{3} \left( -\frac{1}{2}+m \right) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{2}+m, \frac{5}{2}, \frac{5}{2}, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \sec \left[ \frac{1}{2} (e+fx) \right]^2 \tan \left[ \frac{1}{2} (e+fx) \right] \right) \right) \right) / \\
 & \left( \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{1}{2}+m, \frac{5}{2}, \frac{3}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] - \right. \\
 & \quad \left. \frac{1}{3} \left( 5 \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{1}{2}+m, \frac{7}{2}, \frac{5}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] + (1-2m) \right. \right. \right. \\
 & \quad \left. \left. \left. \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{2}+m, \frac{5}{2}, \frac{5}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right) \right) \right) \\
 & \quad \left. \tan \left[ \frac{1}{2} (e+fx) \right]^2 \right) + \left( 5 \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{1}{2}+m, \frac{5}{2}, \frac{5}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \sec \left[ \frac{1}{2} (e+fx) \right]^2 \tan \left[ \frac{1}{2} (e+fx) \right] \right) \right) / \\
 & \left( -5 \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{1}{2}+m, \frac{5}{2}, \frac{5}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] + \right. \\
 & \quad \left( 5 \operatorname{AppellF1} \left[ \frac{5}{2}, -\frac{1}{2}+m, \frac{7}{2}, \frac{7}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] + (1-2m) \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{2}+m, \frac{5}{2}, \frac{7}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right) \right) \\
 & \quad \left. \tan \left[ \frac{1}{2} (e+fx) \right]^2 \right) + \left( 5 \tan \left[ \frac{1}{2} (e+fx) \right]^2 \left( -\frac{3}{2} \operatorname{AppellF1} \left[ \frac{5}{2}, -\frac{1}{2}+m, \frac{7}{2}, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{7}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \sec \left[ \frac{1}{2} (e+fx) \right]^2 \tan \left[ \frac{1}{2} (e+fx) \right] + \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{3}{5} \left( -\frac{1}{2}+m \right) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{2}+m, \frac{5}{2}, \frac{7}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \sec \left[ \frac{1}{2} (e+fx) \right]^2 \tan \left[ \frac{1}{2} (e+fx) \right] \right) \right) \right) / \\
 & \left( -5 \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{1}{2}+m, \frac{5}{2}, \frac{5}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] + \left( 5 \operatorname{AppellF1} \left[ \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{5}{2}, -\frac{1}{2}+m, \frac{7}{2}, \frac{7}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] + (1-2m) \operatorname{AppellF1} \left[ \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{5}{2}, \frac{1}{2}+m, \frac{5}{2}, \frac{7}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right) \right) \tan \left[ \frac{1}{2} (e+fx) \right]^2 \right) - \\
 & \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{1}{2}+m, \frac{5}{2}, \frac{3}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right. \\
 & \quad \left( -\frac{5}{6} \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{1}{2}+m, \frac{7}{2}, \frac{5}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right) \\
 & \quad \left. \left. \sec \left[ \frac{1}{2} (e+fx) \right]^2 \tan \left[ \frac{1}{2} (e+fx) \right] + \frac{1}{3} \left( -\frac{1}{2}+m \right) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{2}+m, \frac{5}{2}, \frac{5}{2}, \right. \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
& \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2 \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] - \\
& \frac{1}{3} \left( 5 \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+m, \frac{7}{2}, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
& \quad \left. (1-2m) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+m, \frac{5}{2}, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \\
& \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] - \frac{1}{3} \tan\left[\frac{1}{2}(e+fx)\right]^2 \\
& \left( 5 \left( -\frac{21}{10} \operatorname{AppellF1}\left[\frac{5}{2}, -\frac{1}{2}+m, \frac{9}{2}, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \\
& \quad \left. \left. \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \frac{3}{5} \left(-\frac{1}{2}+m\right) \right. \right. \\
& \quad \left. \left. \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{2}+m, \frac{7}{2}, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \\
& \quad \left. \left. \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) + (1-2m) \left( -\frac{3}{2} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{2}+m, \right. \right. \right. \\
& \quad \left. \left. \frac{7}{2}, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right. \right. \\
& \quad \left. \left. + \frac{3}{5} \left(\frac{1}{2}+m\right) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{3}{2}+m, \frac{5}{2}, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \\
& \quad \left. \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) \right) \right) / \\
& \left( \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+m, \frac{5}{2}, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] - \right. \\
& \quad \left. \frac{1}{3} \left( 5 \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+m, \frac{7}{2}, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \\
& \quad \left. \left. (1-2m) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+m, \frac{5}{2}, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \\
& \quad \left. \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \right)^2 - \right. \\
& \left. \left( 5 \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+m, \frac{5}{2}, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2 \left( \left( 5 \operatorname{AppellF1}\left[\frac{5}{2}, -\frac{1}{2}+m, \frac{7}{2}, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \right. \right. \\
& \quad \left. \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + (1-2m) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{2}+m, \frac{5}{2}, \frac{7}{2}, \right. \right. \right. \right. \\
& \quad \left. \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] - \right. \right. \\
& \quad \left. \left. 5 \left( -\frac{3}{2} \operatorname{AppellF1}\left[\frac{5}{2}, -\frac{1}{2}+m, \frac{7}{2}, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \right. \\
& \quad \left. \left. \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \frac{3}{5} \left(-\frac{1}{2}+m\right) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{2}+m, \frac{5}{2}, \frac{7}{2}, \right. \right. \right. \\
& \quad \left. \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) \right) + \right. \\
& \quad \left. \tan\left[\frac{1}{2}(e+fx)\right]^2 \left( 5 \left( -\frac{5}{2} \operatorname{AppellF1}\left[\frac{7}{2}, -\frac{1}{2}+m, \frac{9}{2}, \frac{9}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \right. \right.
\end{aligned}$$



$$\left( -\cos\left[\frac{1}{2}(e+fx)\right] \sec[e+fx] \sin\left[\frac{1}{2}(e+fx)\right] + \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \tan[e+fx] \right)$$

**Problem 351: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos[c+dx]^{7/2} (a+a \sec[c+dx]) dx$$

Optimal (type 4, 111 leaves, 7 steps):

$$\frac{6 a \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right]}{5 d} + \frac{10 a \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right]}{21 d} + \frac{10 a \sqrt{\cos[c+dx]} \sin[c+dx]}{21 d} + \frac{2 a \cos[c+dx]^{3/2} \sin[c+dx]}{5 d} + \frac{2 a \cos[c+dx]^{5/2} \sin[c+dx]}{7 d}$$

Result (type 5, 490 leaves):

$$\begin{aligned}
 & a \left( \sqrt{\cos[c+dx]} (1 + \cos[c+dx]) \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \right. \\
 & \quad \left( -\frac{3 \cot[c]}{5d} + \frac{23 \cos[dx] \sin[c]}{84d} + \frac{\cos[2dx] \sin[2c]}{10d} + \frac{\cos[3dx] \sin[3c]}{28d} + \right. \\
 & \quad \left. \frac{23 \cos[c] \sin[dx]}{84d} + \frac{\cos[2c] \sin[2dx]}{10d} + \frac{\cos[3c] \sin[3dx]}{28d} \right) - \\
 & \quad \left( 5 (1 + \cos[c+dx]) \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \operatorname{ArcTan}[\cot[c]]]\right]^2 \right. \\
 & \quad \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \operatorname{Sec}[dx - \operatorname{ArcTan}[\cot[c]]] \sqrt{1 - \sin[dx - \operatorname{ArcTan}[\cot[c]]]} \\
 & \quad \left. \sqrt{-\sqrt{1 + \cot[c]^2} \sin[c] \sin[dx - \operatorname{ArcTan}[\cot[c]]]} \sqrt{1 + \sin[dx - \operatorname{ArcTan}[\cot[c]]]} \right) / \\
 & \quad \left( 21d \sqrt{1 + \cot[c]^2} \right) - \frac{1}{10d} 3 (1 + \cos[c+dx]) \operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \\
 & \quad \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos[dx + \operatorname{ArcTan}[\tan[c]]]\right]^2 \right. \\
 & \quad \left. \sin[dx + \operatorname{ArcTan}[\tan[c]]] \tan[c] \right) / \\
 & \quad \left( \sqrt{1 - \cos[dx + \operatorname{ArcTan}[\tan[c]]]} \sqrt{1 + \cos[dx + \operatorname{ArcTan}[\tan[c]]]} \right. \\
 & \quad \left. \sqrt{\cos[c] \cos[dx + \operatorname{ArcTan}[\tan[c]]]} \sqrt{1 + \tan[c]^2} \sqrt{1 + \tan[c]^2} \right) - \\
 & \quad \left. \frac{\frac{\sin[dx + \operatorname{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \frac{2 \cos[c]^2 \cos[dx + \operatorname{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}{\cos[c]^2 + \sin[c]^2}}{\sqrt{\cos[c] \cos[dx + \operatorname{ArcTan}[\tan[c]]]} \sqrt{1 + \tan[c]^2}} \right)
 \end{aligned}$$

**Problem 352: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos[c+dx]^{5/2} (a + a \operatorname{Sec}[c+dx]) dx$$

Optimal (type 4, 87 leaves, 6 steps):

$$\frac{6 a \text{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{5 d} + \frac{2 a \text{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{3 d} + \frac{2 a \sqrt{\text{Cos}[c+d x]} \text{Sin}[c+d x]}{3 d} + \frac{2 a \text{Cos}[c+d x]^{3/2} \text{Sin}[c+d x]}{5 d}$$

Result (type 5, 458 leaves):

$$a \left( \sqrt{\text{Cos}[c+d x]} (1 + \text{Cos}[c+d x]) \text{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \left( -\frac{3 \text{Cot}[c]}{5 d} + \frac{\text{Cos}[d x] \text{Sin}[c]}{3 d} + \frac{\text{Cos}[2 d x] \text{Sin}[2 c]}{10 d} + \frac{\text{Cos}[c] \text{Sin}[d x]}{3 d} + \frac{\text{Cos}[2 c] \text{Sin}[2 d x]}{10 d} \right) - \left( (1 + \text{Cos}[c+d x]) \text{Csc}[c] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \text{Sin}[d x - \text{ArcTan}[\text{Cot}[c]]\right]^2\right] \text{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \text{Sec}[d x - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 - \text{Sin}[d x - \text{ArcTan}[\text{Cot}[c]]]} \sqrt{-\sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[d x - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 + \text{Sin}[d x - \text{ArcTan}[\text{Cot}[c]]}} \right) / \left( 3 d \sqrt{1 + \text{Cot}[c]^2} \right) - \frac{1}{10 d} 3 (1 + \text{Cos}[c+d x]) \text{Csc}[c] \text{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \left( \text{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \text{Cos}[d x + \text{ArcTan}[\text{Tan}[c]]\right]^2\right] \text{Sin}[d x + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c] \right) / \left( \sqrt{1 - \text{Cos}[d x + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Cos}[d x + \text{ArcTan}[\text{Tan}[c]]]} \sqrt{\text{Cos}[c] \text{Cos}[d x + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \sqrt{1 + \text{Tan}[c]^2}} \right) - \frac{\frac{\text{Sin}[d x + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c]}{\sqrt{1 + \text{Tan}[c]^2}} + \frac{2 \text{Cos}[c]^2 \text{Cos}[d x + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}}{\text{Cos}[c]^2 + \text{Sin}[c]^2}}{\sqrt{\text{Cos}[c] \text{Cos}[d x + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}}} \right) /$$

Problem 353: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \cos [c+d x]^{3 / 2} (a+a \operatorname{Sec}[c+d x]) d x$$

Optimal (type 4, 61 leaves, 5 steps):

$$\frac{2 a \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{d} + \frac{2 a \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{3 d} + \frac{2 a \sqrt{\cos [c+d x]} \sin [c+d x]}{3 d}$$

Result (type 5, 424 leaves):

$$a \left( \sqrt{\cos [c+d x]} (1+\cos [c+d x]) \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^2 \left(-\frac{\cot [c]}{d}+\frac{\cos [d x] \sin [c]}{3 d}+\frac{\cos [c] \sin [d x]}{3 d}\right) - \left( (1+\cos [c+d x]) \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]]\right]^2 \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^2 \operatorname{Sec}[d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]]} \sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]]} \sqrt{1+\sin [d x-\operatorname{ArcTan}[\cot [c]]]} \right) / \left( 3 d \sqrt{1+\cot [c]^2} \right) - \frac{1}{2 d} (1+\cos [c+d x]) \operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^2 \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2},-\frac{1}{4}\right\},\left\{\frac{3}{4}\right\}, \cos [d x+\operatorname{ArcTan}[\tan [c]]]\right]^2 \sin [d x+\operatorname{ArcTan}[\tan [c]]] \tan [c] \right) / \left( \sqrt{1-\cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{1+\cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{1+\tan [c]^2} \sqrt{1+\tan [c]^2} \right) - \frac{\sin [d x+\operatorname{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1+\tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x+\operatorname{ArcTan}[\tan [c]]] \sqrt{1+\tan [c]^2}}{\cos [c]^2+\sin [c]^2} \right) / \sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{1+\tan [c]^2} \right)$$

**Problem 354: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \sqrt{\cos [c+d x]} (a+a \operatorname{Sec}[c+d x]) d x$$

Optimal (type 4, 35 leaves, 4 steps):

$$\frac{2 a \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{d} + \frac{2 a \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{d}$$

Result (type 5, 155 leaves):

$$\frac{1}{2 d} a \sqrt{\cos [c+d x]} (1+\cos [c+d x]) \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \left(-2 \sqrt{\cos [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]^2} \sqrt{\operatorname{Csc}[c]^2} \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \operatorname{Sec}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]] \sin [c]+\tan [d x+\operatorname{ArcTan}[\tan [c]]]-\left(\operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2},-\frac{1}{4}\right\},\left\{\frac{3}{4}\right\}, \cos [d x+\operatorname{ArcTan}[\tan [c]]]^2\right] \tan [d x+\operatorname{ArcTan}[\tan [c]]]\right) / \left(\sqrt{\sin [d x+\operatorname{ArcTan}[\tan [c]]]^2}\right)\right)$$

**Problem 355: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{a+a \operatorname{Sec}[c+d x]}{\sqrt{\cos [c+d x]}} d x$$

Optimal (type 4, 57 leaves, 5 steps):

$$-\frac{2 a \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{d} + \frac{2 a \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{d} + \frac{2 a \sin [c+d x]}{d \sqrt{\cos [c+d x]}}$$

Result (type 5, 413 leaves):



$$\begin{aligned}
 & a \left( \sqrt{\cos[c+dx]} (1 + \cos[c+dx]) \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \right. \\
 & \quad \left( \frac{\operatorname{Csc}[c] \operatorname{Sec}[c]}{d} + \frac{\operatorname{Sec}[c] \operatorname{Sec}[c+dx] \operatorname{Sin}[dx]}{d} \right) - \frac{1}{d \sqrt{1 + \operatorname{Cot}[c]^2}} \\
 & \quad (1 + \cos[c+dx]) \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]\right]^2 \right] \\
 & \quad \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \operatorname{Sec}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \\
 & \quad \sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 + \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} + \\
 & \quad \frac{1}{2d} (1 + \cos[c+dx]) \operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \\
 & \quad \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \operatorname{Cos}[dx + \operatorname{ArcTan}[\operatorname{Tan}[c]]]\right]^2 \right. \\
 & \quad \left. \operatorname{Sin}[dx + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c] \right) / \left( \sqrt{1 - \operatorname{Cos}[dx + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \right. \\
 & \quad \left. \sqrt{1 + \operatorname{Cos}[dx + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{\operatorname{Cos}[c] \operatorname{Cos}[dx + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1 + \operatorname{Tan}[c]^2} \right. \\
 & \quad \left. \left. \sqrt{1 + \operatorname{Tan}[c]^2} \right) - \frac{\frac{\operatorname{Sin}[dx + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c]}{\sqrt{1 + \operatorname{Tan}[c]^2}} + \frac{2 \operatorname{Cos}[c]^2 \operatorname{Cos}[dx + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1 + \operatorname{Tan}[c]^2}}{\operatorname{Cos}[c]^2 + \operatorname{Sin}[c]^2}}{\sqrt{\operatorname{Cos}[c] \operatorname{Cos}[dx + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1 + \operatorname{Tan}[c]^2}} \right) \right)
 \end{aligned}$$

**Problem 356: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{a + a \operatorname{Sec}[c+dx]}{\operatorname{Cos}[c+dx]^{3/2}} dx$$

Optimal (type 4, 83 leaves, 6 steps):

$$\begin{aligned}
 & -\frac{2a \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right]}{d} + \\
 & \frac{2a \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right]}{3d} + \frac{2a \operatorname{Sin}[c+dx]}{3d \operatorname{Cos}[c+dx]^{3/2}} + \frac{2a \operatorname{Sin}[c+dx]}{d \sqrt{\operatorname{Cos}[c+dx]}}
 \end{aligned}$$

Result (type 5, 444 leaves):

$$\begin{aligned}
 & a \left( \sqrt{\cos [c+d x]} \left(1+\cos [c+d x]\right) \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^2 \right. \\
 & \left. \left( \frac{\csc [c] \sec [c]}{d}+\frac{\sec [c] \sec [c+d x]^2 \sin [d x]}{3 d}+\frac{\sec [c] \sec [c+d x] \left(\sin [c]+3 \sin [d x]\right)}{3 d} \right) - \right. \\
 & \left. \left( \left(1+\cos [c+d x]\right) \csc [c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]]\right]^2 \right) \right. \\
 & \left. \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^2 \sec [d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]]} \right. \\
 & \left. \sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1+\sin [d x-\operatorname{ArcTan}[\cot [c]]]} \right) \Bigg/ \\
 & \left(3 d \sqrt{1+\cot [c]^2}\right)+\frac{1}{2 d}\left(1+\cos [c+d x]\right) \csc [c] \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^2 \\
 & \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2},-\frac{1}{4}\right\},\left\{\frac{3}{4}\right\}, \cos [d x+\operatorname{ArcTan}[\tan [c]]]\right]^2 \right) - \\
 & \left. \sin [d x+\operatorname{ArcTan}[\tan [c]]] \tan [c] \right) \Bigg/ \\
 & \left( \sqrt{1-\cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{1+\cos [d x+\operatorname{ArcTan}[\tan [c]]]} \right. \\
 & \left. \sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{1+\tan [c]^2} \sqrt{1+\tan [c]^2} \right) - \\
 & \left. \frac{\frac{\sin [d x+\operatorname{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1+\tan [c]^2}}+\frac{2 \cos [c]^2 \cos [d x+\operatorname{ArcTan}[\tan [c]]] \sqrt{1+\tan [c]^2}}{\cos [c]^2+\sin [c]^2}}{\sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{1+\tan [c]^2}} \right) \Bigg)
 \end{aligned}$$

**Problem 357: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{a+a \sec [c+d x]}{\cos [c+d x]^{5 / 2}} d x$$

Optimal (type 4, 111 leaves, 7 steps):

$$\begin{aligned}
 & - \frac{6 a \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{5 d} + \frac{2 a \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{3 d} + \\
 & \frac{2 a \sin [c+d x]}{5 d \cos [c+d x]^{5 / 2}} + \frac{2 a \sin [c+d x]}{3 d \cos [c+d x]^{3 / 2}} + \frac{6 a \sin [c+d x]}{5 d \sqrt{\cos [c+d x]}}
 \end{aligned}$$

Result (type 5, 477 leaves):

$$\begin{aligned}
 & a \left( \sqrt{\cos [c+d x]} (1+\cos [c+d x]) \right. \\
 & \left. \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^2 \left( \frac{3 \operatorname{Csc}[c] \operatorname{Sec}[c]}{5 d} + \frac{\operatorname{Sec}[c] \operatorname{Sec}[c+d x]^3 \sin [d x]}{5 d} + \right. \right. \\
 & \left. \left. \frac{\operatorname{Sec}[c] \operatorname{Sec}[c+d x]^2 (3 \sin [c]+5 \sin [d x])}{15 d} + \frac{\operatorname{Sec}[c] \operatorname{Sec}[c+d x] (5 \sin [c]+9 \sin [d x])}{15 d} \right) \right. \\
 & \left. \left( (1+\cos [c+d x]) \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]\right]^2\right] \right. \right. \\
 & \left. \left. \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^2 \operatorname{Sec}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right. \right. \\
 & \left. \left. \sqrt{-\sqrt{1+\operatorname{Cot}[c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1+\sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]}} \right) \right) / \\
 & \left( 3 d \sqrt{1+\operatorname{Cot}[c]^2} \right) + \frac{1}{10 d} 3 (1+\cos [c+d x]) \operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^2 \\
 & \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2},-\frac{1}{4}\right\},\left\{\frac{3}{4}\right\}, \cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]\right]^2\right] \right. \\
 & \left. \sin [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c] \right) / \\
 & \left( \sqrt{1-\cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1+\cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]} \right. \\
 & \left. \sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1+\operatorname{Tan}[c]^2} \sqrt{1+\operatorname{Tan}[c]^2} \right) - \\
 & \left. \frac{\frac{\sin [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c]}{\sqrt{1+\operatorname{Tan}[c]^2}} + \frac{2 \cos [c]^2 \cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1+\operatorname{Tan}[c]^2}}{\cos [c]^2+\sin [c]^2}}{\sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1+\operatorname{Tan}[c]^2}} \right)
 \end{aligned}$$

Problem 358: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{a + a \operatorname{Sec}[c + d x]}{\operatorname{Cos}[c + d x]^{7/2}} dx$$

Optimal (type 4, 135 leaves, 8 steps):

$$-\frac{6 a \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right]}{5 d} + \frac{10 a \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right]}{21 d} + \frac{2 a \operatorname{Sin}[c + d x]}{7 d \operatorname{Cos}[c + d x]^{7/2}} + \frac{2 a \operatorname{Sin}[c + d x]}{5 d \operatorname{Cos}[c + d x]^{5/2}} + \frac{10 a \operatorname{Sin}[c + d x]}{21 d \operatorname{Cos}[c + d x]^{3/2}} + \frac{6 a \operatorname{Sin}[c + d x]}{5 d \sqrt{\operatorname{Cos}[c + d x]}}$$

Result (type 5, 505 leaves):

$$\begin{aligned}
 & \left( \sqrt{\cos[c+dx]} (1 + \cos[c+dx]) \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \left( \frac{3 \operatorname{Csc}[c] \operatorname{Sec}[c]}{5d} + \right. \right. \\
 & \quad \frac{\operatorname{Sec}[c] \operatorname{Sec}[c+dx]^4 \sin[dx]}{7d} + \frac{\operatorname{Sec}[c] \operatorname{Sec}[c+dx]^3 (5 \sin[c] + 7 \sin[dx])}{35d} + \\
 & \quad \frac{\operatorname{Sec}[c] \operatorname{Sec}[c+dx]^2 (21 \sin[c] + 25 \sin[dx])}{105d} + \\
 & \quad \left. \left. \frac{\operatorname{Sec}[c] \operatorname{Sec}[c+dx] (25 \sin[c] + 63 \sin[dx])}{105d} \right) - \right. \\
 & \left( 5 (1 + \cos[c+dx]) \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]\right]^2 \right) \\
 & \quad \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \operatorname{Sec}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 - \sin[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \\
 & \quad \left. \sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \sin[c] \sin[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1 + \sin[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]}} \right) / \\
 & \left( 21d \sqrt{1 + \operatorname{Cot}[c]^2} \right) + \frac{1}{10d} 3 (1 + \cos[c+dx]) \operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \\
 & \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos[dx + \operatorname{ArcTan}[\operatorname{Tan}[c]]]\right]^2 \right) \\
 & \quad \left. \operatorname{Sin}[dx + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c] \right) / \\
 & \left( \sqrt{1 - \cos[dx + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1 + \cos[dx + \operatorname{ArcTan}[\operatorname{Tan}[c]]]} \right. \\
 & \quad \left. \sqrt{\cos[c] \cos[dx + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1 + \operatorname{Tan}[c]^2} \sqrt{1 + \operatorname{Tan}[c]^2}} \right) - \\
 & \quad \left. \frac{\frac{\operatorname{Sin}[dx + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c]}{\sqrt{1 + \operatorname{Tan}[c]^2}} + \frac{2 \cos[c]^2 \cos[dx + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1 + \operatorname{Tan}[c]^2}}{\cos[c]^2 + \sin[c]^2}}{\sqrt{\cos[c] \cos[dx + \operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1 + \operatorname{Tan}[c]^2}}} \right)
 \end{aligned}$$

**Problem 359: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos [c + d x]^{9/2} (a + a \operatorname{Sec} [c + d x])^2 dx$$

Optimal (type 4, 147 leaves, 10 steps):

$$\frac{32 a^2 \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right]}{15 d} + \frac{20 a^2 \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right]}{21 d} +$$

$$\frac{20 a^2 \sqrt{\cos [c + d x]} \sin [c + d x]}{21 d} + \frac{32 a^2 \cos [c + d x]^{3/2} \sin [c + d x]}{45 d} +$$

$$\frac{4 a^2 \cos [c + d x]^{5/2} \sin [c + d x]}{7 d} + \frac{2 a^2 \cos [c + d x]^{7/2} \sin [c + d x]}{9 d}$$

Result (type 5, 548 leaves):

$$\begin{aligned}
 & \cos [c+d x]^{5 / 2} \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^4\left(a+a \operatorname{Sec}[c+d x]\right)^2 \\
 & \left(-\frac{8 \cot [c]}{15 d}+\frac{23 \cos [d x] \sin [c]}{84 d}+\frac{37 \cos [2 d x] \sin [2 c]}{360 d}+\right. \\
 & \quad \frac{\cos [3 d x] \sin [3 c]}{28 d}+\frac{\cos [4 d x] \sin [4 c]}{144 d}+\frac{23 \cos [c] \sin [d x]}{84 d}+ \\
 & \quad \left.\frac{37 \cos [2 c] \sin [2 d x]}{360 d}+\frac{\cos [3 c] \sin [3 d x]}{28 d}+\frac{\cos [4 c] \sin [4 d x]}{144 d}\right)- \\
 & \left(5 \cos [c+d x]^2 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]]^2\right]\right. \\
 & \quad \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^4\left(a+a \operatorname{Sec}[c+d x]\right)^2 \operatorname{Sec}[d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]]} \\
 & \quad \left.\sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]]} \sqrt{1+\sin [d x-\operatorname{ArcTan}[\cot [c]]]}\right) / \\
 & \left(21 d \sqrt{1+\cot [c]^2}\right)-\frac{1}{15 d} 4 \cos [c+d x]^2 \operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^4\left(a+a \operatorname{Sec}[c+d x]\right)^2 \\
 & \left(\operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2},-\frac{1}{4}\right\},\left\{\frac{3}{4}\right\}, \cos [d x+\operatorname{ArcTan}[\tan [c]]]^2\right]\right) \sin [d x+\operatorname{ArcTan}[\tan [c]]] \\
 & \quad \tan [c]) / \left(\sqrt{1-\cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{1+\cos [d x+\operatorname{ArcTan}[\tan [c]]]}\right. \\
 & \quad \left.\sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{1+\tan [c]^2} \sqrt{1+\tan [c]^2}\right)- \\
 & \quad \left.\frac{\frac{\sin [d x+\operatorname{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1+\tan [c]^2}}+\frac{2 \cos [c]^2 \cos [d x+\operatorname{ArcTan}[\tan [c]]] \sqrt{1+\tan [c]^2}}{\cos [c]^2+\sin [c]^2}}{\sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{1+\tan [c]^2}}\right)
 \end{aligned}$$

**Problem 360: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos [c+d x]^{7 / 2}\left(a+a \operatorname{Sec}[c+d x]\right)^2 d x$$

Optimal (type 4, 121 leaves, 9 steps):

$$\frac{12 a^2 \text{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{5 d} + \frac{8 a^2 \text{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{7 d} + \frac{8 a^2 \sqrt{\cos [c+d x]} \sin [c+d x]}{7 d} + \frac{4 a^2 \cos [c+d x]^{3 / 2} \sin [c+d x]}{5 d} + \frac{2 a^2 \cos [c+d x]^{5 / 2} \sin [c+d x]}{7 d}$$

Result (type 5, 516 leaves):

$$\begin{aligned} & \cos [c+d x]^{5 / 2} \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \sec [c+d x])^2 \\ & \left(-\frac{3 \cot [c]}{5 d}+\frac{17 \cos [d x] \sin [c]}{56 d}+\frac{\cos [2 d x] \sin [2 c]}{10 d}+\frac{\cos [3 d x] \sin [3 c]}{56 d}+\frac{17 \cos [c] \sin [d x]}{56 d}+\frac{\cos [2 c] \sin [2 d x]}{10 d}+\frac{\cos [3 c] \sin [3 d x]}{56 d}\right)-\frac{1}{7 d \sqrt{1+\cot [c]^2}} \\ & 2 \cos [c+d x]^2 \csc [c] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\text{ArcTan}[\cot [c]]]^2\right] \\ & \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \sec [c+d x])^2 \sec [d x-\text{ArcTan}[\cot [c]]] \sqrt{1-\sin [d x-\text{ArcTan}[\cot [c]]]} \\ & \sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\text{ArcTan}[\cot [c]]] \sqrt{1+\sin [d x-\text{ArcTan}[\cot [c]]]}-} \\ & \frac{1}{10 d} 3 \cos [c+d x]^2 \csc [c] \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \sec [c+d x])^2 \\ & \left(\text{HypergeometricPFQ}\left[\left\{-\frac{1}{2},-\frac{1}{4}\right\},\left\{\frac{3}{4}\right\}, \cos [d x+\text{ArcTan}[\tan [c]]]^2\right] \sin [d x+\text{ArcTan}[\tan [c]]]\right. \\ & \left.\tan [c]\right) / \left(\sqrt{1-\cos [d x+\text{ArcTan}[\tan [c]]]} \sqrt{1+\cos [d x+\text{ArcTan}[\tan [c]]]}\right) \\ & \sqrt{\cos [c] \cos [d x+\text{ArcTan}[\tan [c]]] \sqrt{1+\tan [c]^2} \sqrt{1+\tan [c]^2}}- \\ & \frac{\frac{\sin [d x+\text{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1+\tan [c]^2}}+\frac{2 \cos [c]^2 \cos [d x+\text{ArcTan}[\tan [c]]] \sqrt{1+\tan [c]^2}}{\cos [c]^2+\sin [c]^2}}{\sqrt{\cos [c] \cos [d x+\text{ArcTan}[\tan [c]]] \sqrt{1+\tan [c]^2}}} \end{aligned}$$

**Problem 361: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos [c+d x]^{5 / 2}(a+a \sec [c+d x])^2 d x$$

Optimal (type 4, 95 leaves, 8 steps):



$$\frac{16 a^2 \text{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{5 d} + \frac{4 a^2 \text{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{3 d} + \frac{4 a^2 \sqrt{\cos [c+d x]} \sin [c+d x]}{3 d} + \frac{2 a^2 \cos [c+d x]^{3 / 2} \sin [c+d x]}{5 d}$$

Result (type 5, 484 leaves):

$$\begin{aligned} & \cos [c+d x]^{5 / 2} \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \sec [c+d x])^2 \\ & \left(-\frac{4 \cot [c]}{5 d}+\frac{\cos [d x] \sin [c]}{3 d}+\frac{\cos [2 d x] \sin [2 c]}{20 d}+\frac{\cos [c] \sin [d x]}{3 d}+\frac{\cos [2 c] \sin [2 d x]}{20 d}\right) - \\ & \frac{1}{3 d \sqrt{1+\cot [c]^2}} \cos [c+d x]^2 \csc [c] \\ & \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\text{ArcTan}[\cot [c]]]^2\right] \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^4 \\ & (a+a \sec [c+d x])^2 \sec [d x-\text{ArcTan}[\cot [c]]] \sqrt{1-\sin [d x-\text{ArcTan}[\cot [c]]]} \\ & \sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\text{ArcTan}[\cot [c]]] \sqrt{1+\sin [d x-\text{ArcTan}[\cot [c]]]} -} \\ & \frac{1}{5 d} 2 \cos [c+d x]^2 \csc [c] \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \sec [c+d x])^2 \\ & \left(\text{HypergeometricPFQ}\left[\left\{-\frac{1}{2},-\frac{1}{4}\right\},\left\{\frac{3}{4}\right\}, \cos [d x+\text{ArcTan}[\tan [c]]]^2\right] \sin [d x+\text{ArcTan}[\tan [c]]] \right. \\ & \left. \tan [c]\right) / \left(\sqrt{1-\cos [d x+\text{ArcTan}[\tan [c]]]} \sqrt{1+\cos [d x+\text{ArcTan}[\tan [c]]]}\right) \\ & \left(\sqrt{\cos [c] \cos [d x+\text{ArcTan}[\tan [c]]] \sqrt{1+\tan [c]^2} \sqrt{1+\tan [c]^2}} - \right. \\ & \left. \frac{\frac{\sin [d x+\text{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1+\tan [c]^2}}+\frac{2 \cos [c]^2 \cos [d x+\text{ArcTan}[\tan [c]]] \sqrt{1+\tan [c]^2}}{\cos [c]^2+\sin [c]^2}}{\sqrt{\cos [c] \cos [d x+\text{ArcTan}[\tan [c]]] \sqrt{1+\tan [c]^2}}}\right) \end{aligned}$$

**Problem 362: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos [c+d x]^{3 / 2} (a+a \sec [c+d x])^2 d x$$

Optimal (type 4, 67 leaves, 7 steps):

$$\frac{4 a^2 \text{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{d} + \frac{8 a^2 \text{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{3 d} + \frac{2 a^2 \sqrt{\cos [c+d x]} \sin [c+d x]}{3 d}$$

Result (type 5, 450 leaves):

$$\begin{aligned} & \cos [c+d x]^{5 / 2} \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^4\left(a+a \operatorname{Sec}[c+d x]\right)^2 \\ & \left(-\frac{\cot [c]}{d}+\frac{\cos [d x] \sin [c]}{6 d}+\frac{\cos [c] \sin [d x]}{6 d}\right)-\frac{1}{3 d \sqrt{1+\cot [c]^2}} \\ & 2 \cos [c+d x]^2 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]]^2\right] \\ & \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^4\left(a+a \operatorname{Sec}[c+d x]\right)^2 \operatorname{Sec}[d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]]} \\ & \sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1+\sin [d x-\operatorname{ArcTan}[\cot [c]]]}-} \\ & \frac{1}{2 d} \cos [c+d x]^2 \operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^4\left(a+a \operatorname{Sec}[c+d x]\right)^2 \\ & \left(\operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2},-\frac{1}{4}\right\},\left\{\frac{3}{4}\right\}, \cos [d x+\operatorname{ArcTan}[\tan [c]]]^2\right] \sin [d x+\operatorname{ArcTan}[\tan [c]]]\right. \\ & \left.\tan [c]\right) / \left(\sqrt{1-\cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{1+\cos [d x+\operatorname{ArcTan}[\tan [c]]]}\right) \\ & \sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]] \sqrt{1+\tan [c]^2} \sqrt{1+\tan [c]^2}}- \\ & \left.\frac{\frac{\sin [d x+\operatorname{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1+\tan [c]^2}}+\frac{2 \cos [c]^2 \cos [d x+\operatorname{ArcTan}[\tan [c]]] \sqrt{1+\tan [c]^2}}{\cos [c]^2+\sin [c]^2}}{\sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]] \sqrt{1+\tan [c]^2}}}\right) \end{aligned}$$

**Problem 364:** Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(a+a \operatorname{Sec}[c+d x])^2}{\sqrt{\cos [c+d x]}} d x$$

Optimal (type 4, 91 leaves, 8 steps):

$$\begin{aligned}
 & - \frac{4 a^2 \text{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{d} + \\
 & \frac{8 a^2 \text{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{3 d} + \frac{2 a^2 \sin [c+d x]}{3 d \cos [c+d x]^{3 / 2}} + \frac{4 a^2 \sin [c+d x]}{d \sqrt{\cos [c+d x]}}
 \end{aligned}$$

Result (type 5, 470 leaves):

$$\begin{aligned}
 & \cos [c+d x]^{5 / 2} \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \sec [c+d x])^2 \\
 & \left( \frac{\csc [c] \sec [c]}{d} + \frac{\sec [c] \sec [c+d x]^2 \sin [d x]}{6 d} + \frac{\sec [c] \sec [c+d x] (\sin [c]+6 \sin [d x])}{6 d} \right) - \\
 & \frac{1}{3 d \sqrt{1+\cot [c]^2}} 2 \cos [c+d x]^2 \csc [c] \\
 & \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\text{ArcTan}[\cot [c]]]^2\right] \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^4 \\
 & (a+a \sec [c+d x])^2 \sec [d x-\text{ArcTan}[\cot [c]]] \sqrt{1-\sin [d x-\text{ArcTan}[\cot [c]]]} \\
 & \sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\text{ArcTan}[\cot [c]]] \sqrt{1+\sin [d x-\text{ArcTan}[\cot [c]]]} +} \\
 & \frac{1}{2 d} \cos [c+d x]^2 \csc [c] \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \sec [c+d x])^2 \\
 & \left( \text{HypergeometricPFQ}\left[\left\{-\frac{1}{2},-\frac{1}{4}\right\},\left\{\frac{3}{4}\right\}, \cos [d x+\text{ArcTan}[\tan [c]]]^2\right] \sin [d x+\text{ArcTan}[\tan [c]]] \right. \\
 & \left. \tan [c] \right) / \left( \sqrt{1-\cos [d x+\text{ArcTan}[\tan [c]]]} \sqrt{1+\cos [d x+\text{ArcTan}[\tan [c]]]} \right. \\
 & \left. \sqrt{\cos [c] \cos [d x+\text{ArcTan}[\tan [c]]] \sqrt{1+\tan [c]^2} \sqrt{1+\tan [c]^2}} \right) - \\
 & \left( \frac{\sin [d x+\text{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1+\tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x+\text{ArcTan}[\tan [c]]] \sqrt{1+\tan [c]^2}}{\cos [c]^2+\sin [c]^2} \right) \\
 & \left. \sqrt{\cos [c] \cos [d x+\text{ArcTan}[\tan [c]]] \sqrt{1+\tan [c]^2}} \right)
 \end{aligned}$$

**Problem 365: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{(a+a \sec [c+d x])^2}{\cos [c+d x]^{3 / 2}} d x$$

Optimal (type 4, 121 leaves, 9 steps):

$$-\frac{16 a^2 \text{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{5 d} + \frac{4 a^2 \text{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{3 d} + \frac{2 a^2 \sin [c+d x]}{5 d \cos [c+d x]^{5 / 2}} + \frac{4 a^2 \sin [c+d x]}{3 d \cos [c+d x]^{3 / 2}} + \frac{16 a^2 \sin [c+d x]}{5 d \sqrt{\cos [c+d x]}}$$

Result (type 5, 503 leaves):

$$\begin{aligned} & \cos [c+d x]^{5 / 2} \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \sec [c+d x])^2 \\ & \left(\frac{4 \operatorname{Csc}[c] \sec [c]}{5 d}+\frac{\sec [c] \sec [c+d x]^3 \sin [d x]}{10 d}+\frac{\sec [c] \sec [c+d x]^2(3 \sin [c]+10 \sin [d x])}{30 d}+\frac{\sec [c] \sec [c+d x](5 \sin [c]+12 \sin [d x])}{15 d}\right)- \\ & \frac{1}{3 d \sqrt{1+\cot [c]^2}} \cos [c+d x]^2 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\},\right. \\ & \left.\sin [d x-\operatorname{ArcTan}[\cot [c]]]^2\right] \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \sec [c+d x])^2 \\ & \sec [d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]]} \\ & \sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1+\sin [d x-\operatorname{ArcTan}[\cot [c]]]}+} \\ & \frac{1}{5 d} 2 \cos [c+d x]^2 \operatorname{Csc}[c] \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \sec [c+d x])^2 \\ & \left(\operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2},-\frac{1}{4}\right\},\left\{\frac{3}{4}\right\}, \cos [d x+\operatorname{ArcTan}[\tan [c]]]^2\right] \sin [d x+\operatorname{ArcTan}[\tan [c]]]\right. \\ & \left.\tan [c]\right) / \left(\sqrt{1-\cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{1+\cos [d x+\operatorname{ArcTan}[\tan [c]]]}\right) \\ & \sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]] \sqrt{1+\tan [c]^2} \sqrt{1+\tan [c]^2}}- \\ & \frac{\frac{\sin [d x+\operatorname{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1+\tan [c]^2}}+\frac{2 \cos [c]^2 \cos [d x+\operatorname{ArcTan}[\tan [c]]] \sqrt{1+\tan [c]^2}}{\cos [c]^2+\sin [c]^2}}{\sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]] \sqrt{1+\tan [c]^2}}} \end{aligned}$$

Problem 366: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(a + a \operatorname{Sec}[c + d x])^2}{\operatorname{Cos}[c + d x]^{5/2}} dx$$

Optimal (type 4, 147 leaves, 10 steps):

$$-\frac{12 a^2 \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right]}{5 d} + \frac{8 a^2 \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right]}{7 d} + \frac{2 a^2 \operatorname{Sin}[c + d x]}{7 d \operatorname{Cos}[c + d x]^{7/2}} + \frac{4 a^2 \operatorname{Sin}[c + d x]}{5 d \operatorname{Cos}[c + d x]^{5/2}} + \frac{8 a^2 \operatorname{Sin}[c + d x]}{7 d \operatorname{Cos}[c + d x]^{3/2}} + \frac{12 a^2 \operatorname{Sin}[c + d x]}{5 d \sqrt{\operatorname{Cos}[c + d x]}}$$

Result (type 5, 531 leaves):

$$\begin{aligned} & \cos [c+d x]^{5 / 2} \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^4\left(a+a \operatorname{Sec}[c+d x]\right)^2 \\ & \left(\frac{3 \operatorname{Csc}[c] \operatorname{Sec}[c]}{5 d}+\frac{\operatorname{Sec}[c] \operatorname{Sec}[c+d x]^4 \operatorname{Sin}[d x]}{14 d}+\right. \\ & \left.\frac{\operatorname{Sec}[c] \operatorname{Sec}[c+d x]^2\left(7 \operatorname{Sin}[c]+10 \operatorname{Sin}[d x]\right)}{35 d}+\frac{\operatorname{Sec}[c] \operatorname{Sec}[c+d x]^3\left(5 \operatorname{Sin}[c]+14 \operatorname{Sin}[d x]\right)}{70 d}+\right. \\ & \left.\frac{\operatorname{Sec}[c] \operatorname{Sec}[c+d x]\left(10 \operatorname{Sin}[c]+21 \operatorname{Sin}[d x]\right)}{35 d}\right)-\frac{1}{7 d \sqrt{1+\operatorname{Cot}[c]^2}} \\ & 2 \cos [c+d x]^2 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \operatorname{Sin}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \\ & \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^4\left(a+a \operatorname{Sec}[c+d x]\right)^2 \operatorname{Sec}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1-\operatorname{Sin}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} \\ & \sqrt{-\sqrt{1+\operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1+\operatorname{Sin}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]}+} \\ & \frac{1}{10 d} 3 \cos [c+d x]^2 \operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^4\left(a+a \operatorname{Sec}[c+d x]\right)^2 \\ & \left(\operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2},-\frac{1}{4}\right\},\left\{\frac{3}{4}\right\}, \cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]^2\right] \operatorname{Sin}[d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]\right. \\ & \left.\operatorname{Tan}[c]\right) / \left(\sqrt{1-\cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1+\cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]} \right. \\ & \left.\sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1+\operatorname{Tan}[c]^2} \sqrt{1+\operatorname{Tan}[c]^2}}\right)- \\ & \left.\frac{\frac{\operatorname{Sin}[d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c]}{\sqrt{1+\operatorname{Tan}[c]^2}}+\frac{2 \cos [c]^2 \cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1+\operatorname{Tan}[c]^2}}{\cos [c]^2+\operatorname{Sin}[c]^2}}{\sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1+\operatorname{Tan}[c]^2}}}\right) \end{aligned}$$

**Problem 367: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos [c+d x]^{9 / 2}\left(a+a \operatorname{Sec}[c+d x]\right)^3 d x$$

Optimal (type 4, 147 leaves, 17 steps):

$$\frac{68 a^3 \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right]}{15 d} + \frac{44 a^3 \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right]}{21 d} +$$

$$\frac{44 a^3 \sqrt{\cos [c+dx]} \sin [c+dx]}{21 d} + \frac{68 a^3 \cos [c+dx]^{3/2} \sin [c+dx]}{45 d} +$$

$$\frac{6 a^3 \cos [c+dx]^{5/2} \sin [c+dx]}{7 d} + \frac{2 a^3 \cos [c+dx]^{7/2} \sin [c+dx]}{9 d}$$

Result (type 5, 548 leaves):

$$\cos [c+dx]^{7/2} \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a+a \operatorname{Sec}[c+dx])^3$$

$$\left(-\frac{17 \cot [c]}{30 d} + \frac{97 \cos [dx] \sin [c]}{336 d} + \frac{73 \cos [2 dx] \sin [2 c]}{720 d} + \frac{3 \cos [3 dx] \sin [3 c]}{112 d} + \frac{\cos [4 dx] \sin [4 c]}{288 d} + \frac{97 \cos [c] \sin [dx]}{336 d} + \frac{73 \cos [2 c] \sin [2 dx]}{720 d} + \frac{3 \cos [3 c] \sin [3 dx]}{112 d} + \frac{\cos [4 c] \sin [4 dx]}{288 d}\right) -$$

$$\left(11 \cos [c+dx]^3 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin [dx - \operatorname{ArcTan}[\cot [c]]]^2\right]\right.$$

$$\operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a+a \operatorname{Sec}[c+dx])^3 \operatorname{Sec}[dx - \operatorname{ArcTan}[\cot [c]]] \sqrt{1 - \sin [dx - \operatorname{ArcTan}[\cot [c]]]}$$

$$\left.\sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [dx - \operatorname{ArcTan}[\cot [c]]] \sqrt{1 + \sin [dx - \operatorname{ArcTan}[\cot [c]]}}\right) /$$

$$\left(42 d \sqrt{1 + \cot [c]^2}\right) - \frac{1}{60 d} 17 \cos [c+dx]^3 \operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a+a \operatorname{Sec}[c+dx])^3$$

$$\left(\operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos [dx + \operatorname{ArcTan}[\tan [c]]]^2\right] \sin [dx + \operatorname{ArcTan}[\tan [c]]]\right.$$

$$\left.\tan [c]\right) / \left(\sqrt{1 - \cos [dx + \operatorname{ArcTan}[\tan [c]]]} \sqrt{1 + \cos [dx + \operatorname{ArcTan}[\tan [c]]]}\right.$$

$$\left.\sqrt{\cos [c] \cos [dx + \operatorname{ArcTan}[\tan [c]]]} \sqrt{1 + \tan [c]^2} \sqrt{1 + \tan [c]^2}\right) -$$

$$\frac{\frac{\sin [dx + \operatorname{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1 + \tan [c]^2}} + \frac{2 \cos [c]^2 \cos [dx + \operatorname{ArcTan}[\tan [c]]] \sqrt{1 + \tan [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [dx + \operatorname{ArcTan}[\tan [c]]]} \sqrt{1 + \tan [c]^2}}$$

Problem 368: Result unnecessarily involves higher level functions and more

than twice size of optimal antiderivative.

$$\int \cos [c+d x]^{7 / 2}(a+a \operatorname{Sec}[c+d x])^3 d x$$

Optimal (type 4, 121 leaves, 15 steps):

$$\frac{28 a^3 \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{5 d} + \frac{52 a^3 \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{21 d} + \frac{52 a^3 \sqrt{\cos [c+d x]} \sin [c+d x]}{21 d} + \frac{6 a^3 \cos [c+d x]^{3 / 2} \sin [c+d x]}{5 d} + \frac{2 a^3 \cos [c+d x]^{5 / 2} \sin [c+d x]}{7 d}$$

Result (type 5, 516 leaves):

$$\begin{aligned} & \cos [c+d x]^{7 / 2} \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^6(a+a \operatorname{Sec}[c+d x])^3 \\ & \left(-\frac{7 \cot [c]}{10 d}+\frac{107 \cos [d x] \sin [c]}{336 d}+\frac{3 \cos [2 d x] \sin [2 c]}{40 d}+\frac{\cos [3 d x] \sin [3 c]}{112 d}+\right. \\ & \left.\frac{107 \cos [c] \sin [d x]}{336 d}+\frac{3 \cos [2 c] \sin [2 d x]}{40 d}+\frac{\cos [3 c] \sin [3 d x]}{112 d}\right)- \\ & \left(13 \cos [c+d x]^3 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]]^2\right]\right. \\ & \left.\operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^6(a+a \operatorname{Sec}[c+d x])^3 \operatorname{Sec}[d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]]}\right. \\ & \left.\sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1+\sin [d x-\operatorname{ArcTan}[\cot [c]]]}}\right) / \\ & \left(42 d \sqrt{1+\cot [c]^2}\right)-\frac{1}{20 d} 7 \cos [c+d x]^3 \operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^6(a+a \operatorname{Sec}[c+d x])^3 \\ & \left(\operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2},-\frac{1}{4}\right\},\left\{\frac{3}{4}\right\}, \cos [d x+\operatorname{ArcTan}[\tan [c]]]^2\right]\right) \sin [d x+\operatorname{ArcTan}[\tan [c]]] \\ & \left.\tan [c]\right) / \left(\sqrt{1-\cos [d x+\operatorname{ArcTan}[\tan [c]]] \sqrt{1+\cos [d x+\operatorname{ArcTan}[\tan [c]]]}\right. \\ & \left.\sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]] \sqrt{1+\tan [c]^2} \sqrt{1+\tan [c]^2}}\right)- \\ & \left.\frac{\frac{\sin [d x+\operatorname{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1+\tan [c]^2}}+\frac{2 \cos [c]^2 \cos [d x+\operatorname{ArcTan}[\tan [c]]] \sqrt{1+\tan [c]^2}}{\cos [c]^2+\sin [c]^2}}{\sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]] \sqrt{1+\tan [c]^2}}}\right) \end{aligned}$$



**Problem 369: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos [c+d x]^{5 / 2} (a+a \operatorname{Sec}[c+d x])^3 d x$$

Optimal (type 4, 91 leaves, 13 steps):

$$\frac{36 a^3 \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{5 d} + \frac{4 a^3 \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{d} + \frac{2 a^3 \sqrt{\cos [c+d x]} \sin [c+d x]}{d} + \frac{2 a^3 \cos [c+d x]^{3 / 2} \sin [c+d x]}{5 d}$$

Result (type 5, 484 leaves):

$$\begin{aligned} & \cos [c+d x]^{7 / 2} \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \operatorname{Sec}[c+d x])^3 \\ & \left(-\frac{9 \cot [c]}{10 d}+\frac{\cos [d x] \sin [c]}{4 d}+\frac{\cos [2 d x] \sin [2 c]}{40 d}+\frac{\cos [c] \sin [d x]}{4 d}+\frac{\cos [2 c] \sin [2 d x]}{40 d}\right) - \\ & \frac{1}{2 d \sqrt{1+\cot [c]^2}} \cos [c+d x]^3 \operatorname{Csc}[c] \\ & \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]]^2\right] \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^6 \\ & (a+a \operatorname{Sec}[c+d x])^3 \operatorname{Sec}[d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]]} \\ & \sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1+\sin [d x-\operatorname{ArcTan}[\cot [c]]]} - \\ & \frac{1}{20 d} 9 \cos [c+d x]^3 \operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \operatorname{Sec}[c+d x])^3 \\ & \left(\operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2},-\frac{1}{4}\right\},\left\{\frac{3}{4}\right\}, \cos [d x+\operatorname{ArcTan}[\tan [c]]]^2\right] \sin [d x+\operatorname{ArcTan}[\tan [c]]] \right. \\ & \left. \tan [c]\right) / \left(\sqrt{1-\cos [d x+\operatorname{ArcTan}[\tan [c]]] \sqrt{1+\cos [d x+\operatorname{ArcTan}[\tan [c]]]} \right. \\ & \left. \sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]] \sqrt{1+\tan [c]^2} \sqrt{1+\tan [c]^2}}\right) - \\ & \left. \frac{\sin [d x+\operatorname{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1+\tan [c]^2}}+\frac{2 \cos [c]^2 \cos [d x+\operatorname{ArcTan}[\tan [c]]] \sqrt{1+\tan [c]^2}}{\cos [c]^2+\sin [c]^2}\right) \\ & \left. \sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]] \sqrt{1+\tan [c]^2}}\right) \end{aligned}$$

Problem 370: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \cos [c + d x]^{3/2} (a + a \operatorname{Sec} [c + d x])^3 dx$$

Optimal (type 4, 91 leaves, 13 steps):

$$\frac{4 a^3 \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right]}{d} + \frac{20 a^3 \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right]}{3 d} +$$

$$\frac{2 a^3 \operatorname{Sin}[c + d x]}{d \sqrt{\operatorname{Cos}[c + d x]}} + \frac{2 a^3 \sqrt{\operatorname{Cos}[c + d x]} \operatorname{Sin}[c + d x]}{3 d}$$

Result (type 5, 481 leaves):

$$\begin{aligned}
 & \cos [c+d x]^{7 / 2} \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \operatorname{Sec}[c+d x])^3 \\
 & \left(-\frac{(1+3 \cos [2 c]) \operatorname{Csc}[c] \operatorname{Sec}[c]}{8 d}+\frac{\cos [d x] \sin [c]}{12 d}+\right. \\
 & \left.\frac{\cos [c] \sin [d x]}{12 d}+\frac{\operatorname{Sec}[c] \operatorname{Sec}[c+d x] \sin [d x]}{4 d}\right)-\frac{1}{6 d \sqrt{1+\cot [c]^2}} \\
 & 5 \cos [c+d x]^3 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]]^2\right] \\
 & \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \operatorname{Sec}[c+d x])^3 \operatorname{Sec}[d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]]} \\
 & \sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1+\sin [d x-\operatorname{ArcTan}[\cot [c]]]}-} \\
 & \frac{1}{4 d} \cos [c+d x]^3 \operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \operatorname{Sec}[c+d x])^3 \\
 & \left(\operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2},-\frac{1}{4}\right\},\left\{\frac{3}{4}\right\}, \cos [d x+\operatorname{ArcTan}[\tan [c]]]^2\right] \sin [d x+\operatorname{ArcTan}[\tan [c]]]\right. \\
 & \left.\tan [c]\right) / \left(\sqrt{1-\cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{1+\cos [d x+\operatorname{ArcTan}[\tan [c]]]}\right. \\
 & \left.\sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{1+\tan [c]^2} \sqrt{1+\tan [c]^2}\right)- \\
 & \left.\frac{\frac{\sin [d x+\operatorname{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1+\tan [c]^2}}+\frac{2 \cos [c]^2 \cos [d x+\operatorname{ArcTan}[\tan [c]]] \sqrt{1+\tan [c]^2}}{\cos [c]^2+\sin [c]^2}}{\sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{1+\tan [c]^2}}\right)
 \end{aligned}$$

**Problem 371: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \sqrt{\cos [c+d x]} (a+a \operatorname{Sec}[c+d x])^3 dx$$

Optimal (type 4, 91 leaves, 13 steps):

$$\begin{aligned}
 & -\frac{4 a^3 \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{d}+ \\
 & \frac{20 a^3 \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{3 d}+\frac{2 a^3 \sin [c+d x]}{3 d \cos [c+d x]^{3 / 2}}+\frac{6 a^3 \sin [c+d x]}{d \sqrt{\cos [c+d x]}}
 \end{aligned}$$

Result (type 5, 479 leaves):

$$\begin{aligned} & \cos [c+d x]^{7 / 2} \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \operatorname{Sec}[c+d x])^3 \\ & \left(-\frac{(-5+\cos [2 c]) \operatorname{Csc}[c] \operatorname{Sec}[c]}{8 d}+\frac{\operatorname{Sec}[c] \operatorname{Sec}[c+d x]^2 \sin [d x]}{12 d}+\right. \\ & \left.\frac{\operatorname{Sec}[c] \operatorname{Sec}[c+d x](\sin [c]+9 \sin [d x])}{12 d}\right)-\frac{1}{6 d \sqrt{1+\cot [c]^2}} \\ & 5 \cos [c+d x]^3 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]]^2\right] \\ & \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \operatorname{Sec}[c+d x])^3 \operatorname{Sec}[d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]]} \\ & \sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1+\sin [d x-\operatorname{ArcTan}[\cot [c]]]}+} \\ & \frac{1}{4 d} \cos [c+d x]^3 \operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \operatorname{Sec}[c+d x])^3 \\ & \left(\operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2},-\frac{1}{4}\right\},\left\{\frac{3}{4}\right\}, \cos [d x+\operatorname{ArcTan}[\tan [c]]]^2\right] \sin [d x+\operatorname{ArcTan}[\tan [c]]]\right. \\ & \left.\tan [c]\right) / \left(\sqrt{1-\cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{1+\cos [d x+\operatorname{ArcTan}[\tan [c]]]}\right. \\ & \left.\sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]] \sqrt{1+\tan [c]^2} \sqrt{1+\tan [c]^2}}\right)- \\ & \left.\frac{\frac{\sin [d x+\operatorname{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1+\tan [c]^2}}+\frac{2 \cos [c]^2 \cos [d x+\operatorname{ArcTan}[\tan [c]]] \sqrt{1+\tan [c]^2}}{\cos [c]^2+\sin [c]^2}}{\sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]] \sqrt{1+\tan [c]^2}}}\right) \end{aligned}$$

**Problem 372: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{(a+a \operatorname{Sec}[c+d x])^3}{\sqrt{\cos [c+d x]}} d x$$

Optimal (type 4, 117 leaves, 15 steps):

$$\begin{aligned}
 & - \frac{36 a^3 \text{EllipticE}\left[\frac{1}{2}(c+dx), 2\right]}{5 d} + \frac{4 a^3 \text{EllipticF}\left[\frac{1}{2}(c+dx), 2\right]}{d} + \\
 & \frac{2 a^3 \text{Sin}[c+dx]}{5 d \text{Cos}[c+dx]^{5/2}} + \frac{2 a^3 \text{Sin}[c+dx]}{d \text{Cos}[c+dx]^{3/2}} + \frac{36 a^3 \text{Sin}[c+dx]}{5 d \sqrt{\text{Cos}[c+dx]}}
 \end{aligned}$$

Result (type 5, 501 leaves):

$$\begin{aligned}
 & \text{Cos}[c+dx]^{7/2} \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \text{Sec}[c+dx])^3 \\
 & \left( \frac{9 \text{Csc}[c] \text{Sec}[c]}{10 d} + \frac{\text{Sec}[c] \text{Sec}[c+dx]^3 \text{Sin}[dx]}{20 d} + \frac{\text{Sec}[c] \text{Sec}[c+dx]^2 (\text{Sin}[c] + 5 \text{Sin}[dx])}{20 d} + \right. \\
 & \left. \frac{\text{Sec}[c] \text{Sec}[c+dx] (5 \text{Sin}[c] + 18 \text{Sin}[dx])}{20 d} \right) - \frac{1}{2 d \sqrt{1 + \text{Cot}[c]^2}} \\
 & \text{Cos}[c+dx]^3 \text{Csc}[c] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]^2\right] \\
 & \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \text{Sec}[c+dx])^3 \text{Sec}[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 - \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} \\
 & \sqrt{-\sqrt{1 + \text{Cot}[c]^2} \text{Sin}[c] \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 + \text{Sin}[dx - \text{ArcTan}[\text{Cot}[c]]]} +} \\
 & \frac{1}{20 d} 9 \text{Cos}[c+dx]^3 \text{Csc}[c] \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \text{Sec}[c+dx])^3 \\
 & \left( \text{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]]^2\right] \text{Sin}[dx + \text{ArcTan}[\text{Tan}[c]]] \right. \\
 & \left. \text{Tan}[c] \right) / \left( \sqrt{1 - \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]]} \right. \\
 & \left. \sqrt{\text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2} \sqrt{1 + \text{Tan}[c]^2}} \right) - \\
 & \left. \frac{\frac{\text{Sin}[dx + \text{ArcTan}[\text{Tan}[c]]] \text{Tan}[c]}{\sqrt{1 + \text{Tan}[c]^2}} + \frac{2 \text{Cos}[c]^2 \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}}{\text{Cos}[c]^2 + \text{Sin}[c]^2}}{\sqrt{\text{Cos}[c] \text{Cos}[dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \text{Tan}[c]^2}}} \right)
 \end{aligned}$$

**Problem 373: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{(a + a \text{Sec}[c+dx])^3}{\text{Cos}[c+dx]^{3/2}} dx$$

Optimal (type 4, 147 leaves, 17 steps):

$$-\frac{28 a^3 \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{5 d} + \frac{52 a^3 \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{21 d} + \frac{2 a^3 \sin [c+d x]}{7 d \cos [c+d x]^{7 / 2}} + \frac{6 a^3 \sin [c+d x]}{5 d \cos [c+d x]^{5 / 2}} + \frac{52 a^3 \sin [c+d x]}{21 d \cos [c+d x]^{3 / 2}} + \frac{28 a^3 \sin [c+d x]}{5 d \sqrt{\cos [c+d x]}}$$

Result (type 5, 531 leaves):

$$\begin{aligned} & \cos [c+d x]^{7 / 2} \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \operatorname{Sec}[c+d x])^3 \left( \frac{7 \operatorname{Csc}[c] \operatorname{Sec}[c]}{10 d} + \right. \\ & \quad \frac{\operatorname{Sec}[c] \operatorname{Sec}[c+d x]^4 \sin [d x]}{28 d} + \frac{\operatorname{Sec}[c] \operatorname{Sec}[c+d x]^3 (5 \sin [c]+21 \sin [d x])}{140 d} + \\ & \quad \frac{\operatorname{Sec}[c] \operatorname{Sec}[c+d x]^2 (63 \sin [c]+130 \sin [d x])}{420 d} + \\ & \quad \left. \frac{\operatorname{Sec}[c] \operatorname{Sec}[c+d x] (65 \sin [c]+147 \sin [d x])}{210 d} \right) - \\ & \left( 13 \cos [c+d x]^3 \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]^2\right] \right. \\ & \quad \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \operatorname{Sec}[c+d x])^3 \operatorname{Sec}[d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]]} \\ & \quad \left. \sqrt{-\sqrt{1+\operatorname{Cot}[c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]] \sqrt{1+\sin [d x-\operatorname{ArcTan}[\operatorname{Cot}[c]]}} \right) / \\ & \left( 42 d \sqrt{1+\operatorname{Cot}[c]^2} \right) + \frac{1}{20 d} 7 \cos [c+d x]^3 \operatorname{Csc}[c] \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \operatorname{Sec}[c+d x])^3 \\ & \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2},-\frac{1}{4}\right\},\left\{\frac{3}{4}\right\}, \cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]^2\right] \sin [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]] \right. \\ & \quad \left. \operatorname{Tan}[c] \right) / \left( \sqrt{1-\cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1+\cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]} \right. \\ & \quad \left. \sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1+\operatorname{Tan}[c]^2} \sqrt{1+\operatorname{Tan}[c]^2} \right) - \\ & \left. \frac{\frac{\sin [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]] \operatorname{Tan}[c]}{\sqrt{1+\operatorname{Tan}[c]^2}} + \frac{2 \cos [c]^2 \cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]] \sqrt{1+\operatorname{Tan}[c]^2}}{\cos [c]^2+\sin [c]^2}}{\sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\operatorname{Tan}[c]]]} \sqrt{1+\operatorname{Tan}[c]^2}} \right) \end{aligned}$$

Problem 374: Result unnecessarily involves higher level functions and more

than twice size of optimal antiderivative.

$$\int \frac{\cos [c+d x]^{5 / 2}}{a+a \sec [c+d x]} d x$$

Optimal (type 4, 128 leaves, 9 steps):

$$\frac{21 \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{5 a d} - \frac{5 \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{3 a d} - \frac{5 \sqrt{\cos [c+d x]} \sin [c+d x]}{3 a d} + \frac{7 \cos [c+d x]^{3 / 2} \sin [c+d x]}{5 a d} - \frac{\cos [c+d x]^{3 / 2} \sin [c+d x]}{d(a+a \sec [c+d x])}$$

Result (type 5, 314 leaves):

$$\left(\cos \left[\frac{1}{2}(c+d x)\right]\right)^2 \left(\left(2 i \sqrt{2} e^{-i(c+d x)}\left(63\left(1+e^{2 i(c+d x)}\right)+63\left(-1+e^{2 i c}\right) \sqrt{1+e^{2 i(c+d x)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4},-e^{2 i(c+d x)}\right]+25 e^{i(c+d x)}\left(-1+e^{2 i c}\right) \sqrt{1+e^{2 i(c+d x)}} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, \frac{1}{2}, \frac{5}{4},-e^{2 i(c+d x)}\right]\right) \sec [c+d x]\right) / \left(d\left(-1+e^{2 i c}\right) \sqrt{e^{-i(c+d x)}\left(1+e^{2 i(c+d x)}\right)}\right)+\left(-96 \cot [c]-30 \csc [c]-20 \cos [d x] \sin [c]+6 \cos [2 d x] \sin [2 c]-30 \sec \left[\frac{c}{2}\right] \sec \left[\frac{1}{2}(c+d x)\right] \sin \left[\frac{d x}{2}\right]-20 \cos [c] \sin [d x]+6 \cos [2 c] \sin [2 d x]\right) / \left(d \sqrt{\cos [c+d x]}\right)\right) / \left(15 a\left(1+\sec [c+d x]\right)\right)$$

Problem 375: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\cos [c+d x]^{3 / 2}}{a+a \sec [c+d x]} d x$$

Optimal (type 4, 100 leaves, 8 steps):

$$-\frac{3 \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{a d} + \frac{5 \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{3 a d} + \frac{5 \sqrt{\cos [c+d x]} \sin [c+d x]}{3 a d} - \frac{\sqrt{\cos [c+d x]} \sin [c+d x]}{d(a+a \sec [c+d x])}$$

Result (type 5, 292 leaves):

$$\left( \cos\left[\frac{1}{2}(c+dx)\right]^2 \left( - \left( \left( 2i\sqrt{2} e^{-i(c+dx)} \left( 9(1+e^{2i(c+dx)}) + 9(-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] + 5e^{i(c+dx)}(-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, \frac{1}{2}, \frac{5}{4}, -e^{2i(c+dx)}\right]\right) \operatorname{Sec}[c+dx] \right) / \left( d(-1+e^{2ic}) \sqrt{e^{-i(c+dx)}(1+e^{2i(c+dx)})} \right) \right) + \left( 12 \cot[c] + 6 \csc[c] + 4 \cos[dx] \sin[c] + 6 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right] \sin\left[\frac{dx}{2}\right] + 4 \cos[c] \sin[dx] \right) / \left( d \sqrt{\cos[c+dx]} \right) \right) / \left( 3a(1+\operatorname{Sec}[c+dx]) \right)$$

Problem 376: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\sqrt{\cos[c+dx]}}{a+a \operatorname{Sec}[c+dx]} dx$$

Optimal (type 4, 72 leaves, 7 steps):

$$\frac{3 \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right]}{ad} - \frac{\operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right]}{ad} - \frac{\sin[c+dx]}{d \sqrt{\cos[c+dx]} (a+a \operatorname{Sec}[c+dx])}$$

Result (type 5, 270 leaves):

$$\left( \cos\left[\frac{1}{2}(c+dx)\right]^2 \left( \left( 2i\sqrt{2} e^{-i(c+dx)} \left( 3(1+e^{2i(c+dx)}) + 3(-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] + e^{i(c+dx)}(-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, \frac{1}{2}, \frac{5}{4}, -e^{2i(c+dx)}\right]\right) \operatorname{Sec}[c+dx] \right) / \left( d(-1+e^{2ic}) \sqrt{e^{-i(c+dx)}(1+e^{2i(c+dx)})} \right) - \frac{2 \left( 2 \cot[c] + \csc[c] + \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right] \sin\left[\frac{dx}{2}\right] \right)}{d \sqrt{\cos[c+dx]}} \right) \right) / \left( a(1+\operatorname{Sec}[c+dx]) \right)$$

Problem 377: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{1}{\sqrt{\cos[c+dx]} (a+a \operatorname{Sec}[c+dx])} dx$$

Optimal (type 4, 70 leaves, 7 steps):



$$-\frac{\text{EllipticE}\left[\frac{1}{2}(c+dx), 2\right]}{ad} + \frac{\text{EllipticF}\left[\frac{1}{2}(c+dx), 2\right]}{ad} + \frac{\text{Sin}[c+dx]}{d\sqrt{\text{Cos}[c+dx]}(a+a\text{Sec}[c+dx])}$$

Result (type 5, 262 leaves):

$$\left( \text{Cos}\left[\frac{1}{2}(c+dx)\right]^2 \right. \\ \left. - \left( \left( 2i\sqrt{2}e^{-i(c+dx)} \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic})\sqrt{1 + e^{2i(c+dx)}} \text{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right. \right. \right. \right. \\ \left. \left. \left. - e^{2i(c+dx)} \right) + e^{i(c+dx)}(-1 + e^{2ic})\sqrt{1 + e^{2i(c+dx)}} \text{Hypergeometric2F1}\left[\frac{1}{4}, \frac{1}{2}, \frac{5}{4}, -e^{2i(c+dx)}\right] \right) \text{Sec}[c+dx] \right) / \left( d(-1 + e^{2ic})\sqrt{e^{-i(c+dx)}(1 + e^{2i(c+dx)})} \right) \right) + \\ \left. \frac{2\left(\text{Csc}[c] + \text{Sec}\left[\frac{c}{2}\right]\text{Sec}\left[\frac{1}{2}(c+dx)\right]\text{Sin}\left[\frac{dx}{2}\right]\right)}{d\sqrt{\text{Cos}[c+dx]}} \right) / (a(1 + \text{Sec}[c+dx]))$$

**Problem 378: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{1}{\text{Cos}[c+dx]^{3/2}(a+a\text{Sec}[c+dx])} dx$$

Optimal (type 4, 70 leaves, 7 steps):

$$\frac{\text{EllipticE}\left[\frac{1}{2}(c+dx), 2\right]}{ad} + \frac{\text{EllipticF}\left[\frac{1}{2}(c+dx), 2\right]}{ad} - \frac{\text{Sin}[c+dx]}{d\sqrt{\text{Cos}[c+dx]}(a+a\text{Sec}[c+dx])}$$

Result (type 5, 263 leaves):

$$\left( \text{Cos}\left[\frac{1}{2}(c+dx)\right]^2 \left( \left( 2i\sqrt{2}e^{-i(c+dx)} \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic})\sqrt{1 + e^{2i(c+dx)}} \text{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right. \right. \right. \right. \right. \\ \left. \left. \left. - e^{i(c+dx)}(-1 + e^{2ic})\sqrt{1 + e^{2i(c+dx)}} \text{Hypergeometric2F1}\left[\frac{1}{4}, \frac{1}{2}, \frac{5}{4}, -e^{2i(c+dx)}\right] \right) \text{Sec}[c+dx] \right) / \left( d(-1 + e^{2ic})\sqrt{e^{-i(c+dx)}(1 + e^{2i(c+dx)})} \right) - \right. \\ \left. \frac{2\left(\text{Csc}[c] + \text{Sec}\left[\frac{c}{2}\right]\text{Sec}\left[\frac{1}{2}(c+dx)\right]\text{Sin}\left[\frac{dx}{2}\right]\right)}{d\sqrt{\text{Cos}[c+dx]}} \right) / (a(1 + \text{Sec}[c+dx]))$$

**Problem 379: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{1}{\cos [c+d x]^{5 / 2} (a+a \operatorname{Sec}[c+d x])} d x$$

Optimal (type 4, 96 leaves, 8 steps):

$$\frac{3 \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{a d} - \frac{\operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{a d} + \frac{3 \operatorname{Sin}[c+d x]}{a d \sqrt{\cos [c+d x]}} - \frac{\operatorname{Sin}[c+d x]}{d \cos [c+d x]^{3 / 2} (a+a \operatorname{Sec}[c+d x])}$$

Result (type 5, 303 leaves):

$$\begin{aligned} & \left( \cos \left[ \frac{1}{2}(c+d x) \right] \right)^2 \\ & \left( \left( \left( 2 \cos \left[ \frac{1}{2}(c-d x) \right] + \cos \left[ \frac{1}{2}(3 c+d x) \right] + 3 \cos \left[ \frac{1}{2}(c+3 d x) \right] \right) \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{Sec} \left[ \frac{c}{2} \right] \right. \right. \\ & \quad \left. \left. \operatorname{Sec} \left[ \frac{1}{2}(c+d x) \right] \right) \right) / \left( 2 d \cos [c+d x]^{3 / 2} - \right. \\ & \quad \left( 2 i \sqrt{2} e^{-i(c+d x)} \left( 3 \left( 1+e^{2 i(c+d x)} \right) + 3 \left( -1+e^{2 i c} \right) \sqrt{1+e^{2 i(c+d x)}} \right. \right. \\ & \quad \left. \left. \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i(c+d x)} \right] - e^{i(c+d x)} \left( -1+e^{2 i c} \right) \right. \right. \\ & \quad \left. \left. \sqrt{1+e^{2 i(c+d x)}} \operatorname{Hypergeometric2F1} \left[ \frac{1}{4}, \frac{1}{2}, \frac{5}{4}, -e^{2 i(c+d x)} \right] \right) \operatorname{Sec}[c+d x] \right) / \\ & \quad \left( d \left( -1+e^{2 i c} \right) \sqrt{e^{-i(c+d x)} \left( 1+e^{2 i(c+d x)} \right)} \right) \right) / \left( a \left( 1+\operatorname{Sec}[c+d x] \right) \right) \end{aligned}$$

**Problem 380: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{1}{\cos [c+d x]^{7 / 2} (a+a \operatorname{Sec}[c+d x])} d x$$

Optimal (type 4, 124 leaves, 9 steps):

$$\frac{3 \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{a d} + \frac{5 \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{3 a d} + \frac{5 \operatorname{Sin}[c+d x]}{3 a d \cos [c+d x]^{3 / 2}} - \frac{3 \operatorname{Sin}[c+d x]}{a d \sqrt{\cos [c+d x]}} - \frac{\operatorname{Sin}[c+d x]}{d \cos [c+d x]^{5 / 2} (a+a \operatorname{Sec}[c+d x])}$$

Result (type 5, 338 leaves):

$$\begin{aligned}
 & \left( \cos\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \quad \left. - \left( \left( \left( 10 \cos\left[\frac{1}{2}(c-dx)\right] + 8 \cos\left[\frac{1}{2}(3c+dx)\right] + 4 \cos\left[\frac{1}{2}(c+3dx)\right] + 5 \cos\left[\frac{1}{2}(5c+3dx)\right] + \right. \right. \right. \right. \\
 & \quad \quad \left. \left. \left. 9 \cos\left[\frac{1}{2}(3c+5dx)\right] \right) \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right] \right) \right) / \left( 4d \cos[c+dx]^{5/2} \right) \right) + \\
 & \quad \left( 2i\sqrt{2} e^{-i(c+dx)} \left( 9(1+e^{2i(c+dx)}) + 9(-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \right. \right. \\
 & \quad \quad \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] - 5e^{i(c+dx)}(-1+e^{2ic}) \\
 & \quad \quad \left. \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, \frac{1}{2}, \frac{5}{4}, -e^{2i(c+dx)}\right] \right) \operatorname{Sec}[c+dx] \Big) / \\
 & \quad \left( d(-1+e^{2ic}) \sqrt{e^{-i(c+dx)}(1+e^{2i(c+dx)})} \right) \Big) / \left( 3a(1+\operatorname{Sec}[c+dx]) \right)
 \end{aligned}$$

**Problem 381: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\cos[c+dx]^{5/2}}{(a+a \operatorname{Sec}[c+dx])^2} dx$$

Optimal (type 4, 160 leaves, 10 steps):

$$\begin{aligned}
 & \frac{56 \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right]}{5a^2 d} - \frac{5 \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right]}{a^2 d} - \frac{5\sqrt{\cos[c+dx]} \operatorname{Sin}[c+dx]}{a^2 d} + \\
 & \frac{56 \cos[c+dx]^{3/2} \operatorname{Sin}[c+dx]}{15a^2 d} - \frac{3 \cos[c+dx]^{3/2} \operatorname{Sin}[c+dx]}{a^2 d (1+\operatorname{Sec}[c+dx])} - \frac{\cos[c+dx]^{3/2} \operatorname{Sin}[c+dx]}{3d(a+a \operatorname{Sec}[c+dx])^2}
 \end{aligned}$$

Result (type 5, 366 leaves):

$$\begin{aligned}
 & \frac{1}{5a^2(1+\operatorname{Sec}[c+dx])^2} \\
 & \cos\left[\frac{1}{2}(c+dx)\right]^4 \left( \left( 4i\sqrt{2} e^{-i(c+dx)} \left( 56(1+e^{2i(c+dx)}) + 56(-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \right. \right. \right. \\
 & \quad \quad \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] + \\
 & \quad \quad \left. \left. 25e^{i(c+dx)}(-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, \frac{1}{2}, \frac{5}{4}, -e^{2i(c+dx)}\right] \right) \right) \\
 & \quad \operatorname{Sec}[c+dx]^2 \Big) / \left( d(-1+e^{2ic}) \sqrt{e^{-i(c+dx)}(1+e^{2i(c+dx)})} \right) + \\
 & \left( 2 \left( -216 \operatorname{Cot}[c] - 120 \operatorname{Csc}[c] - 40 \cos[dx] \operatorname{Sin}[c] + 6 \cos[2dx] \operatorname{Sin}[2c] - 120 \operatorname{Sec}\left[\frac{c}{2}\right] \right. \right. \\
 & \quad \quad \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right] \operatorname{Sin}\left[\frac{dx}{2}\right] + 5 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^3 \operatorname{Sin}\left[\frac{dx}{2}\right] - 40 \cos[c] \operatorname{Sin}[dx] + \\
 & \quad \quad \left. \left. 6 \cos[2c] \operatorname{Sin}[2dx] + 5 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{c}{2}\right] \right) \right) / \left( 3d \cos[c+dx]^{3/2} \right)
 \end{aligned}$$

**Problem 382: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\cos [c+d x]^{3 / 2}}{(a+a \operatorname{Sec}[c+d x])^2} d x$$

Optimal (type 4, 138 leaves, 9 steps):

$$\frac{7 \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{a^2 d} + \frac{10 \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{3 a^2 d} + \frac{10 \sqrt{\cos [c+d x]} \sin [c+d x]}{3 a^2 d} - \frac{7 \sqrt{\cos [c+d x]} \sin [c+d x]}{3 a^2 d (1+\operatorname{Sec}[c+d x])} - \frac{\sqrt{\cos [c+d x]} \sin [c+d x]}{3 d (a+a \operatorname{Sec}[c+d x])^2}$$

Result (type 5, 341 leaves):

$$\frac{1}{3 a^2 (1+\operatorname{Sec}[c+d x])^2} \cos \left[\frac{1}{2}(c+d x)\right]^4 \left( - \left( \left( 4 i \sqrt{2} e^{-i(c+d x)} \left( 21 (1+e^{2 i(c+d x)}) + 21 (-1+e^{2 i c}) \sqrt{1+e^{2 i(c+d x)}} \right. \right. \right. \right. \\ \left. \left. \left. \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i(c+d x)}\right] + 10 e^{i(c+d x)} (-1+e^{2 i c}) \right. \right. \right. \\ \left. \left. \left. \sqrt{1+e^{2 i(c+d x)}} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, \frac{1}{2}, \frac{5}{4}, -e^{2 i(c+d x)}\right] \right) \operatorname{Sec}[c+d x]^2 \right) / \right. \\ \left. \left( d (-1+e^{2 i c}) \sqrt{e^{-i(c+d x)} (1+e^{2 i(c+d x)})} \right) \right) + \frac{1}{d \cos [c+d x]^{3 / 2}} \\ \left( 48 \cot [c] + 36 \csc [c] + 8 \cos [d x] \sin [c] + 36 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right] \sin \left[\frac{d x}{2}\right] - \right. \\ \left. 2 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^3 \sin \left[\frac{d x}{2}\right] + 8 \cos [c] \sin [d x] - 2 \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \tan \left[\frac{c}{2}\right] \right)$$

**Problem 383: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\sqrt{\cos [c+d x]}}{(a+a \operatorname{Sec}[c+d x])^2} d x$$

Optimal (type 4, 112 leaves, 8 steps):

$$\frac{4 \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{a^2 d} - \frac{5 \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{3 a^2 d} - \frac{5 \sin [c+d x]}{3 a^2 d \sqrt{\cos [c+d x]} (1+\operatorname{Sec}[c+d x])} - \frac{\sin [c+d x]}{3 d \sqrt{\cos [c+d x]} (a+a \operatorname{Sec}[c+d x])^2}$$

Result (type 5, 374 leaves):

$$\begin{aligned}
 & \left( 4 i \sqrt{2} e^{-i(c+dx)} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \left( 12 (1 + e^{2i(c+dx)}) + \right. \right. \\
 & \quad 12 (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] + 5 e^{i(c+dx)} \\
 & \quad \left. \left. (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, \frac{1}{2}, \frac{5}{4}, -e^{2i(c+dx)}\right]\right) \operatorname{Sec}[c + dx]^2 \right) / \\
 & \left( 3 d (-1 + e^{2ic}) \sqrt{e^{-i(c+dx)} (1 + e^{2i(c+dx)})} (a + a \operatorname{Sec}[c + dx])^2 \right) + \\
 & \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \left( -\frac{8 \operatorname{Cot}\left[\frac{c}{2}\right]}{d} - \frac{8 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right] \operatorname{Sin}\left[\frac{dx}{2}\right]}{d} + \frac{2 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^3 \operatorname{Sin}\left[\frac{dx}{2}\right]}{3 d} \right. \right. \\
 & \quad \left. \left. + \frac{2 \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \operatorname{Tan}\left[\frac{c}{2}\right]}{3 d} \right) \right) / \left( \cos[c + dx]^{3/2} (a + a \operatorname{Sec}[c + dx])^2 \right)
 \end{aligned}$$

**Problem 384:** Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{1}{\sqrt{\cos[c + dx]} (a + a \operatorname{Sec}[c + dx])^2} dx$$

Optimal (type 4, 109 leaves, 8 steps):

$$\begin{aligned}
 & -\frac{\operatorname{EllipticE}\left[\frac{1}{2}(c + dx), 2\right]}{a^2 d} + \frac{2 \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right]}{3 a^2 d} + \\
 & \frac{\operatorname{Sin}[c + dx]}{a^2 d \sqrt{\cos[c + dx]} (1 + \operatorname{Sec}[c + dx])} - \frac{\operatorname{Sin}[c + dx]}{3 d \cos[c + dx]^{3/2} (a + a \operatorname{Sec}[c + dx])^2}
 \end{aligned}$$

Result (type 5, 656 leaves):

$$\begin{aligned}
 & - \frac{1}{2 (a + a \operatorname{Sec}[c + dx])^2} \operatorname{Im} \left[ \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c + dx]^2 \right. \\
 & \quad \left( \left( 2 e^{2 i dx} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i dx} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right] \right. \right. \\
 & \quad \quad \left. \sqrt{e^{-i dx} (2 (1 + e^{2 i dx}) \operatorname{Cos}[c] + 2 i (-1 + e^{2 i dx}) \operatorname{Sin}[c])} \right. \\
 & \quad \quad \left. \left. \sqrt{1 + e^{2 i dx} \operatorname{Cos}[2c] + i e^{2 i dx} \operatorname{Sin}[2c]} \right) \right] / \\
 & \quad (3 i d (1 + e^{2 i dx}) \operatorname{Cos}[c] - 3 d (-1 + e^{2 i dx}) \operatorname{Sin}[c]) - \\
 & \quad \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i dx} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right] \right. \\
 & \quad \quad \left. \sqrt{e^{-i dx} (2 (1 + e^{2 i dx}) \operatorname{Cos}[c] + 2 i (-1 + e^{2 i dx}) \operatorname{Sin}[c])} \right. \\
 & \quad \quad \left. \left. \sqrt{1 + e^{2 i dx} \operatorname{Cos}[2c] + i e^{2 i dx} \operatorname{Sin}[2c]} \right) \right] / \\
 & \quad \left. (-i d (1 + e^{2 i dx}) \operatorname{Cos}[c] + d (-1 + e^{2 i dx}) \operatorname{Sin}[c]) \right) - \\
 & \quad \left( 4 \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]\right]^2 \right) \\
 & \quad \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c + dx]^2 \\
 & \quad \frac{\operatorname{Sec}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}{\sqrt{1 - \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}} \\
 & \quad \left. \sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right. \\
 & \quad \left. \left. \sqrt{1 + \operatorname{Sin}[dx - \operatorname{ArcTan}[\operatorname{Cot}[c]]]} \right) \right] / \\
 & \quad \left( 3 d \sqrt{1 + \operatorname{Cot}[c]^2} (a + a \operatorname{Sec}[c + dx])^2 \right) + \\
 & \quad \left( \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \left( \frac{4 \operatorname{Csc}[c]}{d} + \frac{4 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right] \operatorname{Sin}\left[\frac{dx}{2}\right]}{d} - \frac{2 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^3 \operatorname{Sin}\left[\frac{dx}{2}\right]}{3 d} - \right. \right. \\
 & \quad \left. \left. \frac{2 \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \operatorname{Tan}\left[\frac{c}{2}\right]}{3 d} \right) \right) \right] / \left( \operatorname{Cos}[c + dx]^{3/2} (a + a \operatorname{Sec}[c + dx])^2 \right)
 \end{aligned}$$

**Problem 386: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{1}{\operatorname{Cos}[c + dx]^{5/2} (a + a \operatorname{Sec}[c + dx])^2} dx$$

Optimal (type 4, 109 leaves, 8 steps):

$$\frac{\text{EllipticE}\left[\frac{1}{2}(c+dx), 2\right]}{a^2 d} + \frac{2 \text{EllipticF}\left[\frac{1}{2}(c+dx), 2\right]}{3 a^2 d} - \frac{\text{Sin}[c+dx]}{a^2 d \sqrt{\text{Cos}[c+dx]} (1+\text{Sec}[c+dx])} - \frac{\text{Sin}[c+dx]}{3 d \text{Cos}[c+dx]^{3/2} (a+a \text{Sec}[c+dx])^2}$$

Result (type 5, 370 leaves):

$$\left(4 i \sqrt{2} e^{-i(c+dx)} \text{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \left(3(1+e^{2i(c+dx)}) + 3(-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \text{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] - 2 e^{i(c+dx)} (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \text{Hypergeometric2F1}\left[\frac{1}{4}, \frac{1}{2}, \frac{5}{4}, -e^{2i(c+dx)}\right]\right) \text{Sec}[c+dx]^2 \right) / \left(3 d (-1+e^{2ic}) \sqrt{e^{-i(c+dx)} (1+e^{2i(c+dx)})} (a+a \text{Sec}[c+dx])^2\right) + \left(\text{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \left(-\frac{4 \text{Csc}[c]}{d} - \frac{4 \text{Sec}\left[\frac{c}{2}\right] \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right] \text{Sin}\left[\frac{dx}{2}\right]}{d} - \frac{2 \text{Sec}\left[\frac{c}{2}\right] \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^3 \text{Sin}\left[\frac{dx}{2}\right]}{3 d} - \frac{2 \text{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \text{Tan}\left[\frac{c}{2}\right]}{3 d}\right)\right) / \left(\text{Cos}[c+dx]^{3/2} (a+a \text{Sec}[c+dx])^2\right)$$

**Problem 387: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{1}{\text{Cos}[c+dx]^{7/2} (a+a \text{Sec}[c+dx])^2} dx$$

Optimal (type 4, 136 leaves, 9 steps):

$$-\frac{4 \text{EllipticE}\left[\frac{1}{2}(c+dx), 2\right]}{a^2 d} - \frac{5 \text{EllipticF}\left[\frac{1}{2}(c+dx), 2\right]}{3 a^2 d} + \frac{4 \text{Sin}[c+dx]}{a^2 d \sqrt{\text{Cos}[c+dx]}} - \frac{5 \text{Sin}[c+dx]}{3 a^2 d \text{Cos}[c+dx]^{3/2} (1+\text{Sec}[c+dx])} - \frac{\text{Sin}[c+dx]}{3 d \text{Cos}[c+dx]^{5/2} (a+a \text{Sec}[c+dx])^2}$$

Result (type 5, 393 leaves):

$$\begin{aligned}
 & - \left( \left( 4 i \sqrt{2} e^{-i(c+dx)} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \left( 12 (1 + e^{2i(c+dx)}) + \right. \right. \right. \\
 & \quad 12 (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] - 5 e^{i(c+dx)} \\
 & \quad \left. \left. (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, \frac{1}{2}, \frac{5}{4}, -e^{2i(c+dx)}\right]\right) \operatorname{Sec}[c + dx]^2 \right) / \\
 & \left( 3 d (-1 + e^{2ic}) \sqrt{e^{-i(c+dx)} (1 + e^{2i(c+dx)})} (a + a \operatorname{Sec}[c + dx])^2 \right) + \\
 & \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \left( \frac{8 \cot\left[\frac{c}{2}\right] \operatorname{Sec}[c]}{d} + \frac{8 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right] \sin\left[\frac{dx}{2}\right]}{d} + \right. \right. \\
 & \quad \frac{2 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^3 \sin\left[\frac{dx}{2}\right]}{3 d} + \frac{8 \operatorname{Sec}[c] \operatorname{Sec}[c + dx] \sin[dx]}{d} + \\
 & \quad \left. \left. \frac{2 \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \tan\left[\frac{c}{2}\right]}{3 d} \right) \right) / \left( \cos[c + dx]^{3/2} (a + a \operatorname{Sec}[c + dx])^2 \right)
 \end{aligned}$$

**Problem 388: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{1}{\cos[c + dx]^{9/2} (a + a \operatorname{Sec}[c + dx])^2} dx$$

Optimal (type 4, 162 leaves, 10 steps):

$$\begin{aligned}
 & \frac{7 \operatorname{EllipticE}\left[\frac{1}{2}(c + dx), 2\right]}{a^2 d} + \frac{10 \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right]}{3 a^2 d} + \\
 & \frac{10 \sin[c + dx]}{3 a^2 d \cos[c + dx]^{3/2}} - \frac{7 \sin[c + dx]}{a^2 d \sqrt{\cos[c + dx]}} - \\
 & \frac{7 \sin[c + dx]}{3 a^2 d \cos[c + dx]^{5/2} (1 + \operatorname{Sec}[c + dx])} - \frac{\sin[c + dx]}{3 d \cos[c + dx]^{7/2} (a + a \operatorname{Sec}[c + dx])^2}
 \end{aligned}$$

Result (type 5, 372 leaves):



$$\frac{1}{3 a^2 (1 + \operatorname{Sec}[c + d x])^2} \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right]^4$$

$$\left(-\left(\left(\left(82 \operatorname{Cos}\left[\frac{1}{2}(c - d x)\right] + 65 \operatorname{Cos}\left[\frac{1}{2}(3 c + d x)\right] + 68 \operatorname{Cos}\left[\frac{1}{2}(c + 3 d x)\right] + 37 \operatorname{Cos}\left[\frac{1}{2}(5 c + 3 d x)\right] + 53 \operatorname{Cos}\left[\frac{1}{2}(3 c + 5 d x)\right] + 10 \operatorname{Cos}\left[\frac{1}{2}(7 c + 5 d x)\right] + 21 \operatorname{Cos}\left[\frac{1}{2}(5 c + 7 d x)\right]\right)\right)\right.\right.$$

$$\left.\left.\operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^3\right) / (8 d \operatorname{Cos}[c + d x]^{7/2})\right) +$$

$$\left(4 i \sqrt{2} e^{-i(c+d x)}\left(21\left(1 + e^{2 i(c+d x)}\right) + 21\left(-1 + e^{2 i c}\right) \sqrt{1 + e^{2 i(c+d x)}}\right.\right.$$

$$\left.\operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i(c+d x)}\right] - 10 e^{i(c+d x)}\left(-1 + e^{2 i c}\right) \sqrt{1 + e^{2 i(c+d x)}} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, \frac{1}{2}, \frac{5}{4}, -e^{2 i(c+d x)}\right]\right)$$

$$\left.\operatorname{Sec}[c + d x]^2\right) / \left(d\left(-1 + e^{2 i c}\right) \sqrt{e^{-i(c+d x)}\left(1 + e^{2 i(c+d x)}\right)}\right)$$

**Problem 389: Result unnecessarily involves higher level functions.**

$$\int \frac{\operatorname{Cos}[c + d x]^{5/2}}{(a + a \operatorname{Sec}[c + d x])^3} dx$$

Optimal (type 4, 207 leaves, 11 steps):

$$\frac{231 \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right]}{10 a^3 d} - \frac{21 \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right]}{2 a^3 d}$$

$$\frac{21 \sqrt{\operatorname{Cos}[c + d x]} \operatorname{Sin}[c + d x]}{2 a^3 d} + \frac{77 \operatorname{Cos}[c + d x]^{3/2} \operatorname{Sin}[c + d x]}{10 a^3 d}$$

$$\frac{\operatorname{Cos}[c + d x]^{3/2} \operatorname{Sin}[c + d x]}{5 d (a + a \operatorname{Sec}[c + d x])^3} - \frac{4 \operatorname{Cos}[c + d x]^{3/2} \operatorname{Sin}[c + d x]}{5 a d (a + a \operatorname{Sec}[c + d x])^2} - \frac{63 \operatorname{Cos}[c + d x]^{3/2} \operatorname{Sin}[c + d x]}{10 d (a^3 + a^3 \operatorname{Sec}[c + d x])}$$

Result (type 5, 391 leaves):

$$\frac{1}{5 a^3 d (1 + \operatorname{Sec}[c + d x])^3} \left( 2 \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right]^6 \left( \left( 42 i \sqrt{2} e^{-i(c+d x)} \left( 11 (1 + e^{2 i(c+d x)}) + 11 (-1 + e^{2 i c}) \sqrt{1 + e^{2 i(c+d x)}} \right) \right. \right. \right. \\ \left. \left. \left. \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i(c+d x)}\right] + 5 e^{i(c+d x)} (-1 + e^{2 i c}) \sqrt{1 + e^{2 i(c+d x)}} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, \frac{1}{2}, \frac{5}{4}, -e^{2 i(c+d x)}\right]\right) \operatorname{Sec}[c + d x]^3 \right) / \\ \left( (-1 + e^{2 i c}) \sqrt{e^{-i(c+d x)} (1 + e^{2 i(c+d x)})} \right) + \frac{1}{\operatorname{Cos}[c + d x]^{5/2}} \\ \left( -264 \operatorname{Cot}[c] - 198 \operatorname{Csc}[c] + \frac{1}{16} \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^5 \left( -1210 \operatorname{Sin}\left[\frac{d x}{2}\right] + 770 \operatorname{Sin}\left[c + \frac{d x}{2}\right] - \right. \right. \\ \left. \left. 840 \operatorname{Sin}\left[c + \frac{3 d x}{2}\right] + 150 \operatorname{Sin}\left[2 c + \frac{3 d x}{2}\right] - 238 \operatorname{Sin}\left[2 c + \frac{5 d x}{2}\right] - 40 \operatorname{Sin}\left[3 c + \frac{5 d x}{2}\right] - \right. \right. \\ \left. \left. 5 \operatorname{Sin}\left[3 c + \frac{7 d x}{2}\right] - 5 \operatorname{Sin}\left[4 c + \frac{7 d x}{2}\right] + \operatorname{Sin}\left[4 c + \frac{9 d x}{2}\right] + \operatorname{Sin}\left[5 c + \frac{9 d x}{2}\right] \right) \right)$$

Problem 390: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Cos}[c + d x]^{3/2}}{(a + a \operatorname{Sec}[c + d x])^3} dx$$

Optimal (type 4, 181 leaves, 10 steps):

$$-\frac{119 \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right]}{10 a^3 d} + \frac{11 \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right]}{2 a^3 d} + \frac{11 \sqrt{\operatorname{Cos}[c + d x]} \operatorname{Sin}[c + d x]}{2 a^3 d} - \\ \frac{\sqrt{\operatorname{Cos}[c + d x]} \operatorname{Sin}[c + d x]}{5 d (a + a \operatorname{Sec}[c + d x])^3} - \frac{2 \sqrt{\operatorname{Cos}[c + d x]} \operatorname{Sin}[c + d x]}{3 a d (a + a \operatorname{Sec}[c + d x])^2} - \frac{119 \sqrt{\operatorname{Cos}[c + d x]} \operatorname{Sin}[c + d x]}{30 d (a^3 + a^3 \operatorname{Sec}[c + d x])}$$

Result (type 5, 375 leaves):

$$\frac{1}{5 a^3 (1 + \operatorname{Sec}[c + d x])^3} \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right]^6 \left( - \left( \left( 4 i \sqrt{2} e^{-i(c+d x)} \left( 119 (1 + e^{2 i(c+d x)}) + 119 (-1 + e^{2 i c}) \sqrt{1 + e^{2 i(c+d x)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i(c+d x)}\right] + 55 e^{i(c+d x)} (-1 + e^{2 i c}) \sqrt{1 + e^{2 i(c+d x)}} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, \frac{1}{2}, \frac{5}{4}, -e^{2 i(c+d x)}\right] \right) \operatorname{Sec}[c + d x]^3 \right) / \left( d (-1 + e^{2 i c}) \sqrt{e^{-i(c+d x)} (1 + e^{2 i(c+d x)})} \right) + \left( 720 \operatorname{Cot}[c] + 708 \operatorname{Csc}[c] + \frac{1}{4} \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^5 \left( 1061 \operatorname{Sin}\left[\frac{d x}{2}\right] - 709 \operatorname{Sin}\left[c + \frac{d x}{2}\right] + 715 \operatorname{Sin}\left[c + \frac{3 d x}{2}\right] - 170 \operatorname{Sin}\left[2 c + \frac{3 d x}{2}\right] + 202 \operatorname{Sin}\left[2 c + \frac{5 d x}{2}\right] + 25 \operatorname{Sin}\left[3 c + \frac{5 d x}{2}\right] + 5 \operatorname{Sin}\left[3 c + \frac{7 d x}{2}\right] + 5 \operatorname{Sin}\left[4 c + \frac{7 d x}{2}\right] \right) \right) / (3 d \operatorname{Cos}[c + d x]^{5/2}) \right)$$

**Problem 391: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\sqrt{\operatorname{Cos}[c + d x]}}{(a + a \operatorname{Sec}[c + d x])^3} dx$$

Optimal (type 4, 155 leaves, 9 steps):

$$\frac{49 \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right]}{10 a^3 d} - \frac{13 \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right]}{6 a^3 d} - \frac{\operatorname{Sin}[c + d x]}{5 d \sqrt{\operatorname{Cos}[c + d x]} (a + a \operatorname{Sec}[c + d x])^3} - \frac{8 \operatorname{Sin}[c + d x]}{15 a d \sqrt{\operatorname{Cos}[c + d x]} (a + a \operatorname{Sec}[c + d x])^2} - \frac{13 \operatorname{Sin}[c + d x]}{6 d \sqrt{\operatorname{Cos}[c + d x]} (a^3 + a^3 \operatorname{Sec}[c + d x])}$$

Result (type 5, 357 leaves):

$$\frac{1}{15 a^3 (1 + \operatorname{Sec}[c + d x])^3} \left( \cos\left[\frac{1}{2}(c + d x)\right]^6 \left( \left( \left( \left( 806 \cos\left[\frac{1}{2}(c - d x)\right] + 664 \cos\left[\frac{1}{2}(3 c + d x)\right] + 470 \cos\left[\frac{1}{2}(c + 3 d x)\right] + 265 \cos\left[\frac{1}{2}(5 c + 3 d x)\right] + 117 \cos\left[\frac{1}{2}(3 c + 5 d x)\right] + 30 \cos\left[\frac{1}{2}(7 c + 5 d x)\right] \right) \right) \right) \right) \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^5 \right) / (8 d \cos[c + d x]^{5/2}) + \left( 4 i \sqrt{2} e^{-i(c+d x)} \left( 147 (1 + e^{2 i(c+d x)}) + 147 (-1 + e^{2 i c}) \sqrt{1 + e^{2 i(c+d x)}} \right) \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i(c+d x)}\right] + 65 e^{i(c+d x)} (-1 + e^{2 i c}) \sqrt{1 + e^{2 i(c+d x)}} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, \frac{1}{2}, \frac{5}{4}, -e^{2 i(c+d x)}\right] \right) \operatorname{Sec}[c + d x]^3 \right) / \left( d (-1 + e^{2 i c}) \sqrt{e^{-i(c+d x)} (1 + e^{2 i(c+d x)})} \right)$$

**Problem 392: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{1}{\sqrt{\cos[c + d x]} (a + a \operatorname{Sec}[c + d x])^3} dx$$

Optimal (type 4, 155 leaves, 9 steps):

$$-\frac{9 \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right]}{10 a^3 d} + \frac{\operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right]}{2 a^3 d} - \frac{\operatorname{Sin}[c + d x]}{5 d \cos[c + d x]^{3/2} (a + a \operatorname{Sec}[c + d x])^3} + \frac{2 \operatorname{Sin}[c + d x]}{5 a d \sqrt{\cos[c + d x]} (a + a \operatorname{Sec}[c + d x])^2} + \frac{\operatorname{Sin}[c + d x]}{2 d \sqrt{\cos[c + d x]} (a^3 + a^3 \operatorname{Sec}[c + d x])}$$

Result (type 5, 721 leaves):

$$\begin{aligned}
 & - \frac{1}{10 (a + a \operatorname{Sec}[c + d x])^3} 9 i \operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c + d x]^3 \\
 & \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right] \right. \right. \\
 & \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \operatorname{Cos}[c] + 2 i (-1 + e^{2 i d x}) \operatorname{Sin}[c])}}{\sqrt{1 + e^{2 i d x} \operatorname{Cos}[2 c] + i e^{2 i d x} \operatorname{Sin}[2 c]}} \right) / \\
 & \quad (3 i d (1 + e^{2 i d x}) \operatorname{Cos}[c] - 3 d (-1 + e^{2 i d x}) \operatorname{Sin}[c]) - \\
 & \quad \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right] \right. \\
 & \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \operatorname{Cos}[c] + 2 i (-1 + e^{2 i d x}) \operatorname{Sin}[c])}}{\sqrt{1 + e^{2 i d x} \operatorname{Cos}[2 c] + i e^{2 i d x} \operatorname{Sin}[2 c]}} \right) / \\
 & \quad \left. (-i d (1 + e^{2 i d x}) \operatorname{Cos}[c] + d (-1 + e^{2 i d x}) \operatorname{Sin}[c]) \right) - \\
 & \left( 2 \operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]\right]^2 \right) \\
 & \quad \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c + d x]^3 \\
 & \quad \frac{\operatorname{Sec}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}{\sqrt{1 - \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}} \\
 & \quad \left. \frac{\sqrt{-\sqrt{1 + \operatorname{Cot}[c]^2} \operatorname{Sin}[c] \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}}{\sqrt{1 + \operatorname{Sin}[d x - \operatorname{ArcTan}[\operatorname{Cot}[c]]]}} \right) / \\
 & \quad \left( d \sqrt{1 + \operatorname{Cot}[c]^2} (a + a \operatorname{Sec}[c + d x])^3 \right) + \\
 & \left( \operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right]^6 \left( \frac{36 \operatorname{Csc}[c]}{5 d} + \frac{36 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right] \operatorname{Sin}\left[\frac{d x}{2}\right]}{5 d} - \frac{12 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^3 \operatorname{Sin}\left[\frac{d x}{2}\right]}{5 d} \right. \right. \\
 & \quad \left. \left. + \frac{2 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^5 \operatorname{Sin}\left[\frac{d x}{2}\right]}{5 d} - \frac{12 \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \operatorname{Tan}\left[\frac{c}{2}\right]}{5 d} + \frac{2 \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^4 \operatorname{Tan}\left[\frac{c}{2}\right]}{5 d} \right) \right) / \\
 & \quad \left( \operatorname{Cos}[c + d x]^{5/2} (a + a \operatorname{Sec}[c + d x])^3 \right)
 \end{aligned}$$

**Problem 393:** Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{1}{\operatorname{Cos}[c + d x]^{3/2} (a + a \operatorname{Sec}[c + d x])^3} dx$$

Optimal (type 4, 155 leaves, 9 steps):

$$-\frac{\text{EllipticE}\left[\frac{1}{2}(c+dx), 2\right]}{10a^3d} + \frac{\text{EllipticF}\left[\frac{1}{2}(c+dx), 2\right]}{6a^3d} + \frac{\text{Sin}[c+dx]}{5d\text{Cos}[c+dx]^{3/2}(a+a\text{Sec}[c+dx])^3} - \frac{\text{Sin}[c+dx]}{15ad\sqrt{\text{Cos}[c+dx]}(a+a\text{Sec}[c+dx])^2} + \frac{\text{Sin}[c+dx]}{6d\sqrt{\text{Cos}[c+dx]}(a^3+a^3\text{Sec}[c+dx])}$$

Result (type 5, 342 leaves):

$$\left(\text{Cos}\left[\frac{1}{2}(c+dx)\right]^6 \left(\left(\left(14\text{Cos}\left[\frac{1}{2}(c-dx)\right] + 16\text{Cos}\left[\frac{1}{2}(3c+dx)\right] + 20\text{Cos}\left[\frac{1}{2}(c+3dx)\right] - 5\text{Cos}\left[\frac{1}{2}(5c+3dx)\right] + 3\text{Cos}\left[\frac{1}{2}(3c+5dx)\right]\right)\text{Csc}\left[\frac{c}{2}\right]\text{Sec}\left[\frac{c}{2}\right]\text{Sec}\left[\frac{1}{2}(c+dx)\right]^5\right) / (8d\text{Cos}[c+dx]^{5/2}) - \left(4i\sqrt{2}e^{-i(c+dx)}\left(3(1+e^{2i(c+dx)}) + 3(-1+e^{2ic})\sqrt{1+e^{2i(c+dx)}}\right)\text{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] + 5e^{i(c+dx)}(-1+e^{2ic})\sqrt{1+e^{2i(c+dx)}}\text{Hypergeometric2F1}\left[\frac{1}{4}, \frac{1}{2}, \frac{5}{4}, -e^{2i(c+dx)}\right]\right)\text{Sec}[c+dx]^3) / \left(d(-1+e^{2ic})\sqrt{e^{-i(c+dx)}(1+e^{2i(c+dx)})}\right)\right) / (15a^3(1+\text{Sec}[c+dx])^3)$$

**Problem 394: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{1}{\text{Cos}[c+dx]^{5/2}(a+a\text{Sec}[c+dx])^3} dx$$

Optimal (type 4, 155 leaves, 9 steps):

$$\frac{\text{EllipticE}\left[\frac{1}{2}(c+dx), 2\right]}{10a^3d} + \frac{\text{EllipticF}\left[\frac{1}{2}(c+dx), 2\right]}{6a^3d} - \frac{\text{Sin}[c+dx]}{5d\text{Cos}[c+dx]^{3/2}(a+a\text{Sec}[c+dx])^3} - \frac{4\text{Sin}[c+dx]}{15ad\sqrt{\text{Cos}[c+dx]}(a+a\text{Sec}[c+dx])^2} + \frac{\text{Sin}[c+dx]}{6d\sqrt{\text{Cos}[c+dx]}(a^3+a^3\text{Sec}[c+dx])}$$

Result (type 5, 342 leaves):

$$\begin{aligned}
 & \left( \cos\left[\frac{1}{2}(c+dx)\right] \right)^6 \\
 & \left( - \left( \left( \left( 4 \cos\left[\frac{1}{2}(c-dx)\right] + 26 \cos\left[\frac{1}{2}(3c+dx)\right] + 10 \cos\left[\frac{1}{2}(c+3dx)\right] + 5 \cos\left[\frac{1}{2}(5c+3dx)\right] + \right. \right. \right. \right. \\
 & \quad \left. \left. \left. 3 \cos\left[\frac{1}{2}(3c+5dx)\right] \right) \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^5 \right) \right) / \left( 8d \cos[c+dx]^{5/2} \right) + \right. \\
 & \quad \left( 4i\sqrt{2} e^{-i(c+dx)} \left( 3(1+e^{2i(c+dx)}) + 3(-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \right) \right. \\
 & \quad \left. \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] - 5e^{i(c+dx)}(-1+e^{2ic}) \right. \\
 & \quad \left. \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, \frac{1}{2}, \frac{5}{4}, -e^{2i(c+dx)}\right] \right) \operatorname{Sec}[c+dx]^3 \Big/ \\
 & \quad \left. \left( d(-1+e^{2ic}) \sqrt{e^{-i(c+dx)}(1+e^{2i(c+dx)})} \right) \right) \Big/ \left( 15a^3(1+\operatorname{Sec}[c+dx])^3 \right)
 \end{aligned}$$

**Problem 395:** Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{1}{\cos[c+dx]^{7/2} (a+a \operatorname{Sec}[c+dx])^3} dx$$

Optimal (type 4, 155 leaves, 9 steps):

$$\begin{aligned}
 & \frac{9 \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right]}{10a^3d} + \frac{\operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right]}{2a^3d} - \frac{\operatorname{Sin}[c+dx]}{5d \cos[c+dx]^{5/2} (a+a \operatorname{Sec}[c+dx])^3} - \\
 & \frac{2 \operatorname{Sin}[c+dx]}{5ad \cos[c+dx]^{3/2} (a+a \operatorname{Sec}[c+dx])^2} - \frac{9 \operatorname{Sin}[c+dx]}{10d \sqrt{\cos[c+dx]} (a^3+a^3 \operatorname{Sec}[c+dx])}
 \end{aligned}$$

Result (type 5, 721 leaves):

$$\begin{aligned}
 & \frac{1}{10 (a + a \sec [c + d x])^3} 9 i \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{Sec} \left[ \frac{c}{2} \right] \operatorname{Sec} [c + d x]^3 \\
 & \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos [c] + i \sin [c]) \right]^2 \right) \right. \\
 & \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) / \\
 & \quad (3 i d (1 + e^{2 i d x}) \cos [c] - 3 d (-1 + e^{2 i d x}) \sin [c]) - \\
 & \quad \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c]) \right]^2 \right) \\
 & \quad \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) / \\
 & \quad \left. (-i d (1 + e^{2 i d x}) \cos [c] + d (-1 + e^{2 i d x}) \sin [c]) \right) - \\
 & \left( 2 \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 \operatorname{Csc} \left[ \frac{c}{2} \right] \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]] \right]^2 \right) \\
 & \quad \operatorname{Sec} \left[ \frac{c}{2} \right] \operatorname{Sec} [c + d x]^3 \operatorname{Sec} [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]] \\
 & \quad \frac{\sqrt{1 - \sin [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]]}}{\sqrt{-\sqrt{1 + \operatorname{Cot} [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]]}} \\
 & \quad \left. \frac{\sqrt{1 + \sin [d x - \operatorname{ArcTan} [\operatorname{Cot} [c]]]}}{\right) / \\
 & \quad \left( d \sqrt{1 + \operatorname{Cot} [c]^2} (a + a \sec [c + d x])^3 \right) + \\
 & \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 \left( -\frac{36 \operatorname{Csc} [c]}{5 d} - \frac{36 \operatorname{Sec} \left[ \frac{c}{2} \right] \operatorname{Sec} \left[ \frac{c}{2} + \frac{d x}{2} \right] \sin \left[ \frac{d x}{2} \right]}{5 d} - \frac{8 \operatorname{Sec} \left[ \frac{c}{2} \right] \operatorname{Sec} \left[ \frac{c}{2} + \frac{d x}{2} \right]^3 \sin \left[ \frac{d x}{2} \right]}{5 d} \right. \right. \\
 & \quad \left. \left. - \frac{2 \operatorname{Sec} \left[ \frac{c}{2} \right] \operatorname{Sec} \left[ \frac{c}{2} + \frac{d x}{2} \right]^5 \sin \left[ \frac{d x}{2} \right]}{5 d} - \frac{8 \operatorname{Sec} \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \operatorname{Tan} \left[ \frac{c}{2} \right]}{5 d} - \frac{2 \operatorname{Sec} \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 \operatorname{Tan} \left[ \frac{c}{2} \right]}{5 d} \right) \right) / \\
 & \quad \left( \cos [c + d x]^{5/2} (a + a \sec [c + d x])^3 \right)
 \end{aligned}$$

**Problem 396:** Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{1}{\cos [c + d x]^{9/2} (a + a \sec [c + d x])^3} dx$$

Optimal (type 4, 181 leaves, 10 steps):



$$\begin{aligned}
 & - \frac{49 \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right]}{10 a^3 d} - \frac{13 \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right]}{6 a^3 d} + \\
 & \frac{49 \operatorname{Sin}[c+dx]}{10 a^3 d \sqrt{\operatorname{Cos}[c+dx]}} - \frac{\operatorname{Sin}[c+dx]}{5 d \operatorname{Cos}[c+dx]^{7/2} (a+a \operatorname{Sec}[c+dx])^3} - \\
 & \frac{8 \operatorname{Sin}[c+dx]}{15 a d \operatorname{Cos}[c+dx]^{5/2} (a+a \operatorname{Sec}[c+dx])^2} - \frac{13 \operatorname{Sin}[c+dx]}{6 d \operatorname{Cos}[c+dx]^{3/2} (a^3+a^3 \operatorname{Sec}[c+dx])}
 \end{aligned}$$

Result (type 5, 372 leaves):

$$\begin{aligned}
 & \frac{1}{15 a^3 (1+\operatorname{Sec}[c+dx])^3} \\
 & \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^6 \left( \left( \left( 1284 \operatorname{Cos}\left[\frac{1}{2}(c-dx)\right] + 921 \operatorname{Cos}\left[\frac{1}{2}(3c+dx)\right] + 1243 \operatorname{Cos}\left[\frac{1}{2}(c+3dx)\right] + \right. \right. \right. \\
 & \quad \left. \left. \left. 374 \operatorname{Cos}\left[\frac{1}{2}(5c+3dx)\right] + 670 \operatorname{Cos}\left[\frac{1}{2}(3c+5dx)\right] + 65 \operatorname{Cos}\left[\frac{1}{2}(7c+5dx)\right] + \right. \right. \right. \\
 & \quad \left. \left. \left. 147 \operatorname{Cos}\left[\frac{1}{2}(5c+7dx)\right] \right) \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^5 \right) / \right. \\
 & \quad \left. \left( 16 d \operatorname{Cos}[c+dx]^{7/2} \right) - \left( 4 i \sqrt{2} e^{-i(c+dx)} \left( 147 (1+e^{2i(c+dx)}) + \right. \right. \right. \\
 & \quad \left. \left. \left. 147 (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] - \right. \right. \right. \\
 & \quad \left. \left. \left. 65 e^{i(c+dx)} (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, \frac{1}{2}, \frac{5}{4}, -e^{2i(c+dx)}\right] \right) \right) \right. \\
 & \quad \left. \operatorname{Sec}[c+dx]^3 \right) / \left( d (-1+e^{2ic}) \sqrt{e^{-i(c+dx)} (1+e^{2i(c+dx)})} \right)
 \end{aligned}$$

**Problem 397: Result unnecessarily involves higher level functions.**

$$\int \frac{1}{\operatorname{Cos}[c+dx]^{11/2} (a+a \operatorname{Sec}[c+dx])^3} dx$$

Optimal (type 4, 207 leaves, 11 steps):

$$\begin{aligned}
 & \frac{119 \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right]}{10 a^3 d} + \frac{11 \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right]}{2 a^3 d} + \\
 & \frac{11 \operatorname{Sin}[c+dx]}{2 a^3 d \operatorname{Cos}[c+dx]^{3/2}} - \frac{119 \operatorname{Sin}[c+dx]}{10 a^3 d \sqrt{\operatorname{Cos}[c+dx]}} - \frac{\operatorname{Sin}[c+dx]}{5 d \operatorname{Cos}[c+dx]^{9/2} (a+a \operatorname{Sec}[c+dx])^3} - \\
 & \frac{2 \operatorname{Sin}[c+dx]}{3 a d \operatorname{Cos}[c+dx]^{7/2} (a+a \operatorname{Sec}[c+dx])^2} - \frac{119 \operatorname{Sin}[c+dx]}{30 d \operatorname{Cos}[c+dx]^{5/2} (a^3+a^3 \operatorname{Sec}[c+dx])}
 \end{aligned}$$

Result (type 5, 402 leaves):

$$\frac{1}{5 a^3 (1 + \operatorname{Sec}[c + d x])^3} \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right]^6 \left( - \left( \left( \left( 5134 \operatorname{Cos}\left[\frac{1}{2}(c - d x)\right] + 4148 \operatorname{Cos}\left[\frac{1}{2}(3 c + d x)\right] + 4664 \operatorname{Cos}\left[\frac{1}{2}(c + 3 d x)\right] + 2476 \operatorname{Cos}\left[\frac{1}{2}(5 c + 3 d x)\right] + 3340 \operatorname{Cos}\left[\frac{1}{2}(3 c + 5 d x)\right] + 944 \operatorname{Cos}\left[\frac{1}{2}(7 c + 5 d x)\right] + 1620 \operatorname{Cos}\left[\frac{1}{2}(5 c + 7 d x)\right] + 165 \operatorname{Cos}\left[\frac{1}{2}(9 c + 7 d x)\right] + 357 \operatorname{Cos}\left[\frac{1}{2}(7 c + 9 d x)\right] \right) \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^5 \right) / (96 d \operatorname{Cos}[c + d x]^{9/2}) \right) + \left( 4 i \sqrt{2} e^{-i(c+d x)} \left( 119 (1 + e^{2 i(c+d x)}) + 119 (-1 + e^{2 i c}) \sqrt{1 + e^{2 i(c+d x)}} \right) \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i(c+d x)}\right] - 55 e^{i(c+d x)} (-1 + e^{2 i c}) \sqrt{1 + e^{2 i(c+d x)}} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, \frac{1}{2}, \frac{5}{4}, -e^{2 i(c+d x)}\right] \right) \operatorname{Sec}[c + d x]^3 \right) / \left( d (-1 + e^{2 i c}) \sqrt{e^{-i(c+d x)} (1 + e^{2 i(c+d x)})} \right)$$

**Problem 402: Result unnecessarily involves higher level functions.**

$$\int \frac{\sqrt{a + a \operatorname{Sec}[c + d x]}}{\sqrt{\operatorname{Cos}[c + d x]}} dx$$

Optimal (type 3, 57 leaves, 3 steps):

$$\frac{2 \sqrt{a} \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c+d x]}{\sqrt{a+a \operatorname{Sec}[c+d x]}}\right] \sqrt{\operatorname{Cos}[c+d x]} \sqrt{\operatorname{Sec}[c+d x]}}{d}$$

Result (type 5, 113 leaves):

$$-\frac{1}{3 d} 2 i e^{\frac{1}{2} i(c+d x)} \sqrt{\operatorname{Cos}[c+d x]} \left( 3 \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, 1, \frac{5}{4}, -e^{2 i(c+d x)}\right] + e^{i(c+d x)} \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{7}{4}, -e^{2 i(c+d x)}\right] \right) \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right] \sqrt{a(1 + \operatorname{Sec}[c+d x])}$$

**Problem 403: Result unnecessarily involves higher level functions.**

$$\int \frac{\sqrt{a + a \operatorname{Sec}[c + d x]}}{\operatorname{Cos}[c + d x]^{3/2}} dx$$

Optimal (type 3, 92 leaves, 4 steps):

$$\frac{\sqrt{a} \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c+d x]}{\sqrt{a+a \operatorname{Sec}[c+d x]}}\right] \sqrt{\operatorname{Cos}[c+d x]} \sqrt{\operatorname{Sec}[c+d x]}}{d} + \frac{a \operatorname{Sin}[c+d x]}{d \operatorname{Cos}[c+d x]^{3/2} \sqrt{a+a \operatorname{Sec}[c+d x]}}$$

Result (type 5, 146 leaves):

$$\frac{1}{3d} \sqrt{\cos[c+dx]} \sqrt{a(1+\sec[c+dx])} \left( -3i e^{\frac{1}{2}i(c+dx)} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, 1, \frac{5}{4}, -e^{2i(c+dx)}\right] \sec\left[\frac{1}{2}(c+dx)\right] - i e^{\frac{3}{2}i(c+dx)} \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{7}{4}, -e^{2i(c+dx)}\right] \sec\left[\frac{1}{2}(c+dx)\right] + 3 \sec[c+dx] \tan\left[\frac{1}{2}(c+dx)\right] \right)$$

**Problem 404: Result unnecessarily involves higher level functions.**

$$\int \frac{\sqrt{a+a \sec[c+dx]}}{\cos[c+dx]^{5/2}} dx$$

Optimal (type 3, 136 leaves, 5 steps):

$$\frac{3\sqrt{a} \operatorname{ArcSinh}\left[\frac{-\sqrt{a} \tan[c+dx]}{\sqrt{a+a \sec[c+dx]}}\right] \sqrt{\cos[c+dx]} \sqrt{\sec[c+dx]}}{4d} + \frac{a \sin[c+dx]}{2d \cos[c+dx]^{5/2} \sqrt{a+a \sec[c+dx]}} + \frac{3a \sin[c+dx]}{4d \cos[c+dx]^{3/2} \sqrt{a+a \sec[c+dx]}}$$

Result (type 5, 145 leaves):

$$\frac{1}{4d} \sqrt{\cos[c+dx]} \sec\left[\frac{1}{2}(c+dx)\right] \sqrt{a(1+\sec[c+dx])} \left( -3i e^{\frac{1}{2}i(c+dx)} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, 1, \frac{5}{4}, -e^{2i(c+dx)}\right] - i e^{\frac{3}{2}i(c+dx)} \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{7}{4}, -e^{2i(c+dx)}\right] + \sec[c+dx] (3+2 \sec[c+dx]) \sin\left[\frac{1}{2}(c+dx)\right] \right)$$

**Problem 408: Result unnecessarily involves higher level functions.**

$$\int \sqrt{\cos[c+dx]} (a+a \sec[c+dx])^{3/2} dx$$

Optimal (type 3, 96 leaves, 5 steps):

$$\frac{2a^{3/2} \operatorname{ArcSinh}\left[\frac{-\sqrt{a} \tan[c+dx]}{\sqrt{a+a \sec[c+dx]}}\right] \sqrt{\cos[c+dx]} \sqrt{\sec[c+dx]}}{d} + \frac{2a^2 \sin[c+dx]}{d \sqrt{\cos[c+dx]} \sqrt{a+a \sec[c+dx]}}$$

Result (type 5, 132 leaves):

$$\frac{1}{3d(1+e^{i(c+dx)})} \left( 2ia \sqrt{\cos[c+dx]} \left( -3+3e^{i(c+dx)}+6e^{i(c+dx)} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, 1, \frac{5}{4}, -e^{2i(c+dx)}\right] + 2e^{2i(c+dx)} \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{7}{4}, -e^{2i(c+dx)}\right] \right) \sqrt{a(1+\sec[c+dx])} \right)$$

### Problem 409: Result unnecessarily involves higher level functions.

$$\int \frac{(a + a \operatorname{Sec}[c + d x])^{3/2}}{\sqrt{\operatorname{Cos}[c + d x]}} dx$$

Optimal (type 3, 95 leaves, 5 steps):

$$\frac{3 a^{3/2} \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c+d x]}{\sqrt{a+a \operatorname{Sec}[c+d x]}}\right] \sqrt{\operatorname{Cos}[c+d x]} \sqrt{\operatorname{Sec}[c+d x]}}{d} + \frac{a^2 \operatorname{Sin}[c+d x]}{d \operatorname{Cos}[c+d x]^{3/2} \sqrt{a+a \operatorname{Sec}[c+d x]}}$$

Result (type 5, 171 leaves):

$$\left( a \left( 1 + \operatorname{Cos}[c + d x] \right) \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^2 \sqrt{a \left( 1 + \operatorname{Sec}[c + d x] \right)} \right. \\ \left. \left( -3 i e^{\frac{1}{2} i (c+d x)} \operatorname{Cos}[c + d x] \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, 1, \frac{5}{4}, -e^{2 i (c+d x)}\right] \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right] - \right. \right. \\ \left. \left. i e^{\frac{3}{2} i (c+d x)} \operatorname{Cos}[c + d x] \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{7}{4}, -e^{2 i (c+d x)}\right] \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right] + \right. \right. \\ \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] \right) \right) / \left( 2 d \sqrt{\operatorname{Cos}[c + d x]} \right)$$

### Problem 410: Result unnecessarily involves higher level functions.

$$\int \frac{(a + a \operatorname{Sec}[c + d x])^{3/2}}{\operatorname{Cos}[c + d x]^{3/2}} dx$$

Optimal (type 3, 140 leaves, 6 steps):

$$\frac{7 a^{3/2} \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c+d x]}{\sqrt{a+a \operatorname{Sec}[c+d x]}}\right] \sqrt{\operatorname{Cos}[c+d x]} \sqrt{\operatorname{Sec}[c+d x]}}{4 d} + \frac{a^2 \operatorname{Sin}[c+d x]}{2 d \operatorname{Cos}[c+d x]^{5/2} \sqrt{a+a \operatorname{Sec}[c+d x]}} + \frac{7 a^2 \operatorname{Sin}[c+d x]}{4 d \operatorname{Cos}[c+d x]^{3/2} \sqrt{a+a \operatorname{Sec}[c+d x]}}$$

Result (type 5, 167 leaves):

$$\left( a \left( 1 + \operatorname{Cos}[c + d x] \right) \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^3 \sqrt{a \left( 1 + \operatorname{Sec}[c + d x] \right)} \right. \\ \left( -21 i e^{\frac{1}{2} i (c+d x)} \operatorname{Cos}[c + d x]^2 \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, 1, \frac{5}{4}, -e^{2 i (c+d x)}\right] - \right. \\ \left. 7 i e^{\frac{3}{2} i (c+d x)} \operatorname{Cos}[c + d x]^2 \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{7}{4}, -e^{2 i (c+d x)}\right] + \right. \\ \left. 3 \left( 2 + 7 \operatorname{Cos}[c + d x] \right) \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right) \right) / \left( 24 d \operatorname{Cos}[c + d x]^{3/2} \right)$$

**Problem 411: Result unnecessarily involves higher level functions.**

$$\int \frac{(a + a \operatorname{Sec}[c + d x])^{3/2}}{\operatorname{Cos}[c + d x]^{5/2}} dx$$

Optimal (type 3, 180 leaves, 7 steps):

$$\frac{11 a^{3/2} \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c+d x]}{\sqrt{a+a \operatorname{Sec}[c+d x]}}\right] \sqrt{\operatorname{Cos}[c+d x]} \sqrt{\operatorname{Sec}[c+d x]}}{8 d} +$$

$$\frac{a^2 \operatorname{Sin}[c+d x]}{3 d \operatorname{Cos}[c+d x]^{7/2} \sqrt{a+a \operatorname{Sec}[c+d x]}} +$$

$$\frac{11 a^2 \operatorname{Sin}[c+d x]}{12 d \operatorname{Cos}[c+d x]^{5/2} \sqrt{a+a \operatorname{Sec}[c+d x]}} + \frac{11 a^2 \operatorname{Sin}[c+d x]}{8 d \operatorname{Cos}[c+d x]^{3/2} \sqrt{a+a \operatorname{Sec}[c+d x]}}$$

Result (type 5, 176 leaves):

$$\left( a (1 + \operatorname{Cos}[c + d x]) \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^3 \sqrt{a(1 + \operatorname{Sec}[c + d x])} \right.$$

$$\left( -33 i e^{\frac{1}{2} i (c+d x)} \operatorname{Cos}[c + d x]^3 \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, 1, \frac{5}{4}, -e^{2 i (c+d x)}\right] - \right.$$

$$\left. 11 i e^{\frac{3}{2} i (c+d x)} \operatorname{Cos}[c + d x]^3 \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{7}{4}, -e^{2 i (c+d x)}\right] + \right.$$

$$\left. \left. (8 + 22 \operatorname{Cos}[c + d x] + 33 \operatorname{Cos}[c + d x]^2) \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right) \right) / (48 d \operatorname{Cos}[c + d x]^{5/2})$$

**Problem 415: Result unnecessarily involves higher level functions.**

$$\int \operatorname{Cos}[c + d x]^{3/2} (a + a \operatorname{Sec}[c + d x])^{5/2} dx$$

Optimal (type 3, 138 leaves, 5 steps):

$$\frac{2 a^{5/2} \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c+d x]}{\sqrt{a+a \operatorname{Sec}[c+d x]}}\right] \sqrt{\operatorname{Cos}[c+d x]} \sqrt{\operatorname{Sec}[c+d x]}}{d} +$$

$$\frac{14 a^3 \operatorname{Sin}[c+d x]}{3 d \sqrt{\operatorname{Cos}[c+d x]} \sqrt{a+a \operatorname{Sec}[c+d x]}} + \frac{2 a^2 \sqrt{\operatorname{Cos}[c+d x]} \sqrt{a+a \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{3 d}$$

Result (type 5, 155 leaves):

$$\frac{1}{12 d} a^2 \sqrt{\operatorname{Cos}[c + d x]} (1 + \operatorname{Cos}[c + d x])^2 \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^5$$

$$\sqrt{a(1 + \operatorname{Sec}[c + d x])} \left( -6 i e^{\frac{1}{2} i (c+d x)} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, 1, \frac{5}{4}, -e^{2 i (c+d x)}\right] - \right.$$

$$\left. 2 i e^{\frac{3}{2} i (c+d x)} \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{7}{4}, -e^{2 i (c+d x)}\right] + 15 \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{3}{2}(c + d x)\right] \right)$$

### Problem 416: Result unnecessarily involves higher level functions.

$$\int \sqrt{\cos [c+d x]} (a+a \operatorname{Sec}[c+d x])^{5 / 2} d x$$

Optimal (type 3, 132 leaves, 5 steps):

$$\frac{5 a^{5 / 2} \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c+d x]}{\sqrt{a+a \operatorname{Sec}[c+d x]}}\right] \sqrt{\cos [c+d x]} \sqrt{\operatorname{Sec}[c+d x]}}{d} + \frac{a^3 \operatorname{Sin}[c+d x]}{d \sqrt{\cos [c+d x]} \sqrt{a+a \operatorname{Sec}[c+d x]}} + \frac{a^2 \sqrt{a+a \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{d \sqrt{\cos [c+d x]}}$$

Result (type 5, 167 leaves):

$$\left( a^2 (1+\cos [c+d x])^2 \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^5 \sqrt{a(1+\operatorname{Sec}[c+d x])} \right. \\ \left. \left( -15 i e^{\frac{1}{2} i(c+d x)} \cos [c+d x] \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, 1, \frac{5}{4}, -e^{2 i(c+d x)}\right] - \right. \right. \\ \left. \left. 5 i e^{\frac{3}{2} i(c+d x)} \cos [c+d x] \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{7}{4}, -e^{2 i(c+d x)}\right] + \right. \right. \\ \left. \left. 3(1+2 \cos [c+d x]) \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] \right) \right) / (12 d \sqrt{\cos [c+d x]})$$

### Problem 417: Result unnecessarily involves higher level functions.

$$\int \frac{(a+a \operatorname{Sec}[c+d x])^{5 / 2}}{\sqrt{\cos [c+d x]}} d x$$

Optimal (type 3, 140 leaves, 5 steps):

$$\frac{19 a^{5 / 2} \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c+d x]}{\sqrt{a+a \operatorname{Sec}[c+d x]}}\right] \sqrt{\cos [c+d x]} \sqrt{\operatorname{Sec}[c+d x]}}{4 d} + \frac{9 a^3 \operatorname{Sin}[c+d x]}{4 d \cos [c+d x]^{3 / 2} \sqrt{a+a \operatorname{Sec}[c+d x]}} + \frac{a^2 \sqrt{a+a \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{2 d \cos [c+d x]^{3 / 2}}$$

Result (type 5, 171 leaves):

$$\left( a^2 (1+\cos [c+d x])^2 \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^5 \sqrt{a(1+\operatorname{Sec}[c+d x])} \right. \\ \left. \left( -57 i e^{\frac{1}{2} i(c+d x)} \cos [c+d x]^2 \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, 1, \frac{5}{4}, -e^{2 i(c+d x)}\right] - \right. \right. \\ \left. \left. 19 i e^{\frac{3}{2} i(c+d x)} \cos [c+d x]^2 \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{7}{4}, -e^{2 i(c+d x)}\right] + \right. \right. \\ \left. \left. 3(2+11 \cos [c+d x]) \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] \right) \right) / (48 d \cos [c+d x]^{3 / 2})$$

### Problem 418: Result unnecessarily involves higher level functions.

$$\int \frac{(a + a \operatorname{Sec}[c + d x])^{5/2}}{\operatorname{Cos}[c + d x]^{3/2}} dx$$

Optimal (type 3, 180 leaves, 6 steps):

$$\frac{25 a^{5/2} \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c+d x]}{\sqrt{a+a \operatorname{Sec}[c+d x]}}\right] \sqrt{\operatorname{Cos}[c+d x]} \sqrt{\operatorname{Sec}[c+d x]}}{8 d} +$$

$$\frac{13 a^3 \operatorname{Sin}[c+d x]}{12 d \operatorname{Cos}[c+d x]^{5/2} \sqrt{a+a \operatorname{Sec}[c+d x]}} +$$

$$\frac{25 a^3 \operatorname{Sin}[c+d x]}{8 d \operatorname{Cos}[c+d x]^{3/2} \sqrt{a+a \operatorname{Sec}[c+d x]}} + \frac{a^2 \sqrt{a+a \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{3 d \operatorname{Cos}[c+d x]^{5/2}}$$

Result (type 5, 180 leaves):

$$\left( a^2 (1 + \operatorname{Cos}[c + d x])^2 \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^5 \sqrt{a(1 + \operatorname{Sec}[c + d x])} \right.$$

$$\left( -75 i e^{\frac{1}{2} i (c+d x)} \operatorname{Cos}[c + d x]^3 \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, 1, \frac{5}{4}, -e^{2 i (c+d x)}\right] - \right.$$

$$\left. 25 i e^{\frac{3}{2} i (c+d x)} \operatorname{Cos}[c + d x]^3 \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{7}{4}, -e^{2 i (c+d x)}\right] + \right.$$

$$\left. (8 + 34 \operatorname{Cos}[c + d x] + 75 \operatorname{Cos}[c + d x]^2) \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right) / (96 d \operatorname{Cos}[c + d x]^{5/2})$$

### Problem 419: Result unnecessarily involves higher level functions.

$$\int \frac{(a + a \operatorname{Sec}[c + d x])^{5/2}}{\operatorname{Cos}[c + d x]^{5/2}} dx$$

Optimal (type 3, 220 leaves, 7 steps):

$$\frac{163 a^{5/2} \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c+d x]}{\sqrt{a+a \operatorname{Sec}[c+d x]}}\right] \sqrt{\operatorname{Cos}[c+d x]} \sqrt{\operatorname{Sec}[c+d x]}}{64 d} +$$

$$\frac{17 a^3 \operatorname{Sin}[c+d x]}{24 d \operatorname{Cos}[c+d x]^{7/2} \sqrt{a+a \operatorname{Sec}[c+d x]}} + \frac{163 a^3 \operatorname{Sin}[c+d x]}{96 d \operatorname{Cos}[c+d x]^{5/2} \sqrt{a+a \operatorname{Sec}[c+d x]}} +$$

$$\frac{163 a^3 \operatorname{Sin}[c+d x]}{64 d \operatorname{Cos}[c+d x]^{3/2} \sqrt{a+a \operatorname{Sec}[c+d x]}} + \frac{a^2 \sqrt{a+a \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{4 d \operatorname{Cos}[c+d x]^{7/2}}$$

Result (type 5, 190 leaves):

$$\frac{1}{768 d \cos [c+d x]^{7/2}} a^2 (1+\cos [c+d x])^2 \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^5 \sqrt{a(1+\operatorname{Sec}[c+d x])}$$

$$\left(-489 i e^{\frac{1}{2} i(c+d x)} \cos [c+d x]^4 \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, 1, \frac{5}{4}, -e^{2 i(c+d x)}\right]-\right.$$

$$\left.163 i e^{\frac{3}{2} i(c+d x)} \cos [c+d x]^4 \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{7}{4}, -e^{2 i(c+d x)}\right]+(48+184 \cos [c+d x]+326 \cos [c+d x]^2+489 \cos [c+d x]^3) \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)$$

### Problem 441: Unable to integrate problem.

$$\int (d \cos [e+f x])^n (a+a \operatorname{Sec}[e+f x])^3 dx$$

Optimal (type 5, 244 leaves, 8 steps):

$$-\left(\left(a^3(7-4 n)(d \cos [e+f x])^n \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{n}{2}, \frac{2+n}{2}, \cos [e+f x]^2\right] \operatorname{Sin}[e+f x]\right) / \right.$$

$$\left.\left(f(2-n) n \sqrt{\operatorname{Sin}[e+f x]^2}\right)\right) -\left(a^3(1-4 n) \cos [e+f x](d \cos [e+f x])^n \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1+n}{2}, \frac{3+n}{2}, \cos [e+f x]^2\right] \operatorname{Sin}[e+f x]\right) /$$

$$\left(f(1-n)(1+n) \sqrt{\operatorname{Sin}[e+f x]^2}\right) + \frac{a^3(5-2 n)(d \cos [e+f x])^n \operatorname{Tan}[e+f x]}{f(1-n)(2-n)} +$$

$$\frac{(d \cos [e+f x])^n (a^3+a^3 \operatorname{Sec}[e+f x]) \operatorname{Tan}[e+f x]}{f(2-n)}$$

Result (type 8, 25 leaves):

$$\int (d \cos [e+f x])^n (a+a \operatorname{Sec}[e+f x])^3 dx$$

### Problem 442: Unable to integrate problem.

$$\int (d \cos [e+f x])^n (a+a \operatorname{Sec}[e+f x])^2 dx$$

Optimal (type 5, 179 leaves, 7 steps):

$$-\left(\left(2 a^2(d \cos [e+f x])^n \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{n}{2}, \frac{2+n}{2}, \cos [e+f x]^2\right] \operatorname{Sin}[e+f x]\right) / \right.$$

$$\left.\left(f n \sqrt{\operatorname{Sin}[e+f x]^2}\right)\right) -\left(a^2(1-2 n) \cos [e+f x](d \cos [e+f x])^n \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1+n}{2}, \frac{3+n}{2}, \cos [e+f x]^2\right] \operatorname{Sin}[e+f x]\right) /$$

$$\left(f(1-n)(1+n) \sqrt{\operatorname{Sin}[e+f x]^2}\right) + \frac{a^2(d \cos [e+f x])^n \operatorname{Tan}[e+f x]}{f(1-n)}$$

Result (type 8, 25 leaves):



$$\int (d \cos [e + f x])^n (a + a \sec [e + f x])^2 dx$$

**Problem 443: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int (d \cos [e + f x])^n (a + a \sec [e + f x]) dx$$

Optimal (type 5, 132 leaves, 5 steps):

$$- \left( \left( a (d \cos [e + f x])^n \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{n}{2}, \frac{2+n}{2}, \cos [e + f x]^2 \right] \sin [e + f x] \right) / \left( f n \sqrt{\sin [e + f x]^2} \right) - \left( a (d \cos [e + f x])^{1+n} \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{1+n}{2}, \frac{3+n}{2}, \cos [e + f x]^2 \right] \sin [e + f x] \right) / \left( d f (1+n) \sqrt{\sin [e + f x]^2} \right) \right)$$

Result (type 6, 3856 leaves):

$$\begin{aligned} & \left( a \cos [e + f x]^n (d \cos [e + f x])^n (1 + \sec [e + f x]) \tan \left[ \frac{1}{2} (e + f x) \right] \right. \\ & \left( \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, 1-n, n, \frac{3}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] \right) / \right. \\ & \left( \left( -1 + \tan \left[ \frac{1}{2} (e + f x) \right]^2 \right) \right. \\ & \left( -3 \operatorname{AppellF1} \left[ \frac{1}{2}, 1-n, n, \frac{3}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] + 2 \left( n \operatorname{AppellF1} \left[ \frac{3}{2}, 2- \right. \right. \right. \\ & \left. \left. \left. 1-n, 1+n, \frac{5}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] + (-1+n) \operatorname{AppellF1} \left[ \frac{3}{2}, 2- \right. \right. \right. \\ & \left. \left. \left. n, n, \frac{5}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (e + f x) \right]^2 \right) \right) + \\ & \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, -n, 1+n, \frac{3}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] \cos \left[ \frac{1}{2} (e + f x) \right]^2 \right) / \\ & \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, -n, 1+n, \frac{3}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] - \right. \\ & 2 \left( n \operatorname{AppellF1} \left[ \frac{3}{2}, 1-n, 1+n, \frac{5}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] + \right. \\ & \left. \left. (1+n) \operatorname{AppellF1} \left[ \frac{3}{2}, -n, 2+n, \frac{5}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] \right) \right) \\ & \left. \tan \left[ \frac{1}{2} (e + f x) \right]^2 \right) \right) / \left( f \left( \frac{1}{2} \cos [e + f x]^n \sec \left[ \frac{1}{2} (e + f x) \right]^2 \right) \right. \\ & \left( \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, 1-n, n, \frac{3}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, -\tan \left[ \frac{1}{2} (e + f x) \right]^2 \right] \right) / \right. \\ & \left( \left( -1 + \tan \left[ \frac{1}{2} (e + f x) \right]^2 \right) \right) \left( -3 \operatorname{AppellF1} \left[ \frac{1}{2}, 1-n, n, \frac{3}{2}, \tan \left[ \frac{1}{2} (e + f x) \right]^2, \right. \right. \right. \end{aligned}$$

$$\begin{aligned}
 & -\tan\left[\frac{1}{2}(e+fx)\right]^2 + 2\left(n \operatorname{AppellF1}\left[\frac{3}{2}, 1-n, 1+n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right.\right. \\
 & \quad \left.\left.-\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, 2-n, n, \frac{5}{2}, \right.\right. \\
 & \quad \left.\left.\tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right]\right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \Bigg) + \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -n, 1+n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \quad \left. \cos\left[\frac{1}{2}(e+fx)\right]^2\right) / \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -n, 1+n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] - \right. \\
 & \quad 2\left(n \operatorname{AppellF1}\left[\frac{3}{2}, 1-n, 1+n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left.(1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -n, 2+n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right]\right) \\
 & \quad \left. \tan\left[\frac{1}{2}(e+fx)\right]^2\right) - n \cos[e+fx]^{-1+n} \sin[e+fx] \tan\left[\frac{1}{2}(e+fx)\right] \\
 & \left(\left(3 \operatorname{AppellF1}\left[\frac{1}{2}, 1-n, n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right]\right) / \right. \\
 & \quad \left(\left(-1 + \tan\left[\frac{1}{2}(e+fx)\right]^2\right) \left(-3 \operatorname{AppellF1}\left[\frac{1}{2}, 1-n, n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right.\right. \right. \\
 & \quad \left.\left.-\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + 2\left(n \operatorname{AppellF1}\left[\frac{3}{2}, 1-n, 1+n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right.\right. \right. \\
 & \quad \left.\left.-\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, 2-n, n, \frac{5}{2}, \right.\right. \\
 & \quad \left.\left.\tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right]\right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \Bigg) + \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -n, 1+n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \quad \left. \cos\left[\frac{1}{2}(e+fx)\right]^2\right) / \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -n, 1+n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] - \right. \\
 & \quad 2\left(n \operatorname{AppellF1}\left[\frac{3}{2}, 1-n, 1+n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left.(1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -n, 2+n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right]\right) \\
 & \quad \left. \tan\left[\frac{1}{2}(e+fx)\right]^2\right) + \cos[e+fx]^n \tan\left[\frac{1}{2}(e+fx)\right] \\
 & \left(-\left(\left(3 \operatorname{AppellF1}\left[\frac{1}{2}, 1-n, n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \right. \\
 & \quad \left. \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right]\right) / \left(\left(-1 + \tan\left[\frac{1}{2}(e+fx)\right]^2\right)^2 \left(-3 \operatorname{AppellF1}\left[\frac{1}{2}, \right.\right. \right. \\
 & \quad \left.\left. 1-n, n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + 2\left(n \operatorname{AppellF1}\left[\frac{3}{2}, 1-n, \right.\right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & 1+n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2 + (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, \right. \\
 & \left. 2-n, n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \tan\left[\frac{1}{2}(e+fx)\right]^2 \Big) \Big) + \\
 & \left( 3 \left( -\frac{1}{3} n \operatorname{AppellF1}\left[\frac{3}{2}, 1-n, 1+n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \\
 & \quad \left. \left. \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \frac{1}{3} (1-n) \operatorname{AppellF1}\left[\frac{3}{2}, 2-n, n, \frac{5}{2}, \right. \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right] \right) \Big) \Big) / \\
 & \left( \left( -1 + \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \left( -3 \operatorname{AppellF1}\left[\frac{1}{2}, 1-n, n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + 2 \left( n \operatorname{AppellF1}\left[\frac{3}{2}, 1-n, 1+n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, 2-n, n, \frac{5}{2}, \right. \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \Big) - \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -n, 1+n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\
 & \quad \left. \cos\left[\frac{1}{2}(e+fx)\right] \sin\left[\frac{1}{2}(e+fx)\right] \right) \Big) / \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -n, 1+n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] - \right. \\
 & \quad 2 \left( n \operatorname{AppellF1}\left[\frac{3}{2}, 1-n, 1+n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left. (1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -n, 2+n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \\
 & \quad \left. \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) + \left( 3 \cos\left[\frac{1}{2}(e+fx)\right]^2 \right. \\
 & \quad \left. \left( -\frac{1}{3} n \operatorname{AppellF1}\left[\frac{3}{2}, 1-n, 1+n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \\
 & \quad \left. \left. \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] - \frac{1}{3} (1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -n, 2+n, \frac{5}{2}, \right. \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right] \right) \Big) \Big) / \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -n, 1+n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] - \right. \\
 & \quad 2 \left( n \operatorname{AppellF1}\left[\frac{3}{2}, 1-n, 1+n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
 & \quad \left. (1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -n, 2+n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) - \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, 1-n, n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right.
 \end{aligned}$$

$$\begin{aligned}
& \left( 2 \left( n \operatorname{AppellF1} \left[ \frac{3}{2}, 1-n, 1+n, \frac{5}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] + \right. \right. \\
& \quad (-1+n) \operatorname{AppellF1} \left[ \frac{3}{2}, 2-n, n, \frac{5}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, \right. \\
& \quad \quad \left. \left. -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right) \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \tan \left[ \frac{1}{2} (e+fx) \right] - \\
& 3 \left( -\frac{1}{3} n \operatorname{AppellF1} \left[ \frac{3}{2}, 1-n, 1+n, \frac{5}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right. \\
& \quad \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \tan \left[ \frac{1}{2} (e+fx) \right] + \frac{1}{3} (1-n) \operatorname{AppellF1} \left[ \frac{3}{2}, 2-n, n, \frac{5}{2}, \right. \\
& \quad \quad \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right) \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \tan \left[ \frac{1}{2} (e+fx) \right] \Big) + \\
& 2 \tan \left[ \frac{1}{2} (e+fx) \right]^2 \left( n \left( -\frac{3}{5} (1+n) \operatorname{AppellF1} \left[ \frac{5}{2}, 1-n, 2+n, \frac{7}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, \right. \right. \right. \\
& \quad \left. \left. -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right) \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \tan \left[ \frac{1}{2} (e+fx) \right] + \frac{3}{5} (1-n) \right. \\
& \quad \left. \operatorname{AppellF1} \left[ \frac{5}{2}, 2-n, 1+n, \frac{7}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right. \\
& \quad \left. \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \tan \left[ \frac{1}{2} (e+fx) \right] \right) + (-1+n) \left( -\frac{3}{5} n \operatorname{AppellF1} \left[ \frac{5}{2}, 2-n, \right. \right. \\
& \quad \left. \left. 1+n, \frac{7}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right) \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \right. \\
& \quad \left. \tan \left[ \frac{1}{2} (e+fx) \right] + \frac{3}{5} (2-n) \operatorname{AppellF1} \left[ \frac{5}{2}, 3-n, n, \frac{7}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, \right. \right. \\
& \quad \quad \left. \left. -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right) \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \tan \left[ \frac{1}{2} (e+fx) \right] \right) \Big) \Big) / \\
& \left( \left( -1 + \tan \left[ \frac{1}{2} (e+fx) \right]^2 \right) \left( -3 \operatorname{AppellF1} \left[ \frac{1}{2}, 1-n, n, \frac{3}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, \right. \right. \right. \right. \\
& \quad \left. \left. -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right) + 2 \left( n \operatorname{AppellF1} \left[ \frac{3}{2}, 1-n, 1+n, \frac{5}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, \right. \right. \right. \\
& \quad \quad \left. \left. -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right) + (-1+n) \operatorname{AppellF1} \left[ \frac{3}{2}, 2-n, n, \frac{5}{2}, \right. \right. \\
& \quad \quad \left. \left. \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right) \right) \tan \left[ \frac{1}{2} (e+fx) \right]^2 \Big) \Big) - \\
& \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, -n, 1+n, \frac{3}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right. \\
& \quad \cos \left[ \frac{1}{2} (e+fx) \right]^2 \left( -2 \left( n \operatorname{AppellF1} \left[ \frac{3}{2}, 1-n, 1+n, \frac{5}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, \right. \right. \right. \\
& \quad \quad \left. \left. -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right) + (1+n) \operatorname{AppellF1} \left[ \frac{3}{2}, -n, 2+n, \frac{5}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, \right. \right. \\
& \quad \quad \left. \left. -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right) \right) \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \tan \left[ \frac{1}{2} (e+fx) \right] + \\
& \quad 3 \left( -\frac{1}{3} n \operatorname{AppellF1} \left[ \frac{3}{2}, 1-n, 1+n, \frac{5}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right. \\
& \quad \quad \left. \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \tan \left[ \frac{1}{2} (e+fx) \right] - \frac{1}{3} (1+n) \operatorname{AppellF1} \left[ \frac{3}{2}, -n, 2+n, \frac{5}{2}, \right. \right.
\end{aligned}$$

$$\begin{aligned}
 & \left( \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \Big) - \\
 & 2 \tan\left[\frac{1}{2}(e+fx)\right]^2 \left( n \left( -\frac{3}{5}(1+n) \operatorname{AppellF1}\left[\frac{5}{2}, 1-n, 2+n, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \frac{3}{5}(1-n) \right. \right. \right. \\
 & \quad \left. \operatorname{AppellF1}\left[\frac{5}{2}, 2-n, 1+n, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right] \right. \right. \\
 & \quad \left. \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) + (1+n) \left( -\frac{3}{5} n \operatorname{AppellF1}\left[\frac{5}{2}, 1-n, \right. \right. \\
 & \quad \left. \left. 2+n, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \sec\left[\frac{1}{2}(e+fx)\right]^2 \right. \\
 & \quad \left. \tan\left[\frac{1}{2}(e+fx)\right] - \frac{3}{5}(2+n) \operatorname{AppellF1}\left[\frac{5}{2}, -n, 3+n, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) \Big) \Big) \Big) \Big) \Big) / \\
 & \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, -n, 1+n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right] - \right. \\
 & \quad \left. 2 \left( n \operatorname{AppellF1}\left[\frac{3}{2}, 1-n, 1+n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right] + \right. \right. \\
 & \quad \left. \left. (1+n) \operatorname{AppellF1}\left[\frac{3}{2}, -n, 2+n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \right) \right) \Big) \Big) \Big) \Big) \Big)
 \end{aligned}$$

### Problem 444: Unable to integrate problem.

$$\int \frac{(d \cos[e+fx])^n}{a+a \sec[e+fx]} dx$$

Optimal (type 5, 178 leaves, 7 steps):

$$\begin{aligned}
 & \frac{(d \cos[e+fx])^n \sin[e+fx]}{f(a+a \sec[e+fx])} - \\
 & \left( \cos[e+fx] (d \cos[e+fx])^n \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1+n}{2}, \frac{3+n}{2}, \cos[e+fx]^2\right] \sin[e+fx] \right) / \\
 & \left( a f \sqrt{\sin[e+fx]^2} \right) + \left( (1+n) \cos[e+fx]^2 (d \cos[e+fx])^n \right. \\
 & \quad \left. \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{2+n}{2}, \frac{4+n}{2}, \cos[e+fx]^2\right] \sin[e+fx] \right) / \left( a f (2+n) \sqrt{\sin[e+fx]^2} \right)
 \end{aligned}$$

Result (type 8, 25 leaves):

$$\int \frac{(d \cos[e+fx])^n}{a+a \sec[e+fx]} dx$$

### Problem 445: Unable to integrate problem.

$$\int \frac{(d \cos [e + f x])^n}{(a + a \sec [e + f x])^2} dx$$

Optimal (type 5, 215 leaves, 8 steps):

$$\begin{aligned} & \left( 2 (2+n) (d \cos [e + f x])^n \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{n}{2}, \frac{2+n}{2}, \cos [e + f x]^2 \right] \sin [e + f x] \right) / \\ & \left( 3 a^2 f \sqrt{\sin [e + f x]^2} \right) - \left( (3+2n) \cos [e + f x] (d \cos [e + f x])^n \right. \\ & \left. \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{1+n}{2}, \frac{3+n}{2}, \cos [e + f x]^2 \right] \sin [e + f x] \right) / \left( 3 a^2 f \sqrt{\sin [e + f x]^2} \right) - \\ & \frac{2 (2+n) (d \cos [e + f x])^n \tan [e + f x]}{3 a^2 f (1 + \sec [e + f x])} - \frac{(d \cos [e + f x])^n \tan [e + f x]}{3 f (a + a \sec [e + f x])^2} \end{aligned}$$

Result (type 8, 25 leaves):

$$\int \frac{(d \cos [e + f x])^n}{(a + a \sec [e + f x])^2} dx$$

### Problem 446: Result more than twice size of optimal antiderivative.

$$\int \sec [c + d x]^4 (a + b \sec [c + d x]) dx$$

Optimal (type 3, 85 leaves, 6 steps):

$$\begin{aligned} & \frac{3 b \operatorname{ArcTanh} [\sin [c + d x]]}{8 d} + \frac{a \tan [c + d x]}{d} + \\ & \frac{3 b \sec [c + d x] \tan [c + d x]}{8 d} + \frac{b \sec [c + d x]^3 \tan [c + d x]}{4 d} + \frac{a \tan [c + d x]^3}{3 d} \end{aligned}$$

Result (type 3, 227 leaves):

$$\begin{aligned} & - \frac{3 b \operatorname{Log} \left[ \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right]}{8 d} + \\ & \frac{3 b \operatorname{Log} \left[ \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right]}{8 d} + \frac{b}{16 d \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right)^4} + \\ & \frac{3 b}{16 d \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right)^2} - \frac{b}{16 d \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^4} - \\ & \frac{3 b}{16 d \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^2} + \frac{2 a \tan [c + d x]}{3 d} + \frac{a \sec [c + d x]^2 \tan [c + d x]}{3 d} \end{aligned}$$

**Problem 449: Result more than twice size of optimal antiderivative.**

$$\int \sec [c + d x] (a + b \sec [c + d x]) dx$$

Optimal (type 3, 24 leaves, 4 steps):

$$\frac{a \operatorname{ArcTanh}[\sin [c + d x]]}{d} + \frac{b \tan [c + d x]}{d}$$

Result (type 3, 81 leaves):

$$-\frac{a \operatorname{Log}\left[\cos \left[\frac{c}{2} + \frac{dx}{2}\right] - \sin \left[\frac{c}{2} + \frac{dx}{2}\right]\right]}{d} + \frac{a \operatorname{Log}\left[\cos \left[\frac{c}{2} + \frac{dx}{2}\right] + \sin \left[\frac{c}{2} + \frac{dx}{2}\right]\right]}{d} + \frac{b \tan [c + d x]}{d}$$

**Problem 450: Result more than twice size of optimal antiderivative.**

$$\int (a + b \sec [c + d x]) dx$$

Optimal (type 3, 16 leaves, 2 steps):

$$a x + \frac{b \operatorname{ArcTanh}[\sin [c + d x]]}{d}$$

Result (type 3, 73 leaves):

$$a x - \frac{b \operatorname{Log}\left[\cos \left[\frac{c}{2} + \frac{dx}{2}\right] - \sin \left[\frac{c}{2} + \frac{dx}{2}\right]\right]}{d} + \frac{b \operatorname{Log}\left[\cos \left[\frac{c}{2} + \frac{dx}{2}\right] + \sin \left[\frac{c}{2} + \frac{dx}{2}\right]\right]}{d}$$

**Problem 456: Result more than twice size of optimal antiderivative.**

$$\int \sec [c + d x]^4 (a + b \sec [c + d x])^2 dx$$

Optimal (type 3, 135 leaves, 7 steps):

$$\frac{3 a b \operatorname{ArcTanh}[\sin [c + d x]]}{4 d} + \frac{(5 a^2 + 4 b^2) \tan [c + d x]}{5 d} + \frac{3 a b \sec [c + d x] \tan [c + d x]}{4 d} + \frac{a b \sec [c + d x]^3 \tan [c + d x]}{2 d} + \frac{b^2 \sec [c + d x]^4 \tan [c + d x]}{5 d} + \frac{(5 a^2 + 4 b^2) \tan [c + d x]^3}{15 d}$$

Result (type 3, 301 leaves):

$$\begin{aligned}
& - \frac{3 a b \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+d x)\right]-\sin\left[\frac{1}{2}(c+d x)\right]\right]}{4 d} + \\
& \frac{3 a b \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+d x)\right]+\sin\left[\frac{1}{2}(c+d x)\right]\right]}{4 d} + \frac{a b}{8 d\left(\cos\left[\frac{1}{2}(c+d x)\right]-\sin\left[\frac{1}{2}(c+d x)\right]\right)^4} + \\
& \frac{3 a b}{8 d\left(\cos\left[\frac{1}{2}(c+d x)\right]-\sin\left[\frac{1}{2}(c+d x)\right]\right)^2} - \frac{a b}{8 d\left(\cos\left[\frac{1}{2}(c+d x)\right]+\sin\left[\frac{1}{2}(c+d x)\right]\right)^4} - \\
& \frac{3 a b}{8 d\left(\cos\left[\frac{1}{2}(c+d x)\right]+\sin\left[\frac{1}{2}(c+d x)\right]\right)^2} + \frac{2 a^2 \operatorname{Tan}[c+d x]}{3 d} + \frac{8 b^2 \operatorname{Tan}[c+d x]}{15 d} + \\
& \frac{a^2 \operatorname{Sec}[c+d x]^2 \operatorname{Tan}[c+d x]}{3 d} + \frac{4 b^2 \operatorname{Sec}[c+d x]^2 \operatorname{Tan}[c+d x]}{15 d} + \frac{b^2 \operatorname{Sec}[c+d x]^4 \operatorname{Tan}[c+d x]}{5 d}
\end{aligned}$$

**Problem 457: Result more than twice size of optimal antiderivative.**

$$\int \operatorname{Sec}[c+d x]^3 (a+b \operatorname{Sec}[c+d x])^2 dx$$

Optimal (type 3, 110 leaves, 6 steps):

$$\begin{aligned}
& \frac{(4 a^2+3 b^2) \operatorname{ArcTanh}\left[\sin [c+d x]\right]}{8 d} + \frac{2 a b \operatorname{Tan}[c+d x]}{d} + \\
& \frac{(4 a^2+3 b^2) \operatorname{Sec}[c+d x] \operatorname{Tan}[c+d x]}{8 d} + \frac{b^2 \operatorname{Sec}[c+d x]^3 \operatorname{Tan}[c+d x]}{4 d} + \frac{2 a b \operatorname{Tan}[c+d x]^3}{3 d}
\end{aligned}$$

Result (type 3, 375 leaves):

$$\begin{aligned}
& - \frac{a^2 \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+d x)\right]-\sin\left[\frac{1}{2}(c+d x)\right]\right]}{2 d} - \\
& \frac{3 b^2 \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+d x)\right]-\sin\left[\frac{1}{2}(c+d x)\right]\right]}{8 d} + \frac{a^2 \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+d x)\right]+\sin\left[\frac{1}{2}(c+d x)\right]\right]}{2 d} + \\
& \frac{3 b^2 \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+d x)\right]+\sin\left[\frac{1}{2}(c+d x)\right]\right]}{8 d} + \frac{b^2}{16 d\left(\cos\left[\frac{1}{2}(c+d x)\right]-\sin\left[\frac{1}{2}(c+d x)\right]\right)^4} + \\
& \frac{a^2}{4 d\left(\cos\left[\frac{1}{2}(c+d x)\right]-\sin\left[\frac{1}{2}(c+d x)\right]\right)^2} + \frac{3 b^2}{16 d\left(\cos\left[\frac{1}{2}(c+d x)\right]-\sin\left[\frac{1}{2}(c+d x)\right]\right)^2} - \\
& \frac{b^2}{16 d\left(\cos\left[\frac{1}{2}(c+d x)\right]+\sin\left[\frac{1}{2}(c+d x)\right]\right)^4} - \frac{a^2}{4 d\left(\cos\left[\frac{1}{2}(c+d x)\right]+\sin\left[\frac{1}{2}(c+d x)\right]\right)^2} - \\
& \frac{3 b^2}{16 d\left(\cos\left[\frac{1}{2}(c+d x)\right]+\sin\left[\frac{1}{2}(c+d x)\right]\right)^2} + \frac{4 a b \operatorname{Tan}[c+d x]}{3 d} + \frac{2 a b \operatorname{Sec}[c+d x]^2 \operatorname{Tan}[c+d x]}{3 d}
\end{aligned}$$



**Problem 459: Result more than twice size of optimal antiderivative.**

$$\int \sec [c + d x] (a + b \sec [c + d x])^2 dx$$

Optimal (type 3, 59 leaves, 5 steps):

$$\frac{(2 a^2 + b^2) \operatorname{ArcTanh}[\operatorname{Sin}[c + d x]]}{2 d} + \frac{2 a b \operatorname{Tan}[c + d x]}{d} + \frac{b^2 \sec [c + d x] \operatorname{Tan}[c + d x]}{2 d}$$

Result (type 3, 218 leaves):

$$\begin{aligned} & \frac{1}{4 d} \sec [c + d x]^2 \left( -2 a^2 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] - \right. \\ & \quad b^2 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] - (2 a^2 + b^2) \operatorname{Cos}[2(c + d x)] \\ & \quad \left. \left( \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] - \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] \right) + \right. \\ & \quad 2 a^2 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] + b^2 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] \left. \right) + \\ & \quad 2 b^2 \operatorname{Sin}[c + d x] + 4 a b \operatorname{Sin}[2(c + d x)] \end{aligned}$$

**Problem 460: Result more than twice size of optimal antiderivative.**

$$\int (a + b \sec [c + d x])^2 dx$$

Optimal (type 3, 33 leaves, 4 steps):

$$a^2 x + \frac{2 a b \operatorname{ArcTanh}[\operatorname{Sin}[c + d x]]}{d} + \frac{b^2 \operatorname{Tan}[c + d x]}{d}$$

Result (type 3, 77 leaves):

$$\begin{aligned} & \frac{1}{d} \left( a \left( a c + a d x - 2 b \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] \right) + \right. \\ & \quad \left. 2 b \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] \right) + b^2 \operatorname{Tan}[c + d x] \end{aligned}$$

**Problem 461: Result more than twice size of optimal antiderivative.**

$$\int \cos [c + d x] (a + b \sec [c + d x])^2 dx$$

Optimal (type 3, 33 leaves, 4 steps):

$$2 a b x + \frac{b^2 \operatorname{ArcTanh}[\operatorname{Sin}[c + d x]]}{d} + \frac{a^2 \operatorname{Sin}[c + d x]}{d}$$

Result (type 3, 105 leaves):

$$2 a b x - \frac{b^2 \operatorname{Log}\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] - \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right]}{d} +$$

$$\frac{b^2 \operatorname{Log}\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right]}{d} + \frac{a^2 \cos[dx] \sin[c]}{d} + \frac{a^2 \cos[c] \sin[dx]}{d}$$

**Problem 466: Result more than twice size of optimal antiderivative.**

$$\int \operatorname{Sec}[c + dx]^3 (a + b \operatorname{Sec}[c + dx])^3 dx$$

Optimal (type 3, 189 leaves, 8 steps):

$$\frac{a (4 a^2 + 9 b^2) \operatorname{ArcTanh}[\sin[c + dx]]}{8 d} - \frac{(3 a^4 - 52 a^2 b^2 - 16 b^4) \tan[c + dx]}{30 b d} -$$

$$\frac{a (6 a^2 - 71 b^2) \operatorname{Sec}[c + dx] \tan[c + dx]}{120 d} - \frac{(3 a^2 - 16 b^2) (a + b \operatorname{Sec}[c + dx])^2 \tan[c + dx]}{60 b d} -$$

$$\frac{a (a + b \operatorname{Sec}[c + dx])^3 \tan[c + dx]}{20 b d} + \frac{(a + b \operatorname{Sec}[c + dx])^4 \tan[c + dx]}{5 b d}$$

Result (type 3, 619 leaves):

$$\frac{(-4 a^3 - 9 a b^2) \operatorname{Log}\left[\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right]\right]}{8 d} +$$

$$\frac{(4 a^3 + 9 a b^2) \operatorname{Log}\left[\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right]\right]}{8 d} +$$

$$\frac{15 a b^2 + 2 b^3}{80 d \left(\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right]\right)^4} + \frac{60 a^3 + 60 a^2 b + 135 a b^2 + 19 b^3}{240 d \left(\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right]\right)^2}$$

$$\frac{b^3 \sin\left[\frac{1}{2}(c + dx)\right]}{20 d \left(\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right]\right)^5} + \frac{b^3 \sin\left[\frac{1}{2}(c + dx)\right]}{20 d \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right]\right)^5} +$$

$$\frac{-15 a b^2 - 2 b^3}{80 d \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right]\right)^4} + \frac{-60 a^3 - 60 a^2 b - 135 a b^2 - 19 b^3}{240 d \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right]\right)^2}$$

$$\frac{2 \left(15 a^2 b \sin\left[\frac{1}{2}(c + dx)\right] + 4 b^3 \sin\left[\frac{1}{2}(c + dx)\right]\right)}{15 d \left(\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right]\right)} +$$

$$\frac{2 \left(15 a^2 b \sin\left[\frac{1}{2}(c + dx)\right] + 4 b^3 \sin\left[\frac{1}{2}(c + dx)\right]\right)}{15 d \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right]\right)} +$$

$$\frac{60 a^2 b \sin\left[\frac{1}{2}(c + dx)\right] + 19 b^3 \sin\left[\frac{1}{2}(c + dx)\right]}{120 d \left(\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right]\right)^3} + \frac{60 a^2 b \sin\left[\frac{1}{2}(c + dx)\right] + 19 b^3 \sin\left[\frac{1}{2}(c + dx)\right]}{120 d \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right]\right)^3}$$

**Problem 467: Result more than twice size of optimal antiderivative.**

$$\int \text{Sec}[c + d x]^2 (a + b \text{Sec}[c + d x])^3 dx$$

Optimal (type 3, 130 leaves, 7 steps):

$$\frac{3 b (4 a^2 + b^2) \text{ArcTanh}[\text{Sin}[c + d x]]}{8 d} + \frac{a (a^2 + 4 b^2) \text{Tan}[c + d x]}{2 d} + \frac{b (2 a^2 + 3 b^2) \text{Sec}[c + d x] \text{Tan}[c + d x]}{8 d} + \frac{a (a + b \text{Sec}[c + d x])^2 \text{Tan}[c + d x]}{4 d} + \frac{(a + b \text{Sec}[c + d x])^3 \text{Tan}[c + d x]}{4 d}$$

Result (type 3, 455 leaves):

$$\begin{aligned} & - \frac{3 (4 a^2 b + b^3) \text{Log}\left[\text{Cos}\left[\frac{1}{2} (c + d x)\right] - \text{Sin}\left[\frac{1}{2} (c + d x)\right]\right]}{8 d} + \\ & \frac{3 (4 a^2 b + b^3) \text{Log}\left[\text{Cos}\left[\frac{1}{2} (c + d x)\right] + \text{Sin}\left[\frac{1}{2} (c + d x)\right]\right]}{8 d} + \\ & \frac{b^3}{16 d \left(\text{Cos}\left[\frac{1}{2} (c + d x)\right] - \text{Sin}\left[\frac{1}{2} (c + d x)\right]\right)^4} + \frac{12 a^2 b + 4 a b^2 + 3 b^3}{16 d \left(\text{Cos}\left[\frac{1}{2} (c + d x)\right] - \text{Sin}\left[\frac{1}{2} (c + d x)\right]\right)^2} + \\ & \frac{a b^2 \text{Sin}\left[\frac{1}{2} (c + d x)\right]}{2 d \left(\text{Cos}\left[\frac{1}{2} (c + d x)\right] - \text{Sin}\left[\frac{1}{2} (c + d x)\right]\right)^3} - \frac{b^3}{16 d \left(\text{Cos}\left[\frac{1}{2} (c + d x)\right] + \text{Sin}\left[\frac{1}{2} (c + d x)\right]\right)^4} + \\ & \frac{a b^2 \text{Sin}\left[\frac{1}{2} (c + d x)\right]}{2 d \left(\text{Cos}\left[\frac{1}{2} (c + d x)\right] + \text{Sin}\left[\frac{1}{2} (c + d x)\right]\right)^3} + \frac{-12 a^2 b - 4 a b^2 - 3 b^3}{16 d \left(\text{Cos}\left[\frac{1}{2} (c + d x)\right] + \text{Sin}\left[\frac{1}{2} (c + d x)\right]\right)^2} + \\ & \frac{a^3 \text{Sin}\left[\frac{1}{2} (c + d x)\right] + 2 a b^2 \text{Sin}\left[\frac{1}{2} (c + d x)\right]}{d \left(\text{Cos}\left[\frac{1}{2} (c + d x)\right] - \text{Sin}\left[\frac{1}{2} (c + d x)\right]\right)} + \frac{a^3 \text{Sin}\left[\frac{1}{2} (c + d x)\right] + 2 a b^2 \text{Sin}\left[\frac{1}{2} (c + d x)\right]}{d \left(\text{Cos}\left[\frac{1}{2} (c + d x)\right] + \text{Sin}\left[\frac{1}{2} (c + d x)\right]\right)} \end{aligned}$$

**Problem 468: Result more than twice size of optimal antiderivative.**

$$\int \text{Sec}[c + d x] (a + b \text{Sec}[c + d x])^3 dx$$

Optimal (type 3, 99 leaves, 6 steps):

$$\frac{a (2 a^2 + 3 b^2) \text{ArcTanh}[\text{Sin}[c + d x]]}{2 d} + \frac{2 b (4 a^2 + b^2) \text{Tan}[c + d x]}{3 d} + \frac{5 a b^2 \text{Sec}[c + d x] \text{Tan}[c + d x]}{6 d} + \frac{b (a + b \text{Sec}[c + d x])^2 \text{Tan}[c + d x]}{3 d}$$

Result (type 3, 206 leaves):

$$\begin{aligned}
& -\frac{1}{24d} \operatorname{Sec}[c+dx]^3 \left( 9a(2a^2+3b^2) \operatorname{Cos}[c+dx] \left( \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] - \right. \right. \\
& \quad \left. \left. \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right]\right) + 3a(2a^2+3b^2) \operatorname{Cos}[3(c+dx)] \right) \\
& \quad \left( \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] - \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \right) - \\
& \quad 4b(9a^2+4b^2+9ab \operatorname{Cos}[c+dx] + (9a^2+2b^2) \operatorname{Cos}[2(c+dx)]) \operatorname{Sin}[c+dx] \Big)
\end{aligned}$$

### Problem 469: Result more than twice size of optimal antiderivative.

$$\int (a+b \operatorname{Sec}[c+dx])^3 dx$$

Optimal (type 3, 73 leaves, 5 steps):

$$a^3 x + \frac{b(6a^2+b^2) \operatorname{ArcTanh}[\operatorname{Sin}[c+dx]]}{2d} + \frac{5ab^2 \operatorname{Tan}[c+dx]}{2d} + \frac{b^2(a+b \operatorname{Sec}[c+dx]) \operatorname{Tan}[c+dx]}{2d}$$

Result (type 3, 256 leaves):

$$\begin{aligned}
& \frac{1}{4d} \operatorname{Sec}[c+dx]^2 \left( 2a^3c + 2a^3dx - 6a^2b \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] - \right. \\
& \quad b^3 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] + 6a^2b \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] + \\
& \quad b^3 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] + \operatorname{Cos}[2(c+dx)] \\
& \quad \left( 2a^3(c+dx) - b(6a^2+b^2) \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] + b(6a^2+b^2) \right. \\
& \quad \left. \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \right) + 2b^3 \operatorname{Sin}[c+dx] + 6ab^2 \operatorname{Sin}[2(c+dx)] \Big)
\end{aligned}$$

### Problem 477: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Sec}[c+dx]^2 (a+b \operatorname{Sec}[c+dx])^4 dx$$

Optimal (type 3, 179 leaves, 8 steps):

$$\begin{aligned}
& \frac{ab(4a^2+3b^2) \operatorname{ArcTanh}[\operatorname{Sin}[c+dx]]}{2d} + \frac{2(3a^4+28a^2b^2+4b^4) \operatorname{Tan}[c+dx]}{15d} + \\
& \frac{ab(6a^2+29b^2) \operatorname{Sec}[c+dx] \operatorname{Tan}[c+dx]}{30d} + \frac{(3a^2+4b^2)(a+b \operatorname{Sec}[c+dx])^2 \operatorname{Tan}[c+dx]}{15d} + \\
& \frac{a(a+b \operatorname{Sec}[c+dx])^3 \operatorname{Tan}[c+dx]}{5d} + \frac{(a+b \operatorname{Sec}[c+dx])^4 \operatorname{Tan}[c+dx]}{5d}
\end{aligned}$$

Result (type 3, 663 leaves):

$$\begin{aligned}
 & \frac{(-4 a^3 b - 3 a b^3) \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right]}{2 d} + \\
 & \frac{(4 a^3 b + 3 a b^3) \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right]}{2 d} + \\
 & \frac{10 a b^3 + b^4}{40 d \left(\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right)^4} + \frac{240 a^3 b + 120 a^2 b^2 + 180 a b^3 + 19 b^4}{240 d \left(\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right)^2} + \\
 & \frac{b^4 \sin\left[\frac{1}{2}(c+dx)\right]}{20 d \left(\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right)^5} + \frac{b^4 \sin\left[\frac{1}{2}(c+dx)\right]}{20 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^5} + \\
 & \frac{-10 a b^3 - b^4}{40 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^4} + \frac{-240 a^3 b - 120 a^2 b^2 - 180 a b^3 - 19 b^4}{240 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^2} + \\
 & \frac{\left(15 a^4 \sin\left[\frac{1}{2}(c+dx)\right] + 60 a^2 b^2 \sin\left[\frac{1}{2}(c+dx)\right] + 8 b^4 \sin\left[\frac{1}{2}(c+dx)\right]\right) /}{\left(15 d \left(\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right)\right) +} \\
 & \frac{\left(15 a^4 \sin\left[\frac{1}{2}(c+dx)\right] + 60 a^2 b^2 \sin\left[\frac{1}{2}(c+dx)\right] + 8 b^4 \sin\left[\frac{1}{2}(c+dx)\right]\right) /}{\left(15 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)\right) +} + \frac{120 a^2 b^2 \sin\left[\frac{1}{2}(c+dx)\right] + 19 b^4 \sin\left[\frac{1}{2}(c+dx)\right]}{120 d \left(\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right)^3} + \\
 & \frac{120 a^2 b^2 \sin\left[\frac{1}{2}(c+dx)\right] + 19 b^4 \sin\left[\frac{1}{2}(c+dx)\right]}{120 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^3}
 \end{aligned}$$

**Problem 478: Result more than twice size of optimal antiderivative.**

$$\int \sec[c+dx] (a+b \sec[c+dx])^4 dx$$

Optimal (type 3, 146 leaves, 7 steps):

$$\begin{aligned}
 & \frac{(8 a^4 + 24 a^2 b^2 + 3 b^4) \operatorname{ArcTanh}[\sin[c+dx]]}{8 d} + \\
 & \frac{a b (19 a^2 + 16 b^2) \tan[c+dx]}{6 d} + \frac{b^2 (26 a^2 + 9 b^2) \sec[c+dx] \tan[c+dx]}{24 d} + \\
 & \frac{7 a b (a+b \sec[c+dx])^2 \tan[c+dx]}{12 d} + \frac{b (a+b \sec[c+dx])^3 \tan[c+dx]}{4 d}
 \end{aligned}$$

Result (type 3, 807 leaves):

$$\begin{aligned}
& \left( (-8a^4 - 24a^2b^2 - 3b^4) \cos[c + dx]^4 \right. \\
& \quad \left. \log\left[\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right]\right] (a + b \sec[c + dx])^4 \right) / \left( 8d (b + a \cos[c + dx])^4 \right) + \\
& \left( (8a^4 + 24a^2b^2 + 3b^4) \cos[c + dx]^4 \log\left[\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right]\right] \right. \\
& \quad \left. (a + b \sec[c + dx])^4 \right) / \left( 8d (b + a \cos[c + dx])^4 \right) + \\
& \frac{b^4 \cos[c + dx]^4 (a + b \sec[c + dx])^4}{16d (b + a \cos[c + dx])^4 \left(\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right]\right)^4} + \\
& \frac{(72a^2b^2 + 16ab^3 + 9b^4) \cos[c + dx]^4 (a + b \sec[c + dx])^4}{48d (b + a \cos[c + dx])^4 \left(\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right]\right)^2} + \\
& \frac{2ab^3 \cos[c + dx]^4 (a + b \sec[c + dx])^4 \sin\left[\frac{1}{2}(c + dx)\right]}{3d (b + a \cos[c + dx])^4 \left(\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right]\right)^3} - \\
& \frac{b^4 \cos[c + dx]^4 (a + b \sec[c + dx])^4}{16d (b + a \cos[c + dx])^4 \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right]\right)^4} + \\
& \frac{2ab^3 \cos[c + dx]^4 (a + b \sec[c + dx])^4 \sin\left[\frac{1}{2}(c + dx)\right]}{3d (b + a \cos[c + dx])^4 \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right]\right)^3} + \\
& \frac{(-72a^2b^2 - 16ab^3 - 9b^4) \cos[c + dx]^4 (a + b \sec[c + dx])^4}{48d (b + a \cos[c + dx])^4 \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right]\right)^2} + \\
& \left( 4 \cos[c + dx]^4 (a + b \sec[c + dx])^4 \left( 3a^3b \sin\left[\frac{1}{2}(c + dx)\right] + 2ab^3 \sin\left[\frac{1}{2}(c + dx)\right] \right) \right) / \\
& \left( 3d (b + a \cos[c + dx])^4 \left(\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right]\right) \right) + \\
& \left( 4 \cos[c + dx]^4 (a + b \sec[c + dx])^4 \left( 3a^3b \sin\left[\frac{1}{2}(c + dx)\right] + 2ab^3 \sin\left[\frac{1}{2}(c + dx)\right] \right) \right) / \\
& \left( 3d (b + a \cos[c + dx])^4 \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right]\right) \right)
\end{aligned}$$

**Problem 479: Result more than twice size of optimal antiderivative.**

$$\int (a + b \sec[c + dx])^4 dx$$

Optimal (type 3, 107 leaves, 6 steps):

$$\begin{aligned}
& a^4 x + \frac{2ab(2a^2 + b^2) \operatorname{ArcTanh}[\sin[c + dx]]}{d} + \frac{b^2(17a^2 + 2b^2) \tan[c + dx]}{3d} + \\
& \frac{4ab^3 \sec[c + dx] \tan[c + dx]}{3d} + \frac{b^2(a + b \sec[c + dx])^2 \tan[c + dx]}{3d}
\end{aligned}$$

Result (type 3, 246 leaves):

$$\frac{1}{12d} \operatorname{Sec}[c+dx]^3 \left( 9a \operatorname{Cos}[c+dx] \left( a^3(c+dx) - 2b(2a^2+b^2) \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] + 2b(2a^2+b^2) \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \right) + 3a \operatorname{Cos}[3(c+dx)] \left( a^3(c+dx) - 2b(2a^2+b^2) \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] + 2b(2a^2+b^2) \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \right) + 4b^2(9a^2+2b^2+6ab \operatorname{Cos}[c+dx] + (9a^2+b^2) \operatorname{Cos}[2(c+dx)]) \operatorname{Sin}[c+dx] \right)$$

**Problem 480: Result more than twice size of optimal antiderivative.**

$$\int \operatorname{Cos}[c+dx] (a+b \operatorname{Sec}[c+dx])^4 dx$$

Optimal (type 3, 104 leaves, 6 steps):

$$4a^3bx + \frac{b^2(12a^2+b^2) \operatorname{ArcTanh}[\operatorname{Sin}[c+dx]]}{2d} + \frac{a^2(2a^2-b^2) \operatorname{Sin}[c+dx]}{2d} + \frac{b^2(a+b \operatorname{Sec}[c+dx])^2 \operatorname{Sin}[c+dx]}{2d} + \frac{3ab^3 \operatorname{Tan}[c+dx]}{d}$$

Result (type 3, 280 leaves):

$$\frac{1}{4d} \operatorname{Sec}[c+dx]^2 \left( 8a^3bc + 8a^3bdx - 12a^2b^2 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] - b^4 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] + 12a^2b^2 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] + b^4 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] + b \operatorname{Cos}[2(c+dx)] \left( 8a^3(c+dx) - b(12a^2+b^2) \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] + b(12a^2+b^2) \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \right) + (a^4+2b^4) \operatorname{Sin}[c+dx] + 8ab^3 \operatorname{Sin}[2(c+dx)] + a^4 \operatorname{Sin}[3(c+dx)] \right)$$

**Problem 486: Result more than twice size of optimal antiderivative.**

$$\int (a+b \operatorname{Sec}[c+dx])^5 dx$$

Optimal (type 3, 158 leaves, 7 steps):

$$a^5 x + \frac{b (40 a^4 + 40 a^2 b^2 + 3 b^4) \operatorname{ArcTanh}[\operatorname{Sin}[c + d x]]}{8 d} +$$

$$\frac{a b^2 (53 a^2 + 20 b^2) \operatorname{Tan}[c + d x]}{6 d} + \frac{b^3 (58 a^2 + 9 b^2) \operatorname{Sec}[c + d x] \operatorname{Tan}[c + d x]}{24 d} +$$

$$\frac{11 a b^2 (a + b \operatorname{Sec}[c + d x])^2 \operatorname{Tan}[c + d x]}{12 d} + \frac{b^2 (a + b \operatorname{Sec}[c + d x])^3 \operatorname{Tan}[c + d x]}{4 d}$$

Result (type 3, 855 leaves):

$$\frac{a^5 (c + d x) \operatorname{Cos}[c + d x]^5 (a + b \operatorname{Sec}[c + d x])^5}{d (b + a \operatorname{Cos}[c + d x])^5} +$$

$$\left( (-40 a^4 b - 40 a^2 b^3 - 3 b^5) \operatorname{Cos}[c + d x]^5 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] \right.$$

$$\left. (a + b \operatorname{Sec}[c + d x])^5 \right) / (8 d (b + a \operatorname{Cos}[c + d x])^5) +$$

$$\left( (40 a^4 b + 40 a^2 b^3 + 3 b^5) \operatorname{Cos}[c + d x]^5 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] \right.$$

$$\left. (a + b \operatorname{Sec}[c + d x])^5 \right) / (8 d (b + a \operatorname{Cos}[c + d x])^5) +$$

$$\frac{b^5 \operatorname{Cos}[c + d x]^5 (a + b \operatorname{Sec}[c + d x])^5}{16 d (b + a \operatorname{Cos}[c + d x])^5 \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^4} +$$

$$\frac{(120 a^2 b^3 + 20 a b^4 + 9 b^5) \operatorname{Cos}[c + d x]^5 (a + b \operatorname{Sec}[c + d x])^5}{48 d (b + a \operatorname{Cos}[c + d x])^5 \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^2} +$$

$$\frac{5 a b^4 \operatorname{Cos}[c + d x]^5 (a + b \operatorname{Sec}[c + d x])^5 \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]}{6 d (b + a \operatorname{Cos}[c + d x])^5 \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^3} -$$

$$\frac{b^5 \operatorname{Cos}[c + d x]^5 (a + b \operatorname{Sec}[c + d x])^5}{16 d (b + a \operatorname{Cos}[c + d x])^5 \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^4} +$$

$$\frac{5 a b^4 \operatorname{Cos}[c + d x]^5 (a + b \operatorname{Sec}[c + d x])^5 \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]}{6 d (b + a \operatorname{Cos}[c + d x])^5 \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^3} +$$

$$\frac{(-120 a^2 b^3 - 20 a b^4 - 9 b^5) \operatorname{Cos}[c + d x]^5 (a + b \operatorname{Sec}[c + d x])^5}{48 d (b + a \operatorname{Cos}[c + d x])^5 \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^2} +$$

$$\left( 10 \operatorname{Cos}[c + d x]^5 (a + b \operatorname{Sec}[c + d x])^5 \left( 3 a^3 b^2 \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] + a b^4 \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right) \right) /$$

$$\left( 3 d (b + a \operatorname{Cos}[c + d x])^5 \left( \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right) \right) +$$

$$\left( 10 \operatorname{Cos}[c + d x]^5 (a + b \operatorname{Sec}[c + d x])^5 \left( 3 a^3 b^2 \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] + a b^4 \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right) \right) /$$

$$\left( 3 d (b + a \operatorname{Cos}[c + d x])^5 \left( \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right) \right)$$



**Problem 505: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{\cos [c+d x]^3}{(a+b \sec [c+d x])^2} dx$$

Optimal (type 3, 261 leaves, 8 steps):

$$\begin{aligned} & -\frac{b\left(a^2+4 b^2\right) x}{a^5}+\frac{2 b^4\left(5 a^2-4 b^2\right) \operatorname{ArcTanh}\left[\frac{\sqrt{a-b} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{\sqrt{a+b}}\right]}{a^5(a-b)^{3 / 2}(a+b)^{3 / 2} d}+ \\ & \frac{\left(2 a^4+7 a^2 b^2-12 b^4\right) \operatorname{Sin}[c+d x]}{3 a^4\left(a^2-b^2\right) d}-\frac{b\left(a^2-2 b^2\right) \operatorname{Cos}[c+d x] \operatorname{Sin}[c+d x]}{a^3\left(a^2-b^2\right) d}+ \\ & \frac{\left(a^2-4 b^2\right) \operatorname{Cos}[c+d x]^2 \operatorname{Sin}[c+d x]}{3 a^2\left(a^2-b^2\right) d}+\frac{b^2 \operatorname{Cos}[c+d x]^2 \operatorname{Sin}[c+d x]}{a\left(a^2-b^2\right) d(a+b \sec [c+d x])} \end{aligned}$$

Result (type 3, 176 leaves):

$$\begin{aligned} & \frac{1}{12 a^5 d}\left(-12 b(-i a+2 b)(i a+2 b)(c+d x)+\right. \\ & \frac{24 b^4\left(-5 a^2+4 b^2\right) \operatorname{ArcTanh}\left[\frac{(-a+b) \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{\sqrt{a^2-b^2}}\right]}{\left(a^2-b^2\right)^{3 / 2}}+9 a\left(a^2+4 b^2\right) \operatorname{Sin}[c+d x]+ \\ & \left.\frac{12 a b^5 \operatorname{Sin}[c+d x]}{(-a+b)(a+b)(b+a \operatorname{Cos}[c+d x])}-6 a^2 b \operatorname{Sin}[2(c+d x)]+a^3 \operatorname{Sin}[3(c+d x)]\right) \end{aligned}$$

**Problem 529: Result more than twice size of optimal antiderivative.**

$$\int \frac{1}{(5+3 \sec [c+d x])^3} dx$$

Optimal (type 3, 120 leaves, 6 steps):

$$\begin{aligned} & \frac{x}{125}+\frac{8361 \operatorname{Log}\left[2 \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]-\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right]}{256000 d}- \\ & \frac{8361 \operatorname{Log}\left[2 \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right]}{256000 d}+ \\ & \frac{9 \operatorname{Tan}[c+d x]}{160 d(5+3 \sec [c+d x])^2}+\frac{963 \operatorname{Tan}[c+d x]}{12800 d(5+3 \sec [c+d x])} \end{aligned}$$

Result (type 3, 241 leaves):

$$\frac{1}{512000 d (3 + 5 \cos [c + d x])^2} \left( 88064 c + 88064 d x + 359523 \log \left[ 2 \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right] + 60 \cos [c + d x] \left( 2048 (c + d x) + 8361 \log \left[ 2 \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right] - 8361 \log \left[ 2 \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right] + 25 \cos [2 (c + d x)] \left( 2048 (c + d x) + 8361 \log \left[ 2 \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right] - 8361 \log \left[ 2 \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right] \right) - 359523 \log \left[ 2 \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right] + 115560 \sin [c + d x] + 110700 \sin [2 (c + d x)] \right)$$

**Problem 530: Result more than twice size of optimal antiderivative.**

$$\int \frac{1}{(5 + 3 \sec [c + d x])^4} dx$$

Optimal (type 3, 145 leaves, 7 steps):

$$\frac{x}{625} + \frac{278151 \log \left[ 2 \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right]}{20480000 d} - \frac{278151 \log \left[ 2 \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right]}{20480000 d} + \frac{3 \tan [c + d x]}{80 d (5 + 3 \sec [c + d x])^3} + \frac{519 \tan [c + d x]}{12800 d (5 + 3 \sec [c + d x])^2} + \frac{38733 \tan [c + d x]}{1024000 d (5 + 3 \sec [c + d x])}$$

Result (type 3, 344 leaves):

$$\frac{1}{81920000 d (3 + 5 \cos [c + d x])^3} \left( \begin{aligned} &18284544 c + 18284544 d x + 4096000 c \cos [3 (c + d x)] + 4096000 d x \cos [3 (c + d x)] + \\ &155208258 \log \left[ 2 \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right] + \\ &34768875 \cos [3 (c + d x)] \log \left[ 2 \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right] + \\ &915 \cos [c + d x] \left( 32768 (c + d x) + 278151 \log \left[ 2 \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right] - \right. \\ &\quad \left. 278151 \log \left[ 2 \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right] \right) + \\ &450 \cos [2 (c + d x)] \left( 32768 (c + d x) + 278151 \log \left[ 2 \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right] - \right. \\ &\quad \left. 278151 \log \left[ 2 \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right] \right) - \\ &155208258 \log \left[ 2 \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right] - \\ &34768875 \cos [3 (c + d x)] \log \left[ 2 \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right] + \\ &52174260 \sin [c + d x] + 51462000 \sin [2 (c + d x)] + 24286500 \sin [3 (c + d x)] \end{aligned} \right)$$

### Problem 531: Unable to integrate problem.

$$\int \sec [c + d x]^3 \sqrt{a + b \sec [c + d x]} dx$$

Optimal (type 4, 292 leaves, 5 steps):

$$\begin{aligned} &\frac{1}{15 b^3 d} 2 (a - b) \sqrt{a + b} (2 a^2 - 9 b^2) \cot [c + d x] \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{a + b \sec [c + d x]}}{\sqrt{a + b}} \right], \frac{a + b}{a - b} \right] \\ &\sqrt{\frac{b (1 - \sec [c + d x])}{a + b}} \sqrt{-\frac{b (1 + \sec [c + d x])}{a - b}} + \frac{1}{15 b^2 d} \\ &2 (a - b) \sqrt{a + b} (2 a + 9 b) \cot [c + d x] \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{a + b \sec [c + d x]}}{\sqrt{a + b}} \right], \frac{a + b}{a - b} \right] \\ &\sqrt{\frac{b (1 - \sec [c + d x])}{a + b}} \sqrt{-\frac{b (1 + \sec [c + d x])}{a - b}} - \\ &\frac{4 a \sqrt{a + b \sec [c + d x]} \tan [c + d x]}{15 b d} + \frac{2 (a + b \sec [c + d x])^{3/2} \tan [c + d x]}{5 b d} \end{aligned}$$

Result (type 8, 25 leaves):

$$\int \sec [c + d x]^3 \sqrt{a + b \sec [c + d x]} dx$$

### Problem 532: Unable to integrate problem.

$$\int \sec [c+d x]^2 \sqrt{a+b \sec [c+d x]} d x$$

Optimal (type 4, 241 leaves, 4 steps):

$$-\frac{1}{3 b^2 d} 2 a(a-b) \sqrt{a+b} \cot [c+d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} - \frac{1}{3 b d}$$

$$2(a-b) \sqrt{a+b} \cot [c+d x] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} + \frac{2 \sqrt{a+b \sec [c+d x]} \tan [c+d x]}{3 d}$$

Result (type 8, 25 leaves):

$$\int \sec [c+d x]^2 \sqrt{a+b \sec [c+d x]} d x$$

### Problem 534: Unable to integrate problem.

$$\int \sqrt{a+b \sec [c+d x]} d x$$

Optimal (type 4, 125 leaves, 1 step):

$$-\frac{1}{\sqrt{a+b} d} 2 \cot [c+d x] \operatorname{EllipticPi}\left[\frac{a}{a+b}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b}}{\sqrt{a+b \sec [c+d x]}}\right], \frac{a-b}{a+b}\right]$$

$$\sqrt{-\frac{b(1-\sec [c+d x])}{a+b \sec [c+d x]}} \sqrt{\frac{b(1+\sec [c+d x])}{a+b \sec [c+d x]}} (a+b \sec [c+d x])$$

Result (type 8, 16 leaves):

$$\int \sqrt{a+b \sec [c+d x]} d x$$

### Problem 535: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \cos [c+d x] \sqrt{a+b \sec [c+d x]} d x$$

Optimal (type 4, 330 leaves, 6 steps):

$$\frac{1}{bd} (a-b) \sqrt{a+b} \cot[c+dx] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\operatorname{Sec}[c+dx])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+dx])}{a-b}} + \frac{1}{d} \sqrt{a+b} \cot[c+dx]$$

$$\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+dx])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+dx])}{a-b}}$$

$$\frac{1}{ad} b \sqrt{a+b} \cot[c+dx] \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\operatorname{Sec}[c+dx])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+dx])}{a-b}} + \frac{\sqrt{a+b \operatorname{Sec}[c+dx]} \sin[c+dx]}{d}$$

Result(type 4, 2713 leaves):

$$\left( \cos[c+dx] \sqrt{\cos\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Sec}[c+dx]} \sqrt{a+b \operatorname{Sec}[c+dx]} \right.$$

$$\left( i(a-b) \operatorname{EllipticE}\left[ i \operatorname{ArcSinh}\left[ \sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right] \right], \frac{a+b}{a-b} \right] \right.$$

$$\left. \sqrt{\frac{(b+a \cos[c+dx]) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + 2 i b \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, \right.$$

$$\left. i \operatorname{ArcSinh}\left[ \sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right] \right], \frac{a+b}{a-b} \right] \sqrt{\frac{(b+a \cos[c+dx]) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \right.$$

$$\left. \sqrt{2} \sqrt{\frac{-a+b}{a+b}} \sqrt{\frac{\cos[c+dx]}{1+\cos[c+dx]}} (b+a \cos[c+dx]) \tan\left[\frac{1}{2}(c+dx)\right] \right)$$

$$\left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \left/ \left( \sqrt{\frac{-a+b}{a+b}} d \sqrt{b+a \cos[c+dx]} \right. \right.$$

$$\left. \sqrt{\cos[c+dx] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^4} \right)$$

$$\left( \frac{1}{\sqrt{\frac{-a+b}{a+b}} \sqrt{b+a \cos [c+d x]} \sqrt{\cos [c+d x] \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]}^4} \right.$$

$$\operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \sqrt{\cos\left[\frac{1}{2}(c+d x)\right]^2 \operatorname{Sec}[c+d x] \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}$$

$$\left( i (a-b) \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a+b}{a-b}\right] \right.$$

$$\sqrt{\frac{(b+a \cos [c+d x]) \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} + 2 i b \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a+b}{a-b}\right]$$

$$\left. \sqrt{\frac{(b+a \cos [c+d x]) \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} - \sqrt{2} \sqrt{\frac{-a+b}{a+b}} \sqrt{\frac{\cos [c+d x]}{1+\cos [c+d x]}} (b+a \cos [c+d x]) \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] \right) +$$

$$\frac{1}{2 \sqrt{\frac{-a+b}{a+b}} (b+a \cos [c+d x])^{3/2} \sqrt{\cos [c+d x] \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]}^4}$$

$$a \sqrt{\cos\left[\frac{1}{2}(c+d x)\right]^2 \operatorname{Sec}[c+d x] \operatorname{Sin}[c+d x]}$$

$$\left( i (a-b) \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a+b}{a-b}\right] \right.$$

$$\sqrt{\frac{(b+a \cos [c+d x]) \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} +$$

$$2 i b \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a+b}{a-b}\right]$$

$$\left. \sqrt{\frac{(b+a \cos [c+d x]) \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} - \sqrt{2} \sqrt{\frac{-a+b}{a+b}} \sqrt{\frac{\cos [c+d x]}{1+\cos [c+d x]}} \right)$$

$$\begin{aligned}
 & \left. (b + a \cos [c + d x]) \tan \left[ \frac{1}{2} (c + d x) \right] \right) \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) - \\
 & \frac{1}{2 \sqrt{\frac{-a+b}{a+b}} \sqrt{b + a \cos [c + d x]} \left( \cos [c + d x] \sec \left[ \frac{1}{2} (c + d x) \right]^4 \right)^{3/2}} \\
 & \sqrt{\cos \left[ \frac{1}{2} (c + d x) \right]^2 \sec [c + d x]} \\
 & \left( i (a - b) \operatorname{EllipticE} \left[ i \operatorname{ArcSinh} \left[ \sqrt{\frac{-a+b}{a+b}} \tan \left[ \frac{1}{2} (c + d x) \right] \right], \frac{a+b}{a-b} \right] \right. \\
 & \left. \sqrt{\frac{(b + a \cos [c + d x]) \sec \left[ \frac{1}{2} (c + d x) \right]^2}{a+b}} + 2 i b \operatorname{EllipticPi} \left[ -\frac{a+b}{a-b}, i \operatorname{ArcSinh} \left[ \right. \right. \right. \\
 & \left. \left. \left. \sqrt{\frac{-a+b}{a+b}} \tan \left[ \frac{1}{2} (c + d x) \right] \right], \frac{a+b}{a-b} \right] \sqrt{\frac{(b + a \cos [c + d x]) \sec \left[ \frac{1}{2} (c + d x) \right]^2}{a+b}} - \right. \right. \\
 & \left. \left. \sqrt{2} \sqrt{\frac{-a+b}{a+b}} \sqrt{\frac{\cos [c + d x]}{1 + \cos [c + d x]}} (b + a \cos [c + d x]) \tan \left[ \frac{1}{2} (c + d x) \right] \right) \right) \\
 & \left( -\sec \left[ \frac{1}{2} (c + d x) \right]^4 \sin [c + d x] + 2 \cos [c + d x] \sec \left[ \frac{1}{2} (c + d x) \right]^4 \tan \left[ \frac{1}{2} (c + d x) \right] \right) \\
 & \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) + \\
 & \frac{1}{\sqrt{\frac{-a+b}{a+b}} \sqrt{b + a \cos [c + d x]} \sqrt{\cos [c + d x] \sec \left[ \frac{1}{2} (c + d x) \right]^4}} \\
 & \sqrt{\cos \left[ \frac{1}{2} (c + d x) \right]^2 \sec [c + d x] \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right)} \\
 & \left( -\frac{\sqrt{\frac{-a+b}{a+b}} \sqrt{\frac{\cos [c + d x]}{1 + \cos [c + d x]}} (b + a \cos [c + d x]) \sec \left[ \frac{1}{2} (c + d x) \right]^2}{\sqrt{2}} + \right. \\
 & \left. \sqrt{2} a \sqrt{\frac{-a+b}{a+b}} \sqrt{\frac{\cos [c + d x]}{1 + \cos [c + d x]}} \sin [c + d x] \tan \left[ \frac{1}{2} (c + d x) \right] - \right)
 \end{aligned}$$

$$\begin{aligned}
& \left( \sqrt{\frac{-a+b}{a+b}} (b+a \cos [c+d x]) \left( \frac{\cos [c+d x] \sin [c+d x]}{(1+\cos [c+d x])^2} - \frac{\sin [c+d x]}{1+\cos [c+d x]} \right) \right. \\
& \quad \left. \tan \left[ \frac{1}{2} (c+d x) \right] \right) / \left( \sqrt{2} \sqrt{\frac{\cos [c+d x]}{1+\cos [c+d x]}} \right) + \\
& \left( i (a-b) \operatorname{EllipticE} \left[ i \operatorname{ArcSinh} \left[ \sqrt{\frac{-a+b}{a+b}} \tan \left[ \frac{1}{2} (c+d x) \right] \right], \frac{a+b}{a-b} \right] \right. \\
& \quad \left( -\frac{a \sec \left[ \frac{1}{2} (c+d x) \right]^2 \sin [c+d x]}{a+b} + \frac{1}{a+b} (b+a \cos [c+d x]) \sec \left[ \frac{1}{2} (c+d x) \right]^2 \right. \\
& \quad \left. \left. \tan \left[ \frac{1}{2} (c+d x) \right] \right) \right) / \left( 2 \sqrt{\frac{(b+a \cos [c+d x]) \sec \left[ \frac{1}{2} (c+d x) \right]^2}{a+b}} \right) + \\
& \left( i b \operatorname{EllipticPi} \left[ -\frac{a+b}{a-b}, i \operatorname{ArcSinh} \left[ \sqrt{\frac{-a+b}{a+b}} \tan \left[ \frac{1}{2} (c+d x) \right] \right], \frac{a+b}{a-b} \right] \right. \\
& \quad \left( -\frac{a \sec \left[ \frac{1}{2} (c+d x) \right]^2 \sin [c+d x]}{a+b} + \frac{1}{a+b} (b+a \cos [c+d x]) \sec \left[ \frac{1}{2} (c+d x) \right]^2 \right. \\
& \quad \left. \left. \tan \left[ \frac{1}{2} (c+d x) \right] \right) \right) / \left( \sqrt{\frac{(b+a \cos [c+d x]) \sec \left[ \frac{1}{2} (c+d x) \right]^2}{a+b}} \right) - \\
& \left( b \sqrt{\frac{-a+b}{a+b}} \sec \left[ \frac{1}{2} (c+d x) \right]^2 \sqrt{\frac{(b+a \cos [c+d x]) \sec \left[ \frac{1}{2} (c+d x) \right]^2}{a+b}} \right) / \\
& \left( \left( 1 - \frac{(-a+b) \tan \left[ \frac{1}{2} (c+d x) \right]^2}{a-b} \right) \sqrt{1 + \frac{(-a+b) \tan \left[ \frac{1}{2} (c+d x) \right]^2}{a-b}} \right. \\
& \quad \left. \sqrt{1 + \frac{(-a+b) \tan \left[ \frac{1}{2} (c+d x) \right]^2}{a+b}} \right) - \\
& \left( (a-b) \sqrt{\frac{-a+b}{a+b}} \sec \left[ \frac{1}{2} (c+d x) \right]^2 \sqrt{\frac{(b+a \cos [c+d x]) \sec \left[ \frac{1}{2} (c+d x) \right]^2}{a+b}} \right)
\end{aligned}$$



$$\begin{aligned}
 & \left( \sqrt{1 + \frac{(-a+b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a-b}} \right) / \left( 2 \sqrt{1 + \frac{(-a+b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \right) + \\
 & \left( \left( \operatorname{EllipticE}\left[ \operatorname{ArcSinh}\left[ \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right], \frac{a+b}{a-b} \right] \right. \right. \\
 & \quad \left. \sqrt{\frac{(b+a \operatorname{Cos}[c+dx]) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + 2 \operatorname{EllipticPi}\left[ -\frac{a+b}{a-b}, \operatorname{ArcSinh}\left[ \right. \right. \right. \\
 & \quad \left. \left. \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right], \frac{a+b}{a-b} \right] \sqrt{\frac{(b+a \operatorname{Cos}[c+dx]) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \right. \\
 & \quad \left. \sqrt{2} \sqrt{\frac{-a+b}{a+b}} \sqrt{\frac{\operatorname{Cos}[c+dx]}{1+\operatorname{Cos}[c+dx]}} (b+a \operatorname{Cos}[c+dx]) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \\
 & \quad \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( -\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] \operatorname{Sec}[c+dx] \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \quad \left. \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Sec}[c+dx] \operatorname{Tan}[c+dx] \right) \left. \right) / \\
 & \left( 2 \sqrt{\frac{-a+b}{a+b}} \sqrt{b+a \operatorname{Cos}[c+dx]} \sqrt{\operatorname{Cos}[c+dx] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^4} \right. \\
 & \quad \left. \left. \left. \sqrt{\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Sec}[c+dx]} \right) \right) \right)
 \end{aligned}$$

**Problem 536: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \operatorname{Cos}[c+dx]^2 \sqrt{a+b \operatorname{Sec}[c+dx]} \, dx$$

Optimal (type 4, 396 leaves, 7 steps):

$$\begin{aligned} & \frac{1}{4 a d} (a-b) \sqrt{a+b} \operatorname{Cot}[c+d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\ & \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} + \frac{1}{4 a d} \sqrt{a+b} (2 a+b) \operatorname{Cot}[c+d x] \\ & \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} - \\ & \frac{1}{4 a^2 d} \sqrt{a+b} (4 a^2-b^2) \operatorname{Cot}[c+d x] \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\ & \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} + \\ & \frac{b \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{4 a d} + \frac{\operatorname{Cos}[c+d x] \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{2 d} \end{aligned}$$

Result (type 4, 1173 leaves):

$$\begin{aligned} & \frac{\sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Sin}[2(c+d x)]}{4 d} + \\ & \left( \sqrt{a+b \operatorname{Sec}[c+d x]} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}} \right. \\ & \left. \left( a b \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] + b^2 \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] - 2 a b \sqrt{\frac{-a+b}{a+b}} \right. \right. \\ & \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^3 + a b \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 - b^2 \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 - \right. \right. \\ & \left. \left. 8 i a^2 \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a+b}{a-b}\right] \right. \right. \\ & \left. \left. \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} + \right. \right. \\ & \left. \left. 2 i b^2 \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a+b}{a-b}\right] \right. \right. \\ & \left. \left. \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} - \right. \right. \end{aligned}$$

$$\begin{aligned}
 & 8 i a^2 \text{EllipticPi}\left[-\frac{a+b}{a-b}, i \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
 & 2 i b^2 \text{EllipticPi}\left[-\frac{a+b}{a-b}, i \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 & i (a-b) b \text{EllipticE}\left[i \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \\
 & \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
 & 2 i (2a^2 - ab - b^2) \text{EllipticF}\left[i \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \\
 & \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \Bigg) \Bigg/ \\
 & \left(4 a \sqrt{\frac{-a+b}{a+b}} d \sqrt{b+a \cos[c+dx]} \sqrt{\sec[c+dx]} \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \right. \\
 & \left. \sqrt{\frac{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2}} \right. \\
 & \left. \left(a \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) - b \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)\right) \right)
 \end{aligned}$$

Problem 537: Unable to integrate problem.

$$\int \text{Sec}[c + dx]^4 (a + b \text{Sec}[c + dx])^{3/2} dx$$

Optimal (type 4, 405 leaves, 7 steps):

$$\begin{aligned} & -\frac{1}{315 b^4 d} 2 (a - b) \sqrt{a + b} (8 a^4 + 33 a^2 b^2 + 147 b^4) \text{Cot}[c + dx] \text{EllipticE}\left[ \right. \\ & \quad \left. \text{ArcSin}\left[\frac{\sqrt{a + b \text{Sec}[c + dx]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \sqrt{\frac{b(1 - \text{Sec}[c + dx])}{a + b}} \sqrt{-\frac{b(1 + \text{Sec}[c + dx])}{a - b}} - \\ & \frac{1}{315 b^3 d} 2 (a - b) \sqrt{a + b} (8 a^3 + 6 a^2 b + 39 a b^2 - 147 b^3) \text{Cot}[c + dx] \\ & \quad \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{a + b \text{Sec}[c + dx]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \sqrt{\frac{b(1 - \text{Sec}[c + dx])}{a + b}} \sqrt{-\frac{b(1 + \text{Sec}[c + dx])}{a - b}} + \\ & \frac{2 a (8 a^2 + 39 b^2) \sqrt{a + b \text{Sec}[c + dx]} \text{Tan}[c + dx]}{315 b^2 d} + \\ & \frac{2 (8 a^2 + 49 b^2) (a + b \text{Sec}[c + dx])^{3/2} \text{Tan}[c + dx]}{315 b^2 d} - \\ & \frac{8 a (a + b \text{Sec}[c + dx])^{5/2} \text{Tan}[c + dx]}{63 b^2 d} + \frac{2 \text{Sec}[c + dx] (a + b \text{Sec}[c + dx])^{5/2} \text{Tan}[c + dx]}{9 b d} \end{aligned}$$

Result (type 8, 25 leaves):

$$\int \text{Sec}[c + dx]^4 (a + b \text{Sec}[c + dx])^{3/2} dx$$

**Problem 538: Unable to integrate problem.**

$$\int \text{Sec}[c + dx]^3 (a + b \text{Sec}[c + dx])^{3/2} dx$$

Optimal (type 4, 342 leaves, 6 steps):

$$\begin{aligned} & \frac{1}{105 b^3 d} 4 a (a - b) \sqrt{a + b} (3 a^2 - 41 b^2) \text{Cot}[c + dx] \\ & \quad \text{EllipticE}\left[\text{ArcSin}\left[\frac{\sqrt{a + b \text{Sec}[c + dx]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \sqrt{\frac{b(1 - \text{Sec}[c + dx])}{a + b}} \sqrt{-\frac{b(1 + \text{Sec}[c + dx])}{a - b}} + \\ & \frac{1}{105 b^2 d} 2 (a - b) \sqrt{a + b} (6 a^2 + 57 a b - 25 b^2) \text{Cot}[c + dx] \\ & \quad \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{a + b \text{Sec}[c + dx]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \sqrt{\frac{b(1 - \text{Sec}[c + dx])}{a + b}} \sqrt{-\frac{b(1 + \text{Sec}[c + dx])}{a - b}} - \\ & \frac{2 (6 a^2 - 25 b^2) \sqrt{a + b \text{Sec}[c + dx]} \text{Tan}[c + dx]}{105 b d} - \frac{4 a (a + b \text{Sec}[c + dx])^{3/2} \text{Tan}[c + dx]}{35 b d} + \\ & \frac{2 (a + b \text{Sec}[c + dx])^{5/2} \text{Tan}[c + dx]}{7 b d} \end{aligned}$$

Result (type 8, 25 leaves):

$$\int \operatorname{Sec}[c + d x]^3 (a + b \operatorname{Sec}[c + d x])^{3/2} dx$$

**Problem 539: Unable to integrate problem.**

$$\int \operatorname{Sec}[c + d x]^2 (a + b \operatorname{Sec}[c + d x])^{3/2} dx$$

Optimal (type 4, 282 leaves, 5 steps):

$$\begin{aligned}
 & -\frac{1}{5 b^2 d} 2 (a - b) \sqrt{a + b} (a^2 + 3 b^2) \operatorname{Cot}[c + d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a + b \operatorname{Sec}[c + d x]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \\
 & \sqrt{\frac{b(1 - \operatorname{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b(1 + \operatorname{Sec}[c + d x])}{a - b}} - \frac{1}{5 b d} \\
 & 2 (a - 3 b) (a - b) \sqrt{a + b} \operatorname{Cot}[c + d x] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a + b \operatorname{Sec}[c + d x]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \\
 & \sqrt{\frac{b(1 - \operatorname{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b(1 + \operatorname{Sec}[c + d x])}{a - b}} + \\
 & \frac{2 a \sqrt{a + b \operatorname{Sec}[c + d x]} \operatorname{Tan}[c + d x]}{5 d} + \frac{2 (a + b \operatorname{Sec}[c + d x])^{3/2} \operatorname{Tan}[c + d x]}{5 d}
 \end{aligned}$$

Result (type 8, 25 leaves):

$$\int \operatorname{Sec}[c + d x]^2 (a + b \operatorname{Sec}[c + d x])^{3/2} dx$$

**Problem 540: Attempted integration timed out after 120 seconds.**

$$\int \operatorname{Sec}[c + d x] (a + b \operatorname{Sec}[c + d x])^{3/2} dx$$

Optimal (type 4, 249 leaves, 4 steps):

$$\begin{aligned}
 & -\frac{1}{3 b d} 8 a (a - b) \sqrt{a + b} \operatorname{Cot}[c + d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a + b \operatorname{Sec}[c + d x]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \\
 & \sqrt{\frac{b(1 - \operatorname{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b(1 + \operatorname{Sec}[c + d x])}{a - b}} + \frac{1}{3 b d} \\
 & 2 (a - b) (3 a - b) \sqrt{a + b} \operatorname{Cot}[c + d x] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a + b \operatorname{Sec}[c + d x]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \\
 & \sqrt{\frac{b(1 - \operatorname{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b(1 + \operatorname{Sec}[c + d x])}{a - b}} + \frac{2 b \sqrt{a + b \operatorname{Sec}[c + d x]} \operatorname{Tan}[c + d x]}{3 d}
 \end{aligned}$$

Result (type 1, 1 leaves):

???

**Problem 541: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int (a + b \sec [c + d x])^{3/2} dx$$

Optimal (type 4, 309 leaves, 5 steps):

$$-\frac{1}{d} 2 (a - b) \sqrt{a + b} \cot [c + d x] \text{EllipticE} \left[ \text{ArcSin} \left[ \frac{\sqrt{a + b \sec [c + d x]}}{\sqrt{a + b}} \right], \frac{a + b}{a - b} \right]$$

$$\sqrt{\frac{b (1 - \sec [c + d x])}{a + b}} \sqrt{-\frac{b (1 + \sec [c + d x])}{a - b}} + \frac{1}{d}$$

$$2 (2 a - b) \sqrt{a + b} \cot [c + d x] \text{EllipticF} \left[ \text{ArcSin} \left[ \frac{\sqrt{a + b \sec [c + d x]}}{\sqrt{a + b}} \right], \frac{a + b}{a - b} \right]$$

$$\sqrt{\frac{b (1 - \sec [c + d x])}{a + b}} \sqrt{-\frac{b (1 + \sec [c + d x])}{a - b}} - \frac{1}{d}$$

$$2 a \sqrt{a + b} \cot [c + d x] \text{EllipticPi} \left[ \frac{a + b}{a}, \text{ArcSin} \left[ \frac{\sqrt{a + b \sec [c + d x]}}{\sqrt{a + b}} \right], \frac{a + b}{a - b} \right]$$

$$\sqrt{\frac{b (1 - \sec [c + d x])}{a + b}} \sqrt{-\frac{b (1 + \sec [c + d x])}{a - b}}$$

Result (type 4, 882 leaves):

$$\frac{2 b \cos [c + d x] (a + b \sec [c + d x])^{3/2} \sin [c + d x]}{d (b + a \cos [c + d x])} +$$

$$\left( 2 (a + b \sec [c + d x])^{3/2} \left( a b \sqrt{\frac{-a + b}{a + b}} \tan \left[ \frac{1}{2} (c + d x) \right] + \right. \right.$$

$$b^2 \sqrt{\frac{-a + b}{a + b}} \tan \left[ \frac{1}{2} (c + d x) \right] - 2 a b \sqrt{\frac{-a + b}{a + b}} \tan \left[ \frac{1}{2} (c + d x) \right]^3 +$$

$$a b \sqrt{\frac{-a + b}{a + b}} \tan \left[ \frac{1}{2} (c + d x) \right]^5 - b^2 \sqrt{\frac{-a + b}{a + b}} \tan \left[ \frac{1}{2} (c + d x) \right]^5 +$$

$$\left. \left. 2 i a^2 \text{EllipticPi} \left[ -\frac{a + b}{a - b}, i \text{ArcSinh} \left[ \sqrt{\frac{-a + b}{a + b}} \tan \left[ \frac{1}{2} (c + d x) \right] \right], \frac{a + b}{a - b} \right] \right)$$

$$\begin{aligned}
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
 & 2i a^2 \text{EllipticPi}\left[-\frac{a+b}{a-b}, i \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 & i(a-b)b \text{EllipticE}\left[i \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \\
 & \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 & i(a-b)^2 \text{EllipticF}\left[i \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \\
 & \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \right) \Bigg) \Bigg/ \\
 & \left( \sqrt{\frac{-a+b}{a+b}} d (b+a \cos[c+dx])^{3/2} \sec[c+dx]^{3/2} \sqrt{\frac{1}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2}} \right. \\
 & \left. \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^{3/2} \right. \\
 & \left. \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}} \right)
 \end{aligned}$$

**Problem 542: Result unnecessarily involves imaginary or complex numbers.**

$$\int \cos[c+dx] (a+b \sec[c+dx])^{3/2} dx$$

Optimal (type 4, 334 leaves, 6 steps):

$$\frac{1}{bd} a (a-b) \sqrt{a+b} \cot[c+dx] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\operatorname{Sec}[c+dx])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+dx])}{a-b}} + \frac{1}{d} \sqrt{a+b} (a+2b) \cot[c+dx]$$

$$\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+dx])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+dx])}{a-b}}$$

$$\frac{1}{d} 3b \sqrt{a+b} \cot[c+dx] \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\operatorname{Sec}[c+dx])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+dx])}{a-b}} + \frac{a \sqrt{a+b \operatorname{Sec}[c+dx]} \sin[c+dx]}{d}$$

Result(type 4, 642 leaves):



$$\begin{aligned}
 & \left( (a + b \operatorname{Sec}[c + dx])^{3/2} \sqrt{\frac{a + b - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2}} \right. \\
 & \left( -i a (a - b) \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{-a + b}{a + b}} \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]\right], \frac{a + b}{a - b}\right] \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2} \right. \\
 & \left. \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2\right) \sqrt{\frac{a + b - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2}{a + b}} + 2i (a - b) \right. \\
 & b \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{-a + b}{a + b}} \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]\right], \frac{a + b}{a - b}\right] \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2} \\
 & \left. \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2\right) \sqrt{\frac{a + b - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2}{a + b}} - 6i a b \right. \\
 & \operatorname{EllipticPi}\left[-\frac{a + b}{a - b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a + b}{a + b}} \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]\right], \frac{a + b}{a - b}\right] \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2} \\
 & \left. \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2\right) \sqrt{\frac{a + b - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2}{a + b}} + \right. \\
 & \left. \left. a \sqrt{\frac{-a + b}{a + b}} \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right] \left( b - b \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^4 + a \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2 \right)^2 \right) \right) \right) / \\
 & \left( \sqrt{\frac{-a + b}{a + b}} d (b + a \operatorname{Cos}[c + dx])^{3/2} \operatorname{Sec}[c + dx]^{3/2} \sqrt{\frac{1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2}{1 - \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2}} \right. \\
 & \left. \left( b - b \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^4 + a \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2 \right)^2 \right) \right)
 \end{aligned}$$

**Problem 543: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \operatorname{Cos}[c + dx]^2 (a + b \operatorname{Sec}[c + dx])^{3/2} dx$$

Optimal (type 4, 390 leaves, 7 steps):

$$\frac{1}{4d} 5 (a-b) \sqrt{a+b} \operatorname{Cot}[c+dx] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\operatorname{Sec}[c+dx])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+dx])}{a-b}} + \frac{1}{4d} \sqrt{a+b} (2a+5b) \operatorname{Cot}[c+dx]$$

$$\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+dx])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+dx])}{a-b}}$$

$$\frac{1}{4ad} \sqrt{a+b} (4a^2+3b^2) \operatorname{Cot}[c+dx] \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\operatorname{Sec}[c+dx])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+dx])}{a-b}} +$$

$$\frac{5b \sqrt{a+b \operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]}{4d} + \frac{a \operatorname{Cos}[c+dx] \sqrt{a+b \operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]}{2d}$$

Result (type 4, 1159 leaves):

$$\frac{a \operatorname{Cos}[c+dx] (a+b \operatorname{Sec}[c+dx])^{3/2} \operatorname{Sin}[2(c+dx)]}{4d (b+a \operatorname{Cos}[c+dx])}$$

$$\left( (a+b \operatorname{Sec}[c+dx])^{3/2} \left( 5ab \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \right.$$

$$5b^2 \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] - 10ab \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^3 +$$

$$5ab \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^5 - 5b^2 \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^5 -$$

$$8i a^2 \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}}$$

$$6i b^2 \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}}$$

$$\begin{aligned}
 & 8 \, i \, a^2 \operatorname{EllipticPi} \left[ -\frac{a+b}{a-b}, i \operatorname{ArcSinh} \left[ \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] \right], \frac{a+b}{a-b} \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right. \\
 & \left. \sqrt{1 - \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2} \sqrt{\frac{a+b - a \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 + b \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b}} \right] - \\
 & 6 \, i \, b^2 \operatorname{EllipticPi} \left[ -\frac{a+b}{a-b}, i \operatorname{ArcSinh} \left[ \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] \right], \frac{a+b}{a-b} \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right. \\
 & \left. \sqrt{1 - \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2} \sqrt{\frac{a+b - a \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 + b \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b}} \right] - \\
 & 5 \, i \, (a-b) \, b \operatorname{EllipticE} \left[ i \operatorname{ArcSinh} \left[ \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] \right], \frac{a+b}{a-b} \right] \\
 & \sqrt{1 - \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2} \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \\
 & \sqrt{\frac{a+b - a \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 + b \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b}} + 2 \, i \, (2a^2 - ab - b^2) \\
 & \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] \right], \frac{a+b}{a-b} \right] \sqrt{1 - \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2} \\
 & \left. \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \sqrt{\frac{a+b - a \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 + b \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b}} \right) \right) / \\
 & \left( 4 \sqrt{\frac{-a+b}{a+b}} d (b + a \operatorname{Cos} [c+dx])^{3/2} \operatorname{Sec} [c+dx]^{3/2} \sqrt{\frac{1}{1 - \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}} \right. \\
 & \left. \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right)^{3/2} \right. \\
 & \left. \sqrt{\frac{a+b - a \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 + b \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}} \right)
 \end{aligned}$$

Problem 544: Attempted integration timed out after 120 seconds.

$$\int \operatorname{Sec} [c+dx]^4 (a+b \operatorname{Sec} [c+dx])^{5/2} dx$$

Optimal (type 4, 463 leaves, 8 steps):

$$\begin{aligned}
 & -\frac{1}{693 b^4 d} 2 a (a-b) \sqrt{a+b} (8 a^4 + 51 a^2 b^2 + 741 b^4) \operatorname{Cot}[c+d x] \operatorname{EllipticE}\left[ \right. \\
 & \quad \left. \operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} - \\
 & \frac{1}{693 b^3 d} 2 (a-b) \sqrt{a+b} (8 a^4 + 6 a^3 b + 57 a^2 b^2 - 606 a b^3 + 135 b^4) \operatorname{Cot}[c+d x] \\
 & \quad \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} + \\
 & \frac{2(8 a^4 + 57 a^2 b^2 + 135 b^4) \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Tan}[c+d x]}{693 b^2 d} + \\
 & \frac{2 a (8 a^2 + 67 b^2) (a+b \operatorname{Sec}[c+d x])^{3/2} \operatorname{Tan}[c+d x]}{693 b^2 d} + \\
 & \frac{2(8 a^2 + 81 b^2) (a+b \operatorname{Sec}[c+d x])^{5/2} \operatorname{Tan}[c+d x]}{693 b^2 d} - \\
 & \frac{8 a (a+b \operatorname{Sec}[c+d x])^{7/2} \operatorname{Tan}[c+d x]}{99 b^2 d} + \frac{2 \operatorname{Sec}[c+d x] (a+b \operatorname{Sec}[c+d x])^{7/2} \operatorname{Tan}[c+d x]}{11 b d}
 \end{aligned}$$

Result (type 1, 1 leaves):

???

**Problem 545: Attempted integration timed out after 120 seconds.**

$$\int \operatorname{Sec}[c+d x]^3 (a+b \operatorname{Sec}[c+d x])^{5/2} dx$$

Optimal (type 4, 399 leaves, 7 steps):

$$\frac{1}{315 b^3 d} 2 (a-b) \sqrt{a+b} (10 a^4 - 279 a^2 b^2 - 147 b^4) \operatorname{Cot}[c+d x]$$

$$\operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} +$$

$$\frac{1}{315 b^2 d} 2 (a-b) \sqrt{a+b} (10 a^3 + 165 a^2 b - 114 a b^2 + 147 b^3) \operatorname{Cot}[c+d x]$$

$$\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} -$$

$$\frac{4 a (5 a^2 - 57 b^2) \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Tan}[c+d x]}{315 b d} -$$

$$\frac{2 (10 a^2 - 49 b^2) (a+b \operatorname{Sec}[c+d x])^{3/2} \operatorname{Tan}[c+d x]}{315 b d} -$$

$$\frac{4 a (a+b \operatorname{Sec}[c+d x])^{5/2} \operatorname{Tan}[c+d x]}{63 b d} + \frac{2 (a+b \operatorname{Sec}[c+d x])^{7/2} \operatorname{Tan}[c+d x]}{9 b d}$$

Result(type 1, 1 leaves):

???

**Problem 546: Attempted integration timed out after 120 seconds.**

$$\int \operatorname{Sec}[c+d x]^2 (a+b \operatorname{Sec}[c+d x])^{5/2} dx$$

Optimal (type 4, 333 leaves, 6 steps):

$$-\frac{1}{21 b^2 d}$$

$$2 a (a-b) \sqrt{a+b} (3 a^2 + 29 b^2) \operatorname{Cot}[c+d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} - \frac{1}{21 b d}$$

$$2 (a-b) \sqrt{a+b} (3 a^2 - 24 a b + 5 b^2) \operatorname{Cot}[c+d x] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} + \frac{2 (3 a^2 + 5 b^2) \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Tan}[c+d x]}{21 d} +$$

$$\frac{2 a (a+b \operatorname{Sec}[c+d x])^{3/2} \operatorname{Tan}[c+d x]}{7 d} + \frac{2 (a+b \operatorname{Sec}[c+d x])^{5/2} \operatorname{Tan}[c+d x]}{7 d}$$

Result(type 1, 1 leaves):

???

### Problem 547: Attempted integration timed out after 120 seconds.

$$\int \sec [c + d x] (a + b \sec [c + d x])^{5/2} dx$$

Optimal (type 4, 296 leaves, 5 steps):

$$-\frac{1}{15 b d} 2 (a - b) \sqrt{a + b} (23 a^2 + 9 b^2) \cot [c + d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a + b \sec [c + d x]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right]$$

$$\sqrt{\frac{b (1 - \sec [c + d x])}{a + b}} \sqrt{-\frac{b (1 + \sec [c + d x])}{a - b}} + \frac{1}{15 b d}$$

$$2 (a - b) \sqrt{a + b} (15 a^2 - 8 a b + 9 b^2) \cot [c + d x] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a + b \sec [c + d x]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right]$$

$$\sqrt{\frac{b (1 - \sec [c + d x])}{a + b}} \sqrt{-\frac{b (1 + \sec [c + d x])}{a - b}} +$$

$$\frac{16 a b \sqrt{a + b \sec [c + d x]} \tan [c + d x]}{15 d} + \frac{2 b (a + b \sec [c + d x])^{3/2} \tan [c + d x]}{5 d}$$

Result (type 1, 1 leaves):

???

### Problem 548: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int (a + b \sec [c + d x])^{5/2} dx$$

Optimal (type 4, 352 leaves, 6 steps):

$$\begin{aligned}
 & -\frac{1}{3d} 14 a (a-b) \sqrt{a+b} \operatorname{Cot}[c+dx] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{\frac{b(1-\operatorname{Sec}[c+dx])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+dx])}{a-b}} + \frac{1}{3d} \\
 & 2\sqrt{a+b} (9a^2 - 7ab + b^2) \operatorname{Cot}[c+dx] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{\frac{b(1-\operatorname{Sec}[c+dx])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+dx])}{a-b}} - \frac{1}{d} \\
 & 2a^2 \sqrt{a+b} \operatorname{Cot}[c+dx] \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{\frac{b(1-\operatorname{Sec}[c+dx])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+dx])}{a-b}} + \frac{2b^2 \sqrt{a+b \operatorname{Sec}[c+dx]} \operatorname{Tan}[c+dx]}{3d}
 \end{aligned}$$

Result(type 4, 713 leaves):

$$\left( 2 (a + b \operatorname{Sec}[c + d x])^{5/2} \left( -7 i a (a - b) b \operatorname{EllipticE}\left[ i \operatorname{ArcSinh}\left[ \sqrt{\frac{-a + b}{a + b}} \operatorname{Tan}\left[ \frac{1}{2} (c + d x) \right] \right], \frac{a + b}{a - b} \right] \right. \right.$$

$$\sqrt{1 - \operatorname{Tan}\left[ \frac{1}{2} (c + d x) \right]^2} \left( 1 + \operatorname{Tan}\left[ \frac{1}{2} (c + d x) \right]^2 \right)$$

$$\sqrt{\frac{a + b - a \operatorname{Tan}\left[ \frac{1}{2} (c + d x) \right]^2 + b \operatorname{Tan}\left[ \frac{1}{2} (c + d x) \right]^2}{a + b}} - i (3 a^3 - 9 a^2 b + 7 a b^2 - b^3)$$

$$\operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \sqrt{\frac{-a + b}{a + b}} \operatorname{Tan}\left[ \frac{1}{2} (c + d x) \right] \right], \frac{a + b}{a - b} \right] \sqrt{1 - \operatorname{Tan}\left[ \frac{1}{2} (c + d x) \right]^2}$$

$$\left( 1 + \operatorname{Tan}\left[ \frac{1}{2} (c + d x) \right]^2 \right) \sqrt{\frac{a + b - a \operatorname{Tan}\left[ \frac{1}{2} (c + d x) \right]^2 + b \operatorname{Tan}\left[ \frac{1}{2} (c + d x) \right]^2}{a + b}} + 6 i a^3$$

$$\operatorname{EllipticPi}\left[ -\frac{a + b}{a - b}, i \operatorname{ArcSinh}\left[ \sqrt{\frac{-a + b}{a + b}} \operatorname{Tan}\left[ \frac{1}{2} (c + d x) \right] \right], \frac{a + b}{a - b} \right] \sqrt{1 - \operatorname{Tan}\left[ \frac{1}{2} (c + d x) \right]^2}$$

$$\left( 1 + \operatorname{Tan}\left[ \frac{1}{2} (c + d x) \right]^2 \right) \sqrt{\frac{a + b - a \operatorname{Tan}\left[ \frac{1}{2} (c + d x) \right]^2 + b \operatorname{Tan}\left[ \frac{1}{2} (c + d x) \right]^2}{a + b}} +$$

$$7 a b \sqrt{\frac{-a + b}{a + b}} \operatorname{Tan}\left[ \frac{1}{2} (c + d x) \right] \left( b - b \operatorname{Tan}\left[ \frac{1}{2} (c + d x) \right]^4 + a \left( -1 + \operatorname{Tan}\left[ \frac{1}{2} (c + d x) \right]^2 \right)^2 \right) \Bigg) \Bigg) /$$

$$\left( 3 \sqrt{\frac{-a + b}{a + b}} d (b + a \operatorname{Cos}[c + d x])^{5/2} \operatorname{Sec}[c + d x]^{5/2} \sqrt{\frac{1}{1 - \operatorname{Tan}\left[ \frac{1}{2} (c + d x) \right]^2}} \right.$$

$$\left. \left( -1 + \operatorname{Tan}\left[ \frac{1}{2} (c + d x) \right]^2 \right) \left( 1 + \operatorname{Tan}\left[ \frac{1}{2} (c + d x) \right]^2 \right)^{3/2} \right.$$

$$\left. \sqrt{\frac{a + b - a \operatorname{Tan}\left[ \frac{1}{2} (c + d x) \right]^2 + b \operatorname{Tan}\left[ \frac{1}{2} (c + d x) \right]^2}{1 + \operatorname{Tan}\left[ \frac{1}{2} (c + d x) \right]^2}} \right) +$$

$$\left( \operatorname{Cos}[c + d x]^2 (a + b \operatorname{Sec}[c + d x])^{5/2} \left( \frac{14}{3} a b \operatorname{Sin}[c + d x] + \frac{2}{3} b^2 \operatorname{Tan}[c + d x] \right) \right) /$$

$$\left( d (b + a \operatorname{Cos}[c + d x])^2 \right)$$

**Problem 549: Result more than twice size of optimal antiderivative.**

$$\int \operatorname{Cos}[c + d x] (a + b \operatorname{Sec}[c + d x])^{5/2} dx$$



Optimal (type 4, 353 leaves, 6 steps):

$$\begin{aligned} & \frac{1}{b d} (a-b) \sqrt{a+b} (a^2 - 2 b^2) \cot [c+d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\ & \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} + \frac{1}{d} \sqrt{a+b} (a^2 + 6 a b - 2 b^2) \cot [c+d x] \\ & \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} - \\ & \frac{1}{d} 5 a b \sqrt{a+b} \cot [c+d x] \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\ & \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} + \frac{a^2 \sqrt{a+b \operatorname{Sec}[c+d x]} \sin [c+d x]}{d} \end{aligned}$$

Result (type 4, 784 leaves):

$$\begin{aligned} & \frac{2 b^2 \cos [c+d x]^2 (a+b \operatorname{Sec}[c+d x])^{5/2} \sin [c+d x]}{d (b+a \cos [c+d x])^2} + \\ & \left( (a+b \operatorname{Sec}[c+d x])^{5/2} \sqrt{\frac{1}{1-\tan \left[\frac{1}{2}(c+d x)\right]^2}} \right. \\ & \left. \left( a^3 \tan \left[\frac{1}{2}(c+d x)\right] + a^2 b \tan \left[\frac{1}{2}(c+d x)\right] - 2 a b^2 \tan \left[\frac{1}{2}(c+d x)\right] - \right. \right. \\ & \left. \left. 2 b^3 \tan \left[\frac{1}{2}(c+d x)\right] - 2 a^3 \tan \left[\frac{1}{2}(c+d x)\right]^3 + 4 a b^2 \tan \left[\frac{1}{2}(c+d x)\right]^3 + \right. \right. \\ & \left. \left. a^3 \tan \left[\frac{1}{2}(c+d x)\right]^5 - a^2 b \tan \left[\frac{1}{2}(c+d x)\right]^5 - 2 a b^2 \tan \left[\frac{1}{2}(c+d x)\right]^5 + \right. \right. \\ & \left. \left. 2 b^3 \tan \left[\frac{1}{2}(c+d x)\right]^5 - 10 a^2 b \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan \left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \right. \right. \\ & \left. \left. \sqrt{1-\tan \left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \tan \left[\frac{1}{2}(c+d x)\right]^2+b \tan \left[\frac{1}{2}(c+d x)\right]^2}{a+b}} - \right. \right. \\ & \left. \left. 10 a^2 b \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan \left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \tan \left[\frac{1}{2}(c+d x)\right]^2 \right. \right. \\ & \left. \left. \sqrt{1-\tan \left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \tan \left[\frac{1}{2}(c+d x)\right]^2+b \tan \left[\frac{1}{2}(c+d x)\right]^2}{a+b}} + \right. \right. \\ & \left. \left. (a^3+a^2 b-2 a b^2-2 b^3) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\tan \left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1-\tan \left[\frac{1}{2}(c+d x)\right]^2} \right) \end{aligned}$$

$$\left(1 + \tan\left[\frac{1}{2}(c + dx)\right]\right)^2 \sqrt{\frac{a + b - a \tan\left[\frac{1}{2}(c + dx)\right]^2 + b \tan\left[\frac{1}{2}(c + dx)\right]^2}{a + b}} +$$

$$2b(-3a^2 + 3ab + b^2) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c + dx)\right]\right], \frac{a - b}{a + b}\right] \sqrt{1 - \tan\left[\frac{1}{2}(c + dx)\right]^2}$$

$$\left(1 + \tan\left[\frac{1}{2}(c + dx)\right]\right)^2 \sqrt{\frac{a + b - a \tan\left[\frac{1}{2}(c + dx)\right]^2 + b \tan\left[\frac{1}{2}(c + dx)\right]^2}{a + b}} \right) /$$

$$\left(d(b + a \cos[c + dx])^{5/2} \sec[c + dx]^{5/2} \left(1 + \tan\left[\frac{1}{2}(c + dx)\right]\right)^{3/2} \sqrt{\frac{a + b - a \tan\left[\frac{1}{2}(c + dx)\right]^2 + b \tan\left[\frac{1}{2}(c + dx)\right]^2}{1 + \tan\left[\frac{1}{2}(c + dx)\right]^2}}\right)$$

**Problem 550: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \cos[c + dx]^2 (a + b \sec[c + dx])^{5/2} dx$$

Optimal (type 4, 399 leaves, 7 steps):

$$\frac{1}{4d} 9a(a - b) \sqrt{a + b} \cot[c + dx] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a + b \sec[c + dx]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right]$$

$$\sqrt{\frac{b(1 - \sec[c + dx])}{a + b}} \sqrt{-\frac{b(1 + \sec[c + dx])}{a - b}} + \frac{1}{4d} \sqrt{a + b} (2a^2 + 9ab + 8b^2) \cot[c + dx]$$

$$\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a + b \sec[c + dx]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \sqrt{\frac{b(1 - \sec[c + dx])}{a + b}} \sqrt{-\frac{b(1 + \sec[c + dx])}{a - b}}$$

$$\frac{1}{4d} \sqrt{a + b} (4a^2 + 15b^2) \cot[c + dx] \operatorname{EllipticPi}\left[\frac{a + b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a + b \sec[c + dx]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right]$$

$$\sqrt{\frac{b(1 - \sec[c + dx])}{a + b}} \sqrt{-\frac{b(1 + \sec[c + dx])}{a - b}} +$$

$$\frac{9ab \sqrt{a + b \sec[c + dx]} \sin[c + dx]}{4d} + \frac{a^2 \cos[c + dx] \sqrt{a + b \sec[c + dx]} \sin[c + dx]}{2d}$$

Result (type 4, 4588 leaves):

$$\begin{aligned}
 & \frac{a^2 \cos [c+d x]^2 (a+b \sec [c+d x])^{5/2} \sin [2(c+d x)]}{4 d (b+a \cos [c+d x])^2} + \\
 & \left( \left( \frac{a^3}{2 \sqrt{b+a \cos [c+d x]} \sqrt{\sec [c+d x]}} + \frac{3 a b^2}{\sqrt{b+a \cos [c+d x]} \sqrt{\sec [c+d x]}} + \right. \right. \\
 & \left. \left. \frac{11 a^2 b \sqrt{\sec [c+d x]}}{8 \sqrt{b+a \cos [c+d x]}} + \frac{b^3 \sqrt{\sec [c+d x]}}{\sqrt{b+a \cos [c+d x]}} + \frac{9 a^2 b \cos [2(c+d x)] \sqrt{\sec [c+d x]}}{8 \sqrt{b+a \cos [c+d x]}} \right) \right. \\
 & (a+b \sec [c+d x])^{5/2} \left( 18 i a (a-b) b \sqrt{\frac{\cos [c+d x]}{1+\cos [c+d x]}} \sqrt{\frac{b+a \cos [c+d x]}{(a+b)(1+\cos [c+d x])}} \right. \\
 & \text{EllipticE} \left[ i \operatorname{ArcSinh} \left[ \sqrt{\frac{-a+b}{a+b}} \tan \left[ \frac{1}{2}(c+d x) \right] \right], \frac{a+b}{a-b} \right] - \\
 & 4 i (2 a^3 - a^2 b + 3 a b^2 - 4 b^3) \sqrt{\frac{\cos [c+d x]}{1+\cos [c+d x]}} \sqrt{\frac{b+a \cos [c+d x]}{(a+b)(1+\cos [c+d x])}} \\
 & \text{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \sqrt{\frac{-a+b}{a+b}} \tan \left[ \frac{1}{2}(c+d x) \right] \right], \frac{a+b}{a-b} \right] + \\
 & 4 i a (4 a^2 + 15 b^2) \sqrt{\frac{\cos [c+d x]}{1+\cos [c+d x]}} \sqrt{\frac{b+a \cos [c+d x]}{(a+b)(1+\cos [c+d x])}} \\
 & \text{EllipticPi} \left[ -\frac{a+b}{a-b}, i \operatorname{ArcSinh} \left[ \sqrt{\frac{-a+b}{a+b}} \tan \left[ \frac{1}{2}(c+d x) \right] \right], \frac{a+b}{a-b} \right] - \\
 & \left. \left. 9 a b \sqrt{\frac{-a+b}{a+b}} \cos [c+d x] (b+a \cos [c+d x]) \sec \left[ \frac{1}{2}(c+d x) \right]^2 \tan \left[ \frac{1}{2}(c+d x) \right] \right) \right) / \\
 & \left( 4 \sqrt{\frac{-a+b}{a+b}} d (b+a \cos [c+d x])^3 \sqrt{\sec \left[ \frac{1}{2}(c+d x) \right]^2 \sec [c+d x]^{5/2}} \right. \\
 & \left. \sqrt{\cos \left[ \frac{1}{2}(c+d x) \right]^2 \sec [c+d x] \left( -1 + \tan \left[ \frac{1}{2}(c+d x) \right] \right)^2} \right) \\
 & \left( - \left( \left( \sqrt{\sec \left[ \frac{1}{2}(c+d x) \right]^2 \tan \left[ \frac{1}{2}(c+d x) \right]} \right) \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( 18 i a (a - b) b \sqrt{\frac{\cos [c + d x]}{1 + \cos [c + d x]}} \sqrt{\frac{b + a \cos [c + d x]}{(a + b) (1 + \cos [c + d x])}} \right. \\
 & \quad \text{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{-a + b}{a + b}} \tan\left[\frac{1}{2}(c + d x)\right]\right], \frac{a + b}{a - b}\right] - \\
 & \quad 4 i (2 a^3 - a^2 b + 3 a b^2 - 4 b^3) \sqrt{\frac{\cos [c + d x]}{1 + \cos [c + d x]}} \sqrt{\frac{b + a \cos [c + d x]}{(a + b) (1 + \cos [c + d x])}} \\
 & \quad \text{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{-a + b}{a + b}} \tan\left[\frac{1}{2}(c + d x)\right]\right], \frac{a + b}{a - b}\right] + 4 i a (4 a^2 + 15 b^2) \\
 & \quad \sqrt{\frac{\cos [c + d x]}{1 + \cos [c + d x]}} \sqrt{\frac{b + a \cos [c + d x]}{(a + b) (1 + \cos [c + d x])}} \text{EllipticPi}\left[-\frac{a + b}{a - b}, i \right. \\
 & \quad \left. \operatorname{ArcSinh}\left[\sqrt{\frac{-a + b}{a + b}} \tan\left[\frac{1}{2}(c + d x)\right]\right], \frac{a + b}{a - b}\right] - 9 a b \sqrt{\frac{-a + b}{a + b}} \cos [c + d x] \\
 & \quad \left. \left. (b + a \cos [c + d x]) \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^2 \tan\left[\frac{1}{2}(c + d x)\right]\right] \right) / \left( 4 \sqrt{\frac{-a + b}{a + b}} \right. \\
 & \quad \left. \sqrt{b + a \cos [c + d x]} \sqrt{\cos\left[\frac{1}{2}(c + d x)\right]^2 \operatorname{Sec}[c + d x] \left(-1 + \tan\left[\frac{1}{2}(c + d x)\right]^2\right)^2} \right) \right) + \\
 & \left( a \sin [c + d x] \left( 18 i a (a - b) b \sqrt{\frac{\cos [c + d x]}{1 + \cos [c + d x]}} \sqrt{\frac{b + a \cos [c + d x]}{(a + b) (1 + \cos [c + d x])}} \right. \right. \\
 & \quad \text{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{-a + b}{a + b}} \tan\left[\frac{1}{2}(c + d x)\right]\right], \frac{a + b}{a - b}\right] - \\
 & \quad 4 i (2 a^3 - a^2 b + 3 a b^2 - 4 b^3) \sqrt{\frac{\cos [c + d x]}{1 + \cos [c + d x]}} \sqrt{\frac{b + a \cos [c + d x]}{(a + b) (1 + \cos [c + d x])}} \\
 & \quad \text{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{-a + b}{a + b}} \tan\left[\frac{1}{2}(c + d x)\right]\right], \frac{a + b}{a - b}\right] + \\
 & \quad \left. 4 i a (4 a^2 + 15 b^2) \sqrt{\frac{\cos [c + d x]}{1 + \cos [c + d x]}} \sqrt{\frac{b + a \cos [c + d x]}{(a + b) (1 + \cos [c + d x])}} \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left( \text{EllipticPi} \left[ -\frac{a+b}{a-b}, i \text{ArcSinh} \left[ \sqrt{\frac{-a+b}{a+b}} \tan \left[ \frac{1}{2} (c+dx) \right] \right], \frac{a+b}{a-b} \right] - \right. \right. \\
 & \left. \left. 9ab \sqrt{\frac{-a+b}{a+b}} \cos [c+dx] (b+a \cos [c+dx]) \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \right) \right) / \\
 & \left( 8 \sqrt{\frac{-a+b}{a+b}} (b+a \cos [c+dx])^{3/2} \sqrt{\sec \left[ \frac{1}{2} (c+dx) \right]^2} \right. \\
 & \left. \sqrt{\cos \left[ \frac{1}{2} (c+dx) \right]^2 \sec [c+dx] \left( -1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right)} \right) - \\
 & \left( \tan \left[ \frac{1}{2} (c+dx) \right] \left( 18 i a (a-b) b \sqrt{\frac{\cos [c+dx]}{1+\cos [c+dx]}} \sqrt{\frac{b+a \cos [c+dx]}{(a+b)(1+\cos [c+dx])}} \right. \right. \\
 & \left. \left. \text{EllipticE} \left[ i \text{ArcSinh} \left[ \sqrt{\frac{-a+b}{a+b}} \tan \left[ \frac{1}{2} (c+dx) \right] \right], \frac{a+b}{a-b} \right] - \right. \right. \\
 & \left. \left. 4 i (2a^3 - a^2b + 3ab^2 - 4b^3) \sqrt{\frac{\cos [c+dx]}{1+\cos [c+dx]}} \sqrt{\frac{b+a \cos [c+dx]}{(a+b)(1+\cos [c+dx])}} \right. \right. \\
 & \left. \left. \text{EllipticF} \left[ i \text{ArcSinh} \left[ \sqrt{\frac{-a+b}{a+b}} \tan \left[ \frac{1}{2} (c+dx) \right] \right], \frac{a+b}{a-b} \right] + \right. \right. \\
 & \left. \left. 4 i a (4a^2 + 15b^2) \sqrt{\frac{\cos [c+dx]}{1+\cos [c+dx]}} \sqrt{\frac{b+a \cos [c+dx]}{(a+b)(1+\cos [c+dx])}} \right. \right. \\
 & \left. \left. \text{EllipticPi} \left[ -\frac{a+b}{a-b}, i \text{ArcSinh} \left[ \sqrt{\frac{-a+b}{a+b}} \tan \left[ \frac{1}{2} (c+dx) \right] \right], \frac{a+b}{a-b} \right] - \right. \right. \\
 & \left. \left. 9ab \sqrt{\frac{-a+b}{a+b}} \cos [c+dx] (b+a \cos [c+dx]) \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \right) \right) / \\
 & \left( 8 \sqrt{\frac{-a+b}{a+b}} \sqrt{b+a \cos [c+dx]} \sqrt{\sec \left[ \frac{1}{2} (c+dx) \right]^2} \right. \\
 & \left. \sqrt{\cos \left[ \frac{1}{2} (c+dx) \right]^2 \sec [c+dx] \left( -1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right)} \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \left( -\frac{9}{2} a b \sqrt{\frac{-a+b}{a+b}} \cos [c+d x] (b+a \cos [c+d x]) \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^4 + \right. \\
 & \frac{1}{\sqrt{\frac{\cos [c+d x]}{1+\cos [c+d x]}}} 9 i a (a-b) b \sqrt{\frac{b+a \cos [c+d x]}{(a+b)(1+\cos [c+d x])}} \\
 & \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan \left[\frac{1}{2}(c+d x)\right]\right], \frac{a+b}{a-b}\right] \\
 & \left. \left(\frac{\cos [c+d x] \sin [c+d x]}{(1+\cos [c+d x])^2} - \frac{\sin [c+d x]}{1+\cos [c+d x]}\right) - \frac{1}{\sqrt{\frac{\cos [c+d x]}{1+\cos [c+d x]}}} \right. \\
 & 2 i\left(2 a^3-a^2 b+3 a b^2-4 b^3\right) \sqrt{\frac{b+a \cos [c+d x]}{(a+b)(1+\cos [c+d x])}} \\
 & \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan \left[\frac{1}{2}(c+d x)\right]\right], \frac{a+b}{a-b}\right] \\
 & \left. \left(\frac{\cos [c+d x] \sin [c+d x]}{(1+\cos [c+d x])^2} - \frac{\sin [c+d x]}{1+\cos [c+d x]}\right) + \right. \\
 & \frac{1}{\sqrt{\frac{\cos [c+d x]}{1+\cos [c+d x]}}} 2 i a\left(4 a^2+15 b^2\right) \sqrt{\frac{b+a \cos [c+d x]}{(a+b)(1+\cos [c+d x])}} \\
 & \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan \left[\frac{1}{2}(c+d x)\right]\right], \frac{a+b}{a-b}\right] \\
 & \left. \left(\frac{\cos [c+d x] \sin [c+d x]}{(1+\cos [c+d x])^2} - \frac{\sin [c+d x]}{1+\cos [c+d x]}\right) + \right. \\
 & \left. \left(9 i a(a-b) b \sqrt{\frac{\cos [c+d x]}{1+\cos [c+d x]}} \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan \left[\frac{1}{2}(c+d x)\right]\right], \right. \right. \right. \\
 & \left. \left. \frac{a+b}{a-b}\right] \left(-\frac{a \sin [c+d x]}{(a+b)(1+\cos [c+d x])} + \frac{(b+a \cos [c+d x]) \sin [c+d x]}{(a+b)(1+\cos [c+d x])^2}\right)\right) / \\
 & \left. \left(\sqrt{\frac{b+a \cos [c+d x]}{(a+b)(1+\cos [c+d x])}}\right) - \left(2 i\left(2 a^3-a^2 b+3 a b^2-4 b^3\right) \sqrt{\frac{\cos [c+d x]}{1+\cos [c+d x]}}\right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \text{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \\
 & \left(-\frac{a \sin[c+dx]}{(a+b)(1+\cos[c+dx])} + \frac{(b+a \cos[c+dx]) \sin[c+dx]}{(a+b)(1+\cos[c+dx])^2}\right) / \\
 & \left(\sqrt{\frac{b+a \cos[c+dx]}{(a+b)(1+\cos[c+dx])}}\right) + \left(2 i a (4 a^2 + 15 b^2) \sqrt{\frac{\cos[c+dx]}{1+\cos[c+dx]}}\right. \\
 & \text{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \\
 & \left(-\frac{a \sin[c+dx]}{(a+b)(1+\cos[c+dx])} + \frac{(b+a \cos[c+dx]) \sin[c+dx]}{(a+b)(1+\cos[c+dx])^2}\right) / \\
 & \left(\sqrt{\frac{b+a \cos[c+dx]}{(a+b)(1+\cos[c+dx])}}\right) + 9 a^2 b \sqrt{\frac{-a+b}{a+b}} \cos[c+dx] \\
 & \sec\left[\frac{1}{2}(c+dx)\right]^2 \sin[c+dx] \tan\left[\frac{1}{2}(c+dx)\right] + \\
 & 9 a b \sqrt{\frac{-a+b}{a+b}} (b+a \cos[c+dx]) \sec\left[\frac{1}{2}(c+dx)\right]^2 \sin[c+dx] \tan\left[\frac{1}{2}(c+dx)\right] - \\
 & 9 a b \sqrt{\frac{-a+b}{a+b}} \cos[c+dx] (b+a \cos[c+dx]) \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^2 + \\
 & \left(2 \sqrt{\frac{-a+b}{a+b}} (2 a^3 - a^2 b + 3 a b^2 - 4 b^3) \sqrt{\frac{\cos[c+dx]}{1+\cos[c+dx]}}\right. \\
 & \left.\sqrt{\frac{b+a \cos[c+dx]}{(a+b)(1+\cos[c+dx])}} \sec\left[\frac{1}{2}(c+dx)\right]^2\right) / \\
 & \left(\sqrt{1 + \frac{(-a+b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a-b}} \sqrt{1 + \frac{(-a+b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}}\right) - \\
 & \left(2 a \sqrt{\frac{-a+b}{a+b}} (4 a^2 + 15 b^2) \sqrt{\frac{\cos[c+dx]}{1+\cos[c+dx]}} \sqrt{\frac{b+a \cos[c+dx]}{(a+b)(1+\cos[c+dx])}}\right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right) / \left( \left( 1 - \frac{(-a+b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a-b} \right) \right. \\
 & \left. \sqrt{1 + \frac{(-a+b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a-b}} \sqrt{1 + \frac{(-a+b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \right) - \\
 & \left( 9 a (a-b) b \sqrt{\frac{-a+b}{a+b}} \sqrt{\frac{\operatorname{Cos}[c+dx]}{1+\operatorname{Cos}[c+dx]}} \sqrt{\frac{b+a\operatorname{Cos}[c+dx]}{(a+b)(1+\operatorname{Cos}[c+dx])}} \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \left. \sqrt{1 + \frac{(-a+b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a-b}} \right) / \left( \sqrt{1 + \frac{(-a+b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \right) \right) / \\
 & \left( 4 \sqrt{\frac{-a+b}{a+b}} \sqrt{b+a\operatorname{Cos}[c+dx]} \sqrt{\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Sec}[c+dx]} \right. \\
 & \left. \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) - \\
 & \left( \left( 18 i a (a-b) b \sqrt{\frac{\operatorname{Cos}[c+dx]}{1+\operatorname{Cos}[c+dx]}} \sqrt{\frac{b+a\operatorname{Cos}[c+dx]}{(a+b)(1+\operatorname{Cos}[c+dx])}} \right. \right. \\
 & \left. \left. \operatorname{EllipticE}\left[ i \operatorname{ArcSinh}\left[ \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right], \frac{a+b}{a-b} \right] - \right. \right. \\
 & \left. \left. 4 i (2 a^3 - a^2 b + 3 a b^2 - 4 b^3) \sqrt{\frac{\operatorname{Cos}[c+dx]}{1+\operatorname{Cos}[c+dx]}} \sqrt{\frac{b+a\operatorname{Cos}[c+dx]}{(a+b)(1+\operatorname{Cos}[c+dx])}} \right. \right. \\
 & \left. \left. \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right], \frac{a+b}{a-b} \right] + \right. \right. \\
 & \left. \left. 4 i a (4 a^2 + 15 b^2) \sqrt{\frac{\operatorname{Cos}[c+dx]}{1+\operatorname{Cos}[c+dx]}} \sqrt{\frac{b+a\operatorname{Cos}[c+dx]}{(a+b)(1+\operatorname{Cos}[c+dx])}} \right. \right. \\
 & \left. \left. \operatorname{EllipticPi}\left[ -\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[ \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right], \frac{a+b}{a-b} \right] - \right. \right.
 \end{aligned}$$



$$\left( 9 a b \sqrt{\frac{-a+b}{a+b}} \cos [c+d x] (b+a \cos [c+d x]) \sec \left[ \frac{1}{2} (c+d x) \right]^2 \tan \left[ \frac{1}{2} (c+d x) \right] \right. \\ \left. \left( -\cos \left[ \frac{1}{2} (c+d x) \right] \sec [c+d x] \sin \left[ \frac{1}{2} (c+d x) \right] + \right. \right. \\ \left. \left. \cos \left[ \frac{1}{2} (c+d x) \right]^2 \sec [c+d x] \tan [c+d x] \right) \right) / \\ \left( 8 \sqrt{\frac{-a+b}{a+b}} \sqrt{b+a \cos [c+d x]} \sqrt{\sec \left[ \frac{1}{2} (c+d x) \right]^2} \right. \\ \left. \left( \cos \left[ \frac{1}{2} (c+d x) \right]^2 \sec [c+d x] \right)^{3/2} \left( -1 + \tan \left[ \frac{1}{2} (c+d x) \right]^2 \right) \right) \right)$$

**Problem 551: Result more than twice size of optimal antiderivative.**

$$\int \cos [c+d x]^3 (a+b \sec [c+d x])^{5/2} dx$$

Optimal (type 4, 460 leaves, 8 steps):

$$\frac{1}{24 b d} (a-b) \sqrt{a+b} (16 a^2+33 b^2) \cot [c+d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\ \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} + \frac{1}{24 d} \sqrt{a+b} (16 a^2+26 a b+33 b^2) \cot [c+d x] \\ \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} - \\ \frac{1}{8 a d} 5 b \sqrt{a+b} (4 a^2+b^2) \cot [c+d x] \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\ \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} + \frac{(16 a^2+33 b^2) \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{24 d} + \\ \frac{13 a b \cos [c+d x] \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{12 d} + \\ \frac{a^2 \cos [c+d x]^2 \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{3 d}$$

Result (type 4, 1026 leaves):

$$\begin{aligned}
& \left( \cos [c + d x]^2 (a + b \operatorname{Sec}[c + d x])^{5/2} \right. \\
& \quad \left. \left( \frac{1}{12} a^2 \sin [c + d x] + \frac{13}{24} a b \sin [2 (c + d x)] + \frac{1}{12} a^2 \sin [3 (c + d x)] \right) \right) / \\
& \quad \left( d (b + a \cos [c + d x])^2 \right) + \left( (a + b \operatorname{Sec}[c + d x])^{5/2} \sqrt{\frac{1}{1 - \tan \left[ \frac{1}{2} (c + d x) \right]^2}} \right. \\
& \quad \left( 16 a^3 \tan \left[ \frac{1}{2} (c + d x) \right] + 16 a^2 b \tan \left[ \frac{1}{2} (c + d x) \right] + 33 a b^2 \tan \left[ \frac{1}{2} (c + d x) \right] + \right. \\
& \quad 33 b^3 \tan \left[ \frac{1}{2} (c + d x) \right] - 32 a^3 \tan \left[ \frac{1}{2} (c + d x) \right]^3 - 66 a b^2 \tan \left[ \frac{1}{2} (c + d x) \right]^3 + \\
& \quad 16 a^3 \tan \left[ \frac{1}{2} (c + d x) \right]^5 - 16 a^2 b \tan \left[ \frac{1}{2} (c + d x) \right]^5 + 33 a b^2 \tan \left[ \frac{1}{2} (c + d x) \right]^5 - \\
& \quad \left. 33 b^3 \tan \left[ \frac{1}{2} (c + d x) \right]^5 - 120 a^2 b \operatorname{EllipticPi}[-1, -\operatorname{ArcSin}[\tan \left[ \frac{1}{2} (c + d x) \right]]], \frac{a - b}{a + b} \right] \\
& \quad \sqrt{1 - \tan \left[ \frac{1}{2} (c + d x) \right]^2} \sqrt{\frac{a + b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b}} - \\
& \quad 30 b^3 \operatorname{EllipticPi}[-1, -\operatorname{ArcSin}[\tan \left[ \frac{1}{2} (c + d x) \right]]], \frac{a - b}{a + b} \sqrt{1 - \tan \left[ \frac{1}{2} (c + d x) \right]^2} \\
& \quad \sqrt{\frac{a + b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b}} - \\
& \quad 120 a^2 b \operatorname{EllipticPi}[-1, -\operatorname{ArcSin}[\tan \left[ \frac{1}{2} (c + d x) \right]]], \frac{a - b}{a + b} \tan \left[ \frac{1}{2} (c + d x) \right]^2 \\
& \quad \sqrt{1 - \tan \left[ \frac{1}{2} (c + d x) \right]^2} \sqrt{\frac{a + b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b}} - \\
& \quad 30 b^3 \operatorname{EllipticPi}[-1, -\operatorname{ArcSin}[\tan \left[ \frac{1}{2} (c + d x) \right]]], \frac{a - b}{a + b} \tan \left[ \frac{1}{2} (c + d x) \right]^2 \\
& \quad \sqrt{1 - \tan \left[ \frac{1}{2} (c + d x) \right]^2} \sqrt{\frac{a + b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b}} + \\
& \quad \left( 16 a^3 + 16 a^2 b + 33 a b^2 + 33 b^3 \right) \operatorname{EllipticE}[\operatorname{ArcSin}[\tan \left[ \frac{1}{2} (c + d x) \right]]], \frac{a - b}{a + b} \\
& \quad \sqrt{1 - \tan \left[ \frac{1}{2} (c + d x) \right]^2} \left( 1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right)
\end{aligned}$$

$$\begin{aligned}
 & \sqrt{\frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - 2b(38a^2 - 13ab + 24b^2) \\
 & \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \\
 & \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \right) \Bigg) / \\
 & \left(24d(b+a \operatorname{Cos}[c+dx])^{5/2} \operatorname{Sec}[c+dx]^{5/2} \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)^{3/2} \right. \\
 & \left. \sqrt{\frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}} \right)
 \end{aligned}$$

**Problem 552: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \operatorname{Cos}[c+dx]^4 (a+b \operatorname{Sec}[c+dx])^{5/2} dx$$

Optimal (type 4, 530 leaves, 9 steps):

$$\begin{aligned}
& \frac{1}{192 a d} (a-b) \sqrt{a+b} (284 a^2 + 15 b^2) \operatorname{Cot}[c+d x] \\
& \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} + \\
& \frac{1}{192 a d} \sqrt{a+b} (72 a^3 + 284 a^2 b + 118 a b^2 + 15 b^3) \operatorname{Cot}[c+d x] \\
& \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} - \\
& \frac{1}{64 a^2 d} \sqrt{a+b} (48 a^4 + 120 a^2 b^2 - 5 b^4) \operatorname{Cot}[c+d x] \\
& \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \\
& \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} + \frac{b(284 a^2 + 15 b^2) \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{192 a d} + \\
& \frac{(36 a^2 + 59 b^2) \operatorname{Cos}[c+d x] \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{96 d} + \\
& \frac{17 a b \operatorname{Cos}[c+d x]^2 \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{24 d} + \\
& \frac{a^2 \operatorname{Cos}[c+d x]^3 \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{4 d}
\end{aligned}$$

Result (type 4, 1688 leaves):

$$\begin{aligned}
& \left( \operatorname{Cos}[c+d x]^2 (a+b \operatorname{Sec}[c+d x])^{5/2} \left( \frac{17}{96} a b \operatorname{Sin}[c+d x] + \frac{1}{192} (48 a^2 + 59 b^2) \operatorname{Sin}[2(c+d x)] + \right. \right. \\
& \left. \left. \frac{17}{96} a b \operatorname{Sin}[3(c+d x)] + \frac{1}{32} a^2 \operatorname{Sin}[4(c+d x)] \right) \right) / \left( d (b+a \operatorname{Cos}[c+d x])^2 \right) + \\
& \left( (a+b \operatorname{Sec}[c+d x])^{5/2} \left( -284 a^3 b \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] - 284 a^2 b^2 \sqrt{\frac{-a+b}{a+b}} \right. \right. \\
& \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] - 15 a b^3 \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] - 15 b^4 \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] + \right. \right. \\
& \left. \left. 568 a^3 b \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^3 + 30 a b^3 \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^3 - \right. \right. \\
& \left. \left. 284 a^3 b \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 + 284 a^2 b^2 \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 - \right. \right.
\end{aligned}$$

$$\begin{aligned}
 & 15 a b^3 \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 + 15 b^4 \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 + \\
 & 288 i a^4 \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} + \\
 & 720 i a^2 b^2 \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} - \\
 & 30 i b^4 \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} + 288 i a^4 \\
 & \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a+b}{a-b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2 \\
 & \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} + 720 i a^2 b^2 \\
 & \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a+b}{a-b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2 \\
 & \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} - \\
 & 30 i b^4 \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a+b}{a-b}\right] \\
 & \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2 \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}
 \end{aligned}$$

$$\sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + i b (284 a^3 - 284 a^2 b + 15 a b^2 - 15 b^3)$$

$$\operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}$$

$$\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} -$$

$$2 i (72 a^4 - 36 a^3 b + 38 a^2 b^2 - 59 a b^3 - 15 b^4)$$

$$\operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}$$

$$\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \right) \Bigg/$$

$$\left(192 a \sqrt{\frac{-a+b}{a+b}} d (b+a \operatorname{Cos}[c+dx])^{5/2} \operatorname{Sec}[c+dx]^{5/2} \sqrt{\frac{1}{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}}\right.$$

$$\left. \left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)^{3/2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}}\right)$$

**Problem 553: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int (a+b \operatorname{Sec}[c+dx])^{7/2} dx$$

Optimal (type 4, 403 leaves, 7 steps):

$$\begin{aligned}
 & -\frac{1}{15d} 2(a-b)\sqrt{a+b}(58a^2+9b^2)\cot[c+dx]\operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b\sec[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{\frac{b(1-\sec[c+dx])}{a+b}}\sqrt{-\frac{b(1+\sec[c+dx])}{a-b}}+ \\
 & \frac{1}{15d} 2\sqrt{a+b}(60a^3-58a^2b+22ab^2-9b^3)\cot[c+dx] \\
 & \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b\sec[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]\sqrt{\frac{b(1-\sec[c+dx])}{a+b}}\sqrt{-\frac{b(1+\sec[c+dx])}{a-b}}- \\
 & \frac{1}{d} 2a^3\sqrt{a+b}\cot[c+dx]\operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b\sec[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{\frac{b(1-\sec[c+dx])}{a+b}}\sqrt{-\frac{b(1+\sec[c+dx])}{a-b}}+ \\
 & \frac{26ab^2\sqrt{a+b\sec[c+dx]}\tan[c+dx]}{15d} + \frac{2b^2(a+b\sec[c+dx])^{3/2}\tan[c+dx]}{5d}
 \end{aligned}$$

Result(type 4, 1150 leaves):

$$\begin{aligned}
 & \left(2(a+b\sec[c+dx])^{7/2}\left(58a^3b\sqrt{\frac{-a+b}{a+b}}\tan\left[\frac{1}{2}(c+dx)\right]+58a^2b^2\sqrt{\frac{-a+b}{a+b}}\tan\left[\frac{1}{2}(c+dx)\right]+9ab^3\sqrt{\frac{-a+b}{a+b}}\tan\left[\frac{1}{2}(c+dx)\right]+9b^4\sqrt{\frac{-a+b}{a+b}}\tan\left[\frac{1}{2}(c+dx)\right]-116a^3b\sqrt{\frac{-a+b}{a+b}}\tan\left[\frac{1}{2}(c+dx)\right]^3-18ab^3\sqrt{\frac{-a+b}{a+b}}\tan\left[\frac{1}{2}(c+dx)\right]^3+58a^3b\sqrt{\frac{-a+b}{a+b}}\tan\left[\frac{1}{2}(c+dx)\right]^5-58a^2b^2\sqrt{\frac{-a+b}{a+b}}\tan\left[\frac{1}{2}(c+dx)\right]^5+9ab^3\sqrt{\frac{-a+b}{a+b}}\tan\left[\frac{1}{2}(c+dx)\right]^5-9b^4\sqrt{\frac{-a+b}{a+b}}\tan\left[\frac{1}{2}(c+dx)\right]^5+30i a^4\operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i\operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}}\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right]\sqrt{1-\tan\left[\frac{1}{2}(c+dx)\right]^2}\sqrt{\frac{a+b-a\tan\left[\frac{1}{2}(c+dx)\right]^2+b\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}}\right)
 \end{aligned}$$

$$\begin{aligned}
 & 30 \, i \, a^4 \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, \, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
 & i \, b \, (-58 a^3 + 58 a^2 b - 9 a b^2 + 9 b^3) \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \\
 & \sqrt{\frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 & i \, (15 a^4 - 60 a^3 b + 58 a^2 b^2 - 22 a b^3 + 9 b^4) \\
 & \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \\
 & \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \Bigg) \Bigg/ \\
 & \left(15 \sqrt{\frac{-a+b}{a+b}} d (b+a \operatorname{Cos}[c+dx])^{7/2} \operatorname{Sec}[c+dx]^{7/2} \sqrt{\frac{1}{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}} \right. \\
 & \left. \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)^{3/2} \right. \\
 & \left. \sqrt{\frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}} \right) + \\
 & \left(\operatorname{Cos}[c+dx]^3 (a+b \operatorname{Sec}[c+dx])^{7/2} \left(\frac{2}{15} b (58 a^2 + 9 b^2) \operatorname{Sin}[c+dx] + \right. \right. \\
 & \left. \left. \frac{32}{15} a b^2 \operatorname{Tan}[c+dx] + \frac{2}{5} b^3 \operatorname{Sec}[c+dx] \operatorname{Tan}[c+dx]\right)\right) \Bigg/ (d (b+a \operatorname{Cos}[c+dx])^3)
 \end{aligned}$$

**Problem 554: Unable to integrate problem.**

$$\int \frac{\operatorname{Sec}[c+dx]^5}{\sqrt{a+b \operatorname{Sec}[c+dx]}} dx$$

Optimal (type 4, 359 leaves, 6 steps):



$$\frac{1}{105 b^5 d} 8 a (a-b) \sqrt{a+b} (12 a^2 + 11 b^2) \operatorname{Cot}[c+d x]$$

$$\operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} +$$

$$\frac{1}{105 b^4 d} 2 \sqrt{a+b} (48 a^3 - 12 a^2 b + 44 a b^2 + 25 b^3) \operatorname{Cot}[c+d x]$$

$$\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} +$$

$$\frac{2(24 a^2 + 25 b^2) \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Tan}[c+d x]}{105 b^3 d} -$$

$$\frac{12 a \operatorname{Sec}[c+d x] \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Tan}[c+d x]}{35 b^2 d} + \frac{2 \operatorname{Sec}[c+d x]^2 \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Tan}[c+d x]}{7 b d}$$

Result (type 8, 25 leaves):

$$\int \frac{\operatorname{Sec}[c+d x]^5}{\sqrt{a+b \operatorname{Sec}[c+d x]}} dx$$

**Problem 555: Unable to integrate problem.**

$$\int \frac{\operatorname{Sec}[c+d x]^4}{\sqrt{a+b \operatorname{Sec}[c+d x]}} dx$$

Optimal (type 4, 301 leaves, 5 steps):

$$-\frac{1}{15 b^4 d} 2 (a-b) \sqrt{a+b} (8 a^2 + 9 b^2) \operatorname{Cot}[c+d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} - \frac{1}{15 b^3 d}$$

$$2 \sqrt{a+b} (8 a^2 - 2 a b + 9 b^2) \operatorname{Cot}[c+d x] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} -$$

$$\frac{8 a \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Tan}[c+d x]}{15 b^2 d} + \frac{2 \operatorname{Sec}[c+d x] \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Tan}[c+d x]}{5 b d}$$

Result (type 8, 25 leaves):

$$\int \frac{\operatorname{Sec}[c+d x]^4}{\sqrt{a+b \operatorname{Sec}[c+d x]}} dx$$

### Problem 556: Unable to integrate problem.

$$\int \frac{\operatorname{Sec}[c+dx]^3}{\sqrt{a+b \operatorname{Sec}[c+dx]}} dx$$

Optimal (type 4, 244 leaves, 4 steps):

$$\frac{1}{3b^3d} 4a(a-b)\sqrt{a+b} \operatorname{Cot}[c+dx] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\operatorname{Sec}[c+dx])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+dx])}{a-b}} + \frac{1}{3b^2d}$$

$$2\sqrt{a+b} (2a+b) \operatorname{Cot}[c+dx] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\operatorname{Sec}[c+dx])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+dx])}{a-b}} + \frac{2\sqrt{a+b \operatorname{Sec}[c+dx]} \operatorname{Tan}[c+dx]}{3bd}$$

Result (type 8, 25 leaves):

$$\int \frac{\operatorname{Sec}[c+dx]^3}{\sqrt{a+b \operatorname{Sec}[c+dx]}} dx$$

### Problem 557: Unable to integrate problem.

$$\int \frac{\operatorname{Sec}[c+dx]^2}{\sqrt{a+b \operatorname{Sec}[c+dx]}} dx$$

Optimal (type 4, 204 leaves, 3 steps):

$$-\frac{1}{b^2d} 2(a-b)\sqrt{a+b} \operatorname{Cot}[c+dx] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\operatorname{Sec}[c+dx])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+dx])}{a-b}} - \frac{1}{bd}$$

$$2\sqrt{a+b} \operatorname{Cot}[c+dx] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\operatorname{Sec}[c+dx])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+dx])}{a-b}}$$

Result (type 8, 25 leaves):

$$\int \frac{\operatorname{Sec}[c+dx]^2}{\sqrt{a+b \operatorname{Sec}[c+dx]}} dx$$

### Problem 559: Unable to integrate problem.

$$\int \frac{1}{\sqrt{a+b \sec [c+d x]}} dx$$

Optimal (type 4, 106 leaves, 1 step):

$$-\frac{1}{a d} 2 \sqrt{a+b} \cot [c+d x] \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}}$$

Result (type 8, 16 leaves):

$$\int \frac{1}{\sqrt{a+b \sec [c+d x]}} dx$$

### Problem 560: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\cos [c+d x]}{\sqrt{a+b \sec [c+d x]}} dx$$

Optimal (type 4, 338 leaves, 6 steps):

$$\frac{1}{a b d} (a-b) \sqrt{a+b} \cot [c+d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} + \frac{1}{a d} \sqrt{a+b} \cot [c+d x]$$

$$\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} +$$

$$\frac{1}{a^2 d} b \sqrt{a+b} \cot [c+d x] \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} + \frac{\sqrt{a+b \sec [c+d x]} \sin [c+d x]}{a d}$$

Result (type 4, 795 leaves):

$$\left( \sqrt{b+a \cos [c+d x]} \sqrt{\sec [c+d x]} \sqrt{\frac{1}{1-\tan \left[\frac{1}{2}(c+d x)\right]^2}} \right)$$

$$\begin{aligned}
 & \sqrt{1 - \tan\left[\frac{1}{2}(c + dx)\right]^2} \left( a \sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c + dx)\right] \sqrt{1 - \tan\left[\frac{1}{2}(c + dx)\right]^2} + \right. \\
 & b \sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c + dx)\right] \sqrt{1 - \tan\left[\frac{1}{2}(c + dx)\right]^2} - a \sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c + dx)\right]^3 \\
 & \left. \sqrt{1 - \tan\left[\frac{1}{2}(c + dx)\right]^2} + b \sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c + dx)\right]^3 \sqrt{1 - \tan\left[\frac{1}{2}(c + dx)\right]^2} + \right. \\
 & 2 i b \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c + dx)\right]\right], \frac{a+b}{a-b}\right] \\
 & \left. \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c + dx)\right]^2 + b \tan\left[\frac{1}{2}(c + dx)\right]^2}{a+b}} + \right. \\
 & 2 i b \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c + dx)\right]\right], \frac{a+b}{a-b}\right] \\
 & \tan\left[\frac{1}{2}(c + dx)\right]^2 \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c + dx)\right]^2 + b \tan\left[\frac{1}{2}(c + dx)\right]^2}{a+b}} - \\
 & i (a - b) \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c + dx)\right]\right], \frac{a+b}{a-b}\right] \\
 & \left. \left(1 + \tan\left[\frac{1}{2}(c + dx)\right]\right)^2 \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c + dx)\right]^2 + b \tan\left[\frac{1}{2}(c + dx)\right]^2}{a+b}} - \right. \\
 & 2 i b \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c + dx)\right]\right], \frac{a+b}{a-b}\right] \\
 & \left. \left. \left. \left(1 + \tan\left[\frac{1}{2}(c + dx)\right]\right)^2 \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c + dx)\right]^2 + b \tan\left[\frac{1}{2}(c + dx)\right]^2}{a+b}} \right) \right) \right) \right) / \\
 & \left( a \sqrt{\frac{-a+b}{a+b}} d \sqrt{a+b} \operatorname{Sec}[c + dx] \left(1 + \tan\left[\frac{1}{2}(c + dx)\right]\right)^{3/2} \right. \\
 & \left. \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c + dx)\right]^2 + b \tan\left[\frac{1}{2}(c + dx)\right]^2}{1 + \tan\left[\frac{1}{2}(c + dx)\right]^2}} \right)
 \end{aligned}$$

Problem 561: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\cos [c+d x]^2}{\sqrt{a+b \sec [c+d x]}} d x$$

Optimal (type 4, 401 leaves, 7 steps):

$$-\frac{1}{4 a^2 d} 3(a-b) \sqrt{a+b} \cot [c+d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} + \frac{1}{4 a^2 d}$$

$$(2 a-3 b) \sqrt{a+b} \cot [c+d x] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} - \frac{1}{4 a^3 d}$$

$$\sqrt{a+b} (4 a^2+3 b^2) \cot [c+d x] \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}}$$

$$\frac{3 b \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{4 a^2 d} + \frac{\cos [c+d x] \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{2 a d}$$

Result (type 4, 1195 leaves):

$$\frac{(b+a \cos [c+d x]) \sec [c+d x] \sin [2(c+d x)]}{4 a d \sqrt{a+b \sec [c+d x]}}$$

$$\left(\sqrt{b+a \cos [c+d x]} \sqrt{\sec [c+d x]} \sqrt{\frac{a+b-a \tan \left[\frac{1}{2}(c+d x)\right]^2+b \tan \left[\frac{1}{2}(c+d x)\right]^2}{1+\tan \left[\frac{1}{2}(c+d x)\right]^2}}\right.$$

$$\left(3 a b \sqrt{\frac{-a+b}{a+b}} \tan \left[\frac{1}{2}(c+d x)\right]+3 b^2 \sqrt{\frac{-a+b}{a+b}} \tan \left[\frac{1}{2}(c+d x)\right]-6 a b \sqrt{\frac{-a+b}{a+b}}\right.$$

$$\tan \left[\frac{1}{2}(c+d x)\right]^3+3 a b \sqrt{\frac{-a+b}{a+b}} \tan \left[\frac{1}{2}(c+d x)\right]^5-3 b^2 \sqrt{\frac{-a+b}{a+b}} \tan \left[\frac{1}{2}(c+d x)\right]^5+$$

$$\left.8 i a^2 \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan \left[\frac{1}{2}(c+d x)\right]\right], \frac{a+b}{a-b}\right]\right)$$

$$\begin{aligned}
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
 & 6 i b^2 \text{EllipticPi}\left[-\frac{a+b}{a-b}, i \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
 & 8 i a^2 \text{EllipticPi}\left[-\frac{a+b}{a-b}, i \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
 & 6 i b^2 \text{EllipticPi}\left[-\frac{a+b}{a-b}, i \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 & 3 i (a-b) b \text{EllipticE}\left[i \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \\
 & \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - 2 i (2 a^2 - a b + 3 b^2) \\
 & \text{EllipticF}\left[i \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \\
 & \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \right) \Bigg) \Bigg/ \\
 & \left(4 a^2 \sqrt{\frac{-a+b}{a+b}} d \sqrt{a+b \text{Sec}[c+dx]} \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2}}\right)
 \end{aligned}$$

$$\left( a \left( -1 + \tan \left[ \frac{1}{2} (c + dx) \right] \right)^2 - b \left( 1 + \tan \left[ \frac{1}{2} (c + dx) \right] \right)^2 \right)$$

**Problem 562: Unable to integrate problem.**

$$\int \frac{\sec [c + dx]^5}{(a + b \sec [c + dx])^{3/2}} dx$$

Optimal (type 4, 399 leaves, 6 steps):

$$\begin{aligned} & -\frac{1}{5 b^5 \sqrt{a+b} d} 2 (16 a^4 - 8 a^2 b^2 - 3 b^4) \cot [c + dx] \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{a+b \sec [c + dx]}}{\sqrt{a+b}} \right], \frac{a+b}{a-b} \right] \\ & \sqrt{\frac{b(1-\sec [c + dx])}{a+b}} \sqrt{-\frac{b(1+\sec [c + dx])}{a-b}} - \frac{1}{5 b^4 \sqrt{a+b} d} \\ & 2(4 a+3 b)(4 a^2+b^2) \cot [c + dx] \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{a+b \sec [c + dx]}}{\sqrt{a+b}} \right], \frac{a+b}{a-b} \right] \\ & \sqrt{\frac{b(1-\sec [c + dx])}{a+b}} \sqrt{-\frac{b(1+\sec [c + dx])}{a-b}} - \\ & \frac{2 a^2 \sec [c + dx]^2 \tan [c + dx]}{b(a^2-b^2) d \sqrt{a+b \sec [c + dx]}} - \frac{2 a(8 a^2-3 b^2) \sqrt{a+b \sec [c + dx]} \tan [c + dx]}{5 b^3(a^2-b^2) d} + \\ & \frac{2(6 a^2-b^2) \sec [c + dx] \sqrt{a+b \sec [c + dx]} \tan [c + dx]}{5 b^2(a^2-b^2) d} \end{aligned}$$

Result (type 8, 25 leaves):

$$\int \frac{\sec [c + dx]^5}{(a + b \sec [c + dx])^{3/2}} dx$$

**Problem 563: Unable to integrate problem.**

$$\int \frac{\sec [c + dx]^4}{(a + b \sec [c + dx])^{3/2}} dx$$

Optimal (type 4, 325 leaves, 5 steps):

$$\frac{1}{3 b^4 \sqrt{a+b} d} 2 a (8 a^2 - 5 b^2) \operatorname{Cot}[c+d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} + \frac{1}{3 b^3 \sqrt{a+b} d}$$

$$2(2 a+b)(4 a+b) \operatorname{Cot}[c+d x] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}}$$

$$\frac{2 a^2 \operatorname{Sec}[c+d x] \operatorname{Tan}[c+d x]}{b(a^2-b^2) d \sqrt{a+b \operatorname{Sec}[c+d x]}} + \frac{2(4 a^2-b^2) \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Tan}[c+d x]}{3 b^2(a^2-b^2) d}$$

Result (type 8, 25 leaves):

$$\int \frac{\operatorname{Sec}[c+d x]^4}{(a+b \operatorname{Sec}[c+d x])^{3/2}} dx$$

**Problem 564: Unable to integrate problem.**

$$\int \frac{\operatorname{Sec}[c+d x]^3}{(a+b \operatorname{Sec}[c+d x])^{3/2}} dx$$

Optimal (type 4, 257 leaves, 4 steps):

$$-\frac{1}{b^3 \sqrt{a+b} d} 2(2 a^2-b^2) \operatorname{Cot}[c+d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} - \frac{1}{b^2 \sqrt{a+b} d}$$

$$2(2 a+b) \operatorname{Cot}[c+d x] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} - \frac{2 a^2 \operatorname{Tan}[c+d x]}{b(a^2-b^2) d \sqrt{a+b \operatorname{Sec}[c+d x]}}$$

Result (type 8, 25 leaves):

$$\int \frac{\operatorname{Sec}[c+d x]^3}{(a+b \operatorname{Sec}[c+d x])^{3/2}} dx$$



### Problem 565: Unable to integrate problem.

$$\int \frac{\sec [c+d x]^2}{(a+b \sec [c+d x])^{3/2}} d x$$

Optimal (type 4, 237 leaves, 4 steps):

$$\frac{1}{b^2 \sqrt{a+b} d} 2 a \cot [c+d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} + \frac{1}{b \sqrt{a+b} d}$$

$$2 \cot [c+d x] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} + \frac{2 a \tan [c+d x]}{(a^2-b^2) d \sqrt{a+b \sec [c+d x]}}$$

Result (type 8, 25 leaves):

$$\int \frac{\sec [c+d x]^2}{(a+b \sec [c+d x])^{3/2}} d x$$

### Problem 567: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{1}{(a+b \sec [c+d x])^{3/2}} d x$$

Optimal (type 4, 347 leaves, 6 steps):

$$\frac{1}{a \sqrt{a+b} d} 2 \cot [c+d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} - \frac{1}{a \sqrt{a+b} d} 2 \cot [c+d x]$$

$$\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}}$$

$$\frac{1}{a^2 d} 2 \sqrt{a+b} \cot [c+d x] \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} + \frac{2 b^2 \tan [c+d x]}{a(a^2-b^2) d \sqrt{a+b \sec [c+d x]}}$$

Result (type 4, 1249 leaves):

$$\frac{(b + a \cos [c + d x])^2 \operatorname{Sec}[c + d x]^2 \left( \frac{2 b \sin [c + d x]}{a (-a^2 + b^2)} + \frac{2 b^2 \sin [c + d x]}{a (a^2 - b^2) (b + a \cos [c + d x])} \right)}{d (a + b \operatorname{Sec}[c + d x])^{3/2}} +$$

$$\left( 2 (b + a \cos [c + d x])^{3/2} \operatorname{Sec}[c + d x]^{3/2} \sqrt{\frac{a + b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2}{1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2}} \right.$$

$$\left( a b \sqrt{\frac{-a + b}{a + b}} \tan \left[ \frac{1}{2} (c + d x) \right] + b^2 \sqrt{\frac{-a + b}{a + b}} \tan \left[ \frac{1}{2} (c + d x) \right] - 2 a b \sqrt{\frac{-a + b}{a + b}} \right.$$

$$\tan \left[ \frac{1}{2} (c + d x) \right]^3 + a b \sqrt{\frac{-a + b}{a + b}} \tan \left[ \frac{1}{2} (c + d x) \right]^5 - b^2 \sqrt{\frac{-a + b}{a + b}} \tan \left[ \frac{1}{2} (c + d x) \right]^5 -$$

$$2 i a^2 \operatorname{EllipticPi} \left[ -\frac{a + b}{a - b}, i \operatorname{ArcSinh} \left[ \sqrt{\frac{-a + b}{a + b}} \tan \left[ \frac{1}{2} (c + d x) \right] \right], \frac{a + b}{a - b} \right]$$

$$\sqrt{1 - \tan \left[ \frac{1}{2} (c + d x) \right]^2} \sqrt{\frac{a + b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b}} +$$

$$2 i b^2 \operatorname{EllipticPi} \left[ -\frac{a + b}{a - b}, i \operatorname{ArcSinh} \left[ \sqrt{\frac{-a + b}{a + b}} \tan \left[ \frac{1}{2} (c + d x) \right] \right], \frac{a + b}{a - b} \right]$$

$$\sqrt{1 - \tan \left[ \frac{1}{2} (c + d x) \right]^2} \sqrt{\frac{a + b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b}} -$$

$$2 i a^2 \operatorname{EllipticPi} \left[ -\frac{a + b}{a - b}, i \operatorname{ArcSinh} \left[ \sqrt{\frac{-a + b}{a + b}} \tan \left[ \frac{1}{2} (c + d x) \right] \right], \frac{a + b}{a - b} \right] \tan \left[ \frac{1}{2} (c + d x) \right]^2$$

$$\sqrt{1 - \tan \left[ \frac{1}{2} (c + d x) \right]^2} \sqrt{\frac{a + b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b}} +$$

$$2 i b^2 \operatorname{EllipticPi} \left[ -\frac{a + b}{a - b}, i \operatorname{ArcSinh} \left[ \sqrt{\frac{-a + b}{a + b}} \tan \left[ \frac{1}{2} (c + d x) \right] \right], \frac{a + b}{a - b} \right] \tan \left[ \frac{1}{2} (c + d x) \right]^2$$

$$\sqrt{1 - \tan \left[ \frac{1}{2} (c + d x) \right]^2} \sqrt{\frac{a + b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b}} -$$

$$i (a - b) b \operatorname{EllipticE} \left[ i \operatorname{ArcSinh} \left[ \sqrt{\frac{-a + b}{a + b}} \tan \left[ \frac{1}{2} (c + d x) \right] \right], \frac{a + b}{a - b} \right] \sqrt{1 - \tan \left[ \frac{1}{2} (c + d x) \right]^2}$$

$$\begin{aligned}
 & \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \sqrt{\frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
 & i (a^2 + ab - 2b^2) \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right], \frac{a+b}{a-b} \right] \\
 & \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \\
 & \sqrt{\frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \Bigg) \Bigg) / \\
 & \left( a \sqrt{\frac{-a+b}{a+b}} (a^2 - b^2) d (a+b \operatorname{Sec}[c+dx])^{3/2} \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right. \\
 & \sqrt{\frac{1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}} \\
 & \left. \left( a \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right)
 \end{aligned}$$

**Problem 568: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Cos}[c+dx]}{(a+b \operatorname{Sec}[c+dx])^{3/2}} dx$$

Optimal (type 4, 396 leaves, 7 steps):

$$\frac{1}{a^2 b \sqrt{a+b} d} (a^2 - 3 b^2) \cot [c+d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} + \frac{1}{a^2 \sqrt{a+b} d} (a+3 b) \cot [c+d x]$$

$$\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} +$$

$$\frac{1}{a^3 d} 3 b \sqrt{a+b} \cot [c+d x] \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} +$$

$$\frac{\sin [c+d x]}{a d \sqrt{a+b \operatorname{Sec}[c+d x]}} + \frac{b\left(a^2-3 b^2\right) \tan [c+d x]}{a^2\left(a^2-b^2\right) d \sqrt{a+b \operatorname{Sec}[c+d x]}}$$

Result (type 4, 1077 leaves):

$$\left( (b+a \cos [c+d x])^2 \sec [c+d x]^2 \left( -\frac{2 b^2 \sin [c+d x]}{a^2\left(-a^2+b^2\right)} - \frac{2 b^3 \sin [c+d x]}{a^2\left(a^2-b^2\right)(b+a \cos [c+d x])} \right) \right) /$$

$$\left( d(a+b \operatorname{Sec}[c+d x])^{3/2} \right) - \left( (b+a \cos [c+d x])^{3/2} \sec [c+d x]^{3/2} \right.$$

$$\sqrt{\frac{1}{1-\tan \left[\frac{1}{2}(c+d x)\right]^2}} \sqrt{\frac{a+b-a \tan \left[\frac{1}{2}(c+d x)\right]^2+b \tan \left[\frac{1}{2}(c+d x)\right]^2}{1+\tan \left[\frac{1}{2}(c+d x)\right]^2}}$$

$$\left( a^3 \tan \left[\frac{1}{2}(c+d x)\right] + a^2 b \tan \left[\frac{1}{2}(c+d x)\right] - 3 a b^2 \tan \left[\frac{1}{2}(c+d x)\right] - \right.$$

$$3 b^3 \tan \left[\frac{1}{2}(c+d x)\right] - 2 a^3 \tan \left[\frac{1}{2}(c+d x)\right]^3 + 6 a b^2 \tan \left[\frac{1}{2}(c+d x)\right]^3 +$$

$$a^3 \tan \left[\frac{1}{2}(c+d x)\right]^5 - a^2 b \tan \left[\frac{1}{2}(c+d x)\right]^5 - 3 a b^2 \tan \left[\frac{1}{2}(c+d x)\right]^5 +$$

$$3 b^3 \tan \left[\frac{1}{2}(c+d x)\right]^5 + 6 a^2 b \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan \left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right]$$

$$\sqrt{1-\tan \left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \tan \left[\frac{1}{2}(c+d x)\right]^2+b \tan \left[\frac{1}{2}(c+d x)\right]^2}{a+b}} -$$

$$6 b^3 \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan \left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1-\tan \left[\frac{1}{2}(c+d x)\right]^2}$$

$$\begin{aligned}
 & \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}}+ \\
 & 6 a^2 b \operatorname{EllipticPi}\left[-1,-\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2 \\
 & \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}}- \\
 & 6 b^3 \operatorname{EllipticPi}\left[-1,-\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2 \\
 & \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}}+ \\
 & \left(a^3+a^2 b-3 a b^2-3 b^3\right) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \\
 & \left(1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right) \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}}+ \\
 & 2 a b(a+b) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \\
 & \left(1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right) \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}}\right) / \\
 & \left(a^2\left(a^2-b^2\right) d(a+b \operatorname{Sec}[c+d x])^{3 / 2} \sqrt{1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}\right. \\
 & \left.\left(a\left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right)-b\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right)\right)\right)
 \end{aligned}$$

**Problem 569: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Cos}[c+d x]^2}{(a+b \operatorname{Sec}[c+d x])^{3 / 2}} d x$$

Optimal (type 4, 470 leaves, 8 steps):

$$\begin{aligned}
& -\frac{1}{4a^3\sqrt{a+b}d}(7a^2-15b^2)\operatorname{Cot}[c+dx]\operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b\operatorname{Sec}[c+dx]}}{\sqrt{a+b}}\right],\frac{a+b}{a-b}\right] \\
& \sqrt{\frac{b(1-\operatorname{Sec}[c+dx])}{a+b}}\sqrt{-\frac{b(1+\operatorname{Sec}[c+dx])}{a-b}}+\frac{1}{4a^3\sqrt{a+b}d} \\
& (2a^2-5ab-15b^2)\operatorname{Cot}[c+dx]\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b\operatorname{Sec}[c+dx]}}{\sqrt{a+b}}\right],\frac{a+b}{a-b}\right] \\
& \sqrt{\frac{b(1-\operatorname{Sec}[c+dx])}{a+b}}\sqrt{-\frac{b(1+\operatorname{Sec}[c+dx])}{a-b}}-\frac{1}{4a^4d} \\
& \sqrt{a+b}(4a^2+15b^2)\operatorname{Cot}[c+dx]\operatorname{EllipticPi}\left[\frac{a+b}{a},\operatorname{ArcSin}\left[\frac{\sqrt{a+b\operatorname{Sec}[c+dx]}}{\sqrt{a+b}}\right],\frac{a+b}{a-b}\right] \\
& \sqrt{\frac{b(1-\operatorname{Sec}[c+dx])}{a+b}}\sqrt{-\frac{b(1+\operatorname{Sec}[c+dx])}{a-b}}-\frac{5b\operatorname{Sin}[c+dx]}{4a^2d\sqrt{a+b\operatorname{Sec}[c+dx]}}+ \\
& \frac{\operatorname{Cos}[c+dx]\operatorname{Sin}[c+dx]}{2ad\sqrt{a+b\operatorname{Sec}[c+dx]}}-\frac{b^2(7a^2-15b^2)\operatorname{Tan}[c+dx]}{4a^3(a^2-b^2)d\sqrt{a+b\operatorname{Sec}[c+dx]}}
\end{aligned}$$

Result (type 4, 1745 leaves):

$$\begin{aligned}
& \left( (b+a\operatorname{Cos}[c+dx])^2\operatorname{Sec}[c+dx]^2 \right. \\
& \left. \left( \frac{2b^3\operatorname{Sin}[c+dx]}{a^3(-a^2+b^2)} + \frac{2b^4\operatorname{Sin}[c+dx]}{a^3(a^2-b^2)(b+a\operatorname{Cos}[c+dx])} + \frac{\operatorname{Sin}[2(c+dx)]}{4a^2} \right) \right) / \\
& (d(a+b\operatorname{Sec}[c+dx])^{3/2}) + \\
& \left( (b+a\operatorname{Cos}[c+dx])^{3/2}\operatorname{Sec}[c+dx]^{3/2} \sqrt{\frac{a+b-a\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}} \right. \\
& \left. \left( -7a^3b\sqrt{\frac{-a+b}{a+b}}\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] - 7a^2b^2\sqrt{\frac{-a+b}{a+b}}\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \right. \\
& \left. \left. 15a^3b^3\sqrt{\frac{-a+b}{a+b}}\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + 15b^4\sqrt{\frac{-a+b}{a+b}}\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \right. \\
& \left. \left. 14a^3b\sqrt{\frac{-a+b}{a+b}}\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^3 - 30a^3b^3\sqrt{\frac{-a+b}{a+b}}\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^3 - \right. \right. \\
& \left. \left. 7a^3b\sqrt{\frac{-a+b}{a+b}}\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^5 + 7a^2b^2\sqrt{\frac{-a+b}{a+b}}\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^5 + \right. \right.
\end{aligned}$$

$$15 a b^3 \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^5 - 15 b^4 \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^5 -$$

$$8 i a^4 \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} -$$

$$22 i a^2 b^2 \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} +$$

$$30 i b^4 \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right]$$

$$\sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} -$$

$$8 i a^4 \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2$$

$$\sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - 22 i a^2 b^2$$

$$\operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2$$

$$\sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} +$$

$$30 i b^4 \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2$$

$$\sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} +$$

$$\begin{aligned}
 & i b (7 a^3 - 7 a^2 b - 15 a b^2 + 15 b^3) \text{EllipticE}\left[i \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \\
 & \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + 2 i (2 a^4 - a^3 b + 9 a^2 b^2 + 5 a b^3 - 15 b^4) \\
 & \text{EllipticF}\left[i \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \\
 & \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \right) / \\
 & \left(4 a^3 \sqrt{\frac{-a+b}{a+b}} (a^2 - b^2) d (a + b \text{Sec}[c+dx])^{3/2} \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \right. \\
 & \left. \sqrt{\frac{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2}} \right. \\
 & \left. \left(a \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) - b \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)\right) \right)
 \end{aligned}$$

**Problem 570: Unable to integrate problem.**

$$\int \frac{\text{Sec}[c+dx]^5}{(a+b \text{Sec}[c+dx])^{5/2}} dx$$

Optimal (type 4, 427 leaves, 6 steps):



$$\begin{aligned}
 & \left( 8 a (4 a^4 - 7 a^2 b^2 + 2 b^4) \cot [c + d x] \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{a + b \operatorname{Sec} [c + d x]}}{\sqrt{a + b}} \right], \frac{a + b}{a - b} \right] \right. \\
 & \quad \left. \sqrt{\frac{b (1 - \operatorname{Sec} [c + d x])}{a + b}} \sqrt{-\frac{b (1 + \operatorname{Sec} [c + d x])}{a - b}} \right) / (3 (a - b) b^5 (a + b)^{3/2} d) + \\
 & \left( 2 (16 a^4 + 12 a^3 b - 16 a^2 b^2 - 9 a b^3 - b^4) \cot [c + d x] \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{a + b \operatorname{Sec} [c + d x]}}{\sqrt{a + b}} \right], \right. \right. \\
 & \quad \left. \left. \frac{a + b}{a - b} \right] \sqrt{\frac{b (1 - \operatorname{Sec} [c + d x])}{a + b}} \sqrt{-\frac{b (1 + \operatorname{Sec} [c + d x])}{a - b}} \right) / (3 (a - b) b^4 (a + b)^{3/2} d) - \\
 & \quad \frac{2 a^2 \operatorname{Sec} [c + d x]^2 \operatorname{Tan} [c + d x]}{3 b (a^2 - b^2) d (a + b \operatorname{Sec} [c + d x])^{3/2}} + \frac{4 a^3 (3 a^2 - 5 b^2) \operatorname{Tan} [c + d x]}{3 b^3 (a^2 - b^2)^2 d \sqrt{a + b \operatorname{Sec} [c + d x]}} + \\
 & \quad \frac{2 (2 a^2 - b^2) \sqrt{a + b \operatorname{Sec} [c + d x]} \operatorname{Tan} [c + d x]}{3 b^3 (a^2 - b^2) d}
 \end{aligned}$$

Result (type 8, 25 leaves):

$$\int \frac{\operatorname{Sec} [c + d x]^5}{(a + b \operatorname{Sec} [c + d x])^{5/2}} dx$$

**Problem 571: Unable to integrate problem.**

$$\int \frac{\operatorname{Sec} [c + d x]^4}{(a + b \operatorname{Sec} [c + d x])^{5/2}} dx$$

Optimal (type 4, 362 leaves, 5 steps):

$$\begin{aligned}
& - \left( \left( 2 (8 a^4 - 15 a^2 b^2 + 3 b^4) \operatorname{Cot}[c + d x] \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{a + b \operatorname{Sec}[c + d x]}}{\sqrt{a + b}} \right], \frac{a + b}{a - b} \right] \right. \right. \\
& \quad \left. \left. \sqrt{\frac{b (1 - \operatorname{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b (1 + \operatorname{Sec}[c + d x])}{a - b}} \right) / (3 (a - b) b^4 (a + b)^{3/2} d) \right) - \\
& \left( 2 (8 a^3 + 6 a^2 b - 9 a b^2 - 3 b^3) \operatorname{Cot}[c + d x] \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{a + b \operatorname{Sec}[c + d x]}}{\sqrt{a + b}} \right], \frac{a + b}{a - b} \right] \right. \\
& \quad \left. \sqrt{\frac{b (1 - \operatorname{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b (1 + \operatorname{Sec}[c + d x])}{a - b}} \right) / (3 (a - b) b^3 (a + b)^{3/2} d) - \\
& \frac{2 a^2 \operatorname{Sec}[c + d x] \operatorname{Tan}[c + d x]}{3 b (a^2 - b^2) d (a + b \operatorname{Sec}[c + d x])^{3/2}} - \frac{8 a^2 (a^2 - 2 b^2) \operatorname{Tan}[c + d x]}{3 b^2 (a^2 - b^2)^2 d \sqrt{a + b \operatorname{Sec}[c + d x]}}
\end{aligned}$$

Result (type 8, 25 leaves):

$$\int \frac{\operatorname{Sec}[c + d x]^4}{(a + b \operatorname{Sec}[c + d x])^{5/2}} dx$$

**Problem 572: Unable to integrate problem.**

$$\int \frac{\operatorname{Sec}[c + d x]^3}{(a + b \operatorname{Sec}[c + d x])^{5/2}} dx$$

Optimal (type 4, 337 leaves, 5 steps):

$$\begin{aligned}
& \left( 4 a (a^2 - 3 b^2) \operatorname{Cot}[c + d x] \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{a + b \operatorname{Sec}[c + d x]}}{\sqrt{a + b}} \right], \frac{a + b}{a - b} \right] \right. \\
& \quad \left. \sqrt{\frac{b (1 - \operatorname{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b (1 + \operatorname{Sec}[c + d x])}{a - b}} \right) / (3 (a - b) b^3 (a + b)^{3/2} d) + \\
& \left( 2 (2 a^2 + 3 a b - 3 b^2) \operatorname{Cot}[c + d x] \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{a + b \operatorname{Sec}[c + d x]}}{\sqrt{a + b}} \right], \frac{a + b}{a - b} \right] \right. \\
& \quad \left. \sqrt{\frac{b (1 - \operatorname{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b (1 + \operatorname{Sec}[c + d x])}{a - b}} \right) / (3 (a - b) b^2 (a + b)^{3/2} d) - \\
& \frac{2 a^2 \operatorname{Tan}[c + d x]}{3 b (a^2 - b^2) d (a + b \operatorname{Sec}[c + d x])^{3/2}} + \frac{4 a (a^2 - 3 b^2) \operatorname{Tan}[c + d x]}{3 b (a^2 - b^2)^2 d \sqrt{a + b \operatorname{Sec}[c + d x]}}
\end{aligned}$$

Result (type 8, 25 leaves):

$$\int \frac{\text{Sec}[c + d x]^3}{(a + b \text{Sec}[c + d x])^{5/2}} dx$$

Problem 573: Unable to integrate problem.

$$\int \frac{\text{Sec}[c + d x]^2}{(a + b \text{Sec}[c + d x])^{5/2}} dx$$

Optimal (type 4, 317 leaves, 5 steps):

$$\left( 2 (a^2 + 3 b^2) \text{Cot}[c + d x] \text{EllipticE}\left[\text{ArcSin}\left[\frac{\sqrt{a + b \text{Sec}[c + d x]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \right. \\ \left. \sqrt{\frac{b (1 - \text{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b (1 + \text{Sec}[c + d x])}{a - b}} \right) / (3 (a - b) b^2 (a + b)^{3/2} d) + \\ \left( 2 (a - 3 b) \text{Cot}[c + d x] \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{a + b \text{Sec}[c + d x]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \right. \\ \left. \sqrt{\frac{b (1 - \text{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b (1 + \text{Sec}[c + d x])}{a - b}} \right) / (3 (a - b) b (a + b)^{3/2} d) + \\ \frac{2 a \text{Tan}[c + d x]}{3 (a^2 - b^2) d (a + b \text{Sec}[c + d x])^{3/2}} + \frac{2 (a^2 + 3 b^2) \text{Tan}[c + d x]}{3 (a^2 - b^2)^2 d \sqrt{a + b \text{Sec}[c + d x]}}$$

Result (type 8, 25 leaves):

$$\int \frac{\text{Sec}[c + d x]^2}{(a + b \text{Sec}[c + d x])^{5/2}} dx$$

Problem 574: Unable to integrate problem.

$$\int \frac{\text{Sec}[c + d x]}{(a + b \text{Sec}[c + d x])^{5/2}} dx$$

Optimal (type 4, 304 leaves, 5 steps):

$$\begin{aligned}
 & - \left( \left( 8 a \cot [c+d x] \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}} \right], \frac{a+b}{a-b} \right] \right. \right. \\
 & \quad \left. \left. \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} \right] / \left( 3(a-b) b(a+b)^{3/2} d \right) \right) + \\
 & \left( 2(3 a-b) \cot [c+d x] \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}} \right], \frac{a+b}{a-b} \right] \right. \\
 & \quad \left. \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} \right] / \left( 3(a-b) b(a+b)^{3/2} d \right) - \\
 & \frac{2 b \tan [c+d x]}{3\left(a^2-b^2\right) d(a+b \operatorname{Sec}[c+d x])^{3/2}} - \frac{8 a b \tan [c+d x]}{3\left(a^2-b^2\right)^2 d \sqrt{a+b \operatorname{Sec}[c+d x]}}
 \end{aligned}$$

Result (type 8, 23 leaves):

$$\int \frac{\operatorname{Sec}[c+d x]}{(a+b \operatorname{Sec}[c+d x])^{5/2}} dx$$

**Problem 575: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{1}{(a+b \operatorname{Sec}[c+d x])^{5/2}} dx$$

Optimal (type 4, 448 leaves, 7 steps):

$$\begin{aligned}
 & \left( 2 (7 a^2 - 3 b^2) \cot [c + d x] \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{a + b \operatorname{Sec} [c + d x]}}{\sqrt{a + b}} \right], \frac{a + b}{a - b} \right] \right. \\
 & \quad \left. \sqrt{\frac{b (1 - \operatorname{Sec} [c + d x])}{a + b}} \sqrt{-\frac{b (1 + \operatorname{Sec} [c + d x])}{a - b}} \right) / (3 a^2 (a - b) (a + b)^{3/2} d) - \\
 & \left( 2 (6 a^2 - a b - 3 b^2) \cot [c + d x] \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{a + b \operatorname{Sec} [c + d x]}}{\sqrt{a + b}} \right], \frac{a + b}{a - b} \right] \right. \\
 & \quad \left. \sqrt{\frac{b (1 - \operatorname{Sec} [c + d x])}{a + b}} \sqrt{-\frac{b (1 + \operatorname{Sec} [c + d x])}{a - b}} \right) / (3 a^2 (a - b) (a + b)^{3/2} d) - \\
 & \frac{1}{a^3 d} 2 \sqrt{a + b} \cot [c + d x] \operatorname{EllipticPi} \left[ \frac{a + b}{a}, \operatorname{ArcSin} \left[ \frac{\sqrt{a + b \operatorname{Sec} [c + d x]}}{\sqrt{a + b}} \right], \frac{a + b}{a - b} \right] \\
 & \quad \sqrt{\frac{b (1 - \operatorname{Sec} [c + d x])}{a + b}} \sqrt{-\frac{b (1 + \operatorname{Sec} [c + d x])}{a - b}} + \\
 & \quad \frac{2 b^2 \tan [c + d x]}{3 a (a^2 - b^2) d (a + b \operatorname{Sec} [c + d x])^{3/2}} + \frac{2 b^2 (7 a^2 - 3 b^2) \tan [c + d x]}{3 a^2 (a^2 - b^2)^2 d \sqrt{a + b \operatorname{Sec} [c + d x]}}
 \end{aligned}$$

Result (type 4, 1798 leaves):

$$\begin{aligned}
 & \left( (b + a \cos [c + d x])^3 \sec [c + d x]^3 \right. \\
 & \quad \left( \frac{2 b (-7 a^2 + 3 b^2) \sin [c + d x]}{3 a^2 (-a^2 + b^2)^2} - \frac{2 b^3 \sin [c + d x]}{3 a^2 (a^2 - b^2) (b + a \cos [c + d x])^2} - \right. \\
 & \quad \left. \left. \frac{8 (-2 a^2 b^2 \sin [c + d x] + b^4 \sin [c + d x])}{3 a^2 (a^2 - b^2)^2 (b + a \cos [c + d x])} \right) \right) / (d (a + b \sec [c + d x])^{5/2}) + \\
 & \left( 2 (b + a \cos [c + d x])^{5/2} \sec [c + d x]^{5/2} \sqrt{\frac{a + b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2}{1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2}} \right. \\
 & \quad \left( 7 a^3 b \sqrt{\frac{-a + b}{a + b}} \tan \left[ \frac{1}{2} (c + d x) \right] + 7 a^2 b^2 \sqrt{\frac{-a + b}{a + b}} \tan \left[ \frac{1}{2} (c + d x) \right] - \right. \\
 & \quad \left. 3 a b^3 \sqrt{\frac{-a + b}{a + b}} \tan \left[ \frac{1}{2} (c + d x) \right] - 3 b^4 \sqrt{\frac{-a + b}{a + b}} \tan \left[ \frac{1}{2} (c + d x) \right] - \right.
 \end{aligned}$$

$$\begin{aligned}
& 14 a^3 b \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^3 + 6 a b^3 \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^3 + \\
& 7 a^3 b \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^5 - 7 a^2 b^2 \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^5 - \\
& 3 a b^3 \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^5 + 3 b^4 \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^5 - \\
& 6 i a^4 \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \\
& \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
& 12 i a^2 b^2 \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \\
& \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 6 i b^4 \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \\
& \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 6 i a^4 \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \\
& \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + 12 i a^2 b^2 \\
& \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \\
& \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} -
\end{aligned}$$

$$\begin{aligned}
 & 6 i b^4 \text{EllipticPi}\left[-\frac{a+b}{a-b}, i \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 & i b (7 a^3 - 7 a^2 b - 3 a b^2 + 3 b^3) \text{EllipticE}\left[i \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \\
 & \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + i (3 a^4 + 6 a^3 b - 13 a^2 b^2 - 2 a b^3 + 6 b^4) \\
 & \text{EllipticF}\left[i \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \\
 & \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \right) \Bigg) / \\
 & \left(3 a^2 \sqrt{\frac{-a+b}{a+b}} (a^2 - b^2)^2 d (a+b \text{Sec}[c+dx])^{5/2} \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \right. \\
 & \left. \sqrt{\frac{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2}} \right. \\
 & \left. \left(a \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) - b \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)\right) \right)
 \end{aligned}$$

**Problem 576: Result more than twice size of optimal antiderivative.**

$$\int \frac{\cos[c+dx]}{(a+b \text{Sec}[c+dx])^{5/2}} dx$$

Optimal (type 4, 510 leaves, 8 steps):

$$\left( (3 a^4 - 26 a^2 b^2 + 15 b^4) \operatorname{Cot}[c + d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a + b \operatorname{Sec}[c + d x]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \right. \\ \left. \sqrt{\frac{b(1 - \operatorname{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b(1 + \operatorname{Sec}[c + d x])}{a - b}} \right) / (3 a^3 (a - b) b (a + b)^{3/2} d) + \\ \left( (3 a^3 + 21 a^2 b - 5 a b^2 - 15 b^3) \operatorname{Cot}[c + d x] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a + b \operatorname{Sec}[c + d x]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \right. \\ \left. \sqrt{\frac{b(1 - \operatorname{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b(1 + \operatorname{Sec}[c + d x])}{a - b}} \right) / (3 a^3 (a - b) (a + b)^{3/2} d) + \\ \frac{1}{a^4 d} 5 b \sqrt{a + b} \operatorname{Cot}[c + d x] \operatorname{EllipticPi}\left[\frac{a + b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a + b \operatorname{Sec}[c + d x]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \\ \sqrt{\frac{b(1 - \operatorname{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b(1 + \operatorname{Sec}[c + d x])}{a - b}} + \frac{\operatorname{Sin}[c + d x]}{a d (a + b \operatorname{Sec}[c + d x])^{3/2}} + \\ \frac{b(3 a^2 - 5 b^2) \operatorname{Tan}[c + d x]}{3 a^2 (a^2 - b^2) d (a + b \operatorname{Sec}[c + d x])^{3/2}} + \frac{b(3 a^4 - 26 a^2 b^2 + 15 b^4) \operatorname{Tan}[c + d x]}{3 a^3 (a^2 - b^2)^2 d \sqrt{a + b \operatorname{Sec}[c + d x]}}$$

Result (type 4, 1493 leaves):

$$\left( (b + a \operatorname{Cos}[c + d x])^3 \operatorname{Sec}[c + d x]^3 \left( -\frac{4 b^2 (-5 a^2 + 3 b^2) \operatorname{Sin}[c + d x]}{3 a^3 (-a^2 + b^2)^2} + \right. \right. \\ \left. \frac{2 b^4 \operatorname{Sin}[c + d x]}{3 a^3 (a^2 - b^2) (b + a \operatorname{Cos}[c + d x])^2} + \frac{2 (-11 a^2 b^3 \operatorname{Sin}[c + d x] + 7 b^5 \operatorname{Sin}[c + d x])}{3 a^3 (a^2 - b^2)^2 (b + a \operatorname{Cos}[c + d x])} \right) \Big) / \\ (d (a + b \operatorname{Sec}[c + d x])^{5/2}) - \left( (b + a \operatorname{Cos}[c + d x])^{5/2} \operatorname{Sec}[c + d x]^{5/2} \right. \\ \left. \sqrt{\frac{1}{1 - \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}} \sqrt{\frac{a + b - a \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}} \right) \\ \left( 3 a^5 \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] + 3 a^4 b \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] - 26 a^3 b^2 \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] - \right. \\ \left. 26 a^2 b^3 \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] + 15 a b^4 \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] + 15 b^5 \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] - \right. \\ \left. 6 a^5 \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^3 + 52 a^3 b^2 \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^3 - 30 a b^4 \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^3 + \right.$$



$$\begin{aligned}
 & 3 a^5 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 - 3 a^4 b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 - 26 a^3 b^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 + \\
 & 26 a^2 b^3 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 + 15 a b^4 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 - 15 b^5 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 + \\
 & 30 a^4 b \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \\
 & \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} - \\
 & 60 a^2 b^3 \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \\
 & \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} + \\
 & 30 b^5 \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \\
 & \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} + \\
 & 30 a^4 b \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2 \\
 & \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} - \\
 & 60 a^2 b^3 \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2 \\
 & \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} + \\
 & 30 b^5 \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2 \\
 & \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} + \\
 & (3 a^5+3 a^4 b-26 a^3 b^2-26 a^2 b^3+15 a b^4+15 b^5) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \\
 & \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right) \\
 & \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}}+2 a b\left(6 a^3+9 a^2 b-2 a b^2-5 b^3\right)
 \end{aligned}$$

$$\begin{aligned} & \text{EllipticF}\left[\text{ArcSin}\left[\text{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1-\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \\ & \left(1+\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b-a\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \right) \Bigg) \Bigg) / \\ & \left(3a(a^3-ab^2)^2 d (a+b \text{Sec}[c+dx])^{5/2} \sqrt{1+\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \right. \\ & \left. \left(a\left(-1+\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)-b\left(1+\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)\right)\right) \end{aligned}$$

**Problem 577: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\text{Cos}[c+dx]^2}{(a+b \text{Sec}[c+dx])^{5/2}} dx$$

Optimal (type 4, 562 leaves, 9 steps):

$$\begin{aligned}
 & - \left( \left( (33 a^4 - 170 a^2 b^2 + 105 b^4) \operatorname{Cot}[c + d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a + b \operatorname{Sec}[c + d x]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \right. \right. \\
 & \quad \left. \left. \sqrt{\frac{b(1 - \operatorname{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b(1 + \operatorname{Sec}[c + d x])}{a - b}} \right) / (12 a^4 (a - b) (a + b)^{3/2} d) \right) + \\
 & \left( (a + 3 b) (6 a^3 - 45 a^2 b + 35 b^3) \operatorname{Cot}[c + d x] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a + b \operatorname{Sec}[c + d x]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \right. \\
 & \quad \left. \sqrt{\frac{b(1 - \operatorname{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b(1 + \operatorname{Sec}[c + d x])}{a - b}} \right) / (12 a^4 (a - b) (a + b)^{3/2} d) - \frac{1}{4 a^5 d} \\
 & \sqrt{a + b} (4 a^2 + 35 b^2) \operatorname{Cot}[c + d x] \operatorname{EllipticPi}\left[\frac{a + b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a + b \operatorname{Sec}[c + d x]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \\
 & \quad \sqrt{\frac{b(1 - \operatorname{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b(1 + \operatorname{Sec}[c + d x])}{a - b}} - \\
 & \quad \frac{7 b \operatorname{Sin}[c + d x]}{4 a^2 d (a + b \operatorname{Sec}[c + d x])^{3/2}} + \frac{\operatorname{Cos}[c + d x] \operatorname{Sin}[c + d x]}{2 a d (a + b \operatorname{Sec}[c + d x])^{3/2}} - \\
 & \quad \frac{b^2 (27 a^2 - 35 b^2) \operatorname{Tan}[c + d x]}{12 a^3 (a^2 - b^2) d (a + b \operatorname{Sec}[c + d x])^{3/2}} - \\
 & \quad \frac{b^2 (33 a^4 - 170 a^2 b^2 + 105 b^4) \operatorname{Tan}[c + d x]}{12 a^4 (a^2 - b^2)^2 d \sqrt{a + b \operatorname{Sec}[c + d x]}}
 \end{aligned}$$

Result(type 4, 2285 leaves):

$$\begin{aligned}
 & \left( (b + a \operatorname{Cos}[c + d x])^3 \operatorname{Sec}[c + d x]^3 \right. \\
 & \quad \left( \frac{2 b^3 (-13 a^2 + 9 b^2) \operatorname{Sin}[c + d x]}{3 a^4 (-a^2 + b^2)^2} - \frac{2 b^5 \operatorname{Sin}[c + d x]}{3 a^4 (a^2 - b^2) (b + a \operatorname{Cos}[c + d x])^2} - \right. \\
 & \quad \left. \frac{4 (-7 a^2 b^4 \operatorname{Sin}[c + d x] + 5 b^6 \operatorname{Sin}[c + d x])}{3 a^4 (a^2 - b^2)^2 (b + a \operatorname{Cos}[c + d x])} + \frac{\operatorname{Sin}[2(c + d x)]}{4 a^3} \right) \Bigg) / \\
 & \left( d (a + b \operatorname{Sec}[c + d x])^{5/2} \right) - \left( (b + a \operatorname{Cos}[c + d x])^{5/2} \operatorname{Sec}[c + d x]^{5/2} \right. \\
 & \quad \left. \sqrt{\frac{a + b - a \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}} \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( 33 a^5 b \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + 33 a^4 b^2 \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] - \right. \\
 & 170 a^3 b^3 \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] - 170 a^2 b^4 \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + 105 a b^5 \sqrt{\frac{-a+b}{a+b}} \\
 & \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + 105 b^6 \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] - 66 a^5 b \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^3 + \\
 & 340 a^3 b^3 \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^3 - 210 a b^5 \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^3 + \\
 & 33 a^5 b \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^5 - 33 a^4 b^2 \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^5 - \\
 & 170 a^3 b^3 \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^5 + 170 a^2 b^4 \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^5 + \\
 & 105 a b^5 \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^5 - 105 b^6 \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^5 + \\
 & 24 i a^6 \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
 & 162 i a^4 b^2 \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 & 396 i a^2 b^4 \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} +
 \end{aligned}$$

$$\begin{aligned}
 & 210 i b^6 \text{EllipticPi}\left[-\frac{a+b}{a-b}, i \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
 & 24 i a^6 \text{EllipticPi}\left[-\frac{a+b}{a-b}, i \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + 162 i a^4 b^2 \\
 & \text{EllipticPi}\left[-\frac{a+b}{a-b}, i \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - 396 i a^2 b^4 \\
 & \text{EllipticPi}\left[-\frac{a+b}{a-b}, i \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + 210 i b^6 \\
 & \text{EllipticPi}\left[-\frac{a+b}{a-b}, i \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
 & i b (-33 a^5 + 33 a^4 b + 170 a^3 b^2 - 170 a^2 b^3 - 105 a b^4 + 105 b^5) \\
 & \text{EllipticE}\left[i \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \\
 & \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 & 2 i (6 a^6 - 3 a^5 b + 57 a^4 b^2 + 54 a^3 b^3 - 184 a^2 b^4 - 35 a b^5 + 105 b^6) \\
 & \text{EllipticF}\left[i \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2}
 \end{aligned}$$

$$\left( \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \right) \right) /$$

$$\left( 12 a^4 \sqrt{\frac{-a+b}{a+b}} (a^2 - b^2)^2 d (a+b \sec[c+dx])^{5/2} \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right.$$

$$\sqrt{\frac{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2}} \left. \left( a \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right)$$

**Problem 578: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{1}{(a+b \sec[c+dx])^{7/2}} dx$$

Optimal (type 4, 535 leaves, 8 steps):

$$\begin{aligned}
 & \left( 2 (58 a^4 - 41 a^2 b^2 + 15 b^4) \cot [c + d x] \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{a + b \operatorname{Sec} [c + d x]}}{\sqrt{a + b}} \right], \frac{a + b}{a - b} \right] \right. \\
 & \quad \left. \sqrt{\frac{b (1 - \operatorname{Sec} [c + d x])}{a + b}} \sqrt{-\frac{b (1 + \operatorname{Sec} [c + d x])}{a - b}} \right) / (15 a^3 (a - b)^2 (a + b)^{5/2} d) - \\
 & \left( 2 (45 a^4 - 13 a^3 b - 36 a^2 b^2 + 5 a b^3 + 15 b^4) \cot [c + d x] \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{a + b \operatorname{Sec} [c + d x]}}{\sqrt{a + b}} \right], \right. \right. \\
 & \quad \left. \left. \frac{a + b}{a - b} \right] \sqrt{\frac{b (1 - \operatorname{Sec} [c + d x])}{a + b}} \sqrt{-\frac{b (1 + \operatorname{Sec} [c + d x])}{a - b}} \right) / (15 a^3 (a - b)^2 (a + b)^{5/2} d) - \\
 & \frac{1}{a^4 d} 2 \sqrt{a + b} \cot [c + d x] \operatorname{EllipticPi} \left[ \frac{a + b}{a}, \operatorname{ArcSin} \left[ \frac{\sqrt{a + b \operatorname{Sec} [c + d x]}}{\sqrt{a + b}} \right], \frac{a + b}{a - b} \right] \\
 & \quad \sqrt{\frac{b (1 - \operatorname{Sec} [c + d x])}{a + b}} \sqrt{-\frac{b (1 + \operatorname{Sec} [c + d x])}{a - b}} + \\
 & \quad \frac{2 b^2 \tan [c + d x]}{5 a (a^2 - b^2) d (a + b \operatorname{Sec} [c + d x])^{5/2}} + \frac{2 b^2 (13 a^2 - 5 b^2) \tan [c + d x]}{15 a^2 (a^2 - b^2)^2 d (a + b \operatorname{Sec} [c + d x])^{3/2}} + \\
 & \quad \frac{2 b^2 (58 a^4 - 41 a^2 b^2 + 15 b^4) \tan [c + d x]}{15 a^3 (a^2 - b^2)^3 d \sqrt{a + b \operatorname{Sec} [c + d x]}}
 \end{aligned}$$

Result (type 4, 2346 leaves):

$$\begin{aligned}
 & \left( (b + a \cos [c + d x])^4 \sec [c + d x]^4 \left( \frac{2 b (58 a^4 - 41 a^2 b^2 + 15 b^4) \sin [c + d x]}{15 a^3 (-a^2 + b^2)^3} + \right. \right. \\
 & \quad \frac{2 b^4 \sin [c + d x]}{5 a^3 (a^2 - b^2) (b + a \cos [c + d x])^3} + \frac{2 (-19 a^2 b^3 \sin [c + d x] + 11 b^5 \sin [c + d x])}{15 a^3 (a^2 - b^2)^2 (b + a \cos [c + d x])^2} + \\
 & \quad \left. \left. (2 (74 a^4 b^2 \sin [c + d x] - 65 a^2 b^4 \sin [c + d x] + 23 b^6 \sin [c + d x])) / \right. \right. \\
 & \quad \left. \left. (15 a^3 (a^2 - b^2)^3 (b + a \cos [c + d x])) \right) \right) / (d (a + b \sec [c + d x])^{7/2}) + \\
 & \left( 2 (b + a \cos [c + d x])^{7/2} \sec [c + d x]^{7/2} \sqrt{\frac{a + b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2}{1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2}} \right. \\
 & \quad \left. \left( 58 a^5 b \sqrt{\frac{-a + b}{a + b}} \tan \left[ \frac{1}{2} (c + d x) \right] + 58 a^4 b^2 \sqrt{\frac{-a + b}{a + b}} \tan \left[ \frac{1}{2} (c + d x) \right] \right) - \right.
 \end{aligned}$$

$$\begin{aligned}
 & 41 a^3 b^3 \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] - 41 a^2 b^4 \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + 15 a b^5 \sqrt{\frac{-a+b}{a+b}} \\
 & \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + 15 b^6 \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] - 116 a^5 b \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^3 + \\
 & 82 a^3 b^3 \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^3 - 30 a b^5 \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^3 + \\
 & 58 a^5 b \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^5 - 58 a^4 b^2 \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^5 - \\
 & 41 a^3 b^3 \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^5 + 41 a^2 b^4 \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^5 + \\
 & 15 a b^5 \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^5 - 15 b^6 \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^5 - \\
 & 30 i a^6 \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
 & 90 i a^4 b^2 \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 & 90 i a^2 b^4 \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
 & 30 i b^6 \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} -
 \end{aligned}$$



$$\begin{aligned}
 & 30 \, i \, a^6 \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + 90 \, i \, a^4 b^2 \\
 & \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - 90 \, i \, a^2 b^4 \\
 & \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
 & 30 \, i \, b^6 \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
 & i \, b \, (-58 a^5 + 58 a^4 b + 41 a^3 b^2 - 41 a^2 b^3 - 15 a b^4 + 15 b^5) \\
 & \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \\
 & \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)^2 \sqrt{\frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
 & i \, (15 a^6 + 45 a^5 b - 103 a^4 b^2 - 23 a^3 b^3 + 86 a^2 b^4 + 10 a b^5 - 30 b^6) \\
 & \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \\
 & \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)^2 \sqrt{\frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \Bigg) /
 \end{aligned}$$

$$\left( 15 a^3 \sqrt{\frac{-a+b}{a+b}} (a^2 - b^2)^3 d (a + b \operatorname{Sec}[c + d x])^{7/2} \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2 \right) \sqrt{\frac{1 + \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}{1 - \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}} \left( a \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2 \right) - b \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2 \right) \right) \right)$$

**Problem 615: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec}[c + d x]^{7/2}}{(a + b \operatorname{Sec}[c + d x])^2} dx$$

Optimal (type 4, 279 leaves, 10 steps):

$$\begin{aligned} & - \frac{1}{b^2 (a^2 - b^2) d} (3 a^2 - 2 b^2) \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]} - \\ & \frac{a \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]}}{b (a^2 - b^2) d} - \\ & \left( a (3 a^2 - 5 b^2) \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticPi}\left[\frac{2 a}{a + b}, \frac{1}{2}(c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]} \right) / \\ & \left( (a - b) b^2 (a + b)^2 d \right) + \frac{(3 a^2 - 2 b^2) \sqrt{\operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{b^2 (a^2 - b^2) d} - \frac{a^2 \operatorname{Sec}[c + d x]^{3/2} \operatorname{Sin}[c + d x]}{b (a^2 - b^2) d (a + b \operatorname{Sec}[c + d x])} \end{aligned}$$

Result (type 4, 632 leaves):

$$\frac{\sqrt{\sec [c+d x]}\left(\frac{(-3 a^2+2 b^2) \sin [c+d x]}{b^2\left(-a^2+b^2\right)}+\frac{a^2 \sin [c+d x]}{b\left(-a^2+b^2\right)(b+a \cos [c+d x])}\right)}{d}-$$

$$\frac{1}{4(a-b) b^2(a+b) d}\left(-\left(\left(2\left(8 a^2 b-4 b^3\right) \cos [c+d x]^2\right.\right.\right.$$

$$\left.\left.\left.\text{EllipticPi}\left[-\frac{b}{a},-\text{ArcSin}\left[\sqrt{\sec [c+d x]}\right],-1\right](a+b \sec [c+d x])\right.\right.\right.$$

$$\left.\left.\left.\sqrt{1-\sec [c+d x]^2} \sin [c+d x]\right)\right) / (a(b+a \cos [c+d x])\left(1-\cos [c+d x]^2\right)\right))+$$

$$\left(2\left(9 a^3-10 a b^2\right) \cos [c+d x]^2\left(\text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\sec [c+d x]}\right],-1\right]+$$

$$\left.\text{EllipticPi}\left[-\frac{b}{a},-\text{ArcSin}\left[\sqrt{\sec [c+d x]}\right],-1\right]\right)(a+b \sec [c+d x])\right.$$

$$\left.\sqrt{1-\sec [c+d x]^2} \sin [c+d x]\right) / (b(b+a \cos [c+d x])\left(1-\cos [c+d x]^2\right))-$$

$$\left(2\left(3 a^3-2 a b^2\right) \cos [2(c+d x)](a+b \sec [c+d x])\left(2 a b-2 a b \sec [c+d x]^2+\right.\right.$$

$$\left.\left.2 a b \text{EllipticE}\left[\text{ArcSin}\left[\sqrt{\sec [c+d x]}\right],-1\right] \sqrt{\sec [c+d x]} \sqrt{1-\sec [c+d x]^2}+\right.\right.$$

$$\left.\left.a(a-2 b) \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\sec [c+d x]}\right],-1\right] \sqrt{\sec [c+d x]} \sqrt{1-\sec [c+d x]^2}+\right.\right.$$

$$\left.\left.a^2 \text{EllipticPi}\left[-\frac{b}{a},-\text{ArcSin}\left[\sqrt{\sec [c+d x]}\right],-1\right] \sqrt{\sec [c+d x]} \sqrt{1-\sec [c+d x]^2}-\right.\right.$$

$$\left.\left.2 b^2 \text{EllipticPi}\left[-\frac{b}{a},-\text{ArcSin}\left[\sqrt{\sec [c+d x]}\right],-1\right] \sqrt{\sec [c+d x]} \sqrt{1-\sec [c+d x]^2}\right)$$

$$\left.\sin [c+d x]\right) / \left(a^2 b(b+a \cos [c+d x])\left(1-\cos [c+d x]^2\right)\right.$$

$$\left.\sqrt{\sec [c+d x]}\left(2-\sec [c+d x]^2\right)\right)$$

**Problem 616: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sec [c+d x]^{5 / 2}}{(a+b \sec [c+d x])^2} d x$$

Optimal (type 4, 214 leaves, 9 steps):

$$\frac{a \sqrt{\cos [c+d x]} \text{EllipticE}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}}{b\left(a^2-b^2\right) d}+$$

$$\frac{\sqrt{\cos [c+d x]} \text{EllipticF}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}}{\left(a^2-b^2\right) d}+$$

$$\left(\left(a^2-3 b^2\right) \sqrt{\cos [c+d x]} \text{EllipticPi}\left[\frac{2 a}{a+b}, \frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}\right) /$$

$$\left(\left(a-b\right) b(a+b)^2 d\right)-\frac{a^2 \sqrt{\sec [c+d x]} \sin [c+d x]}{b\left(a^2-b^2\right) d(a+b \sec [c+d x])}$$

Result (type 4, 587 leaves):

$$\frac{\sqrt{\text{Sec}[c+dx]} \left( \frac{a \text{Sin}[c+dx]}{b(-a^2+b^2)} + \frac{a \text{Sin}[c+dx]}{(a^2-b^2)(b+a \text{Cos}[c+dx])} \right)}{d} + \frac{1}{4(a-b)b(a+b)d}$$

$$\left( - \left( \left( 8 b \text{Cos}[c+dx]^2 \text{EllipticPi}\left[-\frac{b}{a}, -\text{ArcSin}\left[\sqrt{\text{Sec}[c+dx]}\right], -1\right] (a+b \text{Sec}[c+dx]) \sqrt{1-\text{Sec}[c+dx]^2} \text{Sin}[c+dx] \right) / \left( (b+a \text{Cos}[c+dx]) (1-\text{Cos}[c+dx]^2) \right) \right) + \right.$$

$$\left( 2 (3 a^2 - 4 b^2) \text{Cos}[c+dx]^2 \left( \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\text{Sec}[c+dx]}\right], -1\right] + \right. \right.$$

$$\left. \left. \text{EllipticPi}\left[-\frac{b}{a}, -\text{ArcSin}\left[\sqrt{\text{Sec}[c+dx]}\right], -1\right] \right) (a+b \text{Sec}[c+dx]) \sqrt{1-\text{Sec}[c+dx]^2} \text{Sin}[c+dx] \right) / \left( b (b+a \text{Cos}[c+dx]) (1-\text{Cos}[c+dx]^2) \right) - \right.$$

$$\left( 2 \text{Cos}[2(c+dx)] (a+b \text{Sec}[c+dx]) \left( 2 a b - 2 a b \text{Sec}[c+dx]^2 + \right. \right.$$

$$2 a b \text{EllipticE}\left[\text{ArcSin}\left[\sqrt{\text{Sec}[c+dx]}\right], -1\right] \sqrt{\text{Sec}[c+dx]} \sqrt{1-\text{Sec}[c+dx]^2} +$$

$$a (a-2 b) \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\text{Sec}[c+dx]}\right], -1\right] \sqrt{\text{Sec}[c+dx]} \sqrt{1-\text{Sec}[c+dx]^2} +$$

$$a^2 \text{EllipticPi}\left[-\frac{b}{a}, -\text{ArcSin}\left[\sqrt{\text{Sec}[c+dx]}\right], -1\right] \sqrt{\text{Sec}[c+dx]} \sqrt{1-\text{Sec}[c+dx]^2} -$$

$$2 b^2 \text{EllipticPi}\left[-\frac{b}{a}, -\text{ArcSin}\left[\sqrt{\text{Sec}[c+dx]}\right], -1\right]$$

$$\left. \left. \sqrt{\text{Sec}[c+dx]} \sqrt{1-\text{Sec}[c+dx]^2} \right) \text{Sin}[c+dx] \right) / \left( b (b+a \text{Cos}[c+dx]) (1-\text{Cos}[c+dx]^2) \sqrt{\text{Sec}[c+dx]} (2-\text{Sec}[c+dx]^2) \right) \right)$$

**Problem 617: Result more than twice size of optimal antiderivative.**

$$\int \frac{\text{Sec}[c+dx]^{3/2}}{(a+b \text{Sec}[c+dx])^2} dx$$

Optimal (type 4, 208 leaves, 9 steps):

$$-\frac{\sqrt{\text{Cos}[c+dx]} \text{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\text{Sec}[c+dx]}}{(a^2-b^2)d} -$$

$$\frac{b \sqrt{\text{Cos}[c+dx]} \text{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\text{Sec}[c+dx]}}{a(a^2-b^2)d} +$$

$$\left( (a^2+b^2) \sqrt{\text{Cos}[c+dx]} \text{EllipticPi}\left[\frac{2a}{a+b}, \frac{1}{2}(c+dx), 2\right] \sqrt{\text{Sec}[c+dx]} \right) /$$

$$\left( a(a-b)(a+b)^2 d \right) + \frac{a \sqrt{\text{Sec}[c+dx]} \text{Sin}[c+dx]}{(a^2-b^2)d(a+b \text{Sec}[c+dx])}$$

Result (type 4, 633 leaves):

$$\begin{aligned}
 & \frac{(b + a \cos [c + d x])^2 \sec [c + d x]^{5/2} \left( -\frac{\sin [c + d x]}{-a^2 + b^2} + \frac{b \sin [c + d x]}{(-a^2 + b^2) (b + a \cos [c + d x])} \right)}{d (a + b \sec [c + d x])^2} + \\
 & \frac{1}{4 (-a + b) (a + b) d (a + b \sec [c + d x])^2} (b + a \cos [c + d x])^2 \sec [c + d x]^2 \\
 & \left( -\left( \left( 8 b \cos [c + d x]^2 \operatorname{EllipticPi} \left[ -\frac{b}{a}, -\operatorname{ArcSin} [\sqrt{\sec [c + d x]}], -1 \right] (a + b \sec [c + d x]) \right. \right. \right. \\
 & \left. \left. \left. \sqrt{1 - \sec [c + d x]^2} \sin [c + d x] \right) / (a (b + a \cos [c + d x]) (1 - \cos [c + d x]^2)) \right) - \right. \\
 & \left( 2 a \cos [c + d x]^2 \left( \operatorname{EllipticF} [\operatorname{ArcSin} [\sqrt{\sec [c + d x]}], -1] + \right. \right. \\
 & \left. \left. \operatorname{EllipticPi} \left[ -\frac{b}{a}, -\operatorname{ArcSin} [\sqrt{\sec [c + d x]}], -1 \right] \right) (a + b \sec [c + d x]) \right. \\
 & \left. \sqrt{1 - \sec [c + d x]^2} \sin [c + d x] \right) / (b (b + a \cos [c + d x]) (1 - \cos [c + d x]^2)) - \\
 & \left( 2 \cos [2 (c + d x)] (a + b \sec [c + d x]) \left( 2 a b - 2 a b \sec [c + d x]^2 + \right. \right. \\
 & \left. \left. 2 a b \operatorname{EllipticE} [\operatorname{ArcSin} [\sqrt{\sec [c + d x]}], -1] \sqrt{\sec [c + d x]} \sqrt{1 - \sec [c + d x]^2} + \right. \right. \\
 & \left. \left. a (a - 2 b) \operatorname{EllipticF} [\operatorname{ArcSin} [\sqrt{\sec [c + d x]}], -1] \sqrt{\sec [c + d x]} \sqrt{1 - \sec [c + d x]^2} + \right. \right. \\
 & \left. \left. a^2 \operatorname{EllipticPi} \left[ -\frac{b}{a}, -\operatorname{ArcSin} [\sqrt{\sec [c + d x]}], -1 \right] \sqrt{\sec [c + d x]} \sqrt{1 - \sec [c + d x]^2} - \right. \right. \\
 & \left. \left. 2 b^2 \operatorname{EllipticPi} \left[ -\frac{b}{a}, -\operatorname{ArcSin} [\sqrt{\sec [c + d x]}], -1 \right] \right. \right. \\
 & \left. \left. \sqrt{\sec [c + d x]} \sqrt{1 - \sec [c + d x]^2} \right) \sin [c + d x] \right) / \\
 & \left( a b (b + a \cos [c + d x]) (1 - \cos [c + d x]^2) \sqrt{\sec [c + d x]} (2 - \sec [c + d x]^2) \right)
 \end{aligned}$$

**Problem 618: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sqrt{\sec [c + d x]}}{(a + b \sec [c + d x])^2} dx$$

Optimal (type 4, 227 leaves, 9 steps):

$$\begin{aligned}
 & \frac{b \sqrt{\cos [c + d x]} \operatorname{EllipticE} \left[ \frac{1}{2} (c + d x), 2 \right] \sqrt{\sec [c + d x]}}{a (a^2 - b^2) d} + \\
 & \frac{(2 a^2 - b^2) \sqrt{\cos [c + d x]} \operatorname{EllipticF} \left[ \frac{1}{2} (c + d x), 2 \right] \sqrt{\sec [c + d x]}}{a^2 (a^2 - b^2) d} - \\
 & \frac{b (3 a^2 - b^2) \sqrt{\cos [c + d x]} \operatorname{EllipticPi} \left[ \frac{2 a}{a + b}, \frac{1}{2} (c + d x), 2 \right] \sqrt{\sec [c + d x]}}{a^2 (a - b) (a + b)^2 d} - \frac{b \sqrt{\sec [c + d x]} \sin [c + d x]}{(a^2 - b^2) d (a + b \sec [c + d x])}
 \end{aligned}$$

Result (type 4, 630 leaves):

$$\frac{(b + a \cos [c + d x])^2 \operatorname{Sec}[c + d x]^{5/2} \left( \frac{b \sin [c + d x]}{a (-a^2 + b^2)} + \frac{b^2 \sin [c + d x]}{a (a^2 - b^2) (b + a \cos [c + d x])} \right)}{d (a + b \operatorname{Sec}[c + d x])^2} +$$

$$\frac{1}{4 (a - b) (a + b) d (a + b \operatorname{Sec}[c + d x])^2} (b + a \cos [c + d x])^2 \operatorname{Sec}[c + d x]^2$$

$$\left( - \left( \left( 8 \cos [c + d x]^2 \operatorname{EllipticPi} \left[ -\frac{b}{a}, -\operatorname{ArcSin}[\sqrt{\operatorname{Sec}[c + d x]}], -1 \right] (a + b \operatorname{Sec}[c + d x]) \right. \right. \right.$$

$$\left. \left. \sqrt{1 - \operatorname{Sec}[c + d x]^2} \sin [c + d x] \right) / \left( (b + a \cos [c + d x]) (1 - \cos [c + d x]^2) \right) \right) -$$

$$\left( 2 \cos [c + d x]^2 \left( \operatorname{EllipticF}[\operatorname{ArcSin}[\sqrt{\operatorname{Sec}[c + d x]}], -1] + \right. \right.$$

$$\left. \left. \operatorname{EllipticPi} \left[ -\frac{b}{a}, -\operatorname{ArcSin}[\sqrt{\operatorname{Sec}[c + d x]}], -1 \right] \right) (a + b \operatorname{Sec}[c + d x]) \right.$$

$$\left. \sqrt{1 - \operatorname{Sec}[c + d x]^2} \sin [c + d x] \right) / \left( (b + a \cos [c + d x]) (1 - \cos [c + d x]^2) \right) -$$

$$\left( 2 \cos [2 (c + d x)] (a + b \operatorname{Sec}[c + d x]) \left( 2 a b - 2 a b \operatorname{Sec}[c + d x]^2 + \right. \right.$$

$$2 a b \operatorname{EllipticE}[\operatorname{ArcSin}[\sqrt{\operatorname{Sec}[c + d x]}], -1] \sqrt{\operatorname{Sec}[c + d x]} \sqrt{1 - \operatorname{Sec}[c + d x]^2} +$$

$$a (a - 2 b) \operatorname{EllipticF}[\operatorname{ArcSin}[\sqrt{\operatorname{Sec}[c + d x]}], -1] \sqrt{\operatorname{Sec}[c + d x]} \sqrt{1 - \operatorname{Sec}[c + d x]^2} +$$

$$a^2 \operatorname{EllipticPi} \left[ -\frac{b}{a}, -\operatorname{ArcSin}[\sqrt{\operatorname{Sec}[c + d x]}], -1 \right] \sqrt{\operatorname{Sec}[c + d x]} \sqrt{1 - \operatorname{Sec}[c + d x]^2} -$$

$$2 b^2 \operatorname{EllipticPi} \left[ -\frac{b}{a}, -\operatorname{ArcSin}[\sqrt{\operatorname{Sec}[c + d x]}], -1 \right]$$

$$\left. \left. \sqrt{\operatorname{Sec}[c + d x]} \sqrt{1 - \operatorname{Sec}[c + d x]^2} \right) \sin [c + d x] \right) /$$

$$\left( a^2 (b + a \cos [c + d x]) (1 - \cos [c + d x]^2) \sqrt{\operatorname{Sec}[c + d x]} (2 - \operatorname{Sec}[c + d x]^2) \right)$$

**Problem 619: Result more than twice size of optimal antiderivative.**

$$\int \frac{1}{\sqrt{\operatorname{Sec}[c + d x]} (a + b \operatorname{Sec}[c + d x])^2} dx$$

Optimal (type 4, 244 leaves, 9 steps):

$$\frac{(2 a^2 - 3 b^2) \sqrt{\cos [c + d x]} \operatorname{EllipticE} \left[ \frac{1}{2} (c + d x), 2 \right] \sqrt{\operatorname{Sec}[c + d x]}}{a^2 (a^2 - b^2) d} -$$

$$\frac{1}{a^3 (a^2 - b^2) d} b (4 a^2 - 3 b^2) \sqrt{\cos [c + d x]} \operatorname{EllipticF} \left[ \frac{1}{2} (c + d x), 2 \right] \sqrt{\operatorname{Sec}[c + d x]} +$$

$$\left( b^2 (5 a^2 - 3 b^2) \sqrt{\cos [c + d x]} \operatorname{EllipticPi} \left[ \frac{2 a}{a + b}, \frac{1}{2} (c + d x), 2 \right] \sqrt{\operatorname{Sec}[c + d x]} \right) /$$

$$\left( a^3 (a - b) (a + b)^2 d \right) + \frac{b^2 \sqrt{\operatorname{Sec}[c + d x]} \sin [c + d x]}{a (a^2 - b^2) d (a + b \operatorname{Sec}[c + d x])}$$

Result (type 4, 608 leaves):

$$\frac{\sqrt{\sec [c+d x]}\left(-\frac{b^2 \sin [c+d x]}{a^2\left(-a^2+b^2\right)}-\frac{b^3 \sin [c+d x]}{a^2\left(a^2-b^2\right)(b+a \cos [c+d x])}\right)}{d}+\frac{1}{4 a(-a+b)(a+b) d}$$

$$\left(-\left(\left(8 b \cos [c+d x]^2 \operatorname{EllipticPi}\left[-\frac{b}{a},-\operatorname{ArcSin}\left[\sqrt{\sec [c+d x]}\right],-1\right](a+b \sec [c+d x])\right.\right.\right.$$

$$\left.\left.\left.\sqrt{1-\sec [c+d x]^2} \sin [c+d x]\right) / \left((b+a \cos [c+d x])\left(1-\cos [c+d x]^2\right)\right)\right)\right)+$$

$$\left(2\left(-2 a^2+b^2\right) \cos [c+d x]^2\left(\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{\sec [c+d x]}\right],-1\right]+$$

$$\operatorname{EllipticPi}\left[-\frac{b}{a},-\operatorname{ArcSin}\left[\sqrt{\sec [c+d x]}\right],-1\right]\right)(a+b \sec [c+d x])$$

$$\sqrt{1-\sec [c+d x]^2} \sin [c+d x]\right) / \left(b(b+a \cos [c+d x])\left(1-\cos [c+d x]^2\right)\right)-$$

$$\left(2\left(-2 a^2+3 b^2\right) \cos [2(c+d x)](a+b \sec [c+d x])\left(2 a b-2 a b \sec [c+d x]^2+\right.\right.$$

$$2 a b \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\sqrt{\sec [c+d x]}\right],-1\right] \sqrt{\sec [c+d x]} \sqrt{1-\sec [c+d x]^2}+$$

$$a(a-2 b) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{\sec [c+d x]}\right],-1\right] \sqrt{\sec [c+d x]} \sqrt{1-\sec [c+d x]^2}+$$

$$a^2 \operatorname{EllipticPi}\left[-\frac{b}{a},-\operatorname{ArcSin}\left[\sqrt{\sec [c+d x]}\right],-1\right] \sqrt{\sec [c+d x]} \sqrt{1-\sec [c+d x]^2}-$$

$$\left.2 b^2 \operatorname{EllipticPi}\left[-\frac{b}{a},-\operatorname{ArcSin}\left[\sqrt{\sec [c+d x]}\right],-1\right] \sqrt{\sec [c+d x]} \sqrt{1-\sec [c+d x]^2}\right)$$

$$\sin [c+d x]\right) / \left(a^2 b(b+a \cos [c+d x])\left(1-\cos [c+d x]^2\right)\right.$$

$$\left.\sqrt{\sec [c+d x]}\left(2-\sec [c+d x]^2\right)\right)$$

**Problem 620: Result more than twice size of optimal antiderivative.**

$$\int \frac{1}{\sec [c+d x]^{3 / 2}(a+b \sec [c+d x])^2} d x$$

Optimal (type 4, 304 leaves, 10 steps):

$$-\frac{1}{a^3\left(a^2-b^2\right) d} b\left(4 a^2-5 b^2\right) \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}+$$

$$\frac{1}{3 a^4\left(a^2-b^2\right) d}\left(2 a^4+16 a^2 b^2-15 b^4\right) \sqrt{\cos [c+d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}-$$

$$\left(b^3\left(7 a^2-5 b^2\right) \sqrt{\cos [c+d x]} \operatorname{EllipticPi}\left[\frac{2 a}{a+b}, \frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}\right) /$$

$$\left(a^4(a-b)(a+b)^2 d\right)+\frac{\left(2 a^2-5 b^2\right) \sin [c+d x]}{3 a^2\left(a^2-b^2\right) d \sqrt{\sec [c+d x]}}+$$

$$\frac{b^2 \sin [c+d x]}{a\left(a^2-b^2\right) d \sqrt{\sec [c+d x]}(a+b \sec [c+d x])}$$

Result (type 4, 639 leaves):

$$\frac{1}{12 a^2 (a-b) (a+b) d} \left( - \left( \left( 2 (4 a^3 + 8 a b^2) \cos [c+d x]^2 \operatorname{EllipticPi} \left[ -\frac{b}{a}, -\operatorname{ArcSin} \left[ \sqrt{\sec [c+d x]} \right], -1 \right] \right. \right. \right. \\ \left. \left. \left. (a+b \sec [c+d x]) \sqrt{1-\sec [c+d x]^2} \sin [c+d x] \right) \right) / \right. \\ \left. \left( a (b+a \cos [c+d x]) (1-\cos [c+d x]^2) \right) \right) + \\ \left( 2 (-8 a^2 b + 5 b^3) \cos [c+d x]^2 \left( \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \sqrt{\sec [c+d x]} \right], -1 \right] + \right. \right. \\ \left. \left. \operatorname{EllipticPi} \left[ -\frac{b}{a}, -\operatorname{ArcSin} \left[ \sqrt{\sec [c+d x]} \right], -1 \right] \right) (a+b \sec [c+d x]) \right. \\ \left. \sqrt{1-\sec [c+d x]^2} \sin [c+d x] \right) / (b (b+a \cos [c+d x]) (1-\cos [c+d x]^2)) - \\ \left( 2 (-12 a^2 b + 15 b^3) \cos [2 (c+d x)] (a+b \sec [c+d x]) (2 a b - 2 a b \sec [c+d x]^2 + \right. \\ \left. 2 a b \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \sqrt{\sec [c+d x]} \right], -1 \right] \sqrt{\sec [c+d x]} \sqrt{1-\sec [c+d x]^2} + \right. \\ \left. a (a-2 b) \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \sqrt{\sec [c+d x]} \right], -1 \right] \sqrt{\sec [c+d x]} \sqrt{1-\sec [c+d x]^2} + \right. \\ \left. a^2 \operatorname{EllipticPi} \left[ -\frac{b}{a}, -\operatorname{ArcSin} \left[ \sqrt{\sec [c+d x]} \right], -1 \right] \sqrt{\sec [c+d x]} \sqrt{1-\sec [c+d x]^2} - \right. \\ \left. \left. 2 b^2 \operatorname{EllipticPi} \left[ -\frac{b}{a}, -\operatorname{ArcSin} \left[ \sqrt{\sec [c+d x]} \right], -1 \right] \sqrt{\sec [c+d x]} \sqrt{1-\sec [c+d x]^2} \right) \\ \left. \sin [c+d x] \right) / \left( a^2 b (b+a \cos [c+d x]) (1-\cos [c+d x]^2) \right. \\ \left. \sqrt{\sec [c+d x]} (2-\sec [c+d x]^2) \right) \right) + \\ \frac{\sqrt{\sec [c+d x]} \left( \frac{b^3 \sin [c+d x]}{a^3 (-a^2+b^2)} + \frac{b^4 \sin [c+d x]}{a^3 (a^2-b^2) (b+a \cos [c+d x])} + \frac{\sin [2 (c+d x)]}{3 a^2} \right)}{d}$$

**Problem 622: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sec [c+d x]^{7/2}}{(a+b \sec [c+d x])^3} dx$$

Optimal (type 4, 315 leaves, 10 steps):



$$\begin{aligned}
 & \frac{3 a (a^2 - 3 b^2) \sqrt{\cos [c + d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\sec [c + d x]}}{4 b^2 (a^2 - b^2)^2 d} + \\
 & \frac{(a^2 - 7 b^2) \sqrt{\cos [c + d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\sec [c + d x]}}{4 b (a^2 - b^2)^2 d} + \\
 & \left( \frac{3 (a^4 - 2 a^2 b^2 + 5 b^4) \sqrt{\cos [c + d x]} \operatorname{EllipticPi}\left[\frac{2 a}{a + b}, \frac{1}{2}(c + d x), 2\right] \sqrt{\sec [c + d x]}}{4 (a - b)^2 b^2 (a + b)^3 d} - \frac{a^2 \sec [c + d x]^{3/2} \sin [c + d x]}{2 b (a^2 - b^2) d (a + b \sec [c + d x])^2} - \right. \\
 & \left. \frac{3 a^2 (a^2 - 3 b^2) \sqrt{\sec [c + d x]} \sin [c + d x]}{4 b^2 (a^2 - b^2)^2 d (a + b \sec [c + d x])} \right)
 \end{aligned}$$

Result (type 4, 697 leaves):

$$\begin{aligned}
 & \frac{1}{16 (a - b)^2 b^2 (a + b)^2 d} \\
 & \left( - \left( \left( 2 (8 a^3 b - 32 a b^3) \cos [c + d x]^2 \operatorname{EllipticPi}\left[-\frac{b}{a}, -\operatorname{ArcSin}\left[\sqrt{\sec [c + d x]}\right], -1\right] \right. \right. \right. \\
 & \quad \left. \left. \left. (a + b \sec [c + d x]) \sqrt{1 - \sec [c + d x]^2} \sin [c + d x] \right) \right) / \right. \\
 & \quad \left. (a (b + a \cos [c + d x]) (1 - \cos [c + d x]^2)) \right) + \\
 & \left( 2 (9 a^4 - 19 a^2 b^2 + 16 b^4) \cos [c + d x]^2 \left( \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{\sec [c + d x]}\right], -1\right] + \right. \right. \\
 & \quad \left. \left. \operatorname{EllipticPi}\left[-\frac{b}{a}, -\operatorname{ArcSin}\left[\sqrt{\sec [c + d x]}\right], -1\right] \right) (a + b \sec [c + d x]) \right. \\
 & \quad \left. \sqrt{1 - \sec [c + d x]^2} \sin [c + d x] \right) / (b (b + a \cos [c + d x]) (1 - \cos [c + d x]^2)) - \\
 & \left( 2 (3 a^4 - 9 a^2 b^2) \cos [2 (c + d x)] (a + b \sec [c + d x]) \left( 2 a b - 2 a b \sec [c + d x]^2 + \right. \right. \\
 & \quad 2 a b \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\sqrt{\sec [c + d x]}\right], -1\right] \sqrt{\sec [c + d x]} \sqrt{1 - \sec [c + d x]^2} + \\
 & \quad a (a - 2 b) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{\sec [c + d x]}\right], -1\right] \sqrt{\sec [c + d x]} \sqrt{1 - \sec [c + d x]^2} + \\
 & \quad a^2 \operatorname{EllipticPi}\left[-\frac{b}{a}, -\operatorname{ArcSin}\left[\sqrt{\sec [c + d x]}\right], -1\right] \sqrt{\sec [c + d x]} \sqrt{1 - \sec [c + d x]^2} - \\
 & \quad \left. \left. 2 b^2 \operatorname{EllipticPi}\left[-\frac{b}{a}, -\operatorname{ArcSin}\left[\sqrt{\sec [c + d x]}\right], -1\right] \sqrt{\sec [c + d x]} \sqrt{1 - \sec [c + d x]^2} \right) \right. \\
 & \quad \left. \sin [c + d x] \right) / \left( a^2 b (b + a \cos [c + d x]) (1 - \cos [c + d x]^2) \right. \\
 & \quad \left. \sqrt{\sec [c + d x]} (2 - \sec [c + d x]^2) \right) + \frac{1}{d} \\
 & \sqrt{\sec [c + d x]} \left( \frac{3 a (-a^2 + 3 b^2) \sin [c + d x]}{4 b^2 (-a^2 + b^2)^2} - \frac{a \sin [c + d x]}{2 (-a^2 + b^2) (b + a \cos [c + d x])^2} + \right. \\
 & \quad \left. \frac{a^3 \sin [c + d x] - 7 a b^2 \sin [c + d x]}{4 b (-a^2 + b^2)^2 (b + a \cos [c + d x])} \right)
 \end{aligned}$$

### Problem 623: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Sec}[c + d x]^{5/2}}{(a + b \text{Sec}[c + d x])^3} dx$$

Optimal (type 4, 313 leaves, 10 steps):

$$\begin{aligned} & \frac{(a^2 + 5 b^2) \sqrt{\text{Cos}[c + d x]} \text{EllipticE}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\text{Sec}[c + d x]}}{4 b (a^2 - b^2)^2 d} + \\ & \frac{3 (a^2 + b^2) \sqrt{\text{Cos}[c + d x]} \text{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\text{Sec}[c + d x]}}{4 a (a^2 - b^2)^2 d} + \\ & \left( (a^4 - 10 a^2 b^2 - 3 b^4) \sqrt{\text{Cos}[c + d x]} \text{EllipticPi}\left[\frac{2 a}{a + b}, \frac{1}{2}(c + d x), 2\right] \sqrt{\text{Sec}[c + d x]} \right) / \\ & (4 a (a - b)^2 b (a + b)^3 d) - \\ & \frac{a^2 \sqrt{\text{Sec}[c + d x]} \text{Sin}[c + d x]}{2 b (a^2 - b^2) d (a + b \text{Sec}[c + d x])^2} + \frac{a (a^2 - 7 b^2) \sqrt{\text{Sec}[c + d x]} \text{Sin}[c + d x]}{4 b (a^2 - b^2)^2 d (a + b \text{Sec}[c + d x])} \end{aligned}$$

Result (type 4, 733 leaves):

$$\frac{1}{16 (a-b)^2 b (a+b)^2 d (a+b \operatorname{Sec}[c+dx])^3}$$

$$\left( (b+a \operatorname{Cos}[c+dx])^3 \operatorname{Sec}[c+dx]^3 \left( - \left( \left( 2 (8 a^2 b + 16 b^3) \operatorname{Cos}[c+dx]^2 \right. \right. \right. \right.$$

$$\left. \left. \left. \operatorname{EllipticPi}\left[-\frac{b}{a}, -\operatorname{ArcSin}\left[\sqrt{\operatorname{Sec}[c+dx]}\right], -1\right] (a+b \operatorname{Sec}[c+dx]) \right. \right. \right.$$

$$\left. \left. \left. \sqrt{1-\operatorname{Sec}[c+dx]^2} \operatorname{Sin}[c+dx] \right) / (a (b+a \operatorname{Cos}[c+dx]) (1-\operatorname{Cos}[c+dx]^2)) \right) \right) +$$

$$\left( 2 (3 a^3 - 9 a b^2) \operatorname{Cos}[c+dx]^2 \left( \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{\operatorname{Sec}[c+dx]}\right], -1\right] + \right. \right.$$

$$\left. \left. \operatorname{EllipticPi}\left[-\frac{b}{a}, -\operatorname{ArcSin}\left[\sqrt{\operatorname{Sec}[c+dx]}\right], -1\right] \right) (a+b \operatorname{Sec}[c+dx]) \right.$$

$$\left. \left. \sqrt{1-\operatorname{Sec}[c+dx]^2} \operatorname{Sin}[c+dx] \right) / (b (b+a \operatorname{Cos}[c+dx]) (1-\operatorname{Cos}[c+dx]^2)) \right) -$$

$$\left( 2 (a^3 + 5 a b^2) \operatorname{Cos}[2(c+dx)] (a+b \operatorname{Sec}[c+dx]) \left( 2 a b - 2 a b \operatorname{Sec}[c+dx]^2 + \right. \right.$$

$$2 a b \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\sqrt{\operatorname{Sec}[c+dx]}\right], -1\right] \sqrt{\operatorname{Sec}[c+dx]} \sqrt{1-\operatorname{Sec}[c+dx]^2} +$$

$$a (a-2 b) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{\operatorname{Sec}[c+dx]}\right], -1\right] \sqrt{\operatorname{Sec}[c+dx]} \sqrt{1-\operatorname{Sec}[c+dx]^2} +$$

$$a^2 \operatorname{EllipticPi}\left[-\frac{b}{a}, -\operatorname{ArcSin}\left[\sqrt{\operatorname{Sec}[c+dx]}\right], -1\right] \sqrt{\operatorname{Sec}[c+dx]} \sqrt{1-\operatorname{Sec}[c+dx]^2} -$$

$$2 b^2 \operatorname{EllipticPi}\left[-\frac{b}{a}, -\operatorname{ArcSin}\left[\sqrt{\operatorname{Sec}[c+dx]}\right], -1\right] \sqrt{\operatorname{Sec}[c+dx]} \sqrt{1-\operatorname{Sec}[c+dx]^2} \right)$$

$$\left. \left. \operatorname{Sin}[c+dx] \right) / (a^2 b (b+a \operatorname{Cos}[c+dx]) (1-\operatorname{Cos}[c+dx]^2)) \right.$$

$$\left. \left. \sqrt{\operatorname{Sec}[c+dx]} (2-\operatorname{Sec}[c+dx]^2) \right) \right) +$$

$$\left( (b+a \operatorname{Cos}[c+dx])^3 \operatorname{Sec}[c+dx]^{7/2} \left( - \frac{(a^2+5 b^2) \operatorname{Sin}[c+dx]}{4 b (-a^2+b^2)^2} + \frac{b \operatorname{Sin}[c+dx]}{2 (-a^2+b^2) (b+a \operatorname{Cos}[c+dx])^2} + \right. \right.$$

$$\left. \left. \frac{3 (a^2 \operatorname{Sin}[c+dx] + b^2 \operatorname{Sin}[c+dx])}{4 (-a^2+b^2)^2 (b+a \operatorname{Cos}[c+dx])} \right) \right) / (d (a+b \operatorname{Sec}[c+dx])^3)$$

**Problem 624: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec}[c+dx]^{3/2}}{(a+b \operatorname{Sec}[c+dx])^3} dx$$

Optimal (type 4, 306 leaves, 10 steps):

$$\begin{aligned}
& - \frac{(5a^2 + b^2) \sqrt{\cos[c + dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c + dx), 2\right] \sqrt{\sec[c + dx]}}{4a(a^2 - b^2)^2 d} - \\
& \frac{b(7a^2 - b^2) \sqrt{\cos[c + dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] \sqrt{\sec[c + dx]}}{4a^2(a^2 - b^2)^2 d} + \\
& \left( (3a^4 + 10a^2b^2 - b^4) \sqrt{\cos[c + dx]} \operatorname{EllipticPi}\left[\frac{2a}{a+b}, \frac{1}{2}(c + dx), 2\right] \sqrt{\sec[c + dx]} \right) / \\
& (4a^2(a-b)^2(a+b)^3d) + \\
& \frac{a \sqrt{\sec[c + dx]} \sin[c + dx]}{2(a^2 - b^2)d(a + b \sec[c + dx])^2} + \frac{3(a^2 + b^2) \sqrt{\sec[c + dx]} \sin[c + dx]}{4(a^2 - b^2)^2 d(a + b \sec[c + dx])}
\end{aligned}$$

Result (type 4, 724 leaves):

$$\begin{aligned}
& - \frac{1}{16(a-b)^2(a+b)^2d(a+b \sec[c + dx])^3} (b + a \cos[c + dx])^3 \sec[c + dx]^3 \\
& \left( - \left( \left( 48b \cos[c + dx]^2 \operatorname{EllipticPi}\left[-\frac{b}{a}, -\operatorname{ArcSin}[\sqrt{\sec[c + dx]}], -1\right] (a + b \sec[c + dx]) \right. \right. \right. \\
& \quad \left. \left. \left. \sqrt{1 - \sec[c + dx]^2} \sin[c + dx] \right) / \left( (b + a \cos[c + dx]) (1 - \cos[c + dx]^2) \right) \right) \right) + \\
& \left( 2(-a^2 - 5b^2) \cos[c + dx]^2 \left( \operatorname{EllipticF}[\operatorname{ArcSin}[\sqrt{\sec[c + dx]}], -1] + \right. \right. \\
& \quad \left. \left. \operatorname{EllipticPi}\left[-\frac{b}{a}, -\operatorname{ArcSin}[\sqrt{\sec[c + dx]}], -1\right] \right) (a + b \sec[c + dx]) \right. \\
& \quad \left. \sqrt{1 - \sec[c + dx]^2} \sin[c + dx] \right) / (b(b + a \cos[c + dx]) (1 - \cos[c + dx]^2)) - \\
& \left( 2(5a^2 + b^2) \cos[2(c + dx)] (a + b \sec[c + dx]) \left( 2ab - 2ab \sec[c + dx]^2 + \right. \right. \\
& \quad 2ab \operatorname{EllipticE}[\operatorname{ArcSin}[\sqrt{\sec[c + dx]}], -1] \sqrt{\sec[c + dx]} \sqrt{1 - \sec[c + dx]^2} + \\
& \quad a(a - 2b) \operatorname{EllipticF}[\operatorname{ArcSin}[\sqrt{\sec[c + dx]}], -1] \sqrt{\sec[c + dx]} \sqrt{1 - \sec[c + dx]^2} + \\
& \quad a^2 \operatorname{EllipticPi}\left[-\frac{b}{a}, -\operatorname{ArcSin}[\sqrt{\sec[c + dx]}], -1\right] \sqrt{\sec[c + dx]} \sqrt{1 - \sec[c + dx]^2} - \\
& \quad 2b^2 \operatorname{EllipticPi}\left[-\frac{b}{a}, -\operatorname{ArcSin}[\sqrt{\sec[c + dx]}], -1\right] \\
& \quad \left. \left. \sqrt{\sec[c + dx]} \sqrt{1 - \sec[c + dx]^2} \right) \sin[c + dx] \right) / \\
& \left( a^2b(b + a \cos[c + dx]) (1 - \cos[c + dx]^2) \sqrt{\sec[c + dx]} (2 - \sec[c + dx]^2) \right) \right) + \\
& \left( (b + a \cos[c + dx])^3 \sec[c + dx]^{7/2} \left( \frac{(5a^2 + b^2) \sin[c + dx]}{4a(a^2 - b^2)^2} + \right. \right. \\
& \quad \left. \left. \frac{b^2 \sin[c + dx]}{2a(a^2 - b^2)(b + a \cos[c + dx])^2} + \right. \right. \\
& \quad \left. \left. \frac{-7a^2b \sin[c + dx] + b^3 \sin[c + dx]}{4a(a^2 - b^2)^2(b + a \cos[c + dx])} \right) \right) / (d(a + b \sec[c + dx])^3)
\end{aligned}$$

### Problem 625: Result more than twice size of optimal antiderivative.

$$\int \frac{\sqrt{\sec [c+d x]}}{(a+b \sec [c+d x])^3} dx$$

Optimal (type 4, 323 leaves, 10 steps):

$$\frac{3 b \left(3 a^2 - b^2\right) \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}}{4 a^2\left(a^2 - b^2\right)^2 d} + \frac{1}{4 a^3\left(a^2 - b^2\right)^2 d}$$

$$\left(8 a^4 - 5 a^2 b^2 + 3 b^4\right) \sqrt{\cos [c+d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]} -$$

$$\left(3 b\left(5 a^4 - 2 a^2 b^2 + b^4\right) \sqrt{\cos [c+d x]} \operatorname{EllipticPi}\left[\frac{2 a}{a+b}, \frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}\right) /$$

$$\left(4 a^3(a-b)^2(a+b)^3 d\right) -$$

$$\frac{b \sqrt{\sec [c+d x]} \sin [c+d x]}{2\left(a^2 - b^2\right) d(a+b \sec [c+d x])^2} - \frac{b\left(7 a^2 - b^2\right) \sqrt{\sec [c+d x]} \sin [c+d x]}{4 a\left(a^2 - b^2\right)^2 d(a+b \sec [c+d x])}$$

Result (type 4, 749 leaves):

$$\frac{1}{16 a (a-b)^2 (a+b)^2 d (a+b \operatorname{Sec}[c+d x])^3} \left( (b+a \operatorname{Cos}[c+d x])^3 \operatorname{Sec}[c+d x]^3 \left( - \left( \left( 2 (16 a^3 + 8 a b^2) \operatorname{Cos}[c+d x]^2 \operatorname{EllipticPi}\left[-\frac{b}{a}, -\operatorname{ArcSin}\left[\sqrt{\operatorname{Sec}[c+d x]}\right], -1\right] (a+b \operatorname{Sec}[c+d x]) \sqrt{1-\operatorname{Sec}[c+d x]^2} \operatorname{Sin}[c+d x]\right) / (a (b+a \operatorname{Cos}[c+d x]) (1-\operatorname{Cos}[c+d x]^2)) \right) + \left( 2 (-5 a^2 b - b^3) \operatorname{Cos}[c+d x]^2 \left( \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{\operatorname{Sec}[c+d x]}\right], -1\right] + \operatorname{EllipticPi}\left[-\frac{b}{a}, -\operatorname{ArcSin}\left[\sqrt{\operatorname{Sec}[c+d x]}\right], -1\right] \right) (a+b \operatorname{Sec}[c+d x]) \sqrt{1-\operatorname{Sec}[c+d x]^2} \operatorname{Sin}[c+d x]\right) / (b (b+a \operatorname{Cos}[c+d x]) (1-\operatorname{Cos}[c+d x]^2)) - \left( 2 (9 a^2 b - 3 b^3) \operatorname{Cos}[2(c+d x)] (a+b \operatorname{Sec}[c+d x]) \left( 2 a b - 2 a b \operatorname{Sec}[c+d x]^2 + 2 a b \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\sqrt{\operatorname{Sec}[c+d x]}\right], -1\right] \sqrt{\operatorname{Sec}[c+d x]} \sqrt{1-\operatorname{Sec}[c+d x]^2} + a (a-2 b) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{\operatorname{Sec}[c+d x]}\right], -1\right] \sqrt{\operatorname{Sec}[c+d x]} \sqrt{1-\operatorname{Sec}[c+d x]^2} + a^2 \operatorname{EllipticPi}\left[-\frac{b}{a}, -\operatorname{ArcSin}\left[\sqrt{\operatorname{Sec}[c+d x]}\right], -1\right] \sqrt{\operatorname{Sec}[c+d x]} \sqrt{1-\operatorname{Sec}[c+d x]^2} - 2 b^2 \operatorname{EllipticPi}\left[-\frac{b}{a}, -\operatorname{ArcSin}\left[\sqrt{\operatorname{Sec}[c+d x]}\right], -1\right] \sqrt{\operatorname{Sec}[c+d x]} \sqrt{1-\operatorname{Sec}[c+d x]^2} \right) \operatorname{Sin}[c+d x]\right) / (a^2 b (b+a \operatorname{Cos}[c+d x]) (1-\operatorname{Cos}[c+d x]^2) \sqrt{\operatorname{Sec}[c+d x]} (2-\operatorname{Sec}[c+d x]^2)) \right) + \left( (b+a \operatorname{Cos}[c+d x])^3 \operatorname{Sec}[c+d x]^{7/2} \left( \frac{3 b (-3 a^2 + b^2) \operatorname{Sin}[c+d x]}{4 a^2 (-a^2 + b^2)^2} - \frac{b^3 \operatorname{Sin}[c+d x]}{2 a^2 (a^2 - b^2) (b+a \operatorname{Cos}[c+d x])^2} + \frac{11 a^2 b^2 \operatorname{Sin}[c+d x] - 5 b^4 \operatorname{Sin}[c+d x]}{4 a^2 (a^2 - b^2)^2 (b+a \operatorname{Cos}[c+d x])} \right) \right) / (d (a+b \operatorname{Sec}[c+d x])^3) \right)$$

**Problem 626: Result more than twice size of optimal antiderivative.**

$$\int \frac{1}{\sqrt{\operatorname{Sec}[c+d x]} (a+b \operatorname{Sec}[c+d x])^3} dx$$

Optimal (type 4, 342 leaves, 10 steps):

$$\frac{1}{4 a^3 (a^2 - b^2)^2 d} (8 a^4 - 29 a^2 b^2 + 15 b^4) \sqrt{\cos [c + d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\sec [c + d x]} -$$

$$\frac{1}{4 a^4 (a^2 - b^2)^2 d} 3 b (8 a^4 - 11 a^2 b^2 + 5 b^4) \sqrt{\cos [c + d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\sec [c + d x]} +$$

$$\left( b^2 (35 a^4 - 38 a^2 b^2 + 15 b^4) \sqrt{\cos [c + d x]} \operatorname{EllipticPi}\left[\frac{2 a}{a + b}, \frac{1}{2}(c + d x), 2\right] \sqrt{\sec [c + d x]} \right) /$$

$$\left( 4 a^4 (a - b)^2 (a + b)^3 d \right) + \frac{b^2 \sqrt{\sec [c + d x]} \sin [c + d x]}{2 a (a^2 - b^2) d (a + b \sec [c + d x])^2} +$$

$$\frac{b^2 (11 a^2 - 5 b^2) \sqrt{\sec [c + d x]} \sin [c + d x]}{4 a^2 (a^2 - b^2)^2 d (a + b \sec [c + d x])}$$

Result(type 4, 712 leaves):

$$\frac{1}{16 a^2 (a - b)^2 (a + b)^2 d}$$

$$\left( - \left( \left( 2 (-32 a^3 b + 8 a b^3) \cos [c + d x]^2 \operatorname{EllipticPi}\left[-\frac{b}{a}, -\operatorname{ArcSin}\left[\sqrt{\sec [c + d x]}\right], -1\right] \right. \right. \right.$$

$$\left. \left. \left. (a + b \sec [c + d x]) \sqrt{1 - \sec [c + d x]^2} \sin [c + d x] \right) \right) / \right.$$

$$\left. \left. \left. (a (b + a \cos [c + d x]) (1 - \cos [c + d x]^2)) \right) \right) + \right.$$

$$\left( 2 (8 a^4 - 7 a^2 b^2 + 5 b^4) \cos [c + d x]^2 \left( \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{\sec [c + d x]}\right], -1\right] + \right. \right.$$

$$\left. \left. \operatorname{EllipticPi}\left[-\frac{b}{a}, -\operatorname{ArcSin}\left[\sqrt{\sec [c + d x]}\right], -1\right] \right) (a + b \sec [c + d x]) \right.$$

$$\left. \left. \sqrt{1 - \sec [c + d x]^2} \sin [c + d x] \right) / \left( b (b + a \cos [c + d x]) (1 - \cos [c + d x]^2) \right) - \right.$$

$$\left( 2 (8 a^4 - 29 a^2 b^2 + 15 b^4) \cos [2 (c + d x)] (a + b \sec [c + d x]) \left( 2 a b - 2 a b \sec [c + d x]^2 + \right. \right.$$

$$2 a b \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\sqrt{\sec [c + d x]}\right], -1\right] \sqrt{\sec [c + d x]} \sqrt{1 - \sec [c + d x]^2} +$$

$$a (a - 2 b) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{\sec [c + d x]}\right], -1\right] \sqrt{\sec [c + d x]} \sqrt{1 - \sec [c + d x]^2} +$$

$$a^2 \operatorname{EllipticPi}\left[-\frac{b}{a}, -\operatorname{ArcSin}\left[\sqrt{\sec [c + d x]}\right], -1\right] \sqrt{\sec [c + d x]} \sqrt{1 - \sec [c + d x]^2} -$$

$$2 b^2 \operatorname{EllipticPi}\left[-\frac{b}{a}, -\operatorname{ArcSin}\left[\sqrt{\sec [c + d x]}\right], -1\right] \sqrt{\sec [c + d x]} \sqrt{1 - \sec [c + d x]^2} \right)$$

$$\sin [c + d x] \left. \right) / \left( a^2 b (b + a \cos [c + d x]) (1 - \cos [c + d x]^2) \right.$$

$$\left. \left. \sqrt{\sec [c + d x]} (2 - \sec [c + d x]^2) \right) \right) + \frac{1}{d}$$

$$\sqrt{\sec [c + d x]} \left( - \frac{b^2 (-13 a^2 + 7 b^2) \sin [c + d x]}{4 a^3 (-a^2 + b^2)^2} + \frac{b^4 \sin [c + d x]}{2 a^3 (a^2 - b^2) (b + a \cos [c + d x])^2} + \right.$$

$$\left. \frac{3 (-5 a^2 b^3 \sin [c + d x] + 3 b^5 \sin [c + d x])}{4 a^3 (a^2 - b^2)^2 (b + a \cos [c + d x])} \right)$$

**Problem 628: Result unnecessarily involves imaginary or complex numbers.**

$$\int \text{Sec}[c + d x]^{3/2} \sqrt{a + b \text{Sec}[c + d x]} dx$$

Optimal (type 4, 237 leaves, 12 steps):

$$\frac{b \sqrt{\frac{b+a \text{Cos}[c+d x]}{a+b}} \text{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2a}{a+b}\right] \sqrt{\text{Sec}[c+d x]}}{d \sqrt{a+b \text{Sec}[c+d x]}} +$$

$$\frac{a \sqrt{\frac{b+a \text{Cos}[c+d x]}{a+b}} \text{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2a}{a+b}\right] \sqrt{\text{Sec}[c+d x]}}{d \sqrt{a+b \text{Sec}[c+d x]}} -$$

$$\frac{\text{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2a}{a+b}\right] \sqrt{a+b \text{Sec}[c+d x]}}{d \sqrt{\frac{b+a \text{Cos}[c+d x]}{a+b}} \sqrt{\text{Sec}[c+d x]}} + \frac{\sqrt{\text{Sec}[c+d x]} \sqrt{a+b \text{Sec}[c+d x]} \text{Sin}[c+d x]}{d}$$

Result (type 4, 321 leaves):

$$\left( \sqrt{a + b \text{Sec}[c + d x]} \right.$$

$$\left. \left( \frac{2 a \text{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2a}{a+b}\right]}{(a+b) \sqrt{\frac{b+a \text{Cos}[c+d x]}{a+b}}} - \left( 2 i \sqrt{\frac{a(-1+\text{Cos}[c+d x])}{a+b}} \sqrt{\frac{a(1+\text{Cos}[c+d x])}{a-b}} \right. \right.

$$\left. \left. \text{Csc}[c+d x] \left( -2 b (a+b) \text{EllipticE}\left[i \text{ArcSinh}\left[\sqrt{\frac{1}{a-b}} \sqrt{b+a \text{Cos}[c+d x]}\right], \frac{-a+b}{a+b}\right] + \right. \right.

$$\left. \left. a \left( 2 b \text{EllipticF}\left[i \text{ArcSinh}\left[\sqrt{\frac{1}{a-b}} \sqrt{b+a \text{Cos}[c+d x]}\right], \frac{-a+b}{a+b}\right] + \right. \right.

$$\left. \left. a \text{EllipticPi}\left[1 - \frac{a}{b}, i \text{ArcSinh}\left[\sqrt{\frac{1}{a-b}} \sqrt{b+a \text{Cos}[c+d x]}\right], \frac{-a+b}{a+b}\right] \right) \right) \right) /$$

$$\left( a \sqrt{\frac{1}{a-b}} b \sqrt{b+a \text{Cos}[c+d x]} + 4 \text{Tan}[c+d x] \right) / (4 d \sqrt{\text{Sec}[c+d x]})$$$$$$$$



Problem 634: Result unnecessarily involves imaginary or complex numbers.

$$\int \sec [c + d x]^{3/2} (a + b \sec [c + d x])^{3/2} dx$$

Optimal (type 4, 299 leaves, 13 steps):

$$\frac{7 a b \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{\sec [c+d x]}}{4 d \sqrt{a+b \sec [c+d x]}} +$$

$$\left( (3 a^2 + 4 b^2) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{\sec [c+d x]} \right) /$$

$$\left( 4 d \sqrt{a+b \sec [c+d x]} \right) - \frac{5 a \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \sec [c+d x]}}{4 d \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \sqrt{\sec [c+d x]}} +$$

$$\frac{5 a \sqrt{\sec [c+d x]} \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{4 d} +$$

$$\frac{b \sec [c+d x]^{3/2} \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{2 d}$$

Result (type 4, 549 leaves):

$$\frac{1}{16 d (b + a \cos [c + d x])^{3/2} \sec [c + d x]^{3/2}}$$

$$(a + b \sec [c + d x])^{3/2} \left( \frac{8 a b \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{\sqrt{b+a \cos [c+d x]}} - \right.$$

$$\frac{2(-a^2-8 b^2) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{\sqrt{b+a \cos [c+d x]}} -$$

$$\left( 10 i a^2 \sqrt{\frac{a-a \cos [c+d x]}{a+b}} \sqrt{\frac{a+a \cos [c+d x]}{a-b}} \cos [2(c+d x)] \right.$$

$$\left. \left( -2 b(a+b) \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a-b}} \sqrt{b+a \cos [c+d x]}\right], \frac{-a+b}{a+b}\right] + \right.$$

$$a \left( 2 b \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a-b}} \sqrt{b+a \cos [c+d x]}\right], \frac{-a+b}{a+b}\right] + \right.$$

$$\left. \left. a \operatorname{EllipticPi}\left[1-\frac{a}{b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a-b}} \sqrt{b+a \cos [c+d x]}\right], \frac{-a+b}{a+b}\right] \right) \right)$$

$$\sin [c+d x] \Big/ \left( \sqrt{\frac{1}{a-b}} b \sqrt{1-\cos [c+d x]^2} \sqrt{\frac{a^2-a^2 \cos [c+d x]^2}{a^2}} \right.$$

$$\left. \left. \left( -a^2+2 b^2-4 b(b+a \cos [c+d x])+2(b+a \cos [c+d x])^2 \right) \right) \right) +$$

$$\left( (a+b \sec [c+d x])^{3/2} \left( \frac{5}{4} a \tan [c+d x] + \frac{1}{2} b \sec [c+d x] \tan [c+d x] \right) \right) \Big/$$

$$(d(b+a \cos [c+d x]) \sec [c+d x]^{3/2})$$

**Problem 635: Result unnecessarily involves imaginary or complex numbers.**

$$\int \sqrt{\sec [c+d x]} (a+b \sec [c+d x])^{3/2} dx$$

Optimal (type 4, 249 leaves, 12 steps):

$$\frac{(2a^2 + b^2) \sqrt{\frac{b+a \cos[c+dx]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), \frac{2a}{a+b}\right] \sqrt{\sec[c+dx]}}{d \sqrt{a+b \sec[c+dx]}} +$$

$$\frac{3ab \sqrt{\frac{b+a \cos[c+dx]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+dx), \frac{2a}{a+b}\right] \sqrt{\sec[c+dx]}}{d \sqrt{a+b \sec[c+dx]}} -$$

$$\frac{b \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), \frac{2a}{a+b}\right] \sqrt{a+b \sec[c+dx]}}{d \sqrt{\frac{b+a \cos[c+dx]}{a+b}} \sqrt{\sec[c+dx]}} +$$

$$\frac{b \sqrt{\sec[c+dx]} \sqrt{a+b \sec[c+dx]} \sin[c+dx]}{d}$$

Result (type 4, 394 leaves):

$$\frac{1}{4d \sec[c+dx]^{3/2}} (a+b \sec[c+dx])^{3/2} \left( \frac{8a^2 \sqrt{\frac{b+a \cos[c+dx]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), \frac{2a}{a+b}\right]}{(b+a \cos[c+dx])^2} + \right.$$

$$\frac{10ab \sqrt{\frac{b+a \cos[c+dx]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+dx), \frac{2a}{a+b}\right]}{(b+a \cos[c+dx])^2} -$$

$$\left( 2i \sqrt{\frac{a(-1+\cos[c+dx])}{a+b}} \sqrt{\frac{a(1+\cos[c+dx])}{a-b}} \operatorname{Csc}[c+dx] \right.$$

$$\left( -2b(a+b) \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a-b}} \sqrt{b+a \cos[c+dx]}\right], \frac{-a+b}{a+b}\right] + \right.$$

$$\left. a \left( 2b \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a-b}} \sqrt{b+a \cos[c+dx]}\right], \frac{-a+b}{a+b}\right] + \right.$$

$$\left. \left. \left. a \operatorname{EllipticPi}\left[1 - \frac{a}{b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a-b}} \sqrt{b+a \cos[c+dx]}\right], \frac{-a+b}{a+b}\right]\right)\right)\right) /$$

$$\left( a \sqrt{\frac{1}{a-b}} (b+a \cos[c+dx])^{3/2} + \frac{4b \tan[c+dx]}{b+a \cos[c+dx]} \right)$$

**Problem 640: Result unnecessarily involves imaginary or complex numbers.**

$$\int \text{Sec}[c + d x]^{3/2} (a + b \text{Sec}[c + d x])^{5/2} dx$$

Optimal (type 4, 369 leaves, 14 steps):

$$\begin{aligned} & \left( b (59 a^2 + 16 b^2) \sqrt{\frac{b + a \text{Cos}[c + d x]}{a + b}} \text{EllipticF}\left[\frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \sqrt{\text{Sec}[c + d x]} \right) / \\ & \left( 24 d \sqrt{a + b \text{Sec}[c + d x]} \right) + \\ & \left( 5 a (a^2 + 4 b^2) \sqrt{\frac{b + a \text{Cos}[c + d x]}{a + b}} \text{EllipticPi}\left[2, \frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \sqrt{\text{Sec}[c + d x]} \right) / \\ & \left( 8 d \sqrt{a + b \text{Sec}[c + d x]} \right) - \frac{(33 a^2 + 16 b^2) \text{EllipticE}\left[\frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \sqrt{a + b \text{Sec}[c + d x]}}{24 d \sqrt{\frac{b + a \text{Cos}[c + d x]}{a + b}} \sqrt{\text{Sec}[c + d x]}} + \\ & \frac{(33 a^2 + 16 b^2) \sqrt{\text{Sec}[c + d x]} \sqrt{a + b \text{Sec}[c + d x]} \text{Sin}[c + d x]}{24 d} + \\ & \frac{13 a b \text{Sec}[c + d x]^{3/2} \sqrt{a + b \text{Sec}[c + d x]} \text{Sin}[c + d x]}{12 d} + \\ & \frac{b^2 \text{Sec}[c + d x]^{5/2} \sqrt{a + b \text{Sec}[c + d x]} \text{Sin}[c + d x]}{3 d} \end{aligned}$$

Result (type 4, 602 leaves):

$$\begin{aligned}
 & \frac{1}{96 d (b + a \cos [c + d x])^{5/2} \sec [c + d x]^{5/2}} \\
 & a (a + b \sec [c + d x])^{5/2} \left( - \frac{104 a b \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{\sqrt{b+a \cos [c+d x]}} + \right. \\
 & \frac{2(3 a^2 - 104 b^2) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{\sqrt{b+a \cos [c+d x]}} + \\
 & \left( 2 i (33 a^2 + 16 b^2) \sqrt{\frac{a-a \cos [c+d x]}{a+b}} \sqrt{\frac{a+a \cos [c+d x]}{a-b}} \cos [2(c+d x)] \right. \\
 & \left. \left( -2 b (a+b) \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a-b}} \sqrt{b+a \cos [c+d x]}\right], \frac{-a+b}{a+b}\right] + \right. \right. \\
 & \left. a \left( 2 b \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a-b}} \sqrt{b+a \cos [c+d x]}\right], \frac{-a+b}{a+b}\right] + \right. \right. \\
 & \left. \left. a \operatorname{EllipticPi}\left[1 - \frac{a}{b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a-b}} \sqrt{b+a \cos [c+d x]}\right], \frac{-a+b}{a+b}\right] \right) \right) \\
 & \left. \sin [c+d x] \right) / \left( \sqrt{\frac{1}{a-b}} b \sqrt{1 - \cos [c+d x]^2} \sqrt{\frac{a^2 - a^2 \cos [c+d x]^2}{a^2}} \right. \\
 & \left. \left. \left( -a^2 + 2 b^2 - 4 b (b + a \cos [c+d x]) + 2 (b + a \cos [c+d x])^2 \right) \right) \right) + \\
 & \left( (a + b \sec [c+d x])^{5/2} \left( \frac{1}{24} \sec [c+d x] (33 a^2 \sin [c+d x] + 16 b^2 \sin [c+d x]) + \right. \right. \\
 & \left. \frac{13}{12} a b \sec [c+d x] \tan [c+d x] + \frac{1}{3} b^2 \sec [c+d x]^2 \tan [c+d x] \right) \right) / \\
 & \left( d (b + a \cos [c+d x])^2 \sec [c+d x]^{5/2} \right)
 \end{aligned}$$

**Problem 641: Result unnecessarily involves imaginary or complex numbers.**

$$\int \sqrt{\sec [c+d x]} (a + b \sec [c+d x])^{5/2} dx$$

Optimal (type 4, 314 leaves, 13 steps):

$$\begin{aligned}
 & \left( a (8 a^2 + 11 b^2) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \sqrt{\sec [c + d x]} \right) / \\
 & \left( 4 d \sqrt{a + b \sec [c + d x]} \right) + \\
 & \left( b (15 a^2 + 4 b^2) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \operatorname{EllipticPi}\left[2, \frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \sqrt{\sec [c + d x]} \right) / \\
 & \left( 4 d \sqrt{a + b \sec [c + d x]} \right) - \frac{9 a b \operatorname{EllipticE}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \sqrt{a + b \sec [c + d x]}}{4 d \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \sqrt{\sec [c + d x]}} + \\
 & \frac{9 a b \sqrt{\sec [c + d x]} \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{4 d} + \\
 & \frac{b^2 \sec [c + d x]^{3/2} \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{2 d}
 \end{aligned}$$

Result (type 4, 560 leaves):

$$\begin{aligned}
& \frac{1}{16 d (b + a \cos [c + d x])^{5/2} \sec [c + d x]^{5/2}} \\
& (a + b \sec [c + d x])^{5/2} \left( \frac{2 (16 a^3 + 4 a b^2) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{\sqrt{b+a \cos [c+d x]}} + \right. \\
& \frac{2 (21 a^2 b + 8 b^3) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{\sqrt{b+a \cos [c+d x]}} - \\
& \left( 18 i a^2 \sqrt{\frac{a-a \cos [c+d x]}{a+b}} \sqrt{\frac{a+a \cos [c+d x]}{a-b}} \cos [2(c+d x)] \right. \\
& \left. \left( -2 b (a+b) \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a-b}} \sqrt{b+a \cos [c+d x]}\right], \frac{-a+b}{a+b}\right] + \right. \right. \\
& \left. \left. a \left( 2 b \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a-b}} \sqrt{b+a \cos [c+d x]}\right], \frac{-a+b}{a+b}\right] + \right. \right. \right. \\
& \left. \left. \left. a \operatorname{EllipticPi}\left[1-\frac{a}{b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a-b}} \sqrt{b+a \cos [c+d x]}\right], \frac{-a+b}{a+b}\right] \right) \right) \right) \\
& \left. \sin [c+d x] \right) / \left( \sqrt{\frac{1}{a-b}} \sqrt{1-\cos [c+d x]^2} \sqrt{\frac{a^2-a^2 \cos [c+d x]^2}{a^2}} \right. \\
& \left. \left. \left( -a^2+2 b^2-4 b(b+a \cos [c+d x])+2(b+a \cos [c+d x])^2 \right) \right) \right) + \\
& \left( (a+b \sec [c+d x])^{5/2} \left( \frac{9}{4} a b \tan [c+d x] + \frac{1}{2} b^2 \sec [c+d x] \tan [c+d x] \right) \right) / \\
& \left( d (b+a \cos [c+d x])^2 \sec [c+d x]^{5/2} \right)
\end{aligned}$$

**Problem 642: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{(a+b \sec [c+d x])^{5/2}}{\sqrt{\sec [c+d x]}} dx$$

Optimal (type 4, 263 leaves, 12 steps):

$$\begin{aligned}
 & \frac{b (4 a^2 + b^2) \sqrt{\frac{b+a \operatorname{Cos}[c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{\operatorname{Sec}[c+d x]}}{d \sqrt{a+b \operatorname{Sec}[c+d x]}} + \\
 & \frac{5 a b^2 \sqrt{\frac{b+a \operatorname{Cos}[c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{\operatorname{Sec}[c+d x]}}{d \sqrt{a+b \operatorname{Sec}[c+d x]}} + \\
 & \frac{(2 a^2 - b^2) \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \operatorname{Sec}[c+d x]}}{d \sqrt{\frac{b+a \operatorname{Cos}[c+d x]}{a+b}} \sqrt{\operatorname{Sec}[c+d x]}} + \\
 & \frac{b^2 \sqrt{\operatorname{Sec}[c+d x]} \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{d}
 \end{aligned}$$

Result (type 4, 538 leaves):



$$\begin{aligned}
 & \frac{b^2 (a + b \operatorname{Sec}[c + d x])^{5/2} \operatorname{Sin}[c + d x]}{d (b + a \operatorname{Cos}[c + d x])^2 \operatorname{Sec}[c + d x]^{3/2}} + \frac{1}{4 d (b + a \operatorname{Cos}[c + d x])^{5/2} \operatorname{Sec}[c + d x]^{5/2}} \\
 & a (a + b \operatorname{Sec}[c + d x])^{5/2} \left( \frac{24 a b \sqrt{\frac{b+a \operatorname{Cos}[c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), \frac{2a}{a+b}\right]}{\sqrt{b + a \operatorname{Cos}[c + d x]}} + \right. \\
 & \frac{2 (2 a^2 + 9 b^2) \sqrt{\frac{b+a \operatorname{Cos}[c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2} (c + d x), \frac{2a}{a+b}\right]}{\sqrt{b + a \operatorname{Cos}[c + d x]}} + \\
 & \left( 2 i (2 a^2 - b^2) \sqrt{\frac{a - a \operatorname{Cos}[c + d x]}{a + b}} \sqrt{\frac{a + a \operatorname{Cos}[c + d x]}{a - b}} \operatorname{Cos}[2 (c + d x)] \right. \\
 & \left. \left( -2 b (a + b) \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a - b}} \sqrt{b + a \operatorname{Cos}[c + d x]}\right], \frac{-a + b}{a + b}\right] + \right. \right. \\
 & \left. \left. a \left( 2 b \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a - b}} \sqrt{b + a \operatorname{Cos}[c + d x]}\right], \frac{-a + b}{a + b}\right] + \right. \right. \\
 & \left. \left. a \operatorname{EllipticPi}\left[1 - \frac{a}{b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a - b}} \sqrt{b + a \operatorname{Cos}[c + d x]}\right], \frac{-a + b}{a + b}\right] \right) \right) \\
 & \left. \operatorname{Sin}[c + d x] \right) / \left( \sqrt{\frac{1}{a - b}} b \sqrt{1 - \operatorname{Cos}[c + d x]}^2 \sqrt{\frac{a^2 - a^2 \operatorname{Cos}[c + d x]^2}{a^2}} \right. \\
 & \left. \left. \left( -a^2 + 2 b^2 - 4 b (b + a \operatorname{Cos}[c + d x]) + 2 (b + a \operatorname{Cos}[c + d x])^2 \right) \right) \right)
 \end{aligned}$$

**Problem 643: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{(a + b \operatorname{Sec}[c + d x])^{5/2}}{\operatorname{Sec}[c + d x]^{3/2}} dx$$

Optimal (type 4, 262 leaves, 12 steps):

$$\left( 2 a (a^2 + 2 b^2) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \sqrt{\sec [c + d x]} \right) /$$

$$\left( 3 d \sqrt{a + b \sec [c + d x]} \right) + \frac{2 b^3 \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \operatorname{EllipticPi}\left[2, \frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \sqrt{\sec [c + d x]}}{d \sqrt{a + b \sec [c + d x]}} +$$

$$\frac{14 a b \operatorname{EllipticE}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \sqrt{a + b \sec [c + d x]}}{3 d \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \sqrt{\sec [c + d x]}} + \frac{2 a^2 \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{3 d \sqrt{\sec [c + d x]}}$$

Result (type 4, 540 leaves):



$$\begin{aligned}
 & - \frac{a \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{\sec [c+d x]}}{4 b d \sqrt{a+b \sec [c+d x]}} + \\
 & \left( (3 a^2+4 b^2) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{\sec [c+d x]} \right) / \\
 & \left( 4 b^2 d \sqrt{a+b \sec [c+d x]} \right) + \frac{3 a \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \sec [c+d x]}}{4 b^2 d \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \sqrt{\sec [c+d x]}} - \\
 & \frac{3 a \sqrt{\sec [c+d x]} \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{4 b^2 d} + \frac{\sec [c+d x]^{3 / 2} \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{2 b d}
 \end{aligned}$$

Result (type 4, 555 leaves):

$$\begin{aligned}
 & \frac{1}{16 b^2 d \sqrt{a+b \sec [c+d x]}} \\
 & \frac{\sqrt{b+a \cos [c+d x]} \sqrt{\sec [c+d x]}}{\left( \frac{8 a b \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{\sqrt{b+a \cos [c+d x]}} + \right. \\
 & \frac{2\left(9 a^2+8 b^2\right) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{\sqrt{b+a \cos [c+d x]}} + \\
 & \left( 6 i a^2 \sqrt{\frac{a-a \cos [c+d x]}{a+b}} \sqrt{\frac{a+a \cos [c+d x]}{a-b}} \cos [2(c+d x)] \right. \\
 & \left. \left( -2 b(a+b) \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a-b}} \sqrt{b+a \cos [c+d x]}\right], \frac{-a+b}{a+b}\right] + \right. \right. \\
 & \left. \left. a\left( 2 b \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a-b}} \sqrt{b+a \cos [c+d x]}\right], \frac{-a+b}{a+b}\right] + \right. \right. \right. \\
 & \left. \left. \left. a \operatorname{EllipticPi}\left[1-\frac{a}{b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a-b}} \sqrt{b+a \cos [c+d x]}\right], \frac{-a+b}{a+b}\right] \right) \right) \right) \\
 & \left. \frac{\sin [c+d x]}{\left( \sqrt{\frac{1}{a-b}} b \sqrt{1-\cos [c+d x]^2} \sqrt{\frac{a^2-a^2 \cos [c+d x]^2}{a^2}} \right)} \right) \\
 & \left. \left( -a^2+2 b^2-4 b(b+a \cos [c+d x])+2(b+a \cos [c+d x])^2 \right) \right) + \\
 & \frac{(b+a \cos [c+d x]) \sqrt{\sec [c+d x]}\left(-\frac{3 a \tan [c+d x]}{4 b^2}+\frac{\sec [c+d x] \tan [c+d x]}{2 b}\right)}{d \sqrt{a+b \sec [c+d x]}}
 \end{aligned}$$

**Problem 648: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{\sec [c+d x]^{5/2}}{\sqrt{a+b \sec [c+d x]}} dx$$

Optimal (type 4, 246 leaves, 12 steps):

$$\frac{\sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{\sec [c+d x]}}{d \sqrt{a+b \sec [c+d x]}} -$$

$$\frac{a \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{\sec [c+d x]}}{b d \sqrt{a+b \sec [c+d x]}} -$$

$$\frac{\operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \sec [c+d x]}}{b d \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \sqrt{\sec [c+d x]}} + \frac{\sqrt{\sec [c+d x]} \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{b d}$$

Result (type 4, 461 leaves):

$$\frac{(b+a \cos [c+d x]) \sec [c+d x]^{3/2} \sin [c+d x]}{b d \sqrt{a+b \sec [c+d x]}} -$$

$$\left( a \sqrt{b+a \cos [c+d x]} \sqrt{\sec [c+d x]} \left( \frac{6 \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{\sqrt{b+a \cos [c+d x]}} + \right. \right.$$

$$\left. \left( 2 i \sqrt{\frac{a-a \cos [c+d x]}{a+b}} \sqrt{\frac{a+a \cos [c+d x]}{a-b}} \cos [2(c+d x)] \right. \right.$$

$$\left. \left( -2 b(a+b) \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a-b}} \sqrt{b+a \cos [c+d x]}\right], \frac{-a+b}{a+b}\right] + \right. \right.$$

$$\left. a \left( 2 b \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a-b}} \sqrt{b+a \cos [c+d x]}\right], \frac{-a+b}{a+b}\right] + a \operatorname{EllipticPi}\left[ \right. \right.$$

$$\left. \left. \left. 1 - \frac{a}{b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a-b}} \sqrt{b+a \cos [c+d x]}\right], \frac{-a+b}{a+b}\right] \right) \sin [c+d x] \right) /$$

$$\left( \sqrt{\frac{1}{a-b}} b \sqrt{1-\cos [c+d x]^2} \sqrt{\frac{a^2-a^2 \cos [c+d x]^2}{a^2}} \left( -a^2+2 b^2 - \right. \right.$$

$$\left. \left. \left. 4 b(b+a \cos [c+d x]) + 2(b+a \cos [c+d x])^2 \right) \right) / \left( 4 b d \sqrt{a+b \sec [c+d x]} \right)$$

**Problem 654: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{\text{Sec}[c + d x]^{7/2}}{(a + b \text{Sec}[c + d x])^{3/2}} dx$$

Optimal (type 4, 345 leaves, 13 steps):

$$\frac{\sqrt{\frac{b+a \cos[c+dx]}{a+b}} \text{EllipticF}\left[\frac{1}{2}(c+dx), \frac{2a}{a+b}\right] \sqrt{\text{Sec}[c+dx]}}{b d \sqrt{a+b \text{Sec}[c+dx]}} -$$

$$\frac{3 a \sqrt{\frac{b+a \cos[c+dx]}{a+b}} \text{EllipticPi}\left[2, \frac{1}{2}(c+dx), \frac{2a}{a+b}\right] \sqrt{\text{Sec}[c+dx]}}{b^2 d \sqrt{a+b \text{Sec}[c+dx]}} -$$

$$\frac{(3 a^2 - b^2) \text{EllipticE}\left[\frac{1}{2}(c+dx), \frac{2a}{a+b}\right] \sqrt{a+b \text{Sec}[c+dx]}}{b^2 (a^2 - b^2) d \sqrt{\frac{b+a \cos[c+dx]}{a+b}} \sqrt{\text{Sec}[c+dx]}} -$$

$$\frac{2 a^2 \text{Sec}[c+dx]^{3/2} \text{Sin}[c+dx]}{b (a^2 - b^2) d \sqrt{a+b \text{Sec}[c+dx]}} + \frac{(3 a^2 - b^2) \sqrt{\text{Sec}[c+dx]} \sqrt{a+b \text{Sec}[c+dx]} \text{Sin}[c+dx]}{b^2 (a^2 - b^2) d}$$

Result (type 4, 592 leaves):





Optimal (type 4, 206 leaves, 9 steps):

$$\frac{2 \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{\sec [c+d x]}}{b d \sqrt{a+b \sec [c+d x]}} +$$

$$\frac{2 a \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \sec [c+d x]}}{b\left(a^2-b^2\right) d \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \sqrt{\sec [c+d x]}} - \frac{2 a^2 \sqrt{\sec [c+d x]} \sin [c+d x]}{b\left(a^2-b^2\right) d \sqrt{a+b \sec [c+d x]}}$$

Result (type 4, 557 leaves):

$$\frac{2 a^2 (b+a \cos [c+d x]) \sec [c+d x]^{3/2} \sin [c+d x]}{b\left(-a^2+b^2\right) d (a+b \sec [c+d x])^{3/2}} + \frac{1}{2(a-b) b (a+b) d (a+b \sec [c+d x])^{3/2}}$$

$$(b+a \cos [c+d x])^{3/2} \sec [c+d x]^{3/2} \left( \frac{4 a b \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{\sqrt{b+a \cos [c+d x]}} + \right.$$

$$\frac{2\left(3 a^2-2 b^2\right) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{\sqrt{b+a \cos [c+d x]}} +$$

$$\left( 2 i a^2 \sqrt{\frac{a-a \cos [c+d x]}{a+b}} \sqrt{\frac{a+a \cos [c+d x]}{a-b}} \cos [2(c+d x)] \right.$$

$$\left. \left( -2 b (a+b) \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a-b}} \sqrt{b+a \cos [c+d x]}\right], \frac{-a+b}{a+b}\right] + \right.$$

$$\left. a \left( 2 b \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a-b}} \sqrt{b+a \cos [c+d x]}\right], \frac{-a+b}{a+b}\right] + \right.$$

$$\left. \left. a \operatorname{EllipticPi}\left[1-\frac{a}{b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a-b}} \sqrt{b+a \cos [c+d x]}\right], \frac{-a+b}{a+b}\right] \right) \right)$$

$$\sin [c+d x] \left/ \left( \sqrt{\frac{1}{a-b}} b \sqrt{1-\cos [c+d x]}^2 \sqrt{\frac{a^2-a^2 \cos [c+d x]^2}{a^2}} \right.$$

$$\left. \left. \left( -a^2+2 b^2-4 b (b+a \cos [c+d x]) + 2 (b+a \cos [c+d x])^2 \right) \right) \right)$$

### Problem 661: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\operatorname{Sec}[c + d x]^{9/2}}{(a + b \operatorname{Sec}[c + d x])^{5/2}} dx$$

Optimal (type 4, 458 leaves, 14 steps):

$$\frac{(5 a^2 - 3 b^2) \sqrt{\frac{b+a \operatorname{Cos}[c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{\operatorname{Sec}[c+d x]}}{3 b^2 (a^2 - b^2) d \sqrt{a+b \operatorname{Sec}[c+d x]}} -$$

$$\frac{5 a \sqrt{\frac{b+a \operatorname{Cos}[c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{\operatorname{Sec}[c+d x]}}{b^3 d \sqrt{a+b \operatorname{Sec}[c+d x]}} -$$

$$\left( (15 a^4 - 26 a^2 b^2 + 3 b^4) \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \operatorname{Sec}[c+d x]} \right) /$$

$$\left( 3 b^3 (a^2 - b^2)^2 d \sqrt{\frac{b+a \operatorname{Cos}[c+d x]}{a+b}} \sqrt{\operatorname{Sec}[c+d x]} \right) -$$

$$\frac{2 a^2 \operatorname{Sec}[c+d x]^{5/2} \operatorname{Sin}[c+d x]}{3 b (a^2 - b^2) d (a+b \operatorname{Sec}[c+d x])^{3/2}} - \frac{2 a^2 (5 a^2 - 9 b^2) \operatorname{Sec}[c+d x]^{3/2} \operatorname{Sin}[c+d x]}{3 b^2 (a^2 - b^2)^2 d \sqrt{a+b \operatorname{Sec}[c+d x]}} +$$

$$\frac{1}{3 b^3 (a^2 - b^2)^2 d} (15 a^4 - 26 a^2 b^2 + 3 b^4) \sqrt{\operatorname{Sec}[c+d x]} \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]$$

Result (type 4, 677 leaves):

$$\begin{aligned}
 & - \frac{1}{12 (a-b)^2 b^3 (a+b)^2 d (a+b \sec [c+d x])^{5/2}} a (b+a \cos [c+d x])^{5/2} \sec [c+d x]^{5/2} \\
 & \left( \frac{2 (20 a^3 b - 36 a b^3) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2} (c+d x), \frac{2 a}{a+b}\right]}{\sqrt{b+a \cos [c+d x]}} + \left( 2 (45 a^4 - 86 a^2 b^2 + 33 b^4) \right. \right. \\
 & \left. \left. \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2} (c+d x), \frac{2 a}{a+b}\right] \right) / \left( \sqrt{b+a \cos [c+d x]} \right) + \right. \\
 & \left( 2 i (15 a^4 - 26 a^2 b^2 + 3 b^4) \sqrt{\frac{a-a \cos [c+d x]}{a+b}} \sqrt{\frac{a+a \cos [c+d x]}{a-b}} \cos [2 (c+d x)] \right. \\
 & \left( -2 b (a+b) \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a-b}} \sqrt{b+a \cos [c+d x]}\right], \frac{-a+b}{a+b}\right] + \right. \\
 & a \left( 2 b \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a-b}} \sqrt{b+a \cos [c+d x]}\right], \frac{-a+b}{a+b}\right] + \right. \\
 & \left. \left. a \operatorname{EllipticPi}\left[1 - \frac{a}{b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a-b}} \sqrt{b+a \cos [c+d x]}\right], \frac{-a+b}{a+b}\right] \right) \right) \\
 & \left. \sin [c+d x] \right) / \left( \sqrt{\frac{1}{a-b}} b \sqrt{1 - \cos [c+d x]} \sqrt{\frac{a^2 - a^2 \cos [c+d x]^2}{a^2}} \right. \\
 & \left. \left. \left( -a^2 + 2 b^2 - 4 b (b+a \cos [c+d x]) + 2 (b+a \cos [c+d x])^2 \right) \right) \right) + \\
 & \left( (b+a \cos [c+d x])^3 \sec [c+d x]^{5/2} \left( -\frac{2 a^3 \sin [c+d x]}{3 b^2 (-a^2 + b^2) (b+a \cos [c+d x])^2} - \right. \right. \\
 & \left. \frac{4 (-3 a^5 \sin [c+d x] + 5 a^3 b^2 \sin [c+d x])}{3 b^3 (-a^2 + b^2)^2 (b+a \cos [c+d x])} + \right. \\
 & \left. \left. \frac{\tan [c+d x]}{b^3} \right) \right) / \left( d (a+b \sec [c+d x])^{5/2} \right)
 \end{aligned}$$

**Problem 662: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{\text{Sec}[c + d x]^{7/2}}{(a + b \text{Sec}[c + d x])^{5/2}} dx$$

Optimal (type 4, 370 leaves, 13 steps):

$$\frac{2 a \sqrt{\frac{b+a \text{Cos}[c+d x]}{a+b}} \text{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{\text{Sec}[c+d x]}}{3 b\left(a^2-b^2\right) d \sqrt{a+b \text{Sec}[c+d x]}} +$$

$$\frac{2 \sqrt{\frac{b+a \text{Cos}[c+d x]}{a+b}} \text{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{\text{Sec}[c+d x]}}{b^2 d \sqrt{a+b \text{Sec}[c+d x]}} +$$

$$\frac{2 a\left(3 a^2-7 b^2\right) \text{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \text{Sec}[c+d x]}}{3 b^2\left(a^2-b^2\right)^2 d \sqrt{\frac{b+a \text{Cos}[c+d x]}{a+b}} \sqrt{\text{Sec}[c+d x]}} -$$

$$\frac{2 a^2 \text{Sec}[c+d x]^{3/2} \text{Sin}[c+d x]}{3 b\left(a^2-b^2\right) d\left(a+b \text{Sec}[c+d x]\right)^{3/2}} - \frac{2 a^2\left(3 a^2-7 b^2\right) \sqrt{\text{Sec}[c+d x]} \text{Sin}[c+d x]}{3 b^2\left(a^2-b^2\right)^2 d \sqrt{a+b \text{Sec}[c+d x]}}$$

Result (type 4, 661 leaves):

$$\frac{1}{6 (a-b)^2 b^2 (a+b)^2 d (a+b \sec [c+dx])^{5/2}} (b+a \cos [c+dx])^{5/2} \sec [c+dx]^{5/2} \left( \frac{2 (4 a^3 b - 12 a b^3) \sqrt{\frac{b+a \cos [c+dx]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2} (c+dx), \frac{2a}{a+b}\right]}{\sqrt{b+a \cos [c+dx]}} + \right.$$

$$\left. \left( 2 (9 a^4 - 19 a^2 b^2 + 6 b^4) \sqrt{\frac{b+a \cos [c+dx]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2} (c+dx), \frac{2a}{a+b}\right] \right) / \left( \sqrt{b+a \cos [c+dx]} \right) + \right.$$

$$\left. \left( 2 i (3 a^4 - 7 a^2 b^2) \sqrt{\frac{a-a \cos [c+dx]}{a+b}} \sqrt{\frac{a+a \cos [c+dx]}{a-b}} \cos [2 (c+dx)] \left( -2 b (a+b) \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a-b}} \sqrt{b+a \cos [c+dx]}\right], \frac{-a+b}{a+b}\right] + \right. \right. \right.$$

$$\left. \left. \left. a \left( 2 b \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a-b}} \sqrt{b+a \cos [c+dx]}\right], \frac{-a+b}{a+b}\right] + a \operatorname{EllipticPi}\left[1 - \frac{a}{b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a-b}} \sqrt{b+a \cos [c+dx]}\right], \frac{-a+b}{a+b}\right] \right) \right) \right) / \left( \sqrt{\frac{1}{a-b}} b \sqrt{1 - \cos [c+dx]}^2 \sqrt{\frac{a^2 - a^2 \cos [c+dx]^2}{a^2}} \right.$$

$$\left. \left. \left. \left( -a^2 + 2 b^2 - 4 b (b+a \cos [c+dx]) + 2 (b+a \cos [c+dx])^2 \right) \right) \right) + \left( (b+a \cos [c+dx])^3 \sec [c+dx]^{5/2} \left( \frac{2 a^2 \sin [c+dx]}{3 b (-a^2 + b^2) (b+a \cos [c+dx])^2} + \frac{2 (-3 a^4 \sin [c+dx] + 7 a^2 b^2 \sin [c+dx])}{3 b^2 (-a^2 + b^2)^2 (b+a \cos [c+dx])} \right) \right) / (d (a+b \sec [c+dx])^{5/2})$$

**Problem 685: Result more than twice size of optimal antiderivative.**

$$\int \sec [c+dx] (a+b \sec [c+dx])^{1/3} dx$$

Optimal (type 6, 105 leaves, 3 steps):

$$\left( \sqrt{2} \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, -\frac{1}{3}, \frac{3}{2}, \frac{1}{2} (1 - \operatorname{Sec}[c + dx]), \frac{b(1 - \operatorname{Sec}[c + dx])}{a+b} \right] \right. \\ \left. (a + b \operatorname{Sec}[c + dx])^{1/3} \operatorname{Tan}[c + dx] \right) / \left( d \sqrt{1 + \operatorname{Sec}[c + dx]} \left( \frac{a + b \operatorname{Sec}[c + dx]}{a+b} \right)^{1/3} \right)$$

Result (type 6, 11281 leaves):

$$\frac{3 (a + b \operatorname{Sec}[c + dx])^{1/3} \operatorname{Sin}[c + dx]}{d} + \\ \left( -\frac{2b}{(b + a \operatorname{Cos}[c + dx])^{2/3} \operatorname{Sec}[c + dx]^{2/3}} - \frac{a \operatorname{Sec}[c + dx]^{1/3}}{2 (b + a \operatorname{Cos}[c + dx])^{2/3}} - \right. \\ \left. \frac{3a \operatorname{Cos}[2(c + dx)] \operatorname{Sec}[c + dx]^{1/3}}{2 (b + a \operatorname{Cos}[c + dx])^{2/3}} \right) (a + b \operatorname{Sec}[c + dx])^{1/3} \\ \left( -\frac{3 \operatorname{Tan}[\frac{1}{2}(c + dx)] \left( \frac{a+b-a \operatorname{Tan}[\frac{1}{2}(c+dx)]^2 + b \operatorname{Tan}[\frac{1}{2}(c+dx)]^2}{1 + \operatorname{Tan}[\frac{1}{2}(c+dx)]^2} \right)^{1/3}}{\left( \frac{1 + \operatorname{Tan}[\frac{1}{2}(c+dx)]^2}{1 - \operatorname{Tan}[\frac{1}{2}(c+dx)]^2} \right)^{2/3}} - \left( 3(a+b) \operatorname{Tan}[\frac{1}{2}(c + dx)] \right) \right. \\ \left. \left( 10(a-b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}[\frac{1}{2}(c + dx)]^2, \frac{(a-b) \operatorname{Tan}[\frac{1}{2}(c + dx)]^2}{a+b} \right] \right. \right. \\ \left. \left( 2(a-b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \operatorname{Tan}[\frac{1}{2}(c + dx)]^2, \frac{(a-b) \operatorname{Tan}[\frac{1}{2}(c + dx)]^2}{a+b} \right] \right. + \right. \\ \left. \left. (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}[\frac{1}{2}(c + dx)]^2, \frac{(a-b) \operatorname{Tan}[\frac{1}{2}(c + dx)]^2}{a+b} \right] \right) \right) \\ \operatorname{Tan}[\frac{1}{2}(c + dx)]^4 + 3(a+b) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan}[\frac{1}{2}(c + dx)]^2, \right. \\ \left. \frac{(a-b) \operatorname{Tan}[\frac{1}{2}(c + dx)]^2}{a+b} \right] \left( -2 \left( 2(a-b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan}[\frac{1}{2}(c + dx)]^2, \right. \right. \right. \\ \left. \left. \frac{(a-b) \operatorname{Tan}[\frac{1}{2}(c + dx)]^2}{a+b} \right] + (a+b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \right. \right. \\ \left. \left. \operatorname{Tan}[\frac{1}{2}(c + dx)]^2, \frac{(a-b) \operatorname{Tan}[\frac{1}{2}(c + dx)]^2}{a+b} \right] \right) \operatorname{Tan}[\frac{1}{2}(c + dx)]^2 + \\ \left. 15 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}[\frac{1}{2}(c + dx)]^2, \frac{(a-b) \operatorname{Tan}[\frac{1}{2}(c + dx)]^2}{a+b} \right] \right)$$

$$\left( \left( \left( \left( \left( \left( a \left( -1 + \tan \left[ \frac{1}{2} (c + dx) \right]^2 \right) - b \left( 1 + \tan \left[ \frac{1}{2} (c + dx) \right]^2 \right) \right) \right) \right) \right) \right) \right) \left( \left( \left( \left( \left( \left( -1 + \tan \left[ \frac{1}{2} (c + dx) \right]^2 \right) \left( \frac{1 + \tan \left[ \frac{1}{2} (c + dx) \right]^2}{1 - \tan \left[ \frac{1}{2} (c + dx) \right]^2} \right)^{2/3} \right. \right. \right. \right. \right. \right. \right.$$

$$\left. \left. \left. \left. \left. \left( \frac{a + b - a \tan \left[ \frac{1}{2} (c + dx) \right]^2 + b \tan \left[ \frac{1}{2} (c + dx) \right]^2}{1 + \tan \left[ \frac{1}{2} (c + dx) \right]^2} \right)^{2/3} \right. \right. \right. \right. \right. \right. \right.$$

$$\left. \left. \left. \left. \left. \left( 9 (a + b) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, \frac{(a - b) \tan \left[ \frac{1}{2} (c + dx) \right]^2}{a + b} \right] + \right. \right. \right. \right. \right. \right. \right.$$

$$\left. \left. \left. \left. \left. \left( 2 \left( 2 (a - b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, \frac{(a - b) \tan \left[ \frac{1}{2} (c + dx) \right]^2}{a + b} \right] + \right. \right. \right. \right. \right. \right. \right.$$

$$\left. \left. \left. \left. \left. \left( (a + b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, \right. \right. \right. \right. \right. \right. \right.$$

$$\left. \left. \left. \left. \left. \left( \frac{(a - b) \tan \left[ \frac{1}{2} (c + dx) \right]^2}{a + b} \right) \tan \left[ \frac{1}{2} (c + dx) \right]^2 \right) \right) \right) \right) \right) \left( \left( \left( \left( \left( \left( 15 (a + b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, \frac{(a - b) \tan \left[ \frac{1}{2} (c + dx) \right]^2}{a + b} \right] + \right. \right. \right. \right. \right. \right. \right.$$

$$\left. \left. \left. \left. \left. \left( 2 \left( 2 (a - b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, \frac{(a - b) \tan \left[ \frac{1}{2} (c + dx) \right]^2}{a + b} \right] + \right. \right. \right. \right. \right. \right. \right.$$

$$\left. \left. \left. \left. \left. \left( (a + b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, \frac{(a - b) \tan \left[ \frac{1}{2} (c + dx) \right]^2}{a + b} \right] \right) \right) \right) \right) \right) \right) \left( \left( \left( \left( \left( \left( \tan \left[ \frac{1}{2} (c + dx) \right]^2 \right) \right) \right) \right) \right) \right) \left( d (b + a \cos [c + dx])^{1/3} \right)$$

$$\operatorname{Sec} [c + dx]^{1/3} \left( - \frac{3 \operatorname{Sec} \left[ \frac{1}{2} (c + dx) \right]^2 \left( \frac{a + b - a \tan \left[ \frac{1}{2} (c + dx) \right]^2 + b \tan \left[ \frac{1}{2} (c + dx) \right]^2}{1 + \tan \left[ \frac{1}{2} (c + dx) \right]^2} \right)^{1/3}}{2 \left( \frac{1 + \tan \left[ \frac{1}{2} (c + dx) \right]^2}{1 - \tan \left[ \frac{1}{2} (c + dx) \right]^2} \right)^{2/3}} + \right.$$

$$\left. \left( 2 \tan \left[ \frac{1}{2} (c + dx) \right] \left( \frac{a + b - a \tan \left[ \frac{1}{2} (c + dx) \right]^2 + b \tan \left[ \frac{1}{2} (c + dx) \right]^2}{1 + \tan \left[ \frac{1}{2} (c + dx) \right]^2} \right)^{1/3} \right)$$

$$\begin{aligned}
& \left( \frac{\text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \text{Tan}\left[\frac{1}{2}(c+dx)\right]}{1 - \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2} + \left( \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \text{Tan}\left[\frac{1}{2}(c+dx)\right] \right. \right. \\
& \quad \left. \left. \left(1 + \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \right) / \left(1 - \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)^2 \right) / \left( \frac{1 + \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1 - \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \right)^{5/3} - \\
& \left( \text{Tan}\left[\frac{1}{2}(c+dx)\right] \left( \left( -a \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \text{Tan}\left[\frac{1}{2}(c+dx)\right] + b \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \right. \\
& \quad \left. \left. \left. \text{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \right) / \left(1 + \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) - \left( \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \text{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \right. \\
& \quad \left. \left( a + b - a \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) / \left(1 + \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)^2 \right) / \\
& \left( \left( \frac{1 + \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1 - \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \right)^{2/3} \left( \frac{a + b - a \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1 + \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \right)^{2/3} \right) + \\
& \left( 3(a+b) \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
& \quad \left( 10(a-b) \text{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
& \quad \left( 2(a-b) \text{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) + \\
& \quad \left. (a+b) \text{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \\
& \quad \text{Tan}\left[\frac{1}{2}(c+dx)\right]^4 + 3(a+b) \text{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
& \quad \left. \frac{(a-b) \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \left( -2 \left( 2(a-b) \text{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
& \quad \left. \left. \left. \frac{(a-b) \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right) \right) + (a+b) \text{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \right. \right. \\
& \quad \left. \left. \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + \\
& \quad \left. 15 \text{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \\
& \quad \left. \left( a \left( -1 + \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) /
\end{aligned}$$



$$\begin{aligned}
 & \left( \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right] \right)^2 \left( \frac{1 + \tan\left[\frac{1}{2}(c+dx)\right]}{1 - \tan\left[\frac{1}{2}(c+dx)\right]} \right)^2 \right)^{2/3} \\
 & \left( \frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right] + b \tan\left[\frac{1}{2}(c+dx)\right]}{1 + \tan\left[\frac{1}{2}(c+dx)\right]} \right)^{2/3} \\
 & \left( 9(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + \\
 & 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + \\
 & (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]\right]^2, \\
 & \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \\
 & \left( 15(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + \\
 & 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + \\
 & (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right) \\
 & \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - \left( 3(a+b) \sec\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \left. \left( 10(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right. \right. \\
 & \left. \left( 2(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + \right. \\
 & \left. \left. (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \right) \\
 & \tan\left[\frac{1}{2}(c+dx)\right]^4 + 3(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]\right]^2, \\
 & \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \left( -2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]\right]^2, \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \right. \right. \right. \\
 & \left. \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + \right. \\
 & \left. 15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \right) \left. \right) \left. \right) / \\
 & \left( 2 \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( \frac{1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \right)^{2/3} \right. \right. \\
 & \left. \left. \left( \frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \right)^{2/3} \right) \right. \\
 & \left. \left( 9(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + \right. \right. \\
 & \left. \left. 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + \right. \right. \right. \\
 & \left. \left. \left. (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) \\
 & \left( 15(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + \right. \\
 & \left. 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + \right. \right. \\
 & \left. \left. \left. (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) + \\
 & \left( 2(a+b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \left( \frac{\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} + \left( \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( \tan\left[\frac{1}{2}(c+dx)\right] \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \right) / \left(1 - \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2 \\
 & \left( 10(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \quad \left. \left( 2(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) + \right. \\
 & \quad \left. (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \right) \\
 & \tan\left[\frac{1}{2}(c+dx)\right]^4 + 3(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \quad \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \left( -2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \right. \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 + \right. \\
 & \quad \left. 15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \right) \right) / \\
 & \left( (-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2) \left( \frac{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^{5/3} \right. \\
 & \quad \left( \frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^{2/3} \\
 & \quad \left( 9(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & \quad \left. 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) + \right. \\
 & \quad \left. (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 \end{aligned}$$

$$\begin{aligned}
& \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) \\
& \left( 15(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
& \quad 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
& \quad \left. \left. (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \right) \\
& \quad \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \Bigg) + \left( 2(a+b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right. \\
& \quad \left( \left( -a \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + b \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) / \right. \\
& \quad \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) - \left( \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right. \\
& \quad \left. \left. \left( a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) / \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \right) \\
& \quad \left( 10(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
& \quad \left( 2(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
& \quad \left. \left. (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \right) \\
& \quad \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^4 + 3(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
& \quad \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \left( -2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
& \quad \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right) + (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \right. \right. \\
& \quad \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + \\
& \quad \left. 15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right)
\end{aligned}$$

$$\begin{aligned}
 & \left( a \left( -1 + \tan \left[ \frac{1}{2} (c + dx) \right]^2 \right) - b \left( 1 + \tan \left[ \frac{1}{2} (c + dx) \right]^2 \right) \right) \Big/ \\
 & \left( -1 + \tan \left[ \frac{1}{2} (c + dx) \right]^2 \right) \left( \frac{1 + \tan \left[ \frac{1}{2} (c + dx) \right]^2}{1 - \tan \left[ \frac{1}{2} (c + dx) \right]^2} \right)^{2/3} \\
 & \left( \frac{a + b - a \tan \left[ \frac{1}{2} (c + dx) \right]^2 + b \tan \left[ \frac{1}{2} (c + dx) \right]^2}{1 + \tan \left[ \frac{1}{2} (c + dx) \right]^2} \right)^{5/3} \\
 & \left( 9 (a + b) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, \frac{(a - b) \tan \left[ \frac{1}{2} (c + dx) \right]^2}{a + b} \right] + \right. \\
 & 2 \left( 2 (a - b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, \frac{(a - b) \tan \left[ \frac{1}{2} (c + dx) \right]^2}{a + b} \right] + \right. \\
 & (a + b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, \right. \\
 & \left. \left. \frac{(a - b) \tan \left[ \frac{1}{2} (c + dx) \right]^2}{a + b} \right] \right) \tan \left[ \frac{1}{2} (c + dx) \right]^2 \Big) \\
 & \left( 15 (a + b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, \frac{(a - b) \tan \left[ \frac{1}{2} (c + dx) \right]^2}{a + b} \right] + \right. \\
 & 2 \left( 2 (a - b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, \frac{(a - b) \tan \left[ \frac{1}{2} (c + dx) \right]^2}{a + b} \right] + \right. \\
 & \left. \left. (a + b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, \frac{(a - b) \tan \left[ \frac{1}{2} (c + dx) \right]^2}{a + b} \right] \right) \right) \\
 & \tan \left[ \frac{1}{2} (c + dx) \right]^2 \Big) + \left( 3 (a + b) \tan \left[ \frac{1}{2} (c + dx) \right] \right. \\
 & \left. 2 \left( 2 (a - b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, \frac{(a - b) \tan \left[ \frac{1}{2} (c + dx) \right]^2}{a + b} \right] + \right. \right. \\
 & \left. \left. (a + b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, \frac{(a - b) \tan \left[ \frac{1}{2} (c + dx) \right]^2}{a + b} \right] \right) \right) \\
 & \operatorname{Sec} \left[ \frac{1}{2} (c + dx) \right]^2 \tan \left[ \frac{1}{2} (c + dx) \right] + 9 (a + b) \left( \frac{1}{9 (a + b)} \right. \\
 & \left. 2 (a - b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, \frac{(a - b) \tan \left[ \frac{1}{2} (c + dx) \right]^2}{a + b} \right] \right)
 \end{aligned}$$

$$\begin{aligned}
& \left. \begin{aligned}
& \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{9} \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]\right]^2, \\
& \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right] + \\
& 2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \left( 2(a-b) \left( \frac{1}{a+b} (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{8}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]\right]^2, \right. \right. \\
& \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right) \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \\
& \left. \frac{1}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{5}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right. \\
& \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + (a+b) \left( \frac{1}{5(a+b)} 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \right. \right. \\
& \left. \left. \frac{4}{3}, \frac{5}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right) \sec\left[\frac{1}{2}(c+dx)\right]^2 \\
& \tan\left[\frac{1}{2}(c+dx)\right] + \frac{4}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{7}{3}, \frac{2}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]\right]^2, \\
& \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right) \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) \\
& \left( 10(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right) \\
& \left( 2(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right) + \\
& \left. (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right) \right) \\
& \tan\left[\frac{1}{2}(c+dx)\right]^4 + 3(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]\right]^2, \\
& \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right) \left( -2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]\right]^2, \right. \right. \\
& \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right) + (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \right. \right. \\
& \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right) \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 +
\end{aligned}$$

$$\begin{aligned}
 & 15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \\
 & \left( a \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Bigg) \Bigg) \Bigg) \Bigg) / \\
 & \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( \frac{1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \right)^{2/3} \\
 & \left( \frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \right)^{2/3} \\
 & \left( 9(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & \left. 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \right. \\
 & \left. \left. (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \\
 & \left( 15(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & \left. 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \right. \\
 & \left. \left. (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \right) \\
 & \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) \Bigg) + \left( 3(a+b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right. \\
 & \left. 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \right. \\
 & \left. \left. (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \right) \\
 & \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + 15(a+b) \left( \frac{1}{5(a+b)} \right)
 \end{aligned}$$

$$\begin{aligned}
& 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \\
& \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
& \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \Bigg) + \\
& 2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \left( 2(a-b) \left( \frac{1}{21(a+b)} 25(a-b) \operatorname{AppellF1}\left[\frac{7}{2}, \frac{1}{3}, \frac{8}{3}, \right. \right. \right. \\
& \left. \left. \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \\
& \left. \left. \tan\left[\frac{1}{2}(c+dx)\right] + \frac{5}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{4}{3}, \frac{5}{3}, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
& \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) + \\
& (a+b) \left( \frac{1}{21(a+b)} 10(a-b) \operatorname{AppellF1}\left[\frac{7}{2}, \frac{4}{3}, \frac{5}{3}, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \\
& \left. \frac{20}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{7}{3}, \frac{2}{3}, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
& \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \Bigg) \\
& \left( 10(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
& \left( 2(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
& \left. (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \\
& \tan\left[\frac{1}{2}(c+dx)\right]^4 + 3(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
& \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \left( -2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right.
\end{aligned}$$



$$\begin{aligned}
 & \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \right. \\
 & \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + \\
 & 15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \\
 & \left. \left( a \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) \right) \Big/ \\
 & \left( \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( \frac{1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \right)^{2/3} \right. \\
 & \left. \left( \frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \right)^{2/3} \right) \\
 & \left( 9(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + \right. \\
 & 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + \right. \\
 & (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \\
 & \left( 15(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + \right. \\
 & 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + \right. \\
 & \left. (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \\
 & \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) - \left( 3(a+b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \\
 & \left( 20(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( 2 (a - b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, \frac{(a - b) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] + \right. \\
 & \quad \left. (a + b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, \frac{(a - b) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] \right) \\
 & \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^3 + 10 (a - b) \\
 & \left( 2 (a - b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, \frac{(a - b) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] + \right. \\
 & \quad \left. (a + b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, \frac{(a - b) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] \right) \\
 & \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^4 \left( \frac{1}{5 (a + b)} 2 (a - b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a - b) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right] + \right. \\
 & \quad \left. \frac{1}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, \frac{(a - b) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] \right. \\
 & \quad \left. \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right] \right) + \\
 & 10 (a - b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, \frac{(a - b) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] \\
 & \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^4 \left( 2 (a - b) \left( \frac{1}{a + b} (a - b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, \frac{8}{3}, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{(a - b) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right] + \right. \\
 & \quad \left. \frac{1}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, \frac{(a - b) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] \right. \\
 & \quad \left. \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right] \right) + (a + b) \left( \frac{1}{5 (a + b)} 2 (a - b) \operatorname{AppellF1} \left[ \frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \frac{4}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, \frac{(a - b) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \right. \\
 & \quad \left. \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right] + \frac{4}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{7}{3}, \frac{2}{3}, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) + \\
 3(a+b) & \left( \frac{1}{9(a+b)} 2(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \left. \frac{1}{9} \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \left( -2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \right. \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \right. \right. \\
 & \left. \left. \frac{2}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + \\
 15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \\
 & \left. \left( a \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) + \\
 3(a+b) & \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \\
 & \left( -2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + \right. \right. \\
 & \left. \left. (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \right) \\
 & \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + 15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \right. \\
 & \left. \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \\
 & \left( a \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] - b \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) - \\
 2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 & \left( 2(a-b) \left( \frac{1}{21(a+b)} 25(a-b) \operatorname{AppellF1}\left[\frac{7}{2}, \frac{1}{3}, \frac{8}{3}, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
& \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \\
& \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \frac{5}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{4}{3}, \frac{5}{3}, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
& \left. \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right) + \\
& (a+b) \left( \frac{1}{21(a+b)} 10(a-b) \operatorname{AppellF1}\left[\frac{7}{2}, \frac{4}{3}, \frac{5}{3}, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \left. \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \\
& \left. \frac{20}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{7}{3}, \frac{2}{3}, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
& \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right] + 15 \left( \frac{1}{5(a+b)} 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \right. \right. \right. \\
& \left. \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
& \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \frac{1}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \left. \left. \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right) \\
& \left. \left. \left. \left( a \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) \right) \right) \right) \Big/ \\
& \left( \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( \frac{1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \right)^{2/3} \right. \\
& \left. \left( \frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \right)^{2/3} \right. \\
& \left. \left( 9(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \right. \\
& \left. \left. 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \right. \right. \\
& \left. \left. (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
 & \left. \left. \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right. \\
 & \left( 15 (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & 2 \left( 2 (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \left. \left. \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) \right)
 \end{aligned}$$

### Problem 687: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Sec}[c+dx]^4 (a+b \operatorname{Sec}[c+dx])^{2/3} dx$$

Optimal (type 6, 362 leaves, 10 steps):

$$\begin{aligned}
 & \frac{3 (9 a^2 + 32 b^2) (a+b \operatorname{Sec}[c+dx])^{2/3} \operatorname{Tan}[c+dx]}{220 b^2 d} - \\
 & \frac{9 a (a+b \operatorname{Sec}[c+dx])^{5/3} \operatorname{Tan}[c+dx]}{44 b^2 d} + \frac{3 \operatorname{Sec}[c+dx] (a+b \operatorname{Sec}[c+dx])^{5/3} \operatorname{Tan}[c+dx]}{11 b d} + \\
 & \left( a (18 a^2 + 49 b^2) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}, -\frac{2}{3}, \frac{3}{2}, \frac{1}{2} (1 - \operatorname{Sec}[c+dx]), \frac{b (1 - \operatorname{Sec}[c+dx])}{a+b}\right] \right. \\
 & \left. (a+b \operatorname{Sec}[c+dx])^{2/3} \operatorname{Tan}[c+dx] \right) / \left( 110 \sqrt{2} b^3 d \sqrt{1 + \operatorname{Sec}[c+dx]} \left( \frac{a+b \operatorname{Sec}[c+dx]}{a+b} \right)^{2/3} \right) - \\
 & \left( (9 a^4 + 23 a^2 b^2 - 32 b^4) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}, \frac{1}{3}, \frac{3}{2}, \frac{1}{2} (1 - \operatorname{Sec}[c+dx]), \frac{b (1 - \operatorname{Sec}[c+dx])}{a+b}\right] \right. \\
 & \left. \left( \frac{a+b \operatorname{Sec}[c+dx]}{a+b} \right)^{1/3} \operatorname{Tan}[c+dx] \right) / \left( 55 \sqrt{2} b^3 d \sqrt{1 + \operatorname{Sec}[c+dx]} (a+b \operatorname{Sec}[c+dx])^{1/3} \right)
 \end{aligned}$$

Result (type 6, 33386 leaves): Display of huge result suppressed!

### Problem 688: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Sec}[c+dx]^3 (a+b \operatorname{Sec}[c+dx])^{2/3} dx$$

Optimal (type 6, 305 leaves, 9 steps):

$$\begin{aligned}
 & - \frac{9 a (a + b \operatorname{Sec}[c + d x])^{2/3} \operatorname{Tan}[c + d x]}{40 b d} + \frac{3 (a + b \operatorname{Sec}[c + d x])^{5/3} \operatorname{Tan}[c + d x]}{8 b d} - \\
 & \left( (6 a^2 - 25 b^2) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}, -\frac{2}{3}, \frac{3}{2}, \frac{1}{2} (1 - \operatorname{Sec}[c + d x]), \frac{b (1 - \operatorname{Sec}[c + d x])}{a + b}\right] \right. \\
 & \quad \left. (a + b \operatorname{Sec}[c + d x])^{2/3} \operatorname{Tan}[c + d x] \right) / \left( 20 \sqrt{2} b^2 d \sqrt{1 + \operatorname{Sec}[c + d x]} \left( \frac{a + b \operatorname{Sec}[c + d x]}{a + b} \right)^{2/3} \right) + \\
 & \left( 3 a (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}, \frac{1}{3}, \frac{3}{2}, \frac{1}{2} (1 - \operatorname{Sec}[c + d x]), \frac{b (1 - \operatorname{Sec}[c + d x])}{a + b}\right] \right. \\
 & \quad \left. \left( \frac{a + b \operatorname{Sec}[c + d x]}{a + b} \right)^{1/3} \operatorname{Tan}[c + d x] \right) / \left( 10 \sqrt{2} b^2 d \sqrt{1 + \operatorname{Sec}[c + d x]} (a + b \operatorname{Sec}[c + d x])^{1/3} \right)
 \end{aligned}$$

Result (type 6, 29862 leaves): Display of huge result suppressed!

**Problem 689: Result more than twice size of optimal antiderivative.**

$$\int \operatorname{Sec}[c + d x]^2 (a + b \operatorname{Sec}[c + d x])^{2/3} dx$$

Optimal (type 6, 260 leaves, 8 steps):

$$\begin{aligned}
 & \frac{3 (a + b \operatorname{Sec}[c + d x])^{2/3} \operatorname{Tan}[c + d x]}{5 d} + \\
 & \left( 2 \sqrt{2} a \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}, -\frac{2}{3}, \frac{3}{2}, \frac{1}{2} (1 - \operatorname{Sec}[c + d x]), \frac{b (1 - \operatorname{Sec}[c + d x])}{a + b}\right] \right. \\
 & \quad \left. (a + b \operatorname{Sec}[c + d x])^{2/3} \operatorname{Tan}[c + d x] \right) / \left( 5 b d \sqrt{1 + \operatorname{Sec}[c + d x]} \left( \frac{a + b \operatorname{Sec}[c + d x]}{a + b} \right)^{2/3} \right) - \\
 & \left( 2 \sqrt{2} (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}, \frac{1}{3}, \frac{3}{2}, \frac{1}{2} (1 - \operatorname{Sec}[c + d x]), \frac{b (1 - \operatorname{Sec}[c + d x])}{a + b}\right] \right. \\
 & \quad \left. \left( \frac{a + b \operatorname{Sec}[c + d x]}{a + b} \right)^{1/3} \operatorname{Tan}[c + d x] \right) / \left( 5 b d \sqrt{1 + \operatorname{Sec}[c + d x]} (a + b \operatorname{Sec}[c + d x])^{1/3} \right)
 \end{aligned}$$

Result (type 6, 9607 leaves):

$$\begin{aligned}
 & \frac{(a + b \operatorname{Sec}[c + d x])^{2/3} \left( \frac{3 a \operatorname{Sin}[c + d x]}{5 b} + \frac{3}{5} \operatorname{Tan}[c + d x] \right)}{d} - \\
 & \left( -2 b + 3 a \operatorname{Cos}[c + d x] \right) (a + b \operatorname{Sec}[c + d x])^{2/3} \\
 & \left( 3 a (b + a \operatorname{Cos}[c + d x])^{2/3} \sqrt{1 - \operatorname{Cos}[c + d x]^2} \operatorname{Sec}[c + d x]^{2/3} - \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( 6 (a^2 - b^2)^2 (b + a \cos [c + d x])^{2/3} \left( 1 - \sqrt{\frac{1}{b^2}} b \sec [c + d x] \right) \left( 1 + \sqrt{\frac{1}{b^2}} b \sec [c + d x] \right) \right. \\
 & \left. - \left( \left( 16 a \operatorname{AppellF1} \left[ \frac{5}{3}, \frac{1}{2}, \frac{1}{2}, \frac{8}{3}, -\frac{a + b \sec [c + d x]}{-a + \frac{1}{\sqrt{\frac{1}{b^2}}}}, \frac{a + b \sec [c + d x]}{a + \frac{1}{\sqrt{\frac{1}{b^2}}}} \right] \right) \right. \right. \\
 & \left. \left( -\frac{1}{\sqrt{\frac{1}{b^2}}} 3 \left( -1 + a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1} \left[ \frac{8}{3}, \frac{1}{2}, \frac{3}{2}, \frac{11}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \sec [c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}} \right], \right. \right. \\
 & \left. \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \sec [c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right) + \left( 1 + a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1} \left[ \frac{8}{3}, \frac{3}{2}, \frac{1}{2}, \right. \right. \\
 & \left. \left. \frac{11}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \sec [c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \frac{\sqrt{\frac{1}{b^2}} (a + b \sec [c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] \right) - \\
 & \left( 16 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{5}{3}, \frac{1}{2}, \frac{1}{2}, \frac{8}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \sec [c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}} \right], \right. \\
 & \left. \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \sec [c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] \right) \left( a + b \sec [c + d x] \right) \right) - \left( 25 \sqrt{\frac{1}{b^2}} (-a^2 + b^2) \right. \\
 & \left. \operatorname{AppellF1} \left[ \frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, -\frac{a + b \sec [c + d x]}{-a + \frac{1}{\sqrt{\frac{1}{b^2}}}}, \frac{a + b \sec [c + d x]}{a + \frac{1}{\sqrt{\frac{1}{b^2}}}} \right] \right) \left. \right) /
 \end{aligned}$$

$$\left( 10 \sqrt{\frac{1}{b^2}} (-a^2 + b^2) \operatorname{AppellF1}\left[\frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}\right], \right.$$

$$\left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] - 3 \left( \left( -1 + a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1}\left[\frac{5}{3}, \frac{1}{2}, \right. \right.$$

$$\left. \left. \frac{3}{2}, \frac{8}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}}\right] \right) +$$

$$\left( 1 + a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1}\left[\frac{5}{3}, \frac{3}{2}, \frac{1}{2}, \frac{8}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}\right],$$

$$\left. \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] (a + b \operatorname{Sec}[c + d x]) \right) \right) \Bigg/$$

$$\left( 5 b (-a^2 + b^2) \sqrt{1 - \operatorname{Cos}[c + d x]^2} \operatorname{Sec}[c + d x]^{1/3} (-1 + \operatorname{Sec}[c + d x]^2) \right) \Bigg/$$

$$\left( 5 b d \left( \frac{3 a (b + a \operatorname{Cos}[c + d x])^{2/3} \operatorname{Sin}[c + d x]}{\sqrt{1 - \operatorname{Cos}[c + d x]^2} \operatorname{Sec}[c + d x]^{1/3}} - \right. \right.$$

$$\left. \frac{2 a^2 \sqrt{1 - \operatorname{Cos}[c + d x]^2} \operatorname{Sec}[c + d x]^{2/3} \operatorname{Sin}[c + d x]}{(b + a \operatorname{Cos}[c + d x])^{1/3}} + \right.$$

$$\left. \frac{2 a (b + a \operatorname{Cos}[c + d x])^{2/3}}{\sqrt{1 - \operatorname{Cos}[c + d x]^2}} \operatorname{Sec}[c + d x]^{5/3} \operatorname{Sin}[c + d x] + \right.$$



$$\begin{aligned}
 & \frac{1}{5 b (-a^2 + b^2) \sqrt{1 - \cos [c + d x]^2} (-1 + \sec [c + d x]^2)^2} \\
 & 12 (a^2 - b^2)^2 (b + a \cos [c + d x])^{2/3} \sec [c + d x]^{8/3} \\
 & \left( 1 - \sqrt{\frac{1}{b^2}} b \sec [c + d x] \right) \left( 1 + \sqrt{\frac{1}{b^2}} b \sec [c + d x] \right) \\
 & \left( \left( \left( 16 a \operatorname{AppellF1} \left[ \frac{5}{3}, \frac{1}{2}, \frac{1}{2}, \frac{8}{3}, -\frac{a + b \sec [c + d x]}{-a + \frac{1}{\sqrt{\frac{1}{b^2}}}}, \frac{a + b \sec [c + d x]}{a + \frac{1}{\sqrt{\frac{1}{b^2}}}} \right] \right) \right) \right) / \\
 & \left( -\frac{1}{\sqrt{\frac{1}{b^2}}} 3 \left( \left( -1 + a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1} \left[ \frac{8}{3}, \frac{1}{2}, \frac{3}{2}, \frac{11}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \sec [c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}} \right], \right. \right. \\
 & \left. \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \sec [c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right) + \left( 1 + a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1} \left[ \frac{8}{3}, \frac{3}{2}, \frac{1}{2}, \right. \right. \\
 & \left. \left. \frac{11}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \sec [c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \frac{\sqrt{\frac{1}{b^2}} (a + b \sec [c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] \right) - \\
 & \left( 16 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{5}{3}, \frac{1}{2}, \frac{1}{2}, \frac{8}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \sec [c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}} \right], \right. \\
 & \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \sec [c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] \right) / (a + b \sec [c + d x]) \left. \right) - \\
 & \left( 25 \sqrt{\frac{1}{b^2}} (-a^2 + b^2) \operatorname{AppellF1} \left[ \frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, -\frac{a + b \sec [c + d x]}{-a + \frac{1}{\sqrt{\frac{1}{b^2}}}}, \frac{a + b \sec [c + d x]}{a + \frac{1}{\sqrt{\frac{1}{b^2}}}} \right] \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( 10 \sqrt{\frac{1}{b^2}} (-a^2 + b^2) \operatorname{AppellF1}\left[\frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}\right], \right. \\
 & \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] - 3 \left( \left( -1 + a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1}\left[\frac{5}{3}, \frac{1}{2}, \right. \right. \\
 & \left. \left. \frac{3}{2}, \frac{8}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}}\right] \right) + \\
 & \left( 1 + a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1}\left[\frac{5}{3}, \frac{3}{2}, \frac{1}{2}, \frac{8}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}\right], \\
 & \left. \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right) (a + b \operatorname{Sec}[c + d x]) \right) \operatorname{Sin}[c + d x] - \\
 & \frac{1}{5 (-a^2 + b^2) \sqrt{1 - \operatorname{Cos}[c + d x]^2} (-1 + \operatorname{Sec}[c + d x]^2) (b + a \operatorname{Cos}[c + d x])^{2/3} \operatorname{Sec}[c + d x]^{5/3}} 6 \sqrt{\frac{1}{b^2}} (a^2 - b^2)^2 \\
 & \left( 1 - \sqrt{\frac{1}{b^2}} b \operatorname{Sec}[c + d x] \right) \\
 & \left( \left( \left( 16 a \operatorname{AppellF1}\left[\frac{5}{3}, \frac{1}{2}, \frac{1}{2}, \frac{8}{3}, -\frac{a + b \operatorname{Sec}[c + d x]}{-a + \frac{1}{\sqrt{\frac{1}{b^2}}}}, \frac{a + b \operatorname{Sec}[c + d x]}{a + \frac{1}{\sqrt{\frac{1}{b^2}}}}\right] \right) \right) \right) / \\
 & \left( -\frac{1}{\sqrt{\frac{1}{b^2}}} 3 \left( \left( -1 + a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1}\left[\frac{8}{3}, \frac{1}{2}, \frac{3}{2}, \frac{11}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}\right], \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] + \left( 1 + a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1}\left[\frac{8}{3}, \frac{3}{2}, \frac{1}{2}, \right. \\
 & \left. \frac{11}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] - \\
 & \left( 16 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{5}{3}, \frac{1}{2}, \frac{1}{2}, \frac{8}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \right. \right. \\
 & \left. \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] / (a + b \operatorname{Sec}[c + d x]) \right) \left. \right) - \\
 & \left( 25 \sqrt{\frac{1}{b^2}} (-a^2 + b^2) \operatorname{AppellF1}\left[\frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, -\frac{a + b \operatorname{Sec}[c + d x]}{-a + \frac{1}{\sqrt{\frac{1}{b^2}}}}, \frac{a + b \operatorname{Sec}[c + d x]}{a + \frac{1}{\sqrt{\frac{1}{b^2}}}} \right] \right) / \\
 & \left( 10 \sqrt{\frac{1}{b^2}} (-a^2 + b^2) \operatorname{AppellF1}\left[\frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \right. \right. \\
 & \left. \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] - 3 \left( \left( -1 + a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1}\left[\frac{5}{3}, \frac{1}{2}, \right. \right. \right. \\
 & \left. \left. \frac{3}{2}, \frac{8}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] + \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( 1 + a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1} \left[ \frac{5}{3}, \frac{3}{2}, \frac{1}{2}, \frac{8}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}} \right], \\
 & \left. \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] (a + b \operatorname{Sec}[c + d x]) \right) \operatorname{Sin}[c + d x] + \\
 & \frac{1}{5 (-a^2 + b^2) \sqrt{1 - \operatorname{Cos}[c + d x]^2} (-1 + \operatorname{Sec}[c + d x]^2)} 6 \sqrt{\frac{1}{b^2}} (a^2 - b^2)^2 \\
 & (b + a \operatorname{Cos}[c + d x])^{2/3} \operatorname{Sec}[c + d x]^{5/3} \\
 & \left( 1 + \sqrt{\frac{1}{b^2}} b \operatorname{Sec}[c + d x] \right) \\
 & \left( \left( \left( 16 a \operatorname{AppellF1} \left[ \frac{5}{3}, \frac{1}{2}, \frac{1}{2}, \frac{8}{3}, -\frac{a + b \operatorname{Sec}[c + d x]}{-a + \frac{1}{\sqrt{\frac{1}{b^2}}}}, \frac{a + b \operatorname{Sec}[c + d x]}{a + \frac{1}{\sqrt{\frac{1}{b^2}}}} \right] \right) \right) \right) / \\
 & \left( -\frac{1}{\sqrt{\frac{1}{b^2}}} 3 \left( \left( -1 + a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1} \left[ \frac{8}{3}, \frac{1}{2}, \frac{3}{2}, \frac{11}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}} \right], \right. \right. \\
 & \left. \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] + \left( 1 + a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1} \left[ \frac{8}{3}, \frac{3}{2}, \frac{1}{2}, \right. \right. \\
 & \left. \left. \frac{11}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] \right) - \\
 & \left( 16 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{5}{3}, \frac{1}{2}, \frac{1}{2}, \frac{8}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}} \right], \right.
 \end{aligned}$$

$$\left. \left. \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right) / (a + b \operatorname{Sec}[c + d x]) \right) \right) -$$

$$\left( 25 \sqrt{\frac{1}{b^2}} (-a^2 + b^2) \operatorname{AppellF1} \left[ \frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, -\frac{a + b \operatorname{Sec}[c + d x]}{-a + \sqrt{\frac{1}{b^2}}}, \frac{a + b \operatorname{Sec}[c + d x]}{a + \sqrt{\frac{1}{b^2}}} \right] \right) /$$

$$\left( 10 \sqrt{\frac{1}{b^2}} (-a^2 + b^2) \operatorname{AppellF1} \left[ \frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \right. \right.$$

$$\left. \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] - 3 \left( \left( -1 + a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1} \left[ \frac{5}{3}, \frac{1}{2}, \right. \right.$$

$$\left. \left. \frac{3}{2}, \frac{8}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] + \right.$$

$$\left. \left( 1 + a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1} \left[ \frac{5}{3}, \frac{3}{2}, \frac{1}{2}, \frac{8}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \right. \right.$$

$$\left. \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] (a + b \operatorname{Sec}[c + d x]) \right) \right) \operatorname{Sin}[c + d x] +$$

$$\left( 6 (a^2 - b^2)^2 (b + a \operatorname{Cos}[c + d x])^{2/3} \left( 1 - \sqrt{\frac{1}{b^2}} b \operatorname{Sec}[c + d x] \right) \left( 1 + \sqrt{\frac{1}{b^2}} b \operatorname{Sec}[c + d x] \right) \right)$$

$$\begin{aligned}
 & \left( - \left( \left( 16 a \operatorname{AppellF1} \left[ \frac{5}{3}, \frac{1}{2}, \frac{1}{2}, \frac{8}{3}, -\frac{a+b \operatorname{Sec}[c+d x]}{-a+\sqrt{\frac{1}{b^2}}}, \frac{a+b \operatorname{Sec}[c+d x]}{a+\sqrt{\frac{1}{b^2}}} \right] \right) \right) \right) / \\
 & \left( -\frac{1}{\sqrt{\frac{1}{b^2}}} 3 \left( \left( -1+a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1} \left[ \frac{8}{3}, \frac{1}{2}, \frac{3}{2}, \frac{11}{3}, \frac{\sqrt{\frac{1}{b^2}} (a+b \operatorname{Sec}[c+d x])}{-1+a \sqrt{\frac{1}{b^2}}}, \right. \right. \right. \\
 & \left. \left. \frac{\sqrt{\frac{1}{b^2}} (a+b \operatorname{Sec}[c+d x])}{1+a \sqrt{\frac{1}{b^2}}} \right] + \left( 1+a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1} \left[ \frac{8}{3}, \frac{3}{2}, \frac{1}{2}, \right. \right. \\
 & \left. \left. \frac{11}{3}, \frac{\sqrt{\frac{1}{b^2}} (a+b \operatorname{Sec}[c+d x])}{-1+a \sqrt{\frac{1}{b^2}}}, \frac{\sqrt{\frac{1}{b^2}} (a+b \operatorname{Sec}[c+d x])}{1+a \sqrt{\frac{1}{b^2}}} \right] \right) - \\
 & \left( \left( 16 (a^2-b^2) \operatorname{AppellF1} \left[ \frac{5}{3}, \frac{1}{2}, \frac{1}{2}, \frac{8}{3}, \frac{\sqrt{\frac{1}{b^2}} (a+b \operatorname{Sec}[c+d x])}{-1+a \sqrt{\frac{1}{b^2}}}, \right. \right. \right. \\
 & \left. \left. \frac{\sqrt{\frac{1}{b^2}} (a+b \operatorname{Sec}[c+d x])}{1+a \sqrt{\frac{1}{b^2}}} \right] \right) / (a+b \operatorname{Sec}[c+d x]) \right) - \left( 25 \sqrt{\frac{1}{b^2}} (-a^2+b^2) \right. \\
 & \left. \operatorname{AppellF1} \left[ \frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, -\frac{a+b \operatorname{Sec}[c+d x]}{-a+\sqrt{\frac{1}{b^2}}}, \frac{a+b \operatorname{Sec}[c+d x]}{a+\sqrt{\frac{1}{b^2}}} \right] \right) / \\
 & \left( 10 \sqrt{\frac{1}{b^2}} (-a^2+b^2) \operatorname{AppellF1} \left[ \frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, \frac{\sqrt{\frac{1}{b^2}} (a+b \operatorname{Sec}[c+d x])}{-1+a \sqrt{\frac{1}{b^2}}}, \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] - 3 \left( \left( -1 + a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1} \left[ \frac{5}{3}, \frac{1}{2}, \right. \right. \\
 & \left. \left. \frac{3}{2}, \frac{8}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] + \right. \\
 & \left. \left( 1 + a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1} \left[ \frac{5}{3}, \frac{3}{2}, \frac{1}{2}, \frac{8}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \right. \right. \\
 & \left. \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] \right) (a + b \operatorname{Sec}[c + d x]) \left. \right) \operatorname{Sin}[c + d x] \Big/ \\
 & \left( 5 b (-a^2 + b^2) (1 - \operatorname{Cos}[c + d x]^2)^{3/2} \operatorname{Sec}[c + d x]^{4/3} (-1 + \operatorname{Sec}[c + d x]^2) \right) + \\
 & \left( 4 a (a^2 - b^2)^2 \left( 1 - \sqrt{\frac{1}{b^2}} b \operatorname{Sec}[c + d x] \right) \left( 1 + \sqrt{\frac{1}{b^2}} b \operatorname{Sec}[c + d x] \right) \right. \\
 & \left. \left( \left( \left( \left( 16 a \operatorname{AppellF1} \left[ \frac{5}{3}, \frac{1}{2}, \frac{1}{2}, \frac{8}{3}, -\frac{a + b \operatorname{Sec}[c + d x]}{-a + \frac{1}{\sqrt{\frac{1}{b^2}}}}, \frac{a + b \operatorname{Sec}[c + d x]}{a + \frac{1}{\sqrt{\frac{1}{b^2}}}} \right] \right) \right) \right. \right. \\
 & \left. \left( -\frac{1}{\sqrt{\frac{1}{b^2}}} 3 \left( \left( -1 + a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1} \left[ \frac{8}{3}, \frac{1}{2}, \frac{3}{2}, \frac{11}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] + \left( 1 + a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1} \left[ \frac{8}{3}, \frac{3}{2}, \frac{1}{2}, \right. \right. \right.
 \end{aligned}$$

$$\left. \frac{11}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] -$$

$$\left( 16 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{5}{3}, \frac{1}{2}, \frac{1}{2}, \frac{8}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}}\right] / (a + b \operatorname{Sec}[c + d x]) \right) - \left( 25 \sqrt{\frac{1}{b^2}} (-a^2 + b^2) \operatorname{AppellF1}\left[\frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, -\frac{a + b \operatorname{Sec}[c + d x]}{-a + \frac{1}{\sqrt{\frac{1}{b^2}}}}, \frac{a + b \operatorname{Sec}[c + d x]}{a + \frac{1}{\sqrt{\frac{1}{b^2}}}}\right] / \left( 10 \sqrt{\frac{1}{b^2}} (-a^2 + b^2) \operatorname{AppellF1}\left[\frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}}\right] - 3 \left( \left( -1 + a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1}\left[\frac{5}{3}, \frac{1}{2}, \frac{3}{2}, \frac{8}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}}\right] + \left( 1 + a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1}\left[\frac{5}{3}, \frac{3}{2}, \frac{1}{2}, \frac{8}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}}\right] \right) \right)$$



$$\left. \left( \frac{\sqrt{\frac{1}{b^2} (a + b \operatorname{Sec}[c + d x])}}{1 + a \sqrt{\frac{1}{b^2}}} \right) (a + b \operatorname{Sec}[c + d x]) \operatorname{Sin}[c + d x] \right) /$$

$$\left( 5 b (-a^2 + b^2) (b + a \operatorname{Cos}[c + d x])^{1/3} \sqrt{1 - \operatorname{Cos}[c + d x]^2} \operatorname{Sec}[c + d x]^{1/3} \right.$$

$$\left. (-1 + \operatorname{Sec}[c + d x]^2) \right) +$$


---


$$\frac{1}{2}$$

$$5 b (-a^2 + b^2) \sqrt{1 - \operatorname{Cos}[c + d x]^2} (-1 + \operatorname{Sec}[c + d x]^2)$$

$$\frac{(a^2 - b^2)^2 (b + a \operatorname{Cos}[c + d x])^{2/3} \operatorname{Sec}[c + d x]^{2/3}}{1 - \sqrt{\frac{1}{b^2} b \operatorname{Sec}[c + d x]}}$$

$$\frac{1 + \sqrt{\frac{1}{b^2} b \operatorname{Sec}[c + d x]}}{1 - \sqrt{\frac{1}{b^2} b \operatorname{Sec}[c + d x]}}$$

$$\left( - \left( \left( 16 a \operatorname{AppellF1} \left[ \frac{5}{3}, \frac{1}{2}, \frac{1}{2}, \frac{8}{3}, -\frac{a + b \operatorname{Sec}[c + d x]}{-a + \sqrt{\frac{1}{b^2}}}, \frac{a + b \operatorname{Sec}[c + d x]}{a + \sqrt{\frac{1}{b^2}}} \right] \right) \right) /$$

$$\left( -\frac{1}{\sqrt{\frac{1}{b^2}}} 3 \left( \left( -1 + a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1} \left[ \frac{8}{3}, \frac{1}{2}, \frac{3}{2}, \frac{11}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}} \right], \right.$$

$$\left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right) + \left( 1 + a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1} \left[ \frac{8}{3}, \frac{3}{2}, \frac{1}{2}, \right.$$

$$\left. \frac{11}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] -$$

$$\left( \frac{16 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{5}{3}, \frac{1}{2}, \frac{1}{2}, \frac{8}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}\right]}{\frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}}} \right) / (a + b \operatorname{Sec}[c + d x]) \Bigg) -$$

$$\left( 25 \sqrt{\frac{1}{b^2}} (-a^2 + b^2) \operatorname{AppellF1}\left[\frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, -\frac{a + b \operatorname{Sec}[c + d x]}{-a + \frac{1}{\sqrt{\frac{1}{b^2}}}}, \frac{a + b \operatorname{Sec}[c + d x]}{a + \frac{1}{\sqrt{\frac{1}{b^2}}}}\right] \right) /$$

$$\left( 10 \sqrt{\frac{1}{b^2}} (-a^2 + b^2) \operatorname{AppellF1}\left[\frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}}\right] - \right.$$

$$3 \left( \left( -1 + a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1}\left[\frac{5}{3}, \frac{1}{2}, \frac{3}{2}, \frac{8}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}\right], \right.$$

$$\left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right) + \left( 1 + a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1}\left[\frac{5}{3}, \frac{3}{2}, \frac{1}{2}, \frac{8}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}}\right] \right) (a + b \operatorname{Sec}[c + d x]) \Bigg)$$

$$\begin{aligned}
 & \sin [c+d x]-\left(6\left(a^2-b^2\right)^2(b+a \cos [c+d x])^{2 / 3}\left(1-\sqrt{\frac{1}{b^2}} b \sec [c+d x]\right)\right. \\
 & \left.\left(1+\sqrt{\frac{1}{b^2}} b \sec [c+d x]\right)\right. \\
 & \left.\left(-\left(\left(25 \sqrt{\frac{1}{b^2}}\left(-a^2+b^2\right)\left(b \operatorname{AppellF1}\left[\frac{5}{3}, \frac{1}{2}, \frac{3}{2}, \frac{8}{3},-\frac{a+b \sec [c+d x]}{-a+\frac{1}{\sqrt{\frac{1}{b^2}}}}\right],\right.\right.\right.\right. \right. \\
 & \left.\left.\left.\frac{a+b \sec [c+d x]}{a+\frac{1}{\sqrt{\frac{1}{b^2}}}}\right] \sec [c+d x] \tan [c+d x]\right) / \left(5\left(a+\frac{1}{\sqrt{\frac{1}{b^2}}}\right)\right)\right)- \\
 & \left.\left(b \operatorname{AppellF1}\left[\frac{5}{3}, \frac{3}{2}, \frac{1}{2}, \frac{8}{3},-\frac{a+b \sec [c+d x]}{-a+\frac{1}{\sqrt{\frac{1}{b^2}}}}, \frac{a+b \sec [c+d x]}{a+\frac{1}{\sqrt{\frac{1}{b^2}}}}\right]\right.\right. \\
 & \left.\left.\sec [c+d x] \tan [c+d x]\right) / \left(5\left(-a+\frac{1}{\sqrt{\frac{1}{b^2}}}\right)\right)\right) \\
 & \left.\left(10 \sqrt{\frac{1}{b^2}}\left(-a^2+b^2\right) \operatorname{AppellF1}\left[\frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, \frac{\sqrt{\frac{1}{b^2}}(a+b \sec [c+d x])}{-1+a \sqrt{\frac{1}{b^2}}}\right],\right.\right. \\
 & \left.\left.\frac{\sqrt{\frac{1}{b^2}}(a+b \sec [c+d x])}{1+a \sqrt{\frac{1}{b^2}}}\right)-3\left(-1+a \sqrt{\frac{1}{b^2}}\right) \operatorname{AppellF1}\left[\frac{5}{3}, \frac{1}{2},\right.\right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \frac{3}{2}, \frac{8}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] + \\
 & \left( 1 + a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1} \left[ \frac{5}{3}, \frac{3}{2}, \frac{1}{2}, \frac{8}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}} \right], \\
 & \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] (a + b \operatorname{Sec}[c + d x]) \Bigg) - \\
 & \left( 16 a \left( \left( 5 b \operatorname{AppellF1} \left[ \frac{8}{3}, \frac{1}{2}, \frac{3}{2}, \frac{11}{3}, -\frac{a + b \operatorname{Sec}[c + d x]}{-a + \frac{1}{\sqrt{\frac{1}{b^2}}}}, \frac{a + b \operatorname{Sec}[c + d x]}{a + \frac{1}{\sqrt{\frac{1}{b^2}}}} \right] \right. \right. \right. \\
 & \left. \left. \operatorname{Sec}[c + d x] \operatorname{Tan}[c + d x] \right) / \left( 16 \left( a + \frac{1}{\sqrt{\frac{1}{b^2}}} \right) \right) \right) - \\
 & \left( 5 b \operatorname{AppellF1} \left[ \frac{8}{3}, \frac{3}{2}, \frac{1}{2}, \frac{11}{3}, -\frac{a + b \operatorname{Sec}[c + d x]}{-a + \frac{1}{\sqrt{\frac{1}{b^2}}}}, \frac{a + b \operatorname{Sec}[c + d x]}{a + \frac{1}{\sqrt{\frac{1}{b^2}}}} \right] \right. \\
 & \left. \left. \operatorname{Sec}[c + d x] \operatorname{Tan}[c + d x] \right) / \left( 16 \left( -a + \frac{1}{\sqrt{\frac{1}{b^2}}} \right) \right) \right) / \\
 & \left( -\frac{1}{\sqrt{\frac{1}{b^2}}} 3 \left( \left( -1 + a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1} \left[ \frac{8}{3}, \frac{1}{2}, \frac{3}{2}, \frac{11}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}} \right], \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] + \left( 1 + a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1}\left[\frac{8}{3}, \frac{3}{2}, \frac{1}{2}, \right. \\
 & \left. \frac{11}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] - \\
 & \left( 16 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{5}{3}, \frac{1}{2}, \frac{1}{2}, \frac{8}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \right. \right. \\
 & \left. \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] / (a + b \operatorname{Sec}[c + d x]) \right) + \\
 & \left( 25 \sqrt{\frac{1}{b^2}} (-a^2 + b^2) \operatorname{AppellF1}\left[\frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, -\frac{a + b \operatorname{Sec}[c + d x]}{-a + \frac{1}{\sqrt{\frac{1}{b^2}}}}, \frac{a + b \operatorname{Sec}[c + d x]}{a + \frac{1}{\sqrt{\frac{1}{b^2}}}} \right] \right. \\
 & \left. -3 b \left( \left( -1 + a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1}\left[\frac{5}{3}, \frac{1}{2}, \frac{3}{2}, \frac{8}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \right. \right. \right. \\
 & \left. \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] + \left( 1 + a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1}\left[\frac{5}{3}, \frac{3}{2}, \frac{1}{2}, \frac{8}{3}, \right. \right. \\
 & \left. \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] \right) \operatorname{Sec}[c + d x]
 \end{aligned}$$

$$\begin{aligned}
 & \tan [c+d x]+10 \sqrt{\frac{1}{b^2}}\left(-a^2+b^2\right)\left(\sqrt{\frac{1}{b^2}} b \operatorname{AppellF1}\left[\frac{5}{3}, \frac{1}{2}, \frac{3}{2}, \frac{8}{3},\right.\right. \\
 & \left.\left.\frac{\sqrt{\frac{1}{b^2}}(a+b \operatorname{Sec}[c+d x])}{-1+a \sqrt{\frac{1}{b^2}}}, \frac{\sqrt{\frac{1}{b^2}}(a+b \operatorname{Sec}[c+d x])}{1+a \sqrt{\frac{1}{b^2}}}\right] \operatorname{Sec}[c+d x]\right. \\
 & \left.\tan [c+d x]\right) / \left(5\left(1+a \sqrt{\frac{1}{b^2}}\right)\right)+\left(\sqrt{\frac{1}{b^2}} b \operatorname{AppellF1}\left[\frac{5}{3}, \frac{3}{2},\right.\right. \\
 & \left.\left.\frac{1}{2}, \frac{8}{3}, \frac{\sqrt{\frac{1}{b^2}}(a+b \operatorname{Sec}[c+d x])}{-1+a \sqrt{\frac{1}{b^2}}}, \frac{\sqrt{\frac{1}{b^2}}(a+b \operatorname{Sec}[c+d x])}{1+a \sqrt{\frac{1}{b^2}}}\right]\right) \\
 & \left.\operatorname{Sec}[c+d x] \tan [c+d x]\right) / \left(5\left(-1+a \sqrt{\frac{1}{b^2}}\right)\right)- \\
 & 3(a+b \operatorname{Sec}[c+d x])\left(\left(-1+a \sqrt{\frac{1}{b^2}}\right)\left(\left(15 \sqrt{\frac{1}{b^2}} b \operatorname{AppellF1}\left[\frac{8}{3}, \frac{1}{2},\right.\right.\right. \\
 & \left.\left.\frac{5}{2}, \frac{11}{3}, \frac{\sqrt{\frac{1}{b^2}}(a+b \operatorname{Sec}[c+d x])}{-1+a \sqrt{\frac{1}{b^2}}}, \frac{\sqrt{\frac{1}{b^2}}(a+b \operatorname{Sec}[c+d x])}{1+a \sqrt{\frac{1}{b^2}}}\right] \operatorname{Sec}[c+d x]\right. \\
 & \left.\left.\tan [c+d x]\right) / \left(16\left(1+a \sqrt{\frac{1}{b^2}}\right)\right)+\left(5 \sqrt{\frac{1}{b^2}} b \operatorname{AppellF1}\left[\frac{8}{3},\right.\right.
 \end{aligned}$$

$$\left[ \frac{3}{2}, \frac{3}{2}, \frac{11}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right]$$

$$\operatorname{Sec}[c + d x] \operatorname{Tan}[c + d x] \left/ \left( 16 \left( -1 + a \sqrt{\frac{1}{b^2}} \right) \right) \right) + \left( 1 + a \sqrt{\frac{1}{b^2}} \right)$$

$$\left( \left( 5 \sqrt{\frac{1}{b^2}} b \operatorname{AppellF1} \left[ \frac{8}{3}, \frac{3}{2}, \frac{3}{2}, \frac{11}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}} \right], \right. \right.$$

$$\left. \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] \operatorname{Sec}[c + d x] \operatorname{Tan}[c + d x] \right/$$

$$\left( 16 \left( 1 + a \sqrt{\frac{1}{b^2}} \right) \right) + \left( 15 \sqrt{\frac{1}{b^2}} b \operatorname{AppellF1} \left[ \frac{8}{3}, \frac{5}{2}, \frac{1}{2}, \frac{11}{3}, \right. \right.$$

$$\left. \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] \right)$$

$$\operatorname{Sec}[c + d x] \operatorname{Tan}[c + d x] \left/ \left( 16 \left( -1 + a \sqrt{\frac{1}{b^2}} \right) \right) \right) \left/ \left( 16 \left( -1 + a \sqrt{\frac{1}{b^2}} \right) \right) \right) \left/ \left( 16 \left( -1 + a \sqrt{\frac{1}{b^2}} \right) \right) \right) \left/ \left( 16 \left( -1 + a \sqrt{\frac{1}{b^2}} \right) \right) \right)$$

$$\left( 10 \sqrt{\frac{1}{b^2}} (-a^2 + b^2) \operatorname{AppellF1} \left[ \frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}} \right], \right.$$

$$\begin{aligned}
 & \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] - 3 \left( \left( -1 + a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1} \left[ \frac{5}{3}, \frac{1}{2}, \right. \right. \\
 & \left. \left. \frac{3}{2}, \frac{8}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] + \right. \\
 & \left. \left( 1 + a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1} \left[ \frac{5}{3}, \frac{3}{2}, \frac{1}{2}, \frac{8}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \right. \right. \\
 & \left. \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] \right) (a + b \operatorname{Sec}[c + d x]) \Big)^2 + \\
 & \left( 16 a \operatorname{AppellF1} \left[ \frac{5}{3}, \frac{1}{2}, \frac{1}{2}, \frac{8}{3}, -\frac{a + b \operatorname{Sec}[c + d x]}{-a + \frac{1}{\sqrt{\frac{1}{b^2}}}}, \frac{a + b \operatorname{Sec}[c + d x]}{a + \frac{1}{\sqrt{\frac{1}{b^2}}}} \right] \right. \\
 & \left. \left( \left( 16 b (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{5}{3}, \frac{1}{2}, \frac{1}{2}, \frac{8}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] \operatorname{Sec}[c + d x] \operatorname{Tan}[c + d x] \right) \right) / \\
 & (a + b \operatorname{Sec}[c + d x])^2 - 16 (a^2 - b^2) \left( \left( 5 \sqrt{\frac{1}{b^2}} b \operatorname{AppellF1} \left[ \frac{8}{3}, \frac{1}{2}, \frac{3}{2}, \frac{11}{3}, \right. \right. \right.
 \end{aligned}$$



$$\begin{aligned}
 & \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] \operatorname{Sec}[c + d x] \\
 & \left. \operatorname{Tan}[c + d x] \right/ \left( 16 \left( 1 + a \sqrt{\frac{1}{b^2}} \right) \right) + \left( 5 \sqrt{\frac{1}{b^2}} b \operatorname{AppellF1} \left[ \frac{8}{3}, \frac{3}{2}, \right. \right. \\
 & \left. \left. \frac{1}{2}, \frac{11}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] \operatorname{Sec}[c + d x] \right. \\
 & \left. \left. \operatorname{Tan}[c + d x] \right/ \left( 16 \left( -1 + a \sqrt{\frac{1}{b^2}} \right) \right) \right) \right/ (a + b \operatorname{Sec}[c + d x]) - \\
 & \frac{1}{\sqrt{\frac{1}{b^2}}} 3 \left( \left( -1 + a \sqrt{\frac{1}{b^2}} \right) \left( \left( 12 \sqrt{\frac{1}{b^2}} b \operatorname{AppellF1} \left[ \frac{11}{3}, \frac{1}{2}, \frac{5}{2}, \frac{14}{3}, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] \operatorname{Sec}[c + d x] \right. \right. \\
 & \left. \left. \operatorname{Tan}[c + d x] \right/ \left( 11 \left( 1 + a \sqrt{\frac{1}{b^2}} \right) \right) + \left( 4 \sqrt{\frac{1}{b^2}} b \operatorname{AppellF1} \left[ \frac{11}{3}, \right. \right. \right. \\
 & \left. \left. \left. \frac{3}{2}, \frac{3}{2}, \frac{14}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] \right) \right)
 \end{aligned}$$



$$\left. \left. \left. \left. \frac{11}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] - \right. \right. \right. \left. \left. \left( 16 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{5}{3}, \frac{1}{2}, \frac{1}{2}, \frac{8}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}} \right], \right. \right. \right. \left. \left. \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] \right) / (a + b \operatorname{Sec}[c + d x]) \right)^2 \right) / \left( 5 b (-a^2 + b^2) \sqrt{1 - \operatorname{Cos}[c + d x]^2} \operatorname{Sec}[c + d x]^{1/3} (-1 + \operatorname{Sec}[c + d x]^2) \right) \right) \right)$$

**Problem 690: Result more than twice size of optimal antiderivative.**

$$\int \operatorname{Sec}[c + d x] (a + b \operatorname{Sec}[c + d x])^{2/3} dx$$

Optimal (type 6, 105 leaves, 3 steps):

$$\left( \sqrt{2} \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, -\frac{2}{3}, \frac{3}{2}, \frac{1}{2} (1 - \operatorname{Sec}[c + d x]), \frac{b (1 - \operatorname{Sec}[c + d x])}{a + b} \right] \right. \\ \left. (a + b \operatorname{Sec}[c + d x])^{2/3} \operatorname{Tan}[c + d x] \right) / \left( d \sqrt{1 + \operatorname{Sec}[c + d x]} \left( \frac{a + b \operatorname{Sec}[c + d x]}{a + b} \right)^{2/3} \right)$$

Result (type 6, 11285 leaves):

$$\frac{3 (a + b \operatorname{Sec}[c + d x])^{2/3} \operatorname{Sin}[c + d x]}{2 d} + \left( \left( -\frac{b}{2 (b + a \operatorname{Cos}[c + d x])^{1/3} \operatorname{Sec}[c + d x]^{1/3}} + \frac{a \operatorname{Sec}[c + d x]^{2/3}}{4 (b + a \operatorname{Cos}[c + d x])^{1/3}} - \frac{3 a \operatorname{Cos}[2 (c + d x)] \operatorname{Sec}[c + d x]^{2/3}}{4 (b + a \operatorname{Cos}[c + d x])^{1/3}} \right) (a + b \operatorname{Sec}[c + d x])^{2/3} \right)$$

$$\begin{aligned}
& \left( \frac{3 \tan\left[\frac{1}{2}(c+dx)\right] \left(\frac{a+b-a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}\right)^{2/3}}{2 \left(\frac{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2}\right)^{1/3}} - 3(a+b) \tan\left[\frac{1}{2}(c+dx)\right] \right. \\
& \left. \left( 10(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \right. \\
& \left. \left( (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) + \right. \\
& \left. 2(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \right. \\
& \left. \tan\left[\frac{1}{2}(c+dx)\right]^4 + 3(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \left( 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
& \left. \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + 2(a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \right. \right. \right. \right. \\
& \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 + \right. \\
& \left. 15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \right. \\
& \left. \left( a+b + a \tan\left[\frac{1}{2}(c+dx)\right]^2 - b \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) / \\
& \left( 2 \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( \frac{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^{1/3} \right. \\
& \left. \left( \frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^{1/3} \right. \\
& \left. \left( 9(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) + \right. \\
& \left. 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) + \right.
\end{aligned}$$



$$\begin{aligned}
& \left( \left( \frac{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^{1/3} \left( \frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^{1/3} \right) + \\
& \left( 3(a+b) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
& \quad \left( 10(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
& \quad \left. \left( (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) + \right. \\
& \quad \left. 2(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \\
& \quad \tan\left[\frac{1}{2}(c+dx)\right]^4 + 3(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
& \quad \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \left( 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
& \quad \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + 2(a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 + \right. \\
& \quad \left. 15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \\
& \quad \left. \left. \left. \left. \left. \left( a+b + a \tan\left[\frac{1}{2}(c+dx)\right]^2 - b \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) \right) \right) \right) / \\
& \left( 2 \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \left( \frac{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^{1/3} \right. \\
& \quad \left( \frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^{1/3} \\
& \quad \left( 9(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) + \\
& \quad \left. 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \right) +
\end{aligned}$$

$$\begin{aligned}
 & 2 (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \\
 & \left( 15 (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & \left. 2 (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \\
 & \left. \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - \left( 3 (a+b) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \left. \left( 10 (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \right. \\
 & \left. \left( (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \right. \\
 & \left. \left. 2 (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \right) \\
 & \tan\left[\frac{1}{2}(c+dx)\right]^4 + 3 (a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \\
 & \left( 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \right. \\
 & \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right) + 2 (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \\
 & \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 + \right. \\
 & \left. 15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \\
 & \left. \left( a+b+a \tan\left[\frac{1}{2}(c+dx)\right]^2 - b \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) \Big/
 \end{aligned}$$

$$\begin{aligned}
 & \left( 4 \left( -1 + \tan \left[ \frac{1}{2} (c + dx) \right] \right)^2 \left( \frac{1 + \tan \left[ \frac{1}{2} (c + dx) \right]^2}{1 - \tan \left[ \frac{1}{2} (c + dx) \right]^2} \right)^{1/3} \right. \\
 & \quad \left. \left( \frac{a + b - a \tan \left[ \frac{1}{2} (c + dx) \right]^2 + b \tan \left[ \frac{1}{2} (c + dx) \right]^2}{1 + \tan \left[ \frac{1}{2} (c + dx) \right]^2} \right)^{1/3} \right. \\
 & \quad \left( 9 (a + b) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, \frac{(a - b) \tan \left[ \frac{1}{2} (c + dx) \right]^2}{a + b} \right] + \right. \\
 & \quad 2 \left( (a - b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, \frac{(a - b) \tan \left[ \frac{1}{2} (c + dx) \right]^2}{a + b} \right] + \right. \\
 & \quad \left. 2 (a + b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a - b) \tan \left[ \frac{1}{2} (c + dx) \right]^2}{a + b} \right] \right) \tan \left[ \frac{1}{2} (c + dx) \right]^2 \left. \right) \\
 & \quad \left( 15 (a + b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, \frac{(a - b) \tan \left[ \frac{1}{2} (c + dx) \right]^2}{a + b} \right] + \right. \\
 & \quad 2 \left( (a - b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, \frac{(a - b) \tan \left[ \frac{1}{2} (c + dx) \right]^2}{a + b} \right] + \right. \\
 & \quad \left. 2 (a + b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a - b) \tan \left[ \frac{1}{2} (c + dx) \right]^2}{a + b} \right] \right) \tan \left[ \frac{1}{2} (c + dx) \right]^2 \left. \right) + \\
 & \quad \left( (a + b) \tan \left[ \frac{1}{2} (c + dx) \right] \left( \frac{\sec \left[ \frac{1}{2} (c + dx) \right]^2 \tan \left[ \frac{1}{2} (c + dx) \right]}{1 - \tan \left[ \frac{1}{2} (c + dx) \right]^2} + \left( \sec \left[ \frac{1}{2} (c + dx) \right] \right)^2 \right. \right. \\
 & \quad \left. \left. \tan \left[ \frac{1}{2} (c + dx) \right] \left( 1 + \tan \left[ \frac{1}{2} (c + dx) \right]^2 \right) \right) / \left( 1 - \tan \left[ \frac{1}{2} (c + dx) \right]^2 \right)^2 \right) \\
 & \quad \left( 10 (a - b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, \frac{(a - b) \tan \left[ \frac{1}{2} (c + dx) \right]^2}{a + b} \right] \right. \\
 & \quad \left( (a - b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, \frac{(a - b) \tan \left[ \frac{1}{2} (c + dx) \right]^2}{a + b} \right] + \right. \\
 & \quad \left. 2 (a + b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, \frac{(a - b) \tan \left[ \frac{1}{2} (c + dx) \right]^2}{a + b} \right] \right) \left. \right)
 \end{aligned}$$



$$\begin{aligned}
 & \tan\left[\frac{1}{2}(c+dx)\right]^4 + 3(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2\right], \\
 & \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \left( 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2\right], \right. \right. \\
 & \quad \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right) + 2(a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \right. \\
 & \quad \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 + \\
 & 15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \\
 & \left. \left. \left. \left. \left. \left. \left( a+b+a \tan\left[\frac{1}{2}(c+dx)\right]^2 - b \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) \right) \right) \right) \right) / \\
 & \left( 2 \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( \frac{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^{4/3} \right. \right. \\
 & \quad \left. \left. \left( \frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^{1/3} \right. \right. \\
 & \quad \left. \left( 9(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + \right. \right. \\
 & \quad 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + \right. \\
 & \quad 2(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \quad \left. \left. \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right. \\
 & \quad \left. \left( 15(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + \right. \right. \\
 & \quad \left. 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + \right. \right. \\
 & \quad \left. \left. 2(a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left. \left. \left. \left. \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) \right) \right) + \left( (a + b) \tan \left[ \frac{1}{2} (c + d x) \right] \right. \right. \\
 & \left. \left. \left( \left( -a \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right] + b \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right] \right) \right/ \right. \right. \\
 & \left. \left( 1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) - \left( \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right] \right. \right. \\
 & \left. \left. \left( a + b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) \right) \right/ \left( 1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right)^2 \right) \\
 & \left( 10 (a - b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \frac{(a - b) \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] \right. \\
 & \left. \left( (a - b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \frac{(a - b) \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] \right) + \right. \\
 & \left. 2 (a + b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \frac{(a - b) \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] \right) \\
 & \tan \left[ \frac{1}{2} (c + d x) \right]^4 + 3 (a + b) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \right. \\
 & \left. \frac{(a - b) \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] \left( 2 \left( (a - b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \right. \right. \right. \\
 & \left. \left. \frac{(a - b) \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] + 2 (a + b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \right. \right. \\
 & \left. \left. \tan \left[ \frac{1}{2} (c + d x) \right]^2, \frac{(a - b) \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] \right) \tan \left[ \frac{1}{2} (c + d x) \right]^2 + \right. \\
 & \left. 15 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \frac{(a - b) \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] \right) \\
 & \left. \left. \left. \left. \left. (a + b + a \tan \left[ \frac{1}{2} (c + d x) \right]^2 - b \tan \left[ \frac{1}{2} (c + d x) \right]^2) \right) \right) \right) \right) \right) \Big/ \\
 & \left( 2 \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) \left( \frac{1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2}{1 - \tan \left[ \frac{1}{2} (c + d x) \right]^2} \right)^{1/3} \right. \\
 & \left. \left( \frac{a + b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2}{1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2} \right)^{4/3} \right) \\
 & \left( 9 (a + b) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \frac{(a - b) \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] \right) +
 \end{aligned}$$

$$\begin{aligned}
 & 2 \left( (a-b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \\
 & \quad \left. 2 (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \\
 & \left( 15 (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \\
 & \quad \left. 2 \left( (a-b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \right. \\
 & \quad \left. \left. 2 (a+b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) + \\
 & \left( 3 (a+b) \tan \left[ \frac{1}{2} (c+dx) \right] \left( 2 \left( (a-b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + 2 (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right) \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + \right. \\
 & \quad \left. 9 (a+b) \left( \frac{1}{9 (a+b)} (a-b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + \right. \right. \\
 & \quad \left. \left. \frac{2}{9} \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \right) \right) + 2 \tan \left[ \frac{1}{2} (c+dx) \right]^2 \\
 & \left( (a-b) \left( \frac{1}{5 (a+b)} 4 (a-b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, \frac{7}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right) \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + \right. \\
 & \quad \left. \frac{2}{9} \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \right) \right) + 2 \tan \left[ \frac{1}{2} (c+dx) \right]^2
 \end{aligned}$$

$$\begin{aligned} & \frac{2}{5} \text{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{4}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \\ & \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + 2(a+b)\left(\frac{1}{5(a+b)}(a-b) \text{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{4}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \\ & \left. \tan\left[\frac{1}{2}(c+dx)\right] + \text{AppellF1}\left[\frac{5}{2}, \frac{8}{3}, \frac{1}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right) \\ & \left(10(a-b) \text{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \left((a-b) \text{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \right. \\ & \left. \left. 2(a+b) \text{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right]\right) \tan\left[\frac{1}{2}(c+dx)\right]^4 + 3(a+b) \text{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\ & \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \left(2\left((a-b) \text{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \right. \right. \\ & \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + 2(a+b) \text{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \right. \\ & \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right]\right) \tan\left[\frac{1}{2}(c+dx)\right]^2 + 15 \text{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\ & \left. \left. \left( a+b+a \tan\left[\frac{1}{2}(c+dx)\right]^2 - b \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) \right) / \\ & \left( 2 \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( \frac{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^{1/3} \right. \\ & \left. \left( \frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^{1/3} \right) \right) \end{aligned}$$

$$\begin{aligned}
 & \left( 9 (a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & 2 (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \left. \right) \\
 & \left( 15 (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & 2 (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \left. \right) \\
 & \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) + \left( 3 (a+b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right. \\
 & \left. \left( 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \right. \right. \\
 & \left. \left. 2 (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \right) \\
 & \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + 15 (a+b) \left( \frac{1}{5(a+b)} \right. \\
 & \left. (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \\
 & \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \frac{2}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \left. \right) + \\
 & 2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \left( (a-b) \left( \frac{1}{21(a+b)} 20 (a-b) \operatorname{AppellF1}\left[\frac{7}{2}, \frac{2}{3}, \frac{7}{3}, \frac{9}{2}, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}& \left( \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \\& \tan\left[\frac{1}{2}(c+dx)\right]^2 + \frac{10}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{5}{3}, \frac{4}{3}, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2\right], \\& \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^2 + \\& 2(a+b) \left( \frac{1}{21(a+b)} 5(a-b) \operatorname{AppellF1}\left[\frac{7}{2}, \frac{5}{3}, \frac{4}{3}, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2\right], \right. \\& \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^2 + \\& \frac{25}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{8}{3}, \frac{1}{3}, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2\right], \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \\& \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)\right) \\& \left( 10(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2\right], \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \\& \left( (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2\right], \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right) + \\& \left. 2(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2\right], \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right) \right) \\& \tan\left[\frac{1}{2}(c+dx)\right]^4 + 3(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2\right], \\& \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \left( 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2\right], \right. \right. \\& \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right) + 2(a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \right. \right. \\& \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 + \\& 15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2\right], \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \\& \left. \left. \left( a+b+a \tan\left[\frac{1}{2}(c+dx)\right]^2 - b \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) / \end{aligned}$$

$$\begin{aligned}
 & \left( 2 \left( -1 + \tan \left[ \frac{1}{2} (c + dx) \right] \right)^2 \left( \frac{1 + \tan \left[ \frac{1}{2} (c + dx) \right]^2}{1 - \tan \left[ \frac{1}{2} (c + dx) \right]^2} \right)^{1/3} \right. \\
 & \left. \left( \frac{a + b - a \tan \left[ \frac{1}{2} (c + dx) \right]^2 + b \tan \left[ \frac{1}{2} (c + dx) \right]^2}{1 + \tan \left[ \frac{1}{2} (c + dx) \right]^2} \right)^{1/3} \right. \\
 & \left. \left( 9 (a + b) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, \frac{(a - b) \tan \left[ \frac{1}{2} (c + dx) \right]^2}{a + b} \right] + \right. \right. \\
 & \left. \left. 2 \left( (a - b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, \frac{(a - b) \tan \left[ \frac{1}{2} (c + dx) \right]^2}{a + b} \right] \right) + \right. \right. \\
 & \left. \left. 2 (a + b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, \right. \right. \right. \\
 & \left. \left. \left. \frac{(a - b) \tan \left[ \frac{1}{2} (c + dx) \right]^2}{a + b} \right] \right) \tan \left[ \frac{1}{2} (c + dx) \right]^2 \right) \right) \\
 & \left( 15 (a + b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, \frac{(a - b) \tan \left[ \frac{1}{2} (c + dx) \right]^2}{a + b} \right] + \right. \\
 & \left. 2 \left( (a - b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, \frac{(a - b) \tan \left[ \frac{1}{2} (c + dx) \right]^2}{a + b} \right] \right) + \right. \\
 & \left. 2 (a + b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, \right. \right. \\
 & \left. \left. \left. \frac{(a - b) \tan \left[ \frac{1}{2} (c + dx) \right]^2}{a + b} \right] \right) \tan \left[ \frac{1}{2} (c + dx) \right]^2 \right) \right) - \\
 & \left( 3 (a + b) \tan \left[ \frac{1}{2} (c + dx) \right] \left( 20 (a - b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, \right. \right. \right. \\
 & \left. \left. \left. \frac{(a - b) \tan \left[ \frac{1}{2} (c + dx) \right]^2}{a + b} \right] \right) \right. \\
 & \left. \left( (a - b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, \frac{(a - b) \tan \left[ \frac{1}{2} (c + dx) \right]^2}{a + b} \right] + \right. \right. \\
 & \left. \left. 2 (a + b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, \frac{(a - b) \tan \left[ \frac{1}{2} (c + dx) \right]^2}{a + b} \right] \right) \right) \\
 & \operatorname{Sec} \left[ \frac{1}{2} (c + dx) \right]^2 \tan \left[ \frac{1}{2} (c + dx) \right]^3 + 10 (a - b)
 \end{aligned}$$

$$\begin{aligned}
 & \left( (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & \quad \left. 2(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \\
 & \tan\left[\frac{1}{2}(c+dx)\right]^4 \left( \frac{1}{5(a+b)} (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \quad \left. \frac{2}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + 10(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \right. \\
 & \quad \left. \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^4 \\
 & \left( (a-b) \left( \frac{1}{5(a+b)} 4(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{7}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \quad \left. \frac{2}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{4}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + 2(a+b) \left( \frac{1}{5(a+b)} (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \frac{5}{3}, \frac{4}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \quad \left. \tan\left[\frac{1}{2}(c+dx)\right] + \operatorname{AppellF1}\left[\frac{5}{2}, \frac{8}{3}, \frac{1}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) + \\
 & 3(a+b) \left( \frac{1}{9(a+b)} (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right.
 \end{aligned}$$



$$\begin{aligned}
 & \frac{2}{9} \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \\
 & \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \left( 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \right. \right. \right. \\
 & \left. \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + 2(a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \right. \right. \right. \\
 & \left. \left. \left. \frac{1}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + \right. \\
 & \left. 15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \left. \left( a+b+a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 - b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) + \\
 & 3(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \\
 & \left( 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \right. \\
 & \left. \left. 2(a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \left. 15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \left. \left( a \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] - b \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) + \right. \\
 & \left. 15 \left( \frac{1}{5(a+b)} (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \right. \\
 & \left. \left. \frac{2}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \right. \\
 & \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \left( a+b+a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 - \right. \right.
 \end{aligned}$$

$$\begin{aligned}
& b \tan\left[\frac{1}{2}(c+dx)\right]^2 + 2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \left( (a-b) \left( \frac{1}{21(a+b)} 20(a-b) \right. \right. \\
& \quad \left. \left. \text{AppellF1}\left[\frac{7}{2}, \frac{2}{3}, \frac{7}{3}, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \right. \\
& \quad \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{10}{21} \text{AppellF1}\left[\frac{7}{2}, \frac{5}{3}, \frac{4}{3}, \frac{9}{2}, \right. \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right] \right) + 2(a+b) \left( \frac{1}{21(a+b)} 5(a-b) \text{AppellF1}\left[\frac{7}{2}, \frac{5}{3}, \right. \right. \right. \\
& \quad \left. \left. \frac{4}{3}, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right] + \frac{25}{21} \text{AppellF1}\left[\frac{7}{2}, \frac{8}{3}, \frac{1}{3}, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
& \quad \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) \Bigg/ \\
& \left( 2 \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( \frac{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^{1/3} \right. \\
& \quad \left. \left( \frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^{1/3} \right. \\
& \quad \left( 9(a+b) \text{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
& \quad 2 \left( (a-b) \text{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
& \quad \left. 2(a+b) \text{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \\
& \quad \left( 15(a+b) \text{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
& \quad \left. 2 \left( (a-b) \text{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \right.
\end{aligned}$$

$$2(a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2\right]$$

**Problem 692: Result more than twice size of optimal antiderivative.**

$$\int \sec[c+dx] (a+b \sec[c+dx])^{4/3} dx$$

Optimal (type 6, 108 leaves, 3 steps):

$$\left(\sqrt{2}(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}, -\frac{4}{3}, \frac{3}{2}, \frac{1}{2}(1-\sec[c+dx]), \frac{b(1-\sec[c+dx])}{a+b}\right] (a+b \sec[c+dx])^{1/3} \tan[c+dx]\right) / \left(d \sqrt{1+\sec[c+dx]} \left(\frac{a+b \sec[c+dx]}{a+b}\right)^{1/3}\right)$$

Result (type 6, 11551 leaves):

$$\left(-\frac{5ab}{2(b+a \cos[c+dx])^{2/3} \sec[c+dx]^{2/3}} - \frac{7a^2 \sec[c+dx]^{1/3}}{8(b+a \cos[c+dx])^{2/3}} + \frac{b^2 \sec[c+dx]^{1/3}}{4(b+a \cos[c+dx])^{2/3}} - \frac{15a^2 \cos[2(c+dx)] \sec[c+dx]^{1/3}}{8(b+a \cos[c+dx])^{2/3}}\right) (a+b \sec[c+dx])^{4/3}$$

$$\left(-\frac{15a \tan\left[\frac{1}{2}(c+dx)\right] \left(\frac{a+b-a \tan\left[\frac{1}{2}(c+dx)\right]^2+b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}\right)^{1/3}}{4 \left(\frac{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}{1-\tan\left[\frac{1}{2}(c+dx)\right]^2}\right)^{2/3}} - \left(3(a+b) \tan\left[\frac{1}{2}(c+dx)\right]\right)\right.$$

$$\left(50a(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \left(2(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right]\right) \right.$$

$$\left. \tan\left[\frac{1}{2}(c+dx)\right]^4 + 3(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right.\right.$$

$$\begin{aligned}
 & \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \left( -2(7a-2b) \left( 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \right. \right. \right. \\
 & \left. \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \right. \right. \right. \\
 & \left. \left. \left. \frac{2}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + \right. \\
 & \left. 15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right. \\
 & \left. \left( 2b^2 - 5ab \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) + a^2 \left( -7 + 5 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) \right) \Big/ \\
 & \left( 4 \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( \frac{1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \right)^{2/3} \right. \\
 & \left. \left( \frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \right)^{2/3} \right. \\
 & \left. \left( 9(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + \right. \right. \\
 & \left. \left. 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + \right. \right. \right. \\
 & \left. \left. \left. (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \\
 & \left( 15(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + \right. \\
 & \left. 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + \right. \right. \\
 & \left. \left. (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \right) \right)
 \end{aligned}$$



$$\begin{aligned}
 & \tan\left[\frac{1}{2}(c+dx)\right]^4 + 3(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \left( -2(7a-2b) \left( 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \right. \right. \right. \\
 & \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \right. \right. \right. \\
 & \left. \left. \left. \frac{2}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 + \\
 & 15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \\
 & \left. \left( 2b^2 - 5ab \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) + a^2 \left( -7 + 5 \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) \right) \Big/ \\
 & \left( 4 \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \left( \frac{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^{2/3} \right. \\
 & \left. \left( \frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^{2/3} \right. \\
 & \left. \left( 9(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \right. \\
 & 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \left. (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right) \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \\
 & \left( 15(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \left. \left. (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \right) \right)
 \end{aligned}$$



$$\begin{aligned}
 & \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right. \\
 & \left( 15(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) + \\
 & \left( (a+b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \left( \frac{\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} + \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) / \left( 1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \right) \\
 & \left( 50a(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \left( 2(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & \left. \left. (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \right) \\
 & \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^4 + 3(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \left( -2(7a-2b) \left( 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \right. \right. \right. \\
 & \left. \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \right. \right. \right. \\
 & \left. \left. \left. \frac{2}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + \\
 & 15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right]
 \end{aligned}$$



$$\begin{aligned}
 & \left( 2 b^2 - 5 a b \left( 1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) + a^2 \left( -7 + 5 \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) \right) \Bigg) \Bigg) \Bigg) / \\
 & \left( 2 \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) \left( \frac{1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2}{1 - \tan \left[ \frac{1}{2} (c + d x) \right]^2} \right)^{5/3} \right. \\
 & \left. \left( \frac{a + b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2}{1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2} \right)^{2/3} \right. \\
 & \left. \left( 9 (a + b) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \frac{(a - b) \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] + \right. \right. \\
 & \left. \left. 2 \left( 2 (a - b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \frac{(a - b) \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] + \right. \right. \right. \\
 & \left. \left. (a + b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \right. \right. \right. \\
 & \left. \left. \left. \frac{(a - b) \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] \right) \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) \right) \\
 & \left( 15 (a + b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \frac{(a - b) \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] + \right. \\
 & \left. 2 \left( 2 (a - b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \frac{(a - b) \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] + \right. \right. \\
 & \left. \left. (a + b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \frac{(a - b) \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] \right) \right) \\
 & \tan \left[ \frac{1}{2} (c + d x) \right]^2 \Bigg) \Bigg) + \left( (a + b) \tan \left[ \frac{1}{2} (c + d x) \right] \right. \\
 & \left. \left( \left( -a \sec \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right] + b \sec \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right] \right) \Bigg) \Bigg) / \right. \\
 & \left. \left( 1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) - \left( \sec \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right] \right. \right. \\
 & \left. \left. \left( a + b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) \right) \Bigg) \Bigg) / \left( 1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right)^2 \right) \\
 & \left( 50 a (a - b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \frac{(a - b) \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] \right)
 \end{aligned}$$

$$\begin{aligned}
& \left( 2 (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
& \quad \left. (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \\
& \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^4 + 3 (a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
& \quad \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \left( -2 (7a-2b) \left( 2 (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \right. \right. \right. \\
& \quad \left. \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \right. \right. \right. \\
& \quad \left. \left. \left. \frac{2}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + \right. \\
& \quad \left. 15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \\
& \quad \left. \left( 2b^2 - 5ab \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) + a^2 \left( -7 + 5 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) \Bigg) / \\
& \left( 2 \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( \frac{1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \right)^{2/3} \right. \\
& \quad \left. \left( \frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \right)^{5/3} \right) \\
& \left( 9 (a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
& \quad 2 \left( 2 (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
& \quad (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
& \quad \quad \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \\
& \left( 15 (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right.
\end{aligned}$$

$$\begin{aligned}
 & 2 \left( 2 (a-b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right]^2 + \right. \\
 & \quad \left. (a+b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right]^2 \right) \\
 & \quad \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) + \left( 3 (a+b) \tan \left[ \frac{1}{2} (c+dx) \right] \right. \\
 & \quad \left. \left( 2 \left( 2 (a-b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right]^2 + \right. \right. \right. \\
 & \quad \left. \left. (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right]^2 \right) \right) \right) \\
 & \quad \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + 9 (a+b) \left( \frac{1}{9 (a+b)} \right. \\
 & \quad \left. 2 (a-b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right]^2 \right. \\
 & \quad \left. \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + \frac{1}{9} \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \right) + \\
 & \quad 2 \tan \left[ \frac{1}{2} (c+dx) \right]^2 \left( 2 (a-b) \left( \frac{1}{a+b} (a-b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, \frac{8}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + \right. \\
 & \quad \left. \frac{1}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}, \frac{5}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right]^2 \right) \right. \\
 & \quad \left. \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \right) + (a+b) \left( \frac{1}{5 (a+b)} 2 (a-b) \operatorname{AppellF1} \left[ \frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \frac{4}{3}, \frac{5}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right]^2 \right) \sec \left[ \frac{1}{2} (c+dx) \right]^2 \\
 & \quad \tan \left[ \frac{1}{2} (c+dx) \right] + \frac{4}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{7}{3}, \frac{2}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \\
 & \quad \left. \left. \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \right) \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( 50 a (a - b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, \frac{(a - b) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] \right. \\
 & \left( 2 (a - b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, \frac{(a - b) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] \right. + \\
 & \left. \left. (a + b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, \frac{(a - b) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] \right) \right) \\
 & \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^4 + 3 (a + b) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, \right. \\
 & \left. \frac{(a - b) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] \left( -2 (7 a - 2 b) \left( 2 (a - b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \right. \right. \right. \\
 & \left. \left. \left. \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, \frac{(a - b) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] + (a + b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}, \right. \right. \right. \\
 & \left. \left. \left. \frac{2}{3}, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, \frac{(a - b) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] \right) \right) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 + \\
 & 15 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, \frac{(a - b) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] \\
 & \left. \left( 2 b^2 - 5 a b \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right) + a^2 \left( -7 + 5 \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right) \right) \right) \right) \Big/ \\
 & \left( 4 \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right) \left( \frac{1 + \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{1 - \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2} \right)^{2/3} \right. \\
 & \left. \left( \frac{a + b - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 + b \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{1 + \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2} \right)^{2/3} \right) \\
 & \left( 9 (a + b) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, \frac{(a - b) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] + \right. \\
 & \left. 2 \left( 2 (a - b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, \frac{(a - b) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] \right. + \right. \\
 & \left. (a + b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, \right. \right. \\
 & \left. \left. \frac{(a - b) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] \right) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right)^2
 \end{aligned}$$

$$\begin{aligned}
 & \left( 15 (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \\
 & 2 \left( 2 (a-b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \\
 & \left. \left. (a+b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \right) \\
 & \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \Bigg) + \left( 3 (a+b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] \right. \\
 & \left. \left( 2 \left( 2 (a-b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \right. \right. \\
 & \left. \left. (a+b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \right) \right) \\
 & \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] + 15 (a+b) \left( \frac{1}{5 (a+b)} \right. \\
 & 2 (a-b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \\
 & \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] + \frac{1}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \right. \\
 & \left. \left. \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] \right) \Bigg) + \\
 & 2 \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \left( 2 (a-b) \left( \frac{1}{21 (a+b)} 25 (a-b) \operatorname{AppellF1} \left[ \frac{7}{2}, \frac{1}{3}, \frac{8}{3}, \right. \right. \right. \\
 & \left. \left. \frac{9}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \right. \right. \\
 & \left. \left. \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] + \frac{5}{21} \operatorname{AppellF1} \left[ \frac{7}{2}, \frac{4}{3}, \frac{5}{3}, \frac{9}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] \right) \right) \Bigg) + \\
 & (a+b) \left( \frac{1}{21 (a+b)} 10 (a-b) \operatorname{AppellF1} \left[ \frac{7}{2}, \frac{4}{3}, \frac{5}{3}, \frac{9}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \right.
 \end{aligned}$$



$$\begin{aligned}
 & 2 \left( 2 (a-b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right]^2 + \right. \\
 & \quad \left. (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right]^2 \right) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \\
 & \left( 15 (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right]^2 + \right. \\
 & \quad \left. 2 \left( 2 (a-b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right]^2 + \right. \right. \\
 & \quad \left. (a+b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right]^2 \right) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \\
 & \left( 3 (a+b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] \left( 100 a (a-b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right]^2 \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right) \right. \\
 & \quad \left( 2 (a-b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right]^2 + \right. \\
 & \quad \left. (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right]^2 \right) \\
 & \quad \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^3 + 50 a (a-b) \\
 & \quad \left( 2 (a-b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right]^2 + \right. \\
 & \quad \left. (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right]^2 \right) \\
 & \quad \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^4 \left( \frac{1}{5 (a+b)} 2 (a-b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right]^2 \right. \\
 & \quad \left. \left. \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right) \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] + \right.
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \\
 & \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right] + \\
 50 a & (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \\
 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^4 & \left( 2(a-b) \left( \frac{1}{a+b} (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{8}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \left. \frac{1}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + (a+b) \left( \frac{1}{5(a+b)} 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \right. \right. \right. \\
 & \left. \left. \frac{4}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \frac{4}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{7}{3}, \frac{2}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \right) + \\
 3(a+b) & \left( \frac{1}{9(a+b)} 2(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \left. \frac{1}{9} \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \left( -2(7a-2b) \left( 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \right. \right. \right. \\
 & \left. \left. \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \right. \right. \\
 & \left. \left. \frac{2}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 +
 \end{aligned}$$



$$\begin{aligned}
 & 15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \\
 & \left(2b^2 - 5ab \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) + a^2 \left(-7 + 5 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)\right) + 3(a+b) \\
 & \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \left(-2(7a-2b)\right. \\
 & \left.2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & \left.(a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right]\right) \\
 & \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + 15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \right. \\
 & \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \left(5a^2 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] - 5ab \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right) - \\
 & 2(7a-2b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \left(2(a-b) \left(\frac{1}{21(a+b)} 25(a-b) \operatorname{AppellF1}\left[\frac{7}{2}, \frac{1}{3}, \right. \right. \right. \\
 & \left. \left. \frac{8}{3}, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \frac{5}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{4}{3}, \frac{5}{3}, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right) + \\
 & (a+b) \left(\frac{1}{21(a+b)} 10(a-b) \operatorname{AppellF1}\left[\frac{7}{2}, \frac{4}{3}, \frac{5}{3}, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \left. \frac{20}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{7}{3}, \frac{2}{3}, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)\right) + 15 \left(\frac{1}{5(a+b)} 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left. \left. \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \frac{1}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) / \\
 & \left( 2b^2 - 5ab \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) + a^2 \left( -7 + 5 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Bigg) \Bigg) \Bigg) / \\
 & \left( 4 \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( \frac{1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \right)^{2/3} \right. \\
 & \left. \left( \frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \right)^{2/3} \right. \\
 & \left. \left( 9(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \right. \\
 & \left. \left. 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \right. \right. \\
 & \left. \left. \left. (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) \right) \\
 & \left( 15(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & \left. 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \right. \\
 & \left. \left. (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) \Bigg) \Bigg) \Bigg) + \\
 & \left( \operatorname{Cos}[c+dx] (a+b \operatorname{Sec}[c+dx])^{4/3} \left( \frac{15}{4} a \operatorname{Sin}[c+dx] + \right. \right.
 \end{aligned}$$

$$\frac{3}{4} \frac{b \operatorname{Tan} [c + d x]}{\left( d (b + a \operatorname{Cos} [c + d x]) \right)}$$

**Problem 694: Result more than twice size of optimal antiderivative.**

$$\int \operatorname{Sec} [c + d x]^4 (a + b \operatorname{Sec} [c + d x])^{5/3} dx$$

Optimal (type 6, 412 leaves, 11 steps):

$$\begin{aligned} & \frac{3 a (18 a^2 + 97 b^2) (a + b \operatorname{Sec} [c + d x])^{2/3} \operatorname{Tan} [c + d x]}{1232 b^2 d} + \\ & \frac{3 (18 a^2 + 121 b^2) (a + b \operatorname{Sec} [c + d x])^{5/3} \operatorname{Tan} [c + d x]}{1232 b^2 d} - \\ & \frac{9 a (a + b \operatorname{Sec} [c + d x])^{8/3} \operatorname{Tan} [c + d x]}{77 b^2 d} + \frac{3 \operatorname{Sec} [c + d x] (a + b \operatorname{Sec} [c + d x])^{8/3} \operatorname{Tan} [c + d x]}{14 b d} + \\ & \left( (36 a^4 + 164 a^2 b^2 + 605 b^4) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, -\frac{2}{3}, \frac{3}{2}, \frac{1}{2} (1 - \operatorname{Sec} [c + d x]), \frac{b (1 - \operatorname{Sec} [c + d x])}{a + b} \right] \right. \\ & \left. (a + b \operatorname{Sec} [c + d x])^{2/3} \operatorname{Tan} [c + d x] \right) / \left( 616 \sqrt{2} b^3 d \sqrt{1 + \operatorname{Sec} [c + d x]} \left( \frac{a + b \operatorname{Sec} [c + d x]}{a + b} \right)^{2/3} \right) - \\ & \left( a (18 a^4 + 79 a^2 b^2 - 97 b^4) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{3}, \frac{3}{2}, \frac{1}{2} (1 - \operatorname{Sec} [c + d x]), \frac{b (1 - \operatorname{Sec} [c + d x])}{a + b} \right] \right. \\ & \left. \left( \frac{a + b \operatorname{Sec} [c + d x]}{a + b} \right)^{1/3} \operatorname{Tan} [c + d x] \right) / \left( 308 \sqrt{2} b^3 d \sqrt{1 + \operatorname{Sec} [c + d x]} (a + b \operatorname{Sec} [c + d x])^{1/3} \right) \end{aligned}$$

Result (type 6, 44 504 leaves): Display of huge result suppressed!

**Problem 695: Result more than twice size of optimal antiderivative.**

$$\int \operatorname{Sec} [c + d x]^3 (a + b \operatorname{Sec} [c + d x])^{5/3} dx$$

Optimal (type 6, 356 leaves, 10 steps):

$$\frac{3 (15 a^2 - 64 b^2) (a + b \operatorname{Sec}[c + d x])^{2/3} \operatorname{Tan}[c + d x]}{440 b d} - \frac{9 a (a + b \operatorname{Sec}[c + d x])^{5/3} \operatorname{Tan}[c + d x]}{88 b d} + \frac{3 (a + b \operatorname{Sec}[c + d x])^{8/3} \operatorname{Tan}[c + d x]}{11 b d} - \left( a (30 a^2 - 373 b^2) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}, -\frac{2}{3}, \frac{3}{2}, \frac{1}{2} (1 - \operatorname{Sec}[c + d x]), \frac{b (1 - \operatorname{Sec}[c + d x])}{a + b}\right] (a + b \operatorname{Sec}[c + d x])^{2/3} \operatorname{Tan}[c + d x] \right) / \left( 220 \sqrt{2} b^2 d \sqrt{1 + \operatorname{Sec}[c + d x]} \left( \frac{a + b \operatorname{Sec}[c + d x]}{a + b} \right)^{2/3} \right) + \left( (15 a^4 - 79 a^2 b^2 + 64 b^4) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}, \frac{1}{3}, \frac{3}{2}, \frac{1}{2} (1 - \operatorname{Sec}[c + d x]), \frac{b (1 - \operatorname{Sec}[c + d x])}{a + b}\right] \left( \frac{a + b \operatorname{Sec}[c + d x]}{a + b} \right)^{1/3} \operatorname{Tan}[c + d x] \right) / \left( 110 \sqrt{2} b^2 d \sqrt{1 + \operatorname{Sec}[c + d x]} (a + b \operatorname{Sec}[c + d x])^{1/3} \right)$$

Result (type 6, 33405 leaves): Display of huge result suppressed!

### Problem 696: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Sec}[c + d x]^2 (a + b \operatorname{Sec}[c + d x])^{5/3} dx$$

Optimal (type 6, 299 leaves, 9 steps):

$$\frac{3 a (a + b \operatorname{Sec}[c + d x])^{2/3} \operatorname{Tan}[c + d x]}{8 d} + \frac{3 (a + b \operatorname{Sec}[c + d x])^{5/3} \operatorname{Tan}[c + d x]}{8 d} + \left( (2 a^2 + 5 b^2) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}, -\frac{2}{3}, \frac{3}{2}, \frac{1}{2} (1 - \operatorname{Sec}[c + d x]), \frac{b (1 - \operatorname{Sec}[c + d x])}{a + b}\right] (a + b \operatorname{Sec}[c + d x])^{2/3} \operatorname{Tan}[c + d x] \right) / \left( 4 \sqrt{2} b d \sqrt{1 + \operatorname{Sec}[c + d x]} \left( \frac{a + b \operatorname{Sec}[c + d x]}{a + b} \right)^{2/3} \right) - \left( a (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}, \frac{1}{3}, \frac{3}{2}, \frac{1}{2} (1 - \operatorname{Sec}[c + d x]), \frac{b (1 - \operatorname{Sec}[c + d x])}{a + b}\right] \left( \frac{a + b \operatorname{Sec}[c + d x]}{a + b} \right)^{1/3} \operatorname{Tan}[c + d x] \right) / \left( 2 \sqrt{2} b d \sqrt{1 + \operatorname{Sec}[c + d x]} (a + b \operatorname{Sec}[c + d x])^{1/3} \right)$$

Result (type 6, 29873 leaves): Display of huge result suppressed!

### Problem 697: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Sec}[c + d x] (a + b \operatorname{Sec}[c + d x])^{5/3} dx$$

Optimal (type 6, 108 leaves, 3 steps):

$$\left( \sqrt{2} (a + b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}, -\frac{5}{3}, \frac{3}{2}, \frac{1}{2} (1 - \operatorname{Sec}[c + d x]), \frac{b (1 - \operatorname{Sec}[c + d x])}{a + b}\right] (a + b \operatorname{Sec}[c + d x])^{2/3} \operatorname{Tan}[c + d x] \right) / \left( d \sqrt{1 + \operatorname{Sec}[c + d x]} \left( \frac{a + b \operatorname{Sec}[c + d x]}{a + b} \right)^{2/3} \right)$$

Result (type 6, 11 531 leaves):

$$\left( -\frac{7 a b}{10 (b+a \cos [c+d x])^{1/3} \sec [c+d x]^{1/3}} - \frac{a^2 \sec [c+d x]^{2/3}}{20 (b+a \cos [c+d x])^{1/3}} + \frac{2 b^2 \sec [c+d x]^{2/3}}{5 (b+a \cos [c+d x])^{1/3}} - \frac{21 a^2 \cos [2 (c+d x)] \sec [c+d x]^{2/3}}{20 (b+a \cos [c+d x])^{1/3}} \right) (a+b \sec [c+d x])^{5/3}$$

$$\left( -\frac{21 a \tan \left[ \frac{1}{2} (c+d x) \right] \left( \frac{a+b-a \tan \left[ \frac{1}{2} (c+d x) \right]^2+b \tan \left[ \frac{1}{2} (c+d x) \right]^2}{1+\tan \left[ \frac{1}{2} (c+d x) \right]^2} \right)^{2/3}}{10 \left( \frac{1+\tan \left[ \frac{1}{2} (c+d x) \right]^2}{1-\tan \left[ \frac{1}{2} (c+d x) \right]^2} \right)^{1/3}} - \left( 3 (a+b) \tan \left[ \frac{1}{2} (c+d x) \right] \right. \right.$$

$$\left. \left. \left( 70 a (a-b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+d x) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+d x) \right]^2}{a+b} \right] \right) \right. \right.$$

$$\left. \left. \left( (a-b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+d x) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+d x) \right]^2}{a+b} \right] \right) + \right. \right.$$

$$\left. \left. 2 (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+d x) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+d x) \right]^2}{a+b} \right] \right) \right. \right.$$

$$\left. \left. \tan \left[ \frac{1}{2} (c+d x) \right]^4 + 3 (a+b) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+d x) \right]^2, \right. \right. \right.$$

$$\left. \left. \left. \frac{(a-b) \tan \left[ \frac{1}{2} (c+d x) \right]^2}{a+b} \right] \left( -2 (a-8 b) \left( (a-b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \right. \right. \right. \right.$$

$$\left. \left. \left. \tan \left[ \frac{1}{2} (c+d x) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+d x) \right]^2}{a+b} \right] + 2 (a+b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, \right. \right. \right.$$

$$\left. \left. \left. \frac{1}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+d x) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+d x) \right]^2}{a+b} \right] \right) \right) \tan \left[ \frac{1}{2} (c+d x) \right]^2 + \right.$$

$$\left. 15 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+d x) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+d x) \right]^2}{a+b} \right] \right.$$

$$\left. \left. \left( 8 b^2 - 7 a b \left( -1 + \tan \left[ \frac{1}{2} (c+d x) \right]^2 \right) + a^2 \left( -1 + 7 \tan \left[ \frac{1}{2} (c+d x) \right]^2 \right) \right) \right) \right) \right) /$$

$$\left( 10 \left( -1 + \tan \left[ \frac{1}{2} (c+d x) \right]^2 \right) \left( \frac{1 + \tan \left[ \frac{1}{2} (c+d x) \right]^2}{1 - \tan \left[ \frac{1}{2} (c+d x) \right]^2} \right)^{1/3} \right)$$



$$\begin{aligned}
 & \left( 10 \left( \frac{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^{4/3} - 7a \tan\left[\frac{1}{2}(c+dx)\right] \right. \\
 & \left. \left( \left( -a \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + b \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) / \right. \right. \\
 & \left. \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - \left( \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right. \right. \\
 & \left. \left. \left( a + b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) / \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \right) \right) / \\
 & \left( 5 \left( \frac{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^{1/3} \left( \frac{a + b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^{1/3} \right) + \\
 & \left( 3(a+b) \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \left. \left( 70a(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \right. \\
 & \left. \left( (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) + \right. \\
 & \left. 2(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \right. \\
 & \left. \tan\left[\frac{1}{2}(c+dx)\right]^4 + 3(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \left( -2(a-8b) \left( (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \right. \right. \right. \right. \\
 & \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + 2(a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \right. \right. \right. \\
 & \left. \left. \left. \frac{1}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 + \right. \\
 & \left. 15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \left. \left. \left( 8b^2 - 7ab \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) + a^2 \left( -1 + 7 \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) \right) \right) / \\
 & \left( 10 \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \left( \frac{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^{1/3} \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( \frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \right)^{1/3} \\
 & \left( 9(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & 2(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \left. \right) \\
 & \left( 15(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & 2(a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \left. \right) \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) - \left( 3(a+b) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right) \\
 & \left( 70a(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \left( (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & 2(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \left. \right) \\
 & \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^4 + 3(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \left( -2(a-8b) \left( (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \right. \right. \right. \\
 & \left. \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + 2(a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \right. \right. \right.
 \end{aligned}$$



$$\begin{aligned}
 & \left. \frac{1}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + \\
 & 15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \\
 & \left. \left(8b^2 - 7ab \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) + a^2 \left(-1 + 7 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)\right)\right) \Big/ \\
 & \left(20 \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \left(\frac{1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}\right)^{1/3}\right. \\
 & \left.\left(\frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}\right)^{1/3}\right. \\
 & \left. \left(9(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \right. \\
 & \left. \left. 2 \left((a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \right. \right. \\
 & \left. \left. 2(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \left. \left. \left.\frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)\right) \right. \\
 & \left. \left(15(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \right. \\
 & \left. \left. 2 \left((a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \right. \right. \\
 & \left. \left. 2(a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \left. \left. \left.\frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)\right) \right. \\
 & \left. \left((a+b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \left(\frac{\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} + \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2\right. \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)\right) \Big/ \left(1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)^2\right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( 70 a (a - b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, \frac{(a - b) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] \right. \\
 & \left( (a - b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, \frac{(a - b) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] + \right. \\
 & \left. \left. 2 (a + b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, \frac{(a - b) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] \right) \right. \\
 & \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^4 + 3 (a + b) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, \right. \\
 & \left. \frac{(a - b) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] \left( -2 (a - 8 b) \left( (a - b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \right. \right. \right. \\
 & \left. \left. \left. \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, \frac{(a - b) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] + 2 (a + b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, \right. \right. \right. \\
 & \left. \left. \left. \frac{1}{3}, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, \frac{(a - b) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] \right) \right) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 + \\
 & 15 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, \frac{(a - b) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] \\
 & \left. \left( 8 b^2 - 7 a b \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right) + a^2 \left( -1 + 7 \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right) \right) \right) \right) / \\
 & \left( 10 \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right) \left( \frac{1 + \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{1 - \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2} \right)^{4/3} \right. \\
 & \left. \left( \frac{a + b - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 + b \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{1 + \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2} \right)^{1/3} \right. \\
 & \left( 9 (a + b) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, \frac{(a - b) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] + \right. \\
 & 2 \left( (a - b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, \frac{(a - b) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] + \right. \\
 & \left. 2 (a + b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, \right. \right. \\
 & \left. \left. \frac{(a - b) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] \right) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( 15 (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & \left. \left. 2 (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \right) \\
 & \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) + \left( (a+b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right. \\
 & \left. \left( \left( -a \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + b \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) / \right. \right. \\
 & \left. \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) - \left( \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \right. \\
 & \left. \left. \left( a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) / \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \right) \right) \\
 & \left( 70 a (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \left( (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & \left. \left. 2 (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \right) \\
 & \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^4 + 3 (a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \left( -2 (a-8b) \left( (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \right. \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + 2 (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \right. \right. \\
 & \left. \left. \frac{1}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + \\
 & 15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \\
 & \left. \left( 8b^2 - 7ab \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) + a^2 \left( -1 + 7 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) /
 \end{aligned}$$

$$\begin{aligned}
& \left( 10 \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( \frac{1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \right)^{1/3} \right. \\
& \quad \left. \left( \frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \right)^{4/3} \right. \\
& \quad \left( 9(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
& \quad 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
& \quad 2(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
& \quad \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \\
& \quad \left( 15(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
& \quad 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
& \quad 2(a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
& \quad \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) + \\
& \quad \left( 3(a+b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \left( 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
& \quad \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + 2(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
& \quad \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \\
& \quad 9(a+b) \left( \frac{1}{9(a+b)} (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right.
\end{aligned}$$

$$\begin{aligned}
 & \frac{2}{9} \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \\
 & \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right] + 2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \left( (a-b) \left( \frac{1}{5(a+b)} 4(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{7}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \right. \\
 & \left. \frac{2}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{4}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right) + 2(a+b) \left( \frac{1}{5(a+b)} (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \right. \right. \\
 & \left. \left. \frac{5}{3}, \frac{4}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \operatorname{AppellF1}\left[\frac{5}{2}, \frac{8}{3}, \frac{1}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right) \right) \\
 & \left( 70 a (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \left. \left( (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \right. \\
 & \left. \left. 2(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \right. \\
 & \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^4 + 3(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \left( -2(a-8b) \left( (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \right. \right. \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + 2(a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \right. \right. \\
 & \left. \left. \frac{1}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 +
 \end{aligned}$$

$$\begin{aligned}
 & 15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \\
 & \left(8b^2 - 7ab \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) + a^2 \left(-1 + 7 \tan\left[\frac{1}{2}(c+dx)\right]^2\right)\right) \Bigg) \Bigg) \Bigg) \Bigg) \Bigg) / \\
 & \left(10 \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \left(\frac{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2}\right)^{1/3}\right. \right. \\
 & \left.\left(\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}\right)^{1/3}\right. \\
 & \left.9(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & 2 \left((a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & 2(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \left.\left.\frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \Bigg)^2 \\
 & \left(15(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & 2 \left((a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & 2(a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \Bigg) \\
 & \tan\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) \Bigg) + \left(3(a+b) \tan\left[\frac{1}{2}(c+dx)\right] \right. \\
 & \left. 2 \left((a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \right. \\
 & \left. 2(a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \Bigg) \\
 & \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + 15(a+b) \left(\frac{1}{5(a+b)}\right.
 \end{aligned}$$

$$\begin{aligned}
 & (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \\
 & \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \frac{2}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \Bigg) + \\
 & 2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \left( (a-b) \left( \frac{1}{21(a+b)} 20(a-b) \operatorname{AppellF1}\left[\frac{7}{2}, \frac{2}{3}, \frac{7}{3}, \frac{9}{2}, \right. \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \frac{10}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{5}{3}, \frac{4}{3}, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \Bigg) + \\
 & 2(a+b) \left( \frac{1}{21(a+b)} 5(a-b) \operatorname{AppellF1}\left[\frac{7}{2}, \frac{5}{3}, \frac{4}{3}, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \left. \frac{25}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{8}{3}, \frac{1}{3}, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \right) \Bigg) \\
 & \left( 70a(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \left. \left( (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \right. \\
 & \left. \left. 2(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \right) \\
 & \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^4 + 3(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \left( -2(a-8b) \left( (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \right. \right. \right.
 \end{aligned}$$





$$\begin{aligned}
 & \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \\
 & \left( (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & \quad \left. 2(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \\
 & \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^3 + 70a(a-b) \\
 & \left( (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & \quad \left. 2(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \\
 & \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^4 \left( \frac{1}{5(a+b)} (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \quad \left. \frac{2}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) + 70a(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \right. \\
 & \quad \left. \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^4 \\
 & \left( (a-b) \left( \frac{1}{5(a+b)} 4(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{7}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \quad \left. \frac{2}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{4}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) + 2(a+b) \left( \frac{1}{5(a+b)} (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \frac{5}{3}, \frac{4}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right.
 \end{aligned}$$



$$\begin{aligned}
 & 2 (a - 8 b) \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2 \left( (a - b) \left( \frac{1}{21(a+b)} 20 (a - b) \operatorname{AppellF1}\left[\frac{7}{2}, \frac{2}{3}, \right. \right. \right. \\
 & \quad \left. \left. \frac{7}{3}, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2, \frac{(a - b) \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}{a + b}\right] \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^2 \right. \\
 & \quad \left. \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] + \frac{10}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{5}{3}, \frac{4}{3}, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a - b) \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}{a + b}\right] \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] \right) + \\
 & 2 (a + b) \left( \frac{1}{21(a+b)} 5 (a - b) \operatorname{AppellF1}\left[\frac{7}{2}, \frac{5}{3}, \frac{4}{3}, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a - b) \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}{a + b}\right] \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] + \right. \\
 & \quad \left. \frac{25}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{8}{3}, \frac{1}{3}, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2, \frac{(a - b) \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}{a + b}\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] \right) + 15 \left( \frac{1}{5(a+b)} (a - b) \operatorname{AppellF1}\left[\frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2, \frac{(a - b) \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}{a + b}\right] \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^2 \right. \\
 & \quad \left. \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] + \frac{2}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a - b) \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}{a + b}\right] \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] \right) \\
 & \left. \left( 8 b^2 - 7 a b \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2 \right) + a^2 \left( -1 + 7 \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2 \right) \right) \right) \Bigg) \Bigg) \Bigg) \Bigg) / \\
 & \left( 10 \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2 \right) \left( \frac{1 + \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}{1 - \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2} \right)^{1/3} \right. \\
 & \quad \left. \left( \frac{a + b - a \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2} \right)^{1/3} \right. \\
 & \quad \left. \left( 9 (a + b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2, \frac{(a - b) \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}{a + b}\right] + \right. \right. \\
 & \quad \left. \left. 2 \left( (a - b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2, \frac{(a - b) \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}{a + b}\right] + \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & 2 (a + b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, \right. \\
 & \quad \left. \frac{(a - b) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \Bigg) \\
 & \left( 15 (a + b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, \frac{(a - b) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] + \right. \\
 & 2 \left( (a - b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, \frac{(a - b) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] + \right. \\
 & 2 (a + b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, \right. \\
 & \quad \left. \frac{(a - b) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \Bigg) \Bigg) \Bigg) + \\
 & \left( \operatorname{Cos} [c + d x] (a + b \operatorname{Sec} [c + d x])^{5/3} \left( \frac{21}{10} a \operatorname{Sin} [c + d x] + \right. \right. \\
 & \quad \frac{3}{5} \\
 & \quad b \\
 & \quad \operatorname{Tan} [ \\
 & \quad \quad c + d x] \Bigg) \Bigg) / (d (b + a \operatorname{Cos} [ \\
 & \quad c + d x] \Bigg) \Bigg)
 \end{aligned}$$

**Problem 699: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec} [c + d x]^4}{(a + b \operatorname{Sec} [c + d x])^{1/3}} dx$$

Optimal (type 6, 313 leaves, 9 steps):

$$\begin{aligned}
 & - \frac{9 a (a+b \operatorname{Sec}[c+d x])^{2/3} \operatorname{Tan}[c+d x]}{20 b^2 d} + \frac{3 \operatorname{Sec}[c+d x] (a+b \operatorname{Sec}[c+d x])^{2/3} \operatorname{Tan}[c+d x]}{8 b d} + \\
 & \left( (18 a^2 + 25 b^2) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}, -\frac{2}{3}, \frac{3}{2}, \frac{1}{2} (1 - \operatorname{Sec}[c+d x]), \frac{b (1 - \operatorname{Sec}[c+d x])}{a+b}\right] \right. \\
 & \quad \left. (a+b \operatorname{Sec}[c+d x])^{2/3} \operatorname{Tan}[c+d x] \right) / \left( 20 \sqrt{2} b^3 d \sqrt{1 + \operatorname{Sec}[c+d x]} \left( \frac{a+b \operatorname{Sec}[c+d x]}{a+b} \right)^{2/3} \right) - \\
 & \left( a (9 a^2 + 11 b^2) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}, \frac{1}{3}, \frac{3}{2}, \frac{1}{2} (1 - \operatorname{Sec}[c+d x]), \frac{b (1 - \operatorname{Sec}[c+d x])}{a+b}\right] \right. \\
 & \quad \left. \left( \frac{a+b \operatorname{Sec}[c+d x]}{a+b} \right)^{1/3} \operatorname{Tan}[c+d x] \right) / \left( 10 \sqrt{2} b^3 d \sqrt{1 + \operatorname{Sec}[c+d x]} (a+b \operatorname{Sec}[c+d x])^{1/3} \right)
 \end{aligned}$$

Result (type 6, 29880 leaves): Display of huge result suppressed!

### Problem 700: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Sec}[c+d x]^3}{(a+b \operatorname{Sec}[c+d x])^{1/3}} dx$$

Optimal (type 6, 265 leaves, 8 steps):

$$\begin{aligned}
 & \frac{3 (a+b \operatorname{Sec}[c+d x])^{2/3} \operatorname{Tan}[c+d x]}{5 b d} - \\
 & \left( 3 \sqrt{2} a \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}, -\frac{2}{3}, \frac{3}{2}, \frac{1}{2} (1 - \operatorname{Sec}[c+d x]), \frac{b (1 - \operatorname{Sec}[c+d x])}{a+b}\right] \right. \\
 & \quad \left. (a+b \operatorname{Sec}[c+d x])^{2/3} \operatorname{Tan}[c+d x] \right) / \left( 5 b^2 d \sqrt{1 + \operatorname{Sec}[c+d x]} \left( \frac{a+b \operatorname{Sec}[c+d x]}{a+b} \right)^{2/3} \right) + \\
 & \left( \sqrt{2} (3 a^2 + 2 b^2) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}, \frac{1}{3}, \frac{3}{2}, \frac{1}{2} (1 - \operatorname{Sec}[c+d x]), \frac{b (1 - \operatorname{Sec}[c+d x])}{a+b}\right] \right. \\
 & \quad \left. \left( \frac{a+b \operatorname{Sec}[c+d x]}{a+b} \right)^{1/3} \operatorname{Tan}[c+d x] \right) / \left( 5 b^2 d \sqrt{1 + \operatorname{Sec}[c+d x]} (a+b \operatorname{Sec}[c+d x])^{1/3} \right)
 \end{aligned}$$

Result (type 6, 18777 leaves):

$$\begin{aligned}
 & \left( 9 (b+a \operatorname{Cos}[c+d x])^{1/3} \left( \frac{3 a}{10 b (b+a \operatorname{Cos}[c+d x])^{1/3} \operatorname{Sec}[c+d x]^{1/3}} + \frac{2 \operatorname{Sec}[c+d x]^{2/3}}{5 (b+a \operatorname{Cos}[c+d x])^{1/3}} \right) \right. \\
 & \quad \left. \frac{9 a^2 \operatorname{Sec}[c+d x]^{2/3}}{20 b^2 (b+a \operatorname{Cos}[c+d x])^{1/3}} + \frac{9 a^2 \operatorname{Cos}[2(c+d x)] \operatorname{Sec}[c+d x]^{2/3}}{20 b^2 (b+a \operatorname{Cos}[c+d x])^{1/3}} \right) \\
 & \operatorname{Sec}[c+d x]^{1/3} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] \left( \frac{1}{1 - \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \right)^{2/3} \\
 & \left( \frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \right)^{2/3} \left( a - a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2 - \right.
 \end{aligned}$$

$$\begin{aligned}
& \left( 8 b^2 (a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
& \left. \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) / \left( \left( a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right. \\
& \left. \left( -9(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] - \right. \right. \\
& \left. \left. 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) + \right. \right. \\
& \left. \left. 2(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \right. \right. \\
& \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) - \left( 9 a^2 (a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \right. \right. \\
& \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) / \\
& \left( \left( 9(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \right. \\
& \left. \left. 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) + \right. \right. \\
& \left. \left. 2(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \right. \right. \\
& \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( a \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) + \\
& \left( 3 a b (a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
& \left. \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) / \\
& \left( \left( 9(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \right.
\end{aligned}$$

$$\begin{aligned}
 & 2 \left( (a-b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \\
 & \quad \left. 2 (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \\
 & \quad \left. \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \left( a \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) - b \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) + \\
 & \left( 5 a^2 (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right. \\
 & \quad \left. \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) / \\
 & \left( \left( 15 (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \right. \\
 & \quad \left. \left. 2 \left( (a-b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \right. \right. \\
 & \quad \left. \left. 2 (a+b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \right) \\
 & \quad \left. \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \left( a \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) - b \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) - \\
 & \left( 5 a b (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right. \\
 & \quad \left. \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) / \\
 & \left( \left( 15 (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \right. \\
 & \quad \left. \left. 2 \left( (a-b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \right. \right. \\
 & \quad \left. \left. 2 (a+b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \right) \right)
 \end{aligned}$$





$$\begin{aligned}
 & \left. \left( \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + 2(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \\
 & \left( a \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Bigg) + \\
 & \left( 3ab(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \left. \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) / \left( \left( 9(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \right. \right. \right. \right. \\
 & \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + 2(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \\
 & \left( a \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Bigg) + \\
 & \left( 5a^2(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \left. \tan\left[\frac{1}{2}(c+dx)\right]^2 \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) / \left( \left( 15(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + 2(a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \right) \right) \\
 & \left. \tan\left[\frac{1}{2}(c+dx)\right]^2 \left( a \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) -
 \end{aligned}$$

$$\begin{aligned}
 & \left( 5 a b (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}\right] \right. \\
 & \quad \left. \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2 \left(1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right)\right) / \\
 & \left( \left( 15 (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}\right] \right) + \right. \\
 & \quad 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}\right] + 2 (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \right. \right. \\
 & \quad \quad \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}\right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2 \right) \\
 & \quad \left. \left( a \left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right) - b \left(1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right) \right) \right) + \\
 & \frac{1}{20 b^2 \left(1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right)^{1/3}} 9 \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \left(\frac{1}{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}\right)^{2/3} \\
 & \quad \left(\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}\right)^{2/3} \\
 & \quad \left(a-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2 - \right. \\
 & \quad \left. \left( 8 b^2 (a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}\right] \right) \right. \\
 & \quad \left. \left(1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right)\right) / \left(\left(a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right)\right) \\
 & \quad \left(-9 (a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}\right] - \right. \\
 & \quad \left. 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}\right] \right) + \right. \\
 & \quad \left. 2 (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2, \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) - \\
 & \left( 9a^2(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \left. \left. \left. \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) \right) / \left( \left( 9(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \right. \right. \right. \right. \\
 & \left. \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + 2(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \\
 & \left. \left. \left. \left( a \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) \right) + \\
 & \left( 3ab(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \left. \left. \left. \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) \right) / \left( \left( 9(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \right. \right. \right. \right. \\
 & \left. \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + 2(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \\
 & \left. \left. \left. \left( a \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) \right) + \\
 & \left( 5a^2(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \left. \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) \right) /
 \end{aligned}$$

$$\begin{aligned}
& \left( \left( 15 (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \right. \\
& \quad 2 \left( (a-b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \\
& \quad \quad 2 (a+b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \right. \\
& \quad \quad \quad \left. \left. \left. \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) \right) \\
& \quad \left( a \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) - b \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) \right) \\
& \left( 5 a b (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right. \\
& \quad \left. \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) / \\
& \left( \left( 15 (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \right. \\
& \quad 2 \left( (a-b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \\
& \quad \quad 2 (a+b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \right. \\
& \quad \quad \quad \left. \left. \left. \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) \right) \\
& \quad \left( a \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) - b \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) \right) \right) + \\
& \frac{1}{5 b^2 \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right)^{1/3}} 3 \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \\
& \left( \frac{1}{1 - \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2} \right)^{5/3} \\
& \left( \frac{a+b - a \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 + b \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2} \right)^{2/3}
\end{aligned}$$

$$\begin{aligned}
 & \left( a - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 - \right. \\
 & \left. \left( 8b^2(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \right. \\
 & \left. \left. \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) / \left( \left( a + b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right. \\
 & \left. \left( -9(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) - \right. \\
 & \left. 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) + \right. \\
 & \left. 2(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) - \\
 & \left( 9a^2(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \left. \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) / \\
 & \left( \left( 9(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) + \right. \\
 & \left. 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) + \right. \\
 & \left. 2(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \\
 & \left( a \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) + \\
 & \left( 3ab(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right)
 \end{aligned}$$

$$\begin{aligned}
& \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \Big/ \\
& \left( \left( 9(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \right. \\
& \quad 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) + \\
& \quad 2(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
& \quad \quad \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \\
& \left( a \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Big) + \\
& \left( 5a^2(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
& \quad \left. \tan\left[\frac{1}{2}(c+dx)\right]^2 \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Big/ \\
& \left( \left( 15(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \right. \\
& \quad 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) + \\
& \quad 2(a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
& \quad \quad \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \\
& \left( a \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Big) - \\
& \left( 5ab(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
& \quad \left. \tan\left[\frac{1}{2}(c+dx)\right]^2 \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Big/
\end{aligned}$$

$$\begin{aligned}
 & \left( \left( 15 (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \right. \\
 & \quad 2 \left( (a-b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \\
 & \quad \quad 2 (a+b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \\
 & \quad \quad \quad \left. \left. \left. \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) \\
 & \quad \left. \left( a \left( -1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) - b \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) \right) \right) \\
 & \left( 1 / \left( 5 b^2 \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right)^{1/3} \left( \frac{a+b - a \tan \left[ \frac{1}{2} (c+dx) \right]^2 + b \tan \left[ \frac{1}{2} (c+dx) \right]^2}{1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2} \right)^{1/3} \right) \right) \\
 & \quad 3 \\
 & \quad \tan \left[ \frac{1}{2} (c+dx) \right] \\
 & \quad \left( \frac{1}{1 - \tan \left[ \frac{1}{2} (c+dx) \right]^2} \right)^{2/3} \\
 & \quad \left( \left( -a \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + b \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \right) / \right. \\
 & \quad \quad \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) - \\
 & \quad \quad \left. \left( \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \left( a+b - a \tan \left[ \frac{1}{2} (c+dx) \right]^2 + b \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) / \right. \\
 & \quad \quad \left. \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right)^2 \right) \left( a - a \tan \left[ \frac{1}{2} (c+dx) \right]^2 - \right. \\
 & \quad \quad \left. \left( 8 b^2 (a+b) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \right. \\
 & \quad \quad \left. \left. \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) / \left( \left( a+b - a \tan \left[ \frac{1}{2} (c+dx) \right]^2 + b \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) \right. \\
 & \quad \quad \left. \left( -9 (a+b) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] - \right. \right. \\
 & \quad \quad \left. \left. 2 \left( (a-b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
& \left. \left( 2 (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \\
& \quad \left. \left. \left. \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) - \\
& \left( 9 a^2 (a+b) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right. \\
& \quad \left. \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) / \\
& \left( \left( 9 (a+b) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \right. \\
& \quad \left. \left. 2 \left( (a-b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) + \right. \right. \\
& \quad \left. \left. 2 (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \\
& \quad \left. \left. \left. \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) \right) + \\
& \left( a \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) - b \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) \\
& \left( 3 a b (a+b) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right. \\
& \quad \left. \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) / \\
& \left( \left( 9 (a+b) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \right. \\
& \quad \left. \left. 2 \left( (a-b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) + \right. \right. \\
& \quad \left. \left. 2 (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \\
& \quad \left. \left. \left. \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) \right)
\end{aligned}$$



$$\begin{aligned}
 & \left( a \left( -1 + \tan \left[ \frac{1}{2} (c + dx) \right]^2 \right) - b \left( 1 + \tan \left[ \frac{1}{2} (c + dx) \right]^2 \right) \right) + \\
 & \left( 5 a^2 (a + b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, \frac{(a - b) \tan \left[ \frac{1}{2} (c + dx) \right]^2}{a + b} \right] \right. \\
 & \left. \tan \left[ \frac{1}{2} (c + dx) \right]^2 \left( 1 + \tan \left[ \frac{1}{2} (c + dx) \right]^2 \right) \right) / \\
 & \left( \left( 15 (a + b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, \frac{(a - b) \tan \left[ \frac{1}{2} (c + dx) \right]^2}{a + b} \right] + \right. \right. \\
 & \left. \left. 2 \left( (a - b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, \frac{(a - b) \tan \left[ \frac{1}{2} (c + dx) \right]^2}{a + b} \right] \right) \right. \right. \\
 & \left. \left. 2 (a + b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, \right. \right. \right. \\
 & \left. \left. \left. \frac{(a - b) \tan \left[ \frac{1}{2} (c + dx) \right]^2}{a + b} \right] \right) \tan \left[ \frac{1}{2} (c + dx) \right]^2 \right) \right) \\
 & \left( a \left( -1 + \tan \left[ \frac{1}{2} (c + dx) \right]^2 \right) - b \left( 1 + \tan \left[ \frac{1}{2} (c + dx) \right]^2 \right) \right) - \\
 & \left( 5 a b (a + b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, \frac{(a - b) \tan \left[ \frac{1}{2} (c + dx) \right]^2}{a + b} \right] \right. \\
 & \left. \tan \left[ \frac{1}{2} (c + dx) \right]^2 \left( 1 + \tan \left[ \frac{1}{2} (c + dx) \right]^2 \right) \right) / \\
 & \left( \left( 15 (a + b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, \frac{(a - b) \tan \left[ \frac{1}{2} (c + dx) \right]^2}{a + b} \right] + \right. \right. \\
 & \left. \left. 2 \left( (a - b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, \frac{(a - b) \tan \left[ \frac{1}{2} (c + dx) \right]^2}{a + b} \right] \right) \right. \right. \\
 & \left. \left. 2 (a + b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, \right. \right. \right. \\
 & \left. \left. \left. \frac{(a - b) \tan \left[ \frac{1}{2} (c + dx) \right]^2}{a + b} \right] \right) \tan \left[ \frac{1}{2} (c + dx) \right]^2 \right) \right) \\
 & \left( a \left( -1 + \tan \left[ \frac{1}{2} (c + dx) \right]^2 \right) - b \left( 1 + \tan \left[ \frac{1}{2} (c + dx) \right]^2 \right) \right) \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{10 b^2 \left(1 + \tan\left[\frac{1}{2}(c + dx)\right]^2\right)^{1/3}} 9 \tan\left[\frac{1}{2}(c + dx)\right] \left(\frac{1}{1 - \tan\left[\frac{1}{2}(c + dx)\right]^2}\right)^{2/3} \\
 & \left(\frac{a + b - a \tan\left[\frac{1}{2}(c + dx)\right]^2 + b \tan\left[\frac{1}{2}(c + dx)\right]^2}{1 + \tan\left[\frac{1}{2}(c + dx)\right]^2}\right)^{2/3} \\
 & \left(-a \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \tan\left[\frac{1}{2}(c + dx)\right] + \right. \\
 & \left. \left(8 b^2 (a + b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, \frac{(a - b) \tan\left[\frac{1}{2}(c + dx)\right]^2}{a + b}\right] \right. \right. \\
 & \left. \left(-a \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \tan\left[\frac{1}{2}(c + dx)\right] + b \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \tan\left[\frac{1}{2}(c + dx)\right] \right) \right. \\
 & \left. \left(1 + \tan\left[\frac{1}{2}(c + dx)\right]^2\right)\right) / \left(\left(a + b - a \tan\left[\frac{1}{2}(c + dx)\right]^2 + b \tan\left[\frac{1}{2}(c + dx)\right]^2\right)^2 \right. \\
 & \left. \left(-9 (a + b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, \frac{(a - b) \tan\left[\frac{1}{2}(c + dx)\right]^2}{a + b}\right] - \right. \right. \\
 & \left. \left. 2 \left((a - b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, \frac{(a - b) \tan\left[\frac{1}{2}(c + dx)\right]^2}{a + b}\right] \right) \right. \right. \\
 & \left. \left. 2 (a + b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, \right. \right. \right. \\
 & \left. \left. \left. \frac{(a - b) \tan\left[\frac{1}{2}(c + dx)\right]^2}{a + b}\right] \right) \tan\left[\frac{1}{2}(c + dx)\right]^2\right) \right) - \\
 & \left(8 b^2 (a + b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, \frac{(a - b) \tan\left[\frac{1}{2}(c + dx)\right]^2}{a + b}\right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \tan\left[\frac{1}{2}(c + dx)\right] \right) / \\
 & \left(\left(a + b - a \tan\left[\frac{1}{2}(c + dx)\right]^2 + b \tan\left[\frac{1}{2}(c + dx)\right]^2\right) \right. \\
 & \left. \left(-9 (a + b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, \frac{(a - b) \tan\left[\frac{1}{2}(c + dx)\right]^2}{a + b}\right] - \right. \right. \\
 & \left. \left. 2 \left((a - b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, \frac{(a - b) \tan\left[\frac{1}{2}(c + dx)\right]^2}{a + b}\right] \right) \right. \right. \\
 & \left. \left. \frac{(a - b) \tan\left[\frac{1}{2}(c + dx)\right]^2}{a + b}\right) \right) \right) +
 \end{aligned}$$

$$\begin{aligned}
 & 2(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \quad \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) - \\
 & \left( 8b^2(a+b) \left( \frac{1}{9(a+b)}(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{2}{9} \right. \right. \\
 & \quad \left. \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \quad \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) / \\
 & \left( \left( a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( -9(a+b) \right. \right. \\
 & \quad \left. \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] - 2 \right. \right. \\
 & \quad \left. \left( (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right)^2 \right. \\
 & \quad \left. \left. + 2(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) + \\
 & \left( 9a^2(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \quad \left. \left( a \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] - b \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right. \\
 & \quad \left. \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) / \\
 & \left( \left( 9(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \right. \\
 & \quad \left. \left. + 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right)^2 \right) \right) +
 \end{aligned}$$

$$\begin{aligned}
 & 2 (a + b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2, \right. \\
 & \quad \left. \frac{(a - b) \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2}{a + b}\right] \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2 \Bigg) \\
 & \left( a \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2 \right) - b \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2 \right) \right)^2 \Bigg) - \\
 & \left( 3 a b (a + b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2, \frac{(a - b) \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2}{a + b}\right] \right. \\
 & \quad \left( a \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right] - b \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right] \right) \\
 & \quad \left. \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2 \right) \right) \Bigg) / \\
 & \left( \left( 9 (a + b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2, \frac{(a - b) \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2}{a + b}\right] \right) + \right. \\
 & \quad 2 \left( (a - b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2, \frac{(a - b) \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2}{a + b}\right] \right) + \\
 & \quad 2 (a + b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2, \right. \\
 & \quad \left. \frac{(a - b) \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2}{a + b}\right] \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2 \Bigg) \\
 & \left. \left( a \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2 \right) - b \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2 \right) \right)^2 \right) \Bigg) - \\
 & \left( 5 a^2 (a + b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2, \frac{(a - b) \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2}{a + b}\right] \right. \\
 & \quad \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2 \left( a \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right] - b \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right] \right) \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2 \right) \Bigg) \Bigg) / \\
 & \left( \left( 15 (a + b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2, \frac{(a - b) \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2}{a + b}\right] \right) + \right. \\
 & \quad 2 \left( (a - b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2, \frac{(a - b) \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2}{a + b}\right] \right) + \right.
 \end{aligned}$$

$$\begin{aligned}
 & 2 (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \quad \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) \\
 & \left( a \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right)^2 \Bigg) + \\
 & \left( 5 a b (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \quad \tan\left[\frac{1}{2}(c+dx)\right]^2 \left( a \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] - b \right. \\
 & \quad \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Bigg) / \\
 & \left( \left( 15 (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) + \right. \\
 & \quad \left. 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) + \right. \\
 & \quad \left. 2 (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) \\
 & \left( a \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right)^2 \Bigg) - \\
 & \left( 9 a^2 (a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \Bigg) / \\
 & \left( \left( 9 (a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) + \right. \\
 & \quad \left. 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) + \right. \\
 & \quad \left. 2 (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) \\
 & \left( a \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Bigg) + \\
 & \left( 3ab(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \Bigg) / \\
 & \left( \left( 9(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right. + \right. \\
 & \left. 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) + \right. \\
 & \left. 2(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) \\
 & \left( a \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Bigg) - \\
 & \left( 9a^2(a+b) \left( \frac{1}{9(a+b)} (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \frac{2}{9} \right. \right. \\
 & \left. \left. \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right. \right. \\
 & \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Bigg) / \\
 & \left( \left( 9(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right. + \right. \\
 & \left. 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) + \right.
 \end{aligned}$$

$$\begin{aligned}
 & 2(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \quad \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) \\
 & \left( a \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Bigg) + \\
 & \left( 3ab(a+b) \left( \frac{1}{9(a+b)} (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{2}{9} \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \right. \\
 & \quad \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Bigg) / \\
 & \left( \left( 9(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) + \right. \\
 & \quad \left. 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) + \right. \\
 & \quad \left. 2(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \\
 & \left( a \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Bigg) + \\
 & \left( 5a^2(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \quad \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^3 \right) \Bigg) / \\
 & \left( \left( 15(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) + \right.
 \end{aligned}$$

$$\begin{aligned}
 & 2 \left( (a-b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \\
 & \quad \left. 2 (a+b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
 & \quad \quad \left. \left. \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \Bigg) \\
 & \left( a \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) - b \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) \Bigg) - \\
 & \left( 5 a b (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right. \\
 & \quad \left. \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^3 \right) / \\
 & \left( \left( 15 (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \right. \\
 & \quad \left. \left. 2 \left( (a-b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \right. \right. \\
 & \quad \left. \left. 2 (a+b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \\
 & \quad \quad \left. \left. \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \\
 & \left( a \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) - b \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) \Bigg) + \\
 & \left( 5 a^2 (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right. \\
 & \quad \left. \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) / \\
 & \left( \left( 15 (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \right. \\
 & \quad \left. \left. 2 \left( (a-b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \right. \right.
 \end{aligned}$$



$$\begin{aligned}
 & 2 (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \quad \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) \\
 & \left( a \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Bigg) - \\
 & \left( 5 a b (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Bigg) / \\
 & \left( \left( 15 (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) + \right. \\
 & \quad \left. 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \right) + \\
 & \quad \left. 2 (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \\
 & \left( a \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Bigg) + \left( 5 a^2 (a+b) \right. \\
 & \quad \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \left( \frac{1}{5(a+b)} (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \quad \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \frac{2}{5} \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \right. \\
 & \quad \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) / \\
 & \left( \left( 15 (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) + \right.
 \end{aligned}$$

$$\begin{aligned}
& 2 \left( (a-b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \\
& \quad \left. 2 (a+b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
& \quad \quad \left. \left. \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \\
& \left( a \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) - b \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) - \left( 5 a b (a+b) \right. \\
& \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \left( \frac{1}{5 (a+b)} (a-b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
& \quad \left. \left. \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] + \frac{2}{5} \right. \\
& \quad \left. \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right. \\
& \quad \left. \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] \right) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \Big/ \\
& \left( \left( 15 (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \right. \\
& \quad \left. \left. 2 \left( (a-b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \right. \right. \\
& \quad \left. \left. 2 (a+b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \\
& \quad \quad \left. \left. \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) \\
& \left( a \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) - b \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) + \\
& \left( 8 b^2 (a+b) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right. \\
& \left. \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) \left( -2 \left( (a-b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \\
& \quad \left. \left. \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + 2 (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \right. \right. \right.
\end{aligned}$$



$$\begin{aligned}
& \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} + 2(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \right. \right. \\
& \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)^2 + \\
& \left(9a^2(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
& \left. \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \left(2 \left( (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
& \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} + 2(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \right. \right. \right. \right. \\
& \left. \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
& \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + 9(a+b) \left( \frac{1}{9(a+b)} (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \right. \right. \right. \\
& \left. \left. \left. \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \\
& \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \frac{2}{9} \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
& \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \right) + 2 \\
& \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \left( (a-b) \left( \frac{1}{5(a+b)} 4(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{7}{3}, \frac{7}{2}, \right. \right. \right. \\
& \left. \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \\
& \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \frac{2}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{4}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
& \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \right) + \\
& 2(a+b) \left( \frac{1}{5(a+b)} (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{4}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right.
\end{aligned}$$

$$\begin{aligned}
 & \left. \left. \left. \left. \left. \text{AppellF1}\left[\frac{5}{2}, \frac{8}{3}, \frac{1}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right]\right.\right.\right.\right. \\
 & \left. \left. \left. \left. \left. \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right]\right]\right]\right]\right] / \\
 & \left( \left( 9(a+b) \text{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right]\right) + \right. \\
 & \quad 2 \left( (a-b) \text{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right.\right. \\
 & \quad \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + 2(a+b) \text{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \right.\right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \\
 & \left. \left. \left. \left. \left. \left( a \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) \right) \right) \right) - \\
 & \left( 3ab(a+b) \text{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \\
 & \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( 2 \left( (a-b) \text{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right.\right. \right. \\
 & \quad \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + 2(a+b) \text{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \right.\right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right) \\
 & \tan\left[\frac{1}{2}(c+dx)\right] + 9(a+b) \left( \frac{1}{9(a+b)} (a-b) \text{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \right.\right. \\
 & \quad \left. \left. \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \quad \left. \tan\left[\frac{1}{2}(c+dx)\right] + \frac{2}{9} \text{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right.\right. \\
 & \quad \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) + 2
 \end{aligned}$$

$$\begin{aligned}
 & \left( \tan\left[\frac{1}{2}(c+dx)\right]^2 \left( (a-b) \left( \frac{1}{5(a+b)} 4(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{7}{3}, \frac{7}{2}, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \right. \\
 & \quad \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right] + \frac{2}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{4}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) + \\
 & 2(a+b) \left( \frac{1}{5(a+b)} (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{4}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \quad \left. \operatorname{AppellF1}\left[\frac{5}{2}, \frac{8}{3}, \frac{1}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right. \\
 & \quad \left. \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) \right) \Big/ \\
 & \left( \left( 9(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \right. \\
 & \quad \left. 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + 2(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \right. \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \\
 & \left( a \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Big) - \\
 & \left( 5a^2(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right. \\
 & \quad \left. \tan\left[\frac{1}{2}(c+dx)\right]^2 \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \\
 & \left( 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \right. \\
 & \quad \left. \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) \Big/
 \end{aligned}$$

$$\begin{aligned}
 & 2(a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \quad \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + 15 \\
 & (a+b) \left( \frac{1}{5(a+b)} (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \quad \left. \frac{2}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + 2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \left( (a-b) \left( \frac{1}{21(a+b)} 20(a-b) \operatorname{AppellF1}\left[\frac{7}{2}, \frac{2}{3}, \frac{7}{3}, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \quad \left. \frac{10}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{5}{3}, \frac{4}{3}, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + 2(a+b) \\
 & \left( \frac{1}{21(a+b)} 5(a-b) \operatorname{AppellF1}\left[\frac{7}{2}, \frac{5}{3}, \frac{4}{3}, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \quad \left. \frac{25}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{8}{3}, \frac{1}{3}, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \Bigg) \Bigg) \Bigg) \Bigg) / \\
 & \left( \left( 15(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \right. \\
 & \quad \left. \left. 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} + 2(a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \Bigg)^2 \\
 & \left( a \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) + \\
 & \left( 5ab(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right. \\
 & \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right. \\
 & \left. \left( 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) + \right. \right. \\
 & \left. \left. 2(a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + 15 \right. \\
 & (a+b) \left( \frac{1}{5(a+b)} (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \left. \frac{2}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right. \\
 & \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \right) + 2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \left( (a-b) \left( \frac{1}{21(a+b)} 20(a-b) \operatorname{AppellF1}\left[\frac{7}{2}, \frac{2}{3}, \frac{7}{3}, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \left. \frac{10}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{5}{3}, \frac{4}{3}, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right. \\
 & \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \right) + 2(a+b)
 \end{aligned}$$





Result (type 6, 10665 leaves):

$$\frac{3 (b + a \cos [c + d x]) \tan [c + d x]}{2 b d (a + b \sec [c + d x])^{1/3}} -$$

$$\left( (b + 3 a \cos [c + d x]) \left( 3 (b + a \cos [c + d x])^{2/3} \sqrt{1 - \cos [c + d x]^2} \sec [c + d x]^{2/3} - \right. \right.$$

$$\left. \left. 6 (a^2 - b^2) (a + b \sec [c + d x]) \left( 1 - \sqrt{\frac{1}{b^2}} b \sec [c + d x] \right) \right) \right)$$

$$\left( 1 + \sqrt{\frac{1}{b^2}} b \sec [c + d x] \right) \left( - \left( \left( 25 a \operatorname{AppellF1} \left[ \frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, \right. \right. \right. \right.$$

$$\left. \left. \left. - \frac{a + b \sec [c + d x]}{-a + \sqrt{\frac{1}{b^2}}}, \frac{a + b \sec [c + d x]}{a + \sqrt{\frac{1}{b^2}}} \right] \right) / (a + b \sec [c + d x]) \right)$$

$$\left( - \frac{1}{\sqrt{\frac{1}{b^2}}} 3 \left( \left( -1 + a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1} \left[ \frac{5}{3}, \frac{1}{2}, \frac{3}{2}, \frac{8}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \sec [c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}} \right], \right. \right.$$

$$\left. \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \sec [c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right) + \left( 1 + a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1} \left[ \frac{5}{3}, \frac{3}{2}, \frac{1}{2}, \right. \right.$$

$$\left. \left. \frac{8}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \sec [c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \frac{\sqrt{\frac{1}{b^2}} (a + b \sec [c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] \right) -$$

$$\left( \left( \left( \left( \left( 10 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}}{-1 + a \sqrt{\frac{1}{b^2}}} \right. \right. \right. \right. \right. \right. \right.$$

$$\left. \left. \left. \left. \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}}{1 + a \sqrt{\frac{1}{b^2}}} \right] \right) / (a + b \operatorname{Sec}[c + d x]) \right) \right) \right) \right) +$$

$$\left( 16 \operatorname{AppellF1} \left[ \frac{5}{3}, \frac{1}{2}, \frac{1}{2}, \frac{8}{3}, -\frac{a + b \operatorname{Sec}[c + d x]}{-a + \frac{1}{\sqrt{\frac{1}{b^2}}}}, \frac{a + b \operatorname{Sec}[c + d x]}{a + \frac{1}{\sqrt{\frac{1}{b^2}}}} \right] \right) /$$

$$\left( -\frac{1}{\sqrt{\frac{1}{b^2}}} 3 \left( \left( -1 + a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1} \left[ \frac{8}{3}, \frac{1}{2}, \frac{3}{2}, \frac{11}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}}{-1 + a \sqrt{\frac{1}{b^2}}} \right. \right. \right.$$

$$\left. \left. \left. \left. \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}}{1 + a \sqrt{\frac{1}{b^2}}} \right] + \left( 1 + a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1} \left[ \frac{8}{3}, \frac{3}{2}, \frac{1}{2}, \right. \right. \right.$$

$$\left. \left. \left. \left. \left. \frac{11}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}}{-1 + a \sqrt{\frac{1}{b^2}}}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}}{1 + a \sqrt{\frac{1}{b^2}}} \right] \right) - \right.$$

$$\left( 16 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{5}{3}, \frac{1}{2}, \frac{1}{2}, \frac{8}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}}{-1 + a \sqrt{\frac{1}{b^2}}} \right. \right.$$

$$\left. \left. \left. \left. \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}}{1 + a \sqrt{\frac{1}{b^2}}} \right] \right) / (a + b \operatorname{Sec}[c + d x]) \right) \right) \right) \right) /$$

$$\left( 5 b (b + a \cos [c + d x])^{1/3} \sqrt{1 - \cos [c + d x]^2} \sec [c + d x]^{4/3} (-1 + \sec [c + d x]^2) \right) \Bigg) \Bigg) /$$

$$\left( 2 b d (a + b \sec [c + d x])^{1/3} \left( \frac{3 (b + a \cos [c + d x])^{2/3} \sin [c + d x]}{\sqrt{1 - \cos [c + d x]^2} \sec [c + d x]^{1/3}} - \right. \right.$$

$$\left. \frac{2 a \sqrt{1 - \cos [c + d x]^2} \sec [c + d x]^{2/3} \sin [c + d x]}{(b + a \cos [c + d x])^{1/3}} + \right.$$

$$\left. \frac{2}{(b + a \cos [c + d x])^{2/3} \sqrt{1 - \cos [c + d x]^2} \sec [c + d x]^{5/3} \sin [c + d x]} + \right.$$

$$\left. \left( \frac{1}{(5 b (b + a \cos [c + d x])^{1/3} \sqrt{1 - \cos [c + d x]^2} (-1 + \sec [c + d x]^2)^2)} \right) \right)$$

$$12 (a^2 - b^2) \sec [c + d x]^{5/3} (a + b \sec [c + d x])$$

$$\left( 1 - \sqrt{\frac{1}{b^2}} b \sec [c + d x] \right) \left( 1 + \sqrt{\frac{1}{b^2}} b \sec [c + d x] \right)$$

$$\left( - \left( \left( 25 a \operatorname{AppellF1} \left[ \frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, -\frac{a + b \sec [c + d x]}{-a + \frac{1}{\sqrt{\frac{1}{b^2}}}}, \frac{a + b \sec [c + d x]}{a + \frac{1}{\sqrt{\frac{1}{b^2}}}} \right] \right) \right) \right) /$$

$$\left( (a + b \sec [c + d x]) \right)$$

$$\left( -\frac{1}{\sqrt{\frac{1}{b^2}}} 3 \left( \left( -1 + a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1} \left[ \frac{5}{3}, \frac{1}{2}, \frac{3}{2}, \frac{8}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \sec [c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}} \right], \right. \right.$$

$$\begin{aligned}
 & \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] + \left( 1 + a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1} \left[ \frac{5}{3}, \frac{3}{2}, \frac{1}{2}, \right. \\
 & \left. \frac{8}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] - \\
 & \left( 10 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \right. \right. \\
 & \left. \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] / (a + b \operatorname{Sec}[c + d x]) \right) + \\
 & \left( 16 \operatorname{AppellF1} \left[ \frac{5}{3}, \frac{1}{2}, \frac{1}{2}, \frac{8}{3}, -\frac{a + b \operatorname{Sec}[c + d x]}{-a + \frac{1}{\sqrt{\frac{1}{b^2}}}}, \frac{a + b \operatorname{Sec}[c + d x]}{a + \frac{1}{\sqrt{\frac{1}{b^2}}}} \right] / \right. \\
 & \left. -\frac{1}{\sqrt{\frac{1}{b^2}}} 3 \left( \left( -1 + a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1} \left[ \frac{8}{3}, \frac{1}{2}, \frac{3}{2}, \frac{11}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \right. \right. \right. \\
 & \left. \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] + \left( 1 + a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1} \left[ \frac{8}{3}, \frac{3}{2}, \frac{1}{2}, \right. \right. \\
 & \left. \left. \frac{11}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] \right) -
 \end{aligned}$$

$$\left( \left( 16 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{5}{3}, \frac{1}{2}, \frac{1}{2}, \frac{8}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}} \right], \right. \right.$$

$$\left. \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] / (a + b \operatorname{Sec}[c + d x]) \right) \operatorname{Sin}[c + d x] -$$

$$\left( 1 / \left( 5 (b + a \operatorname{Cos}[c + d x])^{1/3} \sqrt{1 - \operatorname{Cos}[c + d x]^2} (-1 + \operatorname{Sec}[c + d x]^2) \right) \right)$$

$$6 \sqrt{\frac{1}{b^2}} (a^2 - b^2) \operatorname{Sec}[c + d x]^{2/3}$$

$$(a + b \operatorname{Sec}[c + d x]) \left( 1 - \sqrt{\frac{1}{b^2}} b \operatorname{Sec}[c + d x] \right)$$

$$- \left( \left( 25 a \operatorname{AppellF1} \left[ \frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, -\frac{a + b \operatorname{Sec}[c + d x]}{-a + \frac{1}{\sqrt{\frac{1}{b^2}}}}, \frac{a + b \operatorname{Sec}[c + d x]}{a + \frac{1}{\sqrt{\frac{1}{b^2}}}} \right] / \right. \right.$$

$$\left. \left. (a + b \operatorname{Sec}[c + d x]) \right) \right)$$

$$\left( -\frac{1}{\sqrt{\frac{1}{b^2}}} 3 \left( \left( -1 + a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1} \left[ \frac{5}{3}, \frac{1}{2}, \frac{3}{2}, \frac{8}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}} \right], \right. \right.$$

$$\left. \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] + \left( 1 + a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1} \left[ \frac{5}{3}, \frac{3}{2}, \frac{1}{2}, \right. \right.$$

$$\begin{aligned}
 & \left. \frac{8}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] - \\
 & \left( 10 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \right. \right. \\
 & \left. \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] / (a + b \operatorname{Sec}[c + d x]) \right) + \\
 & \left( 16 \operatorname{AppellF1} \left[ \frac{5}{3}, \frac{1}{2}, \frac{1}{2}, \frac{8}{3}, -\frac{a + b \operatorname{Sec}[c + d x]}{-a + \frac{1}{\sqrt{\frac{1}{b^2}}}}, \frac{a + b \operatorname{Sec}[c + d x]}{a + \frac{1}{\sqrt{\frac{1}{b^2}}}} \right] / \right. \\
 & \left. -\frac{1}{\sqrt{\frac{1}{b^2}}} 3 \left( \left( -1 + a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1} \left[ \frac{8}{3}, \frac{1}{2}, \frac{3}{2}, \frac{11}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \right. \right. \right. \\
 & \left. \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] + \left( 1 + a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1} \left[ \frac{8}{3}, \frac{3}{2}, \frac{1}{2}, \right. \right. \\
 & \left. \left. \frac{11}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] \right) - \\
 & \left( 16 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{5}{3}, \frac{1}{2}, \frac{1}{2}, \frac{8}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \right. \right.
 \end{aligned}$$

$$\left. \left. \left. \left. \frac{\sqrt{\frac{1}{b^2} (a + b \operatorname{Sec}[c + d x])}}{1 + a \sqrt{\frac{1}{b^2}}} \right) / (a + b \operatorname{Sec}[c + d x]) \right) \right) \operatorname{Sin}[c + d x] + \right.$$

$$\left. \left( \frac{1}{5 (b + a \operatorname{Cos}[c + d x])^{1/3} \sqrt{1 - \operatorname{Cos}[c + d x]^2} (-1 + \operatorname{Sec}[c + d x]^2)} \right) \right)$$

$$6 \sqrt{\frac{1}{b^2} (a^2 - b^2)}$$

$$\operatorname{Sec}[c + d x]^{2/3} (a + b \operatorname{Sec}[c + d x])$$

$$\left( 1 + \sqrt{\frac{1}{b^2} b \operatorname{Sec}[c + d x]} \right)$$

$$\left( - \left( \left( \left( 25 a \operatorname{AppellF1} \left[ \frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, -\frac{a + b \operatorname{Sec}[c + d x]}{-a + \sqrt{\frac{1}{b^2}}}, \frac{a + b \operatorname{Sec}[c + d x]}{a + \sqrt{\frac{1}{b^2}}} \right] \right) / \right. \right. \right.$$

$$\left. \left. \left( a + b \operatorname{Sec}[c + d x] \right) \right. \right.$$

$$\left. \left. \left( -\frac{1}{\sqrt{\frac{1}{b^2}}} 3 \left( \left( -1 + a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1} \left[ \frac{5}{3}, \frac{1}{2}, \frac{3}{2}, \frac{8}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}} \right], \right. \right. \right.$$

$$\left. \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right) + \left( 1 + a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1} \left[ \frac{5}{3}, \frac{3}{2}, \frac{1}{2}, \right. \right.$$

$$\left. \left. \frac{8}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] \right) -$$



$$\begin{aligned}
 & \left( 10 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \right. \right. \\
 & \quad \left. \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] / (a + b \operatorname{Sec}[c + d x]) \right) + \\
 & \left( 16 \operatorname{AppellF1} \left[ \frac{5}{3}, \frac{1}{2}, \frac{1}{2}, \frac{8}{3}, -\frac{a + b \operatorname{Sec}[c + d x]}{-a + \frac{1}{\sqrt{\frac{1}{b^2}}}}, \frac{a + b \operatorname{Sec}[c + d x]}{a + \frac{1}{\sqrt{\frac{1}{b^2}}}} \right] / \right. \\
 & \left. - \frac{1}{\sqrt{\frac{1}{b^2}}} 3 \left( \left( -1 + a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1} \left[ \frac{8}{3}, \frac{1}{2}, \frac{3}{2}, \frac{11}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \right. \right. \right. \\
 & \quad \left. \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] + \left( 1 + a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1} \left[ \frac{8}{3}, \frac{3}{2}, \frac{1}{2}, \right. \right. \\
 & \quad \left. \left. \frac{11}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] - \right. \\
 & \left. \left( 16 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{5}{3}, \frac{1}{2}, \frac{1}{2}, \frac{8}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \right. \right. \right. \\
 & \quad \left. \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] / (a + b \operatorname{Sec}[c + d x]) \right) \operatorname{Sin}[c + d x] - \\
 & \left. \left( 1 / \left( 5 (b + a \operatorname{Cos}[c + d x])^{1/3} \sqrt{1 - \operatorname{Cos}[c + d x]^2} (-1 + \operatorname{Sec}[c + d x]^2) \right) \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & 6 (a^2 - b^2) \operatorname{Sec}[c + d x]^{2/3} \\
 & \left( 1 - \sqrt{\frac{1}{b^2}} b \operatorname{Sec}[c + d x] \right) \\
 & \left( 1 + \sqrt{\frac{1}{b^2}} b \operatorname{Sec}[c + d x] \right) \\
 & \left( - \left( \left( 25 a \operatorname{AppellF1} \left[ \frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, -\frac{a + b \operatorname{Sec}[c + d x]}{-a + \sqrt{\frac{1}{b^2}}}, \frac{a + b \operatorname{Sec}[c + d x]}{a + \sqrt{\frac{1}{b^2}}} \right] \right) \right) \right) \\
 & \left( (a + b \operatorname{Sec}[c + d x]) \right) \\
 & \left( -\frac{1}{\sqrt{\frac{1}{b^2}}} 3 \left( \left( -1 + a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1} \left[ \frac{5}{3}, \frac{1}{2}, \frac{3}{2}, \frac{8}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}} \right], \right. \right. \\
 & \left. \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right) + \left( 1 + a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1} \left[ \frac{5}{3}, \frac{3}{2}, \frac{1}{2}, \right. \right. \\
 & \left. \left. \frac{8}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] \right) - \\
 & \left( 10 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}} \right], \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left. \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] / (a + b \operatorname{Sec}[c + d x]) \right) \right) + \\
 & \left( 16 \operatorname{AppellF1} \left[ \frac{5}{3}, \frac{1}{2}, \frac{1}{2}, \frac{8}{3}, -\frac{a + b \operatorname{Sec}[c + d x]}{-a + \sqrt{\frac{1}{b^2}}}, \frac{a + b \operatorname{Sec}[c + d x]}{a + \sqrt{\frac{1}{b^2}}} \right] / \right. \\
 & \left. \left( -\frac{1}{\sqrt{\frac{1}{b^2}}} 3 \left( \left( -1 + a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1} \left[ \frac{8}{3}, \frac{1}{2}, \frac{3}{2}, \frac{11}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \right. \right. \right. \\
 & \left. \left. \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] + \left( 1 + a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1} \left[ \frac{8}{3}, \frac{3}{2}, \frac{1}{2}, \right. \right. \right. \\
 & \left. \left. \left. \frac{11}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] - \right. \right. \\
 & \left. \left. \left( 16 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{5}{3}, \frac{1}{2}, \frac{1}{2}, \frac{8}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \right. \right. \right. \\
 & \left. \left. \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] / (a + b \operatorname{Sec}[c + d x]) \right) \right) \right) \operatorname{Sin}[c + d x] + \\
 & \left( 6 (a^2 - b^2) (a + b \operatorname{Sec}[c + d x]) \left( 1 - \sqrt{\frac{1}{b^2}} b \operatorname{Sec}[c + d x] \right) \left( 1 + \sqrt{\frac{1}{b^2}} b \operatorname{Sec}[c + d x] \right) \right)
 \end{aligned}$$

$$\left( \left( \left( \left( 25 a \operatorname{AppellF1} \left[ \frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, -\frac{a+b \operatorname{Sec}[c+d x]}{-a+\sqrt{\frac{1}{b^2}}}, \frac{a+b \operatorname{Sec}[c+d x]}{a+\sqrt{\frac{1}{b^2}}} \right] \right) \right) \right) \right) /$$

$$\left( (a+b \operatorname{Sec}[c+d x]) \right)$$

$$\left( -\frac{1}{\sqrt{\frac{1}{b^2}}} 3 \left( \left( -1+a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1} \left[ \frac{5}{3}, \frac{1}{2}, \frac{3}{2}, \frac{8}{3}, \frac{\sqrt{\frac{1}{b^2}} (a+b \operatorname{Sec}[c+d x])}{-1+a \sqrt{\frac{1}{b^2}}} \right], \right. \right.$$

$$\left. \left. \frac{\sqrt{\frac{1}{b^2}} (a+b \operatorname{Sec}[c+d x])}{1+a \sqrt{\frac{1}{b^2}}} \right) + \left( 1+a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1} \left[ \frac{5}{3}, \frac{3}{2}, \frac{1}{2}, \right. \right.$$

$$\left. \left. \frac{8}{3}, \frac{\sqrt{\frac{1}{b^2}} (a+b \operatorname{Sec}[c+d x])}{-1+a \sqrt{\frac{1}{b^2}}}, \frac{\sqrt{\frac{1}{b^2}} (a+b \operatorname{Sec}[c+d x])}{1+a \sqrt{\frac{1}{b^2}}} \right] \right) -$$

$$\left( 10 (a^2-b^2) \operatorname{AppellF1} \left[ \frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, \frac{\sqrt{\frac{1}{b^2}} (a+b \operatorname{Sec}[c+d x])}{-1+a \sqrt{\frac{1}{b^2}}} \right], \right.$$

$$\left. \left. \frac{\sqrt{\frac{1}{b^2}} (a+b \operatorname{Sec}[c+d x])}{1+a \sqrt{\frac{1}{b^2}}} \right] \right) / (a+b \operatorname{Sec}[c+d x]) \left. \right) \left. \right) +$$

$$\left( 16 \operatorname{AppellF1} \left[ \frac{5}{3}, \frac{1}{2}, \frac{1}{2}, \frac{8}{3}, -\frac{a+b \operatorname{Sec}[c+d x]}{-a+\sqrt{\frac{1}{b^2}}}, \frac{a+b \operatorname{Sec}[c+d x]}{a+\sqrt{\frac{1}{b^2}}} \right] \right) /$$

$$\begin{aligned}
 & \left( -\frac{1}{\sqrt{\frac{1}{b^2}}} 3 \left( \left( -1 + a \sqrt{\frac{1}{b^2}} \right) \text{AppellF1} \left[ \frac{8}{3}, \frac{1}{2}, \frac{3}{2}, \frac{11}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \text{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \right. \right. \right. \\
 & \left. \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \text{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] + \left( 1 + a \sqrt{\frac{1}{b^2}} \right) \text{AppellF1} \left[ \frac{8}{3}, \frac{3}{2}, \frac{1}{2}, \right. \right. \\
 & \left. \left. \frac{11}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \text{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \frac{\sqrt{\frac{1}{b^2}} (a + b \text{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] \right) - \\
 & \left( \left( 16 (a^2 - b^2) \text{AppellF1} \left[ \frac{5}{3}, \frac{1}{2}, \frac{1}{2}, \frac{8}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \text{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \right. \right. \right. \\
 & \left. \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \text{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] \right) / (a + b \text{Sec}[c + d x]) \right) \left. \right) \text{Sin}[c + d x] \left. \right) / \\
 & \left( 5 b (b + a \text{Cos}[c + d x])^{1/3} (1 - \text{Cos}[c + d x])^{3/2} \text{Sec}[c + d x]^{7/3} \right. \\
 & \left. (-1 + \text{Sec}[c + d x]^2) \right) - \\
 & \left( 2 a (a^2 - b^2) (a + b \text{Sec}[c + d x]) \left( 1 - \sqrt{\frac{1}{b^2}} b \text{Sec}[c + d x] \right) \right. \\
 & \left. \left( 1 + \sqrt{\frac{1}{b^2}} b \text{Sec}[c + d x] \right) \right) \\
 & \left( - \left( \left( 25 a \text{AppellF1} \left[ \frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, -\frac{a + b \text{Sec}[c + d x]}{-a + \frac{1}{\sqrt{\frac{1}{b^2}}}}, \frac{a + b \text{Sec}[c + d x]}{a + \frac{1}{\sqrt{\frac{1}{b^2}}}} \right] \right) / \right. \right.
 \end{aligned}$$

$$\left( (a + b \operatorname{Sec}[c + d x]) \right.$$

$$\left. \left( -\frac{1}{\sqrt{\frac{1}{b^2}}} 3 \left( \left( -1 + a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1} \left[ \frac{5}{3}, \frac{1}{2}, \frac{3}{2}, \frac{8}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}} \right], \right. \right. \right.$$

$$\left. \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right) + \left( 1 + a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1} \left[ \frac{5}{3}, \frac{3}{2}, \frac{1}{2}, \right. \right.$$

$$\left. \left. \frac{8}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] \right) -$$

$$\left( 10 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}} \right], \right.$$

$$\left. \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] \right) / (a + b \operatorname{Sec}[c + d x]) \left. \right) +$$

$$\left( 16 \operatorname{AppellF1} \left[ \frac{5}{3}, \frac{1}{2}, \frac{1}{2}, \frac{8}{3}, -\frac{a + b \operatorname{Sec}[c + d x]}{-a + \frac{1}{\sqrt{\frac{1}{b^2}}}}, \frac{a + b \operatorname{Sec}[c + d x]}{a + \frac{1}{\sqrt{\frac{1}{b^2}}}} \right] \right) /$$

$$\left( -\frac{1}{\sqrt{\frac{1}{b^2}}} 3 \left( \left( -1 + a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1} \left[ \frac{8}{3}, \frac{1}{2}, \frac{3}{2}, \frac{11}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}} \right], \right. \right.$$

$$\begin{aligned}
 & \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] + \left( 1 + a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1}\left[\frac{8}{3}, \frac{3}{2}, \frac{1}{2}, \right. \\
 & \left. \frac{11}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] - \\
 & \left( 16 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{5}{3}, \frac{1}{2}, \frac{1}{2}, \frac{8}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \right. \right. \\
 & \left. \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] / (a + b \operatorname{Sec}[c + d x]) \right) \operatorname{Sin}[c + d x] / \\
 & \left( 5 b (b + a \operatorname{Cos}[c + d x])^{4/3} \sqrt{1 - \operatorname{Cos}[c + d x]^2} \operatorname{Sec}[c + d x]^{4/3} (-1 + \operatorname{Sec}[c + d x]^2) \right) + \\
 & \left( 8 (a^2 - b^2) (a + b \operatorname{Sec}[c + d x]) \left( 1 - \sqrt{\frac{1}{b^2}} b \operatorname{Sec}[c + d x] \right) \right. \\
 & \left. \left( 1 + \sqrt{\frac{1}{b^2}} b \operatorname{Sec}[c + d x] \right) \right. \\
 & \left. - \left( \left( \left( 25 a \operatorname{AppellF1}\left[\frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, -\frac{a + b \operatorname{Sec}[c + d x]}{-a + \frac{1}{\sqrt{\frac{1}{b^2}}}}, \frac{a + b \operatorname{Sec}[c + d x]}{a + \frac{1}{\sqrt{\frac{1}{b^2}}}} \right] / \right. \right. \right. \right. \\
 & \left. \left. \left( a + b \operatorname{Sec}[c + d x] \right) \right) \right)
 \end{aligned}$$

$$\left( -\frac{1}{\sqrt{\frac{1}{b^2}}} 3 \left( \left( -1 + a \sqrt{\frac{1}{b^2}} \right) \text{AppellF1} \left[ \frac{5}{3}, \frac{1}{2}, \frac{3}{2}, \frac{8}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \text{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}} \right], \right. \right.$$

$$\left. \frac{\sqrt{\frac{1}{b^2}} (a + b \text{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right) + \left( 1 + a \sqrt{\frac{1}{b^2}} \right) \text{AppellF1} \left[ \frac{5}{3}, \frac{3}{2}, \frac{1}{2}, \right.$$

$$\left. \frac{8}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \text{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \frac{\sqrt{\frac{1}{b^2}} (a + b \text{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] -$$

$$\left( 10 (a^2 - b^2) \text{AppellF1} \left[ \frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \text{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}} \right], \right.$$

$$\left. \frac{\sqrt{\frac{1}{b^2}} (a + b \text{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] / (a + b \text{Sec}[c + d x]) \Bigg) +$$

$$\left( 16 \text{AppellF1} \left[ \frac{5}{3}, \frac{1}{2}, \frac{1}{2}, \frac{8}{3}, -\frac{a + b \text{Sec}[c + d x]}{-a + \frac{1}{\sqrt{\frac{1}{b^2}}}}, \frac{a + b \text{Sec}[c + d x]}{a + \frac{1}{\sqrt{\frac{1}{b^2}}}} \right] / \right.$$

$$\left. -\frac{1}{\sqrt{\frac{1}{b^2}}} 3 \left( \left( -1 + a \sqrt{\frac{1}{b^2}} \right) \text{AppellF1} \left[ \frac{8}{3}, \frac{1}{2}, \frac{3}{2}, \frac{11}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \text{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}} \right], \right. \right.$$

$$\left. \frac{\sqrt{\frac{1}{b^2}} (a + b \text{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right) + \left( 1 + a \sqrt{\frac{1}{b^2}} \right) \text{AppellF1} \left[ \frac{8}{3}, \frac{3}{2}, \frac{1}{2}, \right.$$



$$\left. \frac{11}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] -$$

$$\left( 16 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{5}{3}, \frac{1}{2}, \frac{1}{2}, \frac{8}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \right. \right.$$

$$\left. \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] / (a + b \operatorname{Sec}[c + d x]) \right) \operatorname{Sin}[c + d x] /$$

$$\left( 5 b (b + a \operatorname{Cos}[c + d x])^{1/3} \sqrt{1 - \operatorname{Cos}[c + d x]^2} \operatorname{Sec}[c + d x]^{1/3} (-1 + \operatorname{Sec}[c + d x]^2) \right) -$$

$$\left( 6 (a^2 - b^2) (a + b \operatorname{Sec}[c + d x]) \left( 1 - \sqrt{\frac{1}{b^2}} b \operatorname{Sec}[c + d x] \right) \right.$$

$$\left. \left( 1 + \sqrt{\frac{1}{b^2}} b \operatorname{Sec}[c + d x] \right) \right.$$

$$\left( 25 a b \operatorname{AppellF1} \left[ \frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, -\frac{a + b \operatorname{Sec}[c + d x]}{-a + \frac{1}{\sqrt{\frac{1}{b^2}}}}, \frac{a + b \operatorname{Sec}[c + d x]}{a + \frac{1}{\sqrt{\frac{1}{b^2}}}} \right] \right.$$

$$\left. \left. \operatorname{Sec}[c + d x] \operatorname{Tan}[c + d x] \right) / (a + b \operatorname{Sec}[c + d x])^2 \right)$$

$$\left( -\frac{1}{\sqrt{\frac{1}{b^2}}} 3 \left( \left( -1 + a \sqrt{\frac{1}{b^2}} \right) \text{AppellF1} \left[ \frac{5}{3}, \frac{1}{2}, \frac{3}{2}, \frac{8}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \text{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}} \right], \right. \right.$$

$$\left. \frac{\sqrt{\frac{1}{b^2}} (a + b \text{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right) + \left( 1 + a \sqrt{\frac{1}{b^2}} \right) \text{AppellF1} \left[ \frac{5}{3}, \frac{3}{2}, \frac{1}{2}, \right.$$

$$\left. \frac{8}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \text{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \frac{\sqrt{\frac{1}{b^2}} (a + b \text{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] -$$

$$\left( 10 (a^2 - b^2) \text{AppellF1} \left[ \frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \text{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}} \right], \right.$$

$$\left. \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \text{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] / (a + b \text{Sec}[c + d x]) \right) -$$

$$\left( 25 a \left( \frac{1}{5 \left( a + \frac{1}{\sqrt{\frac{1}{b^2}}} \right)} b \text{AppellF1} \left[ \frac{5}{3}, \frac{1}{2}, \frac{3}{2}, \frac{8}{3}, -\frac{a + b \text{Sec}[c + d x]}{-a + \frac{1}{\sqrt{\frac{1}{b^2}}}} \right], \right. \right.$$

$$\left. \frac{a + b \text{Sec}[c + d x]}{a + \frac{1}{\sqrt{\frac{1}{b^2}}}} \right] \text{Sec}[c + d x] \text{Tan}[c + d x] -$$

$$\left( b \text{AppellF1} \left[ \frac{5}{3}, \frac{3}{2}, \frac{1}{2}, \frac{8}{3}, -\frac{a + b \text{Sec}[c + d x]}{-a + \frac{1}{\sqrt{\frac{1}{b^2}}}}, \frac{a + b \text{Sec}[c + d x]}{a + \frac{1}{\sqrt{\frac{1}{b^2}}}} \right] \right)$$



$$\left( 5 b \operatorname{AppellF1} \left[ \frac{8}{3}, \frac{3}{2}, \frac{1}{2}, \frac{11}{3}, -\frac{a+b \operatorname{Sec}[c+d x]}{-a+\sqrt{\frac{1}{b^2}}}, \frac{a+b \operatorname{Sec}[c+d x]}{a+\sqrt{\frac{1}{b^2}}} \right] \right.$$

$$\left. \operatorname{Sec}[c+d x] \operatorname{Tan}[c+d x] \right) / \left( 16 \left( -a+\sqrt{\frac{1}{b^2}} \right) \right)$$

$$\left( -\frac{1}{\sqrt{\frac{1}{b^2}}} 3 \left( \left( -1+a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1} \left[ \frac{8}{3}, \frac{1}{2}, \frac{3}{2}, \frac{11}{3}, \frac{\sqrt{\frac{1}{b^2}} (a+b \operatorname{Sec}[c+d x])}{-1+a \sqrt{\frac{1}{b^2}}}, \right. \right. \right.$$

$$\left. \left. \frac{\sqrt{\frac{1}{b^2}} (a+b \operatorname{Sec}[c+d x])}{1+a \sqrt{\frac{1}{b^2}}} \right] + \left( 1+a \sqrt{\frac{1}{b^2}} \right) \operatorname{AppellF1} \left[ \frac{8}{3}, \frac{3}{2}, \frac{1}{2}, \right. \right.$$

$$\left. \left. \frac{11}{3}, \frac{\sqrt{\frac{1}{b^2}} (a+b \operatorname{Sec}[c+d x])}{-1+a \sqrt{\frac{1}{b^2}}}, \frac{\sqrt{\frac{1}{b^2}} (a+b \operatorname{Sec}[c+d x])}{1+a \sqrt{\frac{1}{b^2}}} \right] - \right.$$

$$\left( 16 (a^2-b^2) \operatorname{AppellF1} \left[ \frac{5}{3}, \frac{1}{2}, \frac{1}{2}, \frac{8}{3}, \frac{\sqrt{\frac{1}{b^2}} (a+b \operatorname{Sec}[c+d x])}{-1+a \sqrt{\frac{1}{b^2}}}, \right. \right.$$

$$\left. \left. \frac{\sqrt{\frac{1}{b^2}} (a+b \operatorname{Sec}[c+d x])}{1+a \sqrt{\frac{1}{b^2}}} \right] / (a+b \operatorname{Sec}[c+d x]) \right) +$$

$$\left( 25 a \operatorname{AppellF1} \left[ \frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, -\frac{a+b \operatorname{Sec}[c+d x]}{-a+\sqrt{\frac{1}{b^2}}}, \frac{a+b \operatorname{Sec}[c+d x]}{a+\sqrt{\frac{1}{b^2}}} \right] \right)$$

$$\left( \left( 10 b (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + dx])}{-1 + a \sqrt{\frac{1}{b^2}}} \right], \right. \right.$$

$$\left. \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + dx])}{1 + a \sqrt{\frac{1}{b^2}}} \right] \operatorname{Sec}[c + dx] \operatorname{Tan}[c + dx] \right) /$$

$$(a + b \operatorname{Sec}[c + dx])^2 - \left( 10 (a^2 - b^2) \left( \left( \sqrt{\frac{1}{b^2}} b \operatorname{AppellF1} \left[ \frac{5}{3}, \frac{1}{2}, \frac{3}{2}, \frac{8}{3}, \right. \right. \right.$$

$$\left. \left. \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + dx])}{-1 + a \sqrt{\frac{1}{b^2}}}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + dx])}{1 + a \sqrt{\frac{1}{b^2}}} \right] \operatorname{Sec}[c + dx] \right. \right.$$

$$\left. \left. \operatorname{Tan}[c + dx] \right) / \left( 5 \left( 1 + a \sqrt{\frac{1}{b^2}} \right) \right) + \left( \sqrt{\frac{1}{b^2}} b \operatorname{AppellF1} \left[ \frac{5}{3}, \frac{3}{2}, \frac{1}{2}, \frac{8}{3}, \right. \right. \right.$$

$$\left. \left. \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + dx])}{-1 + a \sqrt{\frac{1}{b^2}}}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + dx])}{1 + a \sqrt{\frac{1}{b^2}}} \right] \operatorname{Sec}[c + dx] \right. \right.$$

$$\left. \left. \operatorname{Tan}[c + dx] \right) / \left( 5 \left( -1 + a \sqrt{\frac{1}{b^2}} \right) \right) \right) / (a + b \operatorname{Sec}[c + dx]) -$$

$$\frac{1}{\sqrt{\frac{1}{b^2}}} 3 \left( \left( -1 + a \sqrt{\frac{1}{b^2}} \right) \left( \left( 15 \sqrt{\frac{1}{b^2}} b \operatorname{AppellF1} \left[ \frac{8}{3}, \frac{1}{2}, \frac{5}{2}, \frac{11}{3}, \right. \right. \right. \right.$$

$$\left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] \operatorname{Sec}[c + d x]$$

$$\operatorname{Tan}[c + d x] \left/ \left( 16 \left( 1 + a \sqrt{\frac{1}{b^2}} \right) \right) + \left( 5 \sqrt{\frac{1}{b^2}} b \operatorname{AppellF1} \left[ \frac{8}{3}, \right. \right. \right.$$

$$\left. \left. \frac{3}{2}, \frac{3}{2}, \frac{11}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] \right)$$

$$\operatorname{Sec}[c + d x] \operatorname{Tan}[c + d x] \left/ \left( 16 \left( -1 + a \sqrt{\frac{1}{b^2}} \right) \right) + \left( 1 + a \sqrt{\frac{1}{b^2}} \right) \right.$$

$$\left. \left( 5 \sqrt{\frac{1}{b^2}} b \operatorname{AppellF1} \left[ \frac{8}{3}, \frac{3}{2}, \frac{3}{2}, \frac{11}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \right. \right. \right.$$

$$\left. \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] \operatorname{Sec}[c + d x] \operatorname{Tan}[c + d x] \right/$$

$$\left( 16 \left( 1 + a \sqrt{\frac{1}{b^2}} \right) \right) + \left( 15 \sqrt{\frac{1}{b^2}} b \operatorname{AppellF1} \left[ \frac{8}{3}, \frac{5}{2}, \frac{1}{2}, \frac{11}{3}, \right. \right.$$

$$\left. \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] \operatorname{Sec}[c + d x] \right)$$



$$\left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] \operatorname{Sec}[c + d x] \operatorname{Tan}[c + d x] \Big/$$

$$(a + b \operatorname{Sec}[c + d x])^2 - \left( 16 (a^2 - b^2) \left( \left( 5 \sqrt{\frac{1}{b^2}} b \operatorname{AppellF1}\left[\frac{8}{3}, \frac{1}{2}, \frac{3}{2}, \frac{11}{3}\right], \right. \right. \right.$$

$$\left. \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] \operatorname{Sec}[c + d x] \right.$$

$$\left. \operatorname{Tan}[c + d x] \right) \Big/ \left( 16 \left( 1 + a \sqrt{\frac{1}{b^2}} \right) \right) + \left( 5 \sqrt{\frac{1}{b^2}} b \operatorname{AppellF1}\left[\frac{8}{3}, \frac{3}{2}, \right. \right.$$

$$\left. \frac{1}{2}, \frac{11}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] \operatorname{Sec}[$$

$$c + d x] \operatorname{Tan}[c + d x] \Big/ \left( 16 \left( -1 + a \sqrt{\frac{1}{b^2}} \right) \right) \Big/ (a + b \operatorname{Sec}[c + d x]) -$$

$$\frac{1}{\sqrt{\frac{1}{b^2}}} 3 \left( \left( -1 + a \sqrt{\frac{1}{b^2}} \right) \left( \left( 12 \sqrt{\frac{1}{b^2}} b \operatorname{AppellF1}\left[\frac{11}{3}, \frac{1}{2}, \frac{5}{2}, \frac{14}{3}\right], \right. \right. \right.$$

$$\left. \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \frac{\sqrt{\frac{1}{b^2}} (a + b \operatorname{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] \operatorname{Sec}[c + d x] \right)$$





$$\left( -\frac{1}{\sqrt{\frac{1}{b^2}}} 3 \left( \left( -1 + a \sqrt{\frac{1}{b^2}} \right) \text{AppellF1} \left[ \frac{8}{3}, \frac{1}{2}, \frac{3}{2}, \frac{11}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \text{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}} \right], \right. \right.$$

$$\left. \frac{\sqrt{\frac{1}{b^2}} (a + b \text{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right) + \left( 1 + a \sqrt{\frac{1}{b^2}} \right) \text{AppellF1} \left[ \frac{8}{3}, \frac{3}{2}, \frac{1}{2}, \frac{11}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \text{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] -$$

$$\left. \frac{11}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \text{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}}, \frac{\sqrt{\frac{1}{b^2}} (a + b \text{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right) -$$

$$\left( 16 (a^2 - b^2) \text{AppellF1} \left[ \frac{5}{3}, \frac{1}{2}, \frac{1}{2}, \frac{8}{3}, \frac{\sqrt{\frac{1}{b^2}} (a + b \text{Sec}[c + d x])}{-1 + a \sqrt{\frac{1}{b^2}}} \right], \right.$$

$$\left. \left. \left. \left. \frac{\sqrt{\frac{1}{b^2}} (a + b \text{Sec}[c + d x])}{1 + a \sqrt{\frac{1}{b^2}}} \right] / (a + b \text{Sec}[c + d x]) \right)^2 \right) / \right.$$

$$\left. \left. \left. \left. \left( 5 b (b + a \text{Cos}[c + d x]) \right)^{1/3} \sqrt{1 - \text{Cos}[c + d x]^2} \text{Sec}[c + d x]^{4/3} \right. \right. \right.$$

$$\left. \left. \left. \left. \left. (-1 + \text{Sec}[c + d x]^2) \right) \right) \right) \right) \right)$$

**Problem 702: Result more than twice size of optimal antiderivative.**

$$\int \frac{\text{Sec}[c + d x]}{(a + b \text{Sec}[c + d x])^{1/3}} dx$$

Optimal (type 6, 105 leaves, 3 steps):

$$\left( \sqrt{2} \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{1}{3}, \frac{3}{2}, \frac{1}{2} (1 - \operatorname{Sec}[c + dx]), \frac{b(1 - \operatorname{Sec}[c + dx])}{a+b} \right] \right. \\ \left. \left( \frac{a+b \operatorname{Sec}[c + dx]}{a+b} \right)^{1/3} \operatorname{Tan}[c + dx] \right) / \left( d \sqrt{1 + \operatorname{Sec}[c + dx]} (a+b \operatorname{Sec}[c + dx])^{1/3} \right)$$

Result (type 6, 310 leaves):

$$\left( 15 (a-b)^2 (a+b) \operatorname{AppellF1} \left[ \frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, \frac{a+b \operatorname{Sec}[c + dx]}{a-b}, \frac{a+b \operatorname{Sec}[c + dx]}{a+b} \right] \operatorname{Cos}[c + dx] \right. \\ \left. \operatorname{Cot}[c + dx]^3 (1 + \operatorname{Sec}[c + dx]) (b - b \operatorname{Sec}[c + dx]) (a+b \operatorname{Sec}[c + dx])^{2/3} \right) / \left( b^2 (-a+b) d \right. \\ \left. \left( 3 (a-b) \operatorname{AppellF1} \left[ \frac{5}{3}, \frac{1}{2}, \frac{3}{2}, \frac{8}{3}, \frac{a+b \operatorname{Sec}[c + dx]}{a-b}, \frac{a+b \operatorname{Sec}[c + dx]}{a+b} \right] (b+a \operatorname{Cos}[c + dx]) + \right. \right. \\ \left. \left. (a+b) \left( 10 (a-b) \operatorname{AppellF1} \left[ \frac{2}{3}, \frac{1}{2}, \frac{1}{2}, \frac{5}{3}, \frac{a+b \operatorname{Sec}[c + dx]}{a-b}, \frac{a+b \operatorname{Sec}[c + dx]}{a+b} \right] \operatorname{Cos}[c + dx] + \right. \right. \right. \\ \left. \left. \left. 3 \operatorname{AppellF1} \left[ \frac{5}{3}, \frac{3}{2}, \frac{1}{2}, \frac{8}{3}, \frac{a+b \operatorname{Sec}[c + dx]}{a-b}, \frac{a+b \operatorname{Sec}[c + dx]}{a+b} \right] (b+a \operatorname{Cos}[c + dx]) \right) \right) \right)$$

**Problem 704: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec}[c + dx]}{(a+b \operatorname{Sec}[c + dx])^{2/3}} dx$$

Optimal (type 6, 105 leaves, 3 steps):

$$\left( \sqrt{2} \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{2}{3}, \frac{3}{2}, \frac{1}{2} (1 - \operatorname{Sec}[c + dx]), \frac{b(1 - \operatorname{Sec}[c + dx])}{a+b} \right] \right. \\ \left. \left( \frac{a+b \operatorname{Sec}[c + dx]}{a+b} \right)^{2/3} \operatorname{Tan}[c + dx] \right) / \left( d \sqrt{1 + \operatorname{Sec}[c + dx]} (a+b \operatorname{Sec}[c + dx])^{2/3} \right)$$

Result (type 6, 310 leaves):

$$\left( 24 (a-b)^2 (a+b) \operatorname{AppellF1} \left[ \frac{1}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4}{3}, \frac{a+b \operatorname{Sec}[c + dx]}{a-b}, \frac{a+b \operatorname{Sec}[c + dx]}{a+b} \right] \operatorname{Cos}[c + dx] \right. \\ \left. \operatorname{Cot}[c + dx]^3 (1 + \operatorname{Sec}[c + dx]) (b - b \operatorname{Sec}[c + dx]) (a+b \operatorname{Sec}[c + dx])^{1/3} \right) / \left( b^2 (-a+b) d \right. \\ \left. \left( 3 (a-b) \operatorname{AppellF1} \left[ \frac{4}{3}, \frac{1}{2}, \frac{3}{2}, \frac{7}{3}, \frac{a+b \operatorname{Sec}[c + dx]}{a-b}, \frac{a+b \operatorname{Sec}[c + dx]}{a+b} \right] (b+a \operatorname{Cos}[c + dx]) + \right. \right. \\ \left. \left. (a+b) \left( 8 (a-b) \operatorname{AppellF1} \left[ \frac{1}{3}, \frac{1}{2}, \frac{1}{2}, \frac{4}{3}, \frac{a+b \operatorname{Sec}[c + dx]}{a-b}, \frac{a+b \operatorname{Sec}[c + dx]}{a+b} \right] \operatorname{Cos}[c + dx] + \right. \right. \right. \\ \left. \left. \left. 3 \operatorname{AppellF1} \left[ \frac{4}{3}, \frac{3}{2}, \frac{1}{2}, \frac{7}{3}, \frac{a+b \operatorname{Sec}[c + dx]}{a-b}, \frac{a+b \operatorname{Sec}[c + dx]}{a+b} \right] (b+a \operatorname{Cos}[c + dx]) \right) \right) \right)$$

**Problem 706: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec}[c + dx]}{(a+b \operatorname{Sec}[c + dx])^{4/3}} dx$$

Optimal (type 6, 110 leaves, 3 steps):

$$\left( \sqrt{2} \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2}, \frac{4}{3}, \frac{3}{2}, \frac{1}{2} (1 - \operatorname{Sec}[c + dx]), \frac{b(1 - \operatorname{Sec}[c + dx])}{a + b} \right] \right. \\ \left. \left( \frac{a + b \operatorname{Sec}[c + dx]}{a + b} \right)^{1/3} \operatorname{Tan}[c + dx] \right) / \left( (a + b) d \sqrt{1 + \operatorname{Sec}[c + dx]} (a + b \operatorname{Sec}[c + dx])^{1/3} \right)$$

Result (type 6, 12814 leaves):

$$\frac{(b + a \operatorname{Cos}[c + dx])^2 \operatorname{Sec}[c + dx]^2 \left( -\frac{3 \operatorname{Sin}[c + dx]}{-a^2 + b^2} + \frac{3 b \operatorname{Sin}[c + dx]}{(-a^2 + b^2)(b + a \operatorname{Cos}[c + dx])} \right)}{d (a + b \operatorname{Sec}[c + dx])^{4/3}} +$$

$$\left( (b + a \operatorname{Cos}[c + dx])^{4/3} \left( \frac{b}{(-a^2 + b^2)(b + a \operatorname{Cos}[c + dx])^{1/3} \operatorname{Sec}[c + dx]^{1/3}} + \right. \right.$$

$$\left. \frac{a \operatorname{Sec}[c + dx]^{2/3}}{2(-a^2 + b^2)(b + a \operatorname{Cos}[c + dx])^{1/3}} + \frac{3 a \operatorname{Cos}[2(c + dx)] \operatorname{Sec}[c + dx]^{2/3}}{2(-a^2 + b^2)(b + a \operatorname{Cos}[c + dx])^{1/3}} \right) \operatorname{Sec}[c + dx]^{4/3}$$

$$\left( -\frac{3 \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right] \left( \frac{a + b - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2} \right)^{2/3}}{(a^2 - b^2) \left( \frac{1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2}{1 - \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2} \right)^{1/3}} + \left( 3(a - b)(a + b) \right. \right.$$

$$\left. \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2 \right)^{2/3} \left( \frac{a + b - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2} \right)^{2/3} \right)$$

$$\left( 10 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2, \frac{(a - b) \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2}{a + b} \right] \right.$$

$$\left. \left( (a - b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2, \frac{(a - b) \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2}{a + b} \right] + \right. \right.$$

$$\left. \left. 2(a + b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2, \frac{(a - b) \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2}{a + b} \right] \right) \right)$$

$$\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^5 + 3 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2, \right.$$

$$\left. \frac{(a - b) \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2}{a + b} \right] \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right] \left( -2 \left( (a - b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, \right. \right. \right.$$

$$\left. \left. \frac{4}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2, \frac{(a - b) \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2}{a + b} \right] + 2(a + b) \right)$$

$$\begin{aligned}
 & \left. \left. \left. \left. \left. \text{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right]\right) \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2 + 15(a+b)\text{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)\right)\right)\right)\right) / \\
 & \left( (a^2 - b^2) \left( \frac{1}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^{1/3} \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \right. \\
 & \left( 9(a+b)\text{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & 2 \left( (a-b)\text{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & 2(a+b)\text{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \left. \left. \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right. \\
 & \left( 15(a+b)\text{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & 2 \left( (a-b)\text{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & \left. \left. \left. \left. 2(a+b)\text{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \right) \right) \\
 & \left. \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( a \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) - b \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \right) \right)\right)\right) / \\
 & \left( d(a+b \sec[c+dx])^{4/3} \left( - \frac{3 \sec\left[\frac{1}{2}(c+dx)\right]^2 \left( \frac{a+b-a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^{2/3}}{2(a^2 - b^2) \left( \frac{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^{1/3}} + \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( \tan\left[\frac{1}{2}(c+dx)\right] \left( \frac{a+b-a\tan\left[\frac{1}{2}(c+dx)\right]^2+b\tan\left[\frac{1}{2}(c+dx)\right]^2}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^{2/3} \right. \\
 & \left. \left( \frac{\sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]}{1-\tan\left[\frac{1}{2}(c+dx)\right]^2} + \left( \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right. \right. \right. \\
 & \left. \left. \left. \left( 1+\tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) / \left( 1-\tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \right) \right) / \\
 & \left( (a^2-b^2) \left( \frac{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}{1-\tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^{4/3} \right) - \left( 2 \tan\left[\frac{1}{2}(c+dx)\right] \right. \\
 & \left. \left( \left( -a \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + b \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) / \right. \right. \\
 & \left. \left. \left( 1+\tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - \left( \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right. \right. \right. \\
 & \left. \left. \left. \left( a+b-a\tan\left[\frac{1}{2}(c+dx)\right]^2+b\tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) / \left( 1+\tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \right) \right) / \\
 & \left( (a^2-b^2) \left( \frac{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}{1-\tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^{1/3} \left( \frac{a+b-a\tan\left[\frac{1}{2}(c+dx)\right]^2+b\tan\left[\frac{1}{2}(c+dx)\right]^2}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^{1/3} \right) - \\
 & \left( 3(a-b)(a+b) \left( a \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] - \right. \right. \\
 & \left. \left. b \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \\
 & \left( 1+\tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^{2/3} \left( \frac{a+b-a\tan\left[\frac{1}{2}(c+dx)\right]^2+b\tan\left[\frac{1}{2}(c+dx)\right]^2}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^{2/3} \\
 & \left( 10 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \left. \left( (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) + \right. \\
 & \left. 2(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \\
 & \tan\left[\frac{1}{2}(c+dx)\right]^5 + 3 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \tan\left[\frac{1}{2}(c+dx)\right] \left( -2 \left( (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \frac{4}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \Big] + 2(a+b) \\
 & \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \Big) \\
 & \tan\left[\frac{1}{2}(c+dx)\right]^2 + 15(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \Big) \Big) \Big) \Big) / \\
 & \left( (a^2 - b^2) \left( \frac{1}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^{1/3} \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right. \\
 & \left. \left( 9(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \right. \\
 & \left. \left. 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) + \right. \right. \\
 & \left. \left. 2(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right. \\
 & \left. \left( 15(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \right. \\
 & \left. \left. 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) + \right. \right. \\
 & \left. \left. \left. 2(a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \right) \right. \\
 & \left. \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( a \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right)^2 \Big) + \\
 & \left( 2(a-b)(a+b) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right. \\
 & \left. \left( \frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^{2/3} \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( 10 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right. \\
 & \left( (a-b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \\
 & \left. 2 (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \\
 & \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^5 + 3 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \right. \\
 & \left. \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] \left( -2 \left( (a-b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, \right. \right. \right. \\
 & \left. \left. \frac{4}{3}, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + 2 (a+b) \right. \\
 & \left. \left. \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \right) \right) / \\
 & \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 + 15 (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \right. \\
 & \left. \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) \Bigg) / \\
 & \left( (a^2 - b^2) \left( \frac{1}{1 - \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2} \right)^{1/3} \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right)^{1/3} \right. \\
 & \left( 9 (a+b) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \\
 & 2 \left( (a-b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \\
 & 2 (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \right. \\
 & \left. \left. \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \\
 & \left( 15 (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right.
 \end{aligned}$$



$$\begin{aligned}
 & 2 \left( (a-b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \\
 & \quad \left. 2 (a+b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \\
 & \quad \left. \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \left( a \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) - b \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) - \\
 & \left( 3 (a-b) (a+b) \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right)^{2/3} \right. \\
 & \quad \left. \left( \frac{a+b - a \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 + b \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2} \right)^{2/3} \right) \\
 & \quad \left( 10 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right. \\
 & \quad \left. \left( (a-b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \right. \\
 & \quad \left. \left. 2 (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \right) \\
 & \quad \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^5 + 3 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \right. \\
 & \quad \left. \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] \left( -2 \left( (a-b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, \right. \right. \right. \\
 & \quad \left. \left. \frac{4}{3}, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + 2 (a+b) \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \right) \\
 & \quad \left. \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 + 15 (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) \right) / \\
 & \left( (a^2 - b^2) \left( \frac{1}{1 - \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2} \right)^{1/3} \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right)^2 \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( 9 (a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & 2 (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \left. \right) \\
 & \left( 15 (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & 2 (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \left. \right) \\
 & \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \left( a \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \left. \right) - \\
 & \left( (a-b) (a+b) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \left( \frac{1}{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \right)^{2/3} \right. \\
 & \left. \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right)^{2/3} \left( \frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \right)^{2/3} \right. \\
 & \left( 10 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \left( (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & 2 (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \left. \right) \\
 & \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^5 + 3 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \left( -2 \left( (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \right. \right. \right.
 \end{aligned}$$



$$\begin{aligned}
 & \left( 10 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right. \\
 & \quad \left( (a-b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \\
 & \quad \left. 2(a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \\
 & \quad \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^5 + 3 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \right. \\
 & \quad \left. \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] \left( -2 \left( (a-b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, \right. \right. \right. \\
 & \quad \left. \left. \frac{4}{3}, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + 2(a+b) \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \right) \right) \\
 & \quad \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 + 15(a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \right. \\
 & \quad \left. \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) \Bigg) / \\
 & \left( (a^2 - b^2) \left( \frac{1}{1 - \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2} \right)^{1/3} \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right. \\
 & \quad \left. \left( \frac{a+b - a \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 + b \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2} \right)^{1/3} \right. \\
 & \quad \left( 9(a+b) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \\
 & \quad 2 \left( (a-b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \\
 & \quad \left. 2(a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( 15 (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & \left. \left. 2 (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( a \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) - \\
 & \left( 3 (a-b) (a+b) \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right)^{2/3} \right. \\
 & \left. \left( \frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \right)^{2/3} \right. \\
 & \left. \left( 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \right. \right. \\
 & \left. \left. 2 (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \right) \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + 9 (a+b) \right. \\
 & \left. \left( \frac{1}{9 (a+b)} (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \left. \frac{2}{9} \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) + 2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \\
 & \left( (a-b) \left( \frac{1}{5 (a+b)} 4 (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{7}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \frac{2}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{4}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \\
 & \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \Bigg) + 2(a+b) \left( \frac{1}{5(a+b)}(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \right. \right. \\
 & \left. \left. \frac{5}{3}, \frac{4}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \operatorname{AppellF1}\left[\frac{5}{2}, \frac{8}{3}, \frac{1}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \left. \left. \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \Bigg) \Bigg) \\
 & \left( 10 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \left. \left( (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) + \right. \\
 & \left. 2(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \\
 & \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^5 + 3 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \left. \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \left( -2 \left( (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \right. \right. \right. \\
 & \left. \left. \frac{4}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + 2(a+b) \right. \\
 & \left. \left. \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \right) \\
 & \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + 15(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \left. \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \Bigg) \Bigg) / \\
 & \left( (a^2 - b^2) \left( \frac{1}{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \right)^{1/3} \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right. \\
 & \left. \left( 9(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & 2 \left( (a-b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \\
 & \quad 2 (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \\
 & \quad \quad \left. \left. \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \Bigg)^2 \\
 & \left( 15 (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \\
 & \quad 2 \left( (a-b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \\
 & \quad \quad \left. 2 (a+b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \\
 & \quad \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \left( a \left( -1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) - b \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) \Bigg) - \\
 & \left( 3 (a-b) (a+b) \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right)^{2/3} \right. \\
 & \quad \left. \left( \frac{a+b - a \tan \left[ \frac{1}{2} (c+dx) \right]^2 + b \tan \left[ \frac{1}{2} (c+dx) \right]^2}{1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2} \right)^{2/3} \right) \\
 & \left( 2 \left( (a-b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \right. \\
 & \quad \left. \left. 2 (a+b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \right) \\
 & \quad \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + 15 (a+b) \left( \frac{1}{5 (a+b)} \right. \\
 & \quad \left. (a-b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \\
 & \quad \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + \frac{2}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \\
 & \quad \left. \left. \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \right) \Bigg) +
 \end{aligned}$$

$$\begin{aligned}
 & 2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \left( (a-b) \left( \frac{1}{21(a+b)} 20(a-b) \operatorname{AppellF1}\left[\frac{7}{2}, \frac{2}{3}, \frac{7}{3}, \frac{9}{2}\right], \right. \right. \\
 & \quad \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \quad \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \frac{10}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{5}{3}, \frac{4}{3}, \frac{9}{2}\right], \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \quad \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) + \\
 & 2(a+b) \left( \frac{1}{21(a+b)} 5(a-b) \operatorname{AppellF1}\left[\frac{7}{2}, \frac{5}{3}, \frac{4}{3}, \frac{9}{2}\right], \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \quad \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \\
 & \quad \frac{25}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{8}{3}, \frac{1}{3}, \frac{9}{2}\right], \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right) \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \Bigg) \\
 & \left( 10 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}\right], \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right) \\
 & \quad \left( (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}\right], \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right) + \\
 & \quad \left. 2(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}\right], \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right) \\
 & \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^5 + 3 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}\right], \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \\
 & \quad \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \left( -2 \left( (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \right. \right. \right. \\
 & \quad \left. \left. \frac{4}{3}, \frac{7}{2}\right], \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + 2(a+b) \right. \\
 & \quad \left. \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}\right], \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right) \right) \\
 & \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + 15(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}\right], \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2,
 \end{aligned}$$



$$\begin{aligned}
 & \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) / \\
 & \left( (a^2 - b^2) \left( \frac{1}{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \right)^{1/3} \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right. \\
 & \left( 9(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + \right. \\
 & 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + \right. \\
 & 2(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \\
 & \left( 15(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + \right. \\
 & 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + \right. \\
 & 2(a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \\
 & \left( a \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) + \left( 3(a-b) \right. \\
 & (a+b) \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right)^{2/3} \\
 & \left. \left. \left. \frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \right)^{2/3} \right) \\
 & \left( 25 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right. \\
 & \left. \left( (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & 2(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \\
 & \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^4 + \\
 & 10\left((a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & \left. 2(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right]\right) \\
 & \tan\left[\frac{1}{2}(c+dx)\right]^5 \left(\frac{1}{5(a+b)}(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \left. \frac{2}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right) + 10 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \right. \\
 & \left. \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^5 \\
 & \left((a-b) \left(\frac{1}{5(a+b)} 4(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{7}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \right. \\
 & \left. \left. \frac{2}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{4}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \right. \\
 & \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right) + 2(a+b) \left(\frac{1}{5(a+b)}(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \right. \right. \right. \\
 & \left. \left. \frac{5}{3}, \frac{4}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \left. \tan\left[\frac{1}{2}(c+dx)\right] + \operatorname{AppellF1}\left[\frac{5}{2}, \frac{8}{3}, \frac{1}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right) \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \frac{3}{2} \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \\
 & \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \left(-2 \left( (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \right. \\
 & \quad 2(a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \quad \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + 15(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \right. \\
 & \quad \left. \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \right) + \\
 & 3 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \left( \frac{1}{9(a+b)} (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{4}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \quad \left. \frac{2}{9} \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \quad \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \right) \\
 & \left(-2 \left( (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \right. \\
 & \quad 2(a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \quad \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + 15(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \right. \\
 & \quad \left. \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \right) + \\
 & 3 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, \frac{1}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \\
 & \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \left( 15(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, \frac{1}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \left] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] - \right. \\
 & 2 \left( (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right], \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right) + \\
 & 2(a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right], \\
 & \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \\
 & 15(a+b) \left( \frac{1}{5(a+b)} (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, \frac{4}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right], \right. \\
 & \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \\
 & \left. \frac{2}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, \frac{1}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right], \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \\
 & \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) - \\
 & 2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \left( (a-b) \left( \frac{1}{21(a+b)} 20(a-b) \operatorname{AppellF1}\left[\frac{7}{2}, \frac{2}{3}, \frac{7}{3}, \right. \right. \right. \\
 & \left. \left. \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right], \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \frac{10}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{5}{3}, \frac{4}{3}, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right], \right. \\
 & \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) + \\
 & 2(a+b) \left( \frac{1}{21(a+b)} 5(a-b) \operatorname{AppellF1}\left[\frac{7}{2}, \frac{5}{3}, \frac{4}{3}, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right], \right. \\
 & \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \\
 & \left. \frac{25}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{8}{3}, \frac{1}{3}, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right], \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) \right) \right) \right) /
 \end{aligned}$$



$$\begin{aligned}
& - \frac{3 a^2 \operatorname{Sec}[c+d x] \operatorname{Tan}[c+d x]}{2 b\left(a^2-b^2\right) d\left(a+b \operatorname{Sec}[c+d x]\right)^{2 / 3}} + \frac{3\left(3 a^2-b^2\right)\left(a+b \operatorname{Sec}[c+d x]\right)^{1 / 3} \operatorname{Tan}[c+d x]}{4 b^2\left(a^2-b^2\right) d} \\
& \left( a\left(9 a^2-7 b^2\right) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2},-\frac{1}{3}, \frac{3}{2}, \frac{1}{2}\left(1-\operatorname{Sec}[c+d x]\right), \frac{b\left(1-\operatorname{Sec}[c+d x]\right)}{a+b}\right]\right. \\
& \quad \left. \left(a+b \operatorname{Sec}[c+d x]\right)^{1 / 3} \operatorname{Tan}[c+d x]\right) / \\
& \left(2 \sqrt{2} b^3\left(a^2-b^2\right) d \sqrt{1+\operatorname{Sec}[c+d x]}\left(\frac{a+b \operatorname{Sec}[c+d x]}{a+b}\right)^{1 / 3}\right) + \\
& \left( \left(9 a^4-10 a^2 b^2-b^4\right) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}, \frac{2}{3}, \frac{3}{2}, \frac{1}{2}\left(1-\operatorname{Sec}[c+d x]\right), \frac{b\left(1-\operatorname{Sec}[c+d x]\right)}{a+b}\right]\right. \\
& \quad \left. \left(\frac{a+b \operatorname{Sec}[c+d x]}{a+b}\right)^{2 / 3} \operatorname{Tan}[c+d x]\right) / \\
& \left(2 \sqrt{2} b^3\left(a^2-b^2\right) d \sqrt{1+\operatorname{Sec}[c+d x]}\left(a+b \operatorname{Sec}[c+d x]\right)^{2 / 3}\right)
\end{aligned}$$

Result (type 6, 33538 leaves): Display of huge result suppressed!

### Problem 709: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Sec}[c+d x]^3}{\left(a+b \operatorname{Sec}[c+d x]\right)^{5 / 3}} d x$$

Optimal (type 6, 307 leaves, 8 steps):

$$\begin{aligned}
& - \frac{3 a^2 \operatorname{Tan}[c+d x]}{2 b\left(a^2-b^2\right) d\left(a+b \operatorname{Sec}[c+d x]\right)^{2 / 3}} + \\
& \left( \left(3 a^2-2 b^2\right) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2},-\frac{1}{3}, \frac{3}{2}, \frac{1}{2}\left(1-\operatorname{Sec}[c+d x]\right), \frac{b\left(1-\operatorname{Sec}[c+d x]\right)}{a+b}\right]\right. \\
& \quad \left. \left(a+b \operatorname{Sec}[c+d x]\right)^{1 / 3} \operatorname{Tan}[c+d x]\right) / \\
& \left( \sqrt{2} b^2\left(a^2-b^2\right) d \sqrt{1+\operatorname{Sec}[c+d x]}\left(\frac{a+b \operatorname{Sec}[c+d x]}{a+b}\right)^{1 / 3}\right) - \\
& \left( a\left(3 a^2-4 b^2\right) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}, \frac{2}{3}, \frac{3}{2}, \frac{1}{2}\left(1-\operatorname{Sec}[c+d x]\right), \frac{b\left(1-\operatorname{Sec}[c+d x]\right)}{a+b}\right]\right. \\
& \quad \left. \left(\frac{a+b \operatorname{Sec}[c+d x]}{a+b}\right)^{2 / 3} \operatorname{Tan}[c+d x]\right) / \\
& \left( \sqrt{2} b^2\left(a^2-b^2\right) d \sqrt{1+\operatorname{Sec}[c+d x]}\left(a+b \operatorname{Sec}[c+d x]\right)^{2 / 3}\right)
\end{aligned}$$

Result (type 6, 30028 leaves): Display of huge result suppressed!

### Problem 710: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Sec}[c+d x]^2}{\left(a+b \operatorname{Sec}[c+d x]\right)^{5 / 3}} d x$$

Optimal (type 6, 289 leaves, 8 steps):

$$\frac{3 a \operatorname{Tan}[c+d x]}{2\left(a^2-b^2\right) d\left(a+b \operatorname{Sec}[c+d x]\right)^{2 / 3}} - \left(a \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}, -\frac{1}{3}, \frac{3}{2}, \frac{1}{2}\left(1-\operatorname{Sec}[c+d x]\right), \frac{b\left(1-\operatorname{Sec}[c+d x]\right)}{a+b}\right]\left(a+b \operatorname{Sec}[c+d x]\right)^{1 / 3} \operatorname{Tan}[c+d x]\right) / \left(\sqrt{2} b\left(a^2-b^2\right) d \sqrt{1+\operatorname{Sec}[c+d x]}\left(\frac{a+b \operatorname{Sec}[c+d x]}{a+b}\right)^{1 / 3}\right) + \left(\left(a^2-2 b^2\right) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}, \frac{2}{3}, \frac{3}{2}, \frac{1}{2}\left(1-\operatorname{Sec}[c+d x]\right), \frac{b\left(1-\operatorname{Sec}[c+d x]\right)}{a+b}\right]\left(\frac{a+b \operatorname{Sec}[c+d x]}{a+b}\right)^{2 / 3} \operatorname{Tan}[c+d x]\right) / \left(\sqrt{2} b\left(a^2-b^2\right) d \sqrt{1+\operatorname{Sec}[c+d x]}\left(a+b \operatorname{Sec}[c+d x]\right)^{2 / 3}\right)$$

Result (type 6, 18901 leaves):

$$\frac{\left(b+a \operatorname{Cos}[c+d x]\right)^2 \operatorname{Sec}[c+d x]^2\left(\frac{3 a \operatorname{Sin}[c+d x]}{2 b\left(-a^2+b^2\right)}-\frac{3 a \operatorname{Sin}[c+d x]}{2\left(-a^2+b^2\right)\left(b+a \operatorname{Cos}[c+d x]\right)}\right)}{d\left(a+b \operatorname{Sec}[c+d x]\right)^{5 / 3}} + \left(3\left(b+a \operatorname{Cos}[c+d x]\right)^{5 / 3}\left(-\frac{a}{\left(-a^2+b^2\right)\left(b+a \operatorname{Cos}[c+d x]\right)^{2 / 3} \operatorname{Sec}[c+d x]^{2 / 3}} - \frac{3 a^2 \operatorname{Sec}[c+d x]^{1 / 3}}{4 b\left(-a^2+b^2\right)\left(b+a \operatorname{Cos}[c+d x]\right)^{2 / 3}} + \frac{b \operatorname{Sec}[c+d x]^{1 / 3}}{\left(-a^2+b^2\right)\left(b+a \operatorname{Cos}[c+d x]\right)^{2 / 3}} - \frac{3 a^2 \operatorname{Cos}\left[2(c+d x)\right] \operatorname{Sec}[c+d x]^{1 / 3}}{4 b\left(-a^2+b^2\right)\left(b+a \operatorname{Cos}[c+d x]\right)^{2 / 3}}\right) \operatorname{Sec}[c+d x]^{5 / 3} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] \left(\frac{1}{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}\right)^{1 / 3}\left(\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}\right)^{1 / 3} \left(a\left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right)-\left(12 b^2(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}\right]\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right)\right) / \left(\left(a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right)\left(-9(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}\right]-2\left(2(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}\right]+(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{5}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}\right]\right)\right)$$

$$\begin{aligned}
 & \left. \left. \left. \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) + \\
 & \left( 9a^2(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \right. \\
 & \quad \left. \left. \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) / \\
 & \left( \left( 9(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) + \right. \right. \\
 & \quad \left. \left. 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \right) \right. \right. \\
 & \quad \left. \left. (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \right) \right. \\
 & \quad \left. \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( a \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) + \\
 & \left( 3ab(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \right. \\
 & \quad \left. \left. \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) / \\
 & \left( \left( 9(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) + \right. \right. \\
 & \quad \left. \left. 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \right) \right. \right. \\
 & \quad \left. \left. (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \right) \right. \\
 & \quad \left. \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( a \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) - \\
 & \left( 5a^2(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right)
 \end{aligned}$$





$$\begin{aligned}
& \left( \frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \right)^{1/3} \left( a \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) - \right. \\
& \left. \left( 12 b^2 (a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \right. \\
& \left. \left. \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) / \left( \left( a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right. \\
& \left. \left( -9 (a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) - \right. \\
& \left. 2 \left( 2 (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
& \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \right. \right. \right. \\
& \left. \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) + \\
& \left( 9 a^2 (a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
& \left. \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) / \left( \left( 9 (a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
& \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + 2 \left( 2 (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \right. \right. \right. \right. \\
& \left. \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \right. \right. \right. \\
& \left. \left. \left. \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \\
& \left. \left( a \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) + \\
& \left( 3 a b (a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
& \left. \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) / \left( \left( 9 (a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
 & \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} + 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \right. \right. \\
 & \left. \left. \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \left. \left( a \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) - \\
 & \left( 5a^2(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) / \left( \left( 15(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \right. \right. \right. \\
 & \left. \left. \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + 2 \left( 2(a-b) \operatorname{AppellF1}\left[ \right. \right. \right. \\
 & \left. \left. \frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + (a+b) \right. \right. \\
 & \left. \left. \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \right) \\
 & \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \left( a \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) + \\
 & \left( 5ab(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) / \\
 & \left( \left( 15(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) + \right. \\
 & \left. 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \right. \right. \right.
 \end{aligned}$$



$$\begin{aligned}
 & \left. \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \\
 & \left( a \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Bigg) + \\
 & \left( 3ab(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right. \\
 & \left. \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Bigg) / \left( \left( 9(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \right. \right. \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \right. \right. \right. \\
 & \left. \left. \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \\
 & \left( a \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Bigg) - \\
 & \left( 5a^2(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right. \\
 & \left. \tan\left[\frac{1}{2}(c+dx)\right]^2 \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Bigg) / \\
 & \left( \left( 15(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + \right. \right. \\
 & \left. \left. 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \right. \\
 & \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \right. \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \\
 & \left( a \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Bigg) +
 \end{aligned}$$

$$\begin{aligned}
 & \left( 5 a b (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}\right] \right. \\
 & \quad \left. \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2 \left(1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right)\right) / \\
 & \left( \left( 15 (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}\right] \right) + \right. \\
 & \quad 2 \left( 2 (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}\right] + (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \right. \right. \\
 & \quad \quad \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}\right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2 \right) \\
 & \quad \left. \left( a \left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right) - b \left(1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right) \right) \right) + \\
 & \frac{1}{2(-a^2 b + b^3) \left(1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right)^{2/3}} \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2 \\
 & \left( \frac{1}{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \right)^{4/3} \\
 & \left( \frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \right)^{1/3} \\
 & \left( a \left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right) - \right. \\
 & \quad \left( 12 b^2 (a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}\right] \right) \\
 & \quad \left. \left(1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right) \right) / \left( \left( a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2 \right) \right) \\
 & \left( -9 (a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}\right] \right) -
 \end{aligned}$$

$$\begin{aligned}
 & 2 \left( 2 (a-b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \Bigg) + \\
 & \left( 9 a^2 (a+b) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right. \\
 & \quad \left. \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) / \left( \left( 9 (a+b) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + 2 \left( 2 (a-b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \right. \right. \right. \right. \\
 & \quad \left. \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}, \right. \right. \\
 & \quad \left. \left. \frac{2}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \Bigg) \\
 & \quad \left. \left( a \left( -1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) - b \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) \right) + \\
 & \left( 3 a b (a+b) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right. \\
 & \quad \left. \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) / \left( \left( 9 (a+b) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + 2 \left( 2 (a-b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \right. \right. \right. \right. \\
 & \quad \left. \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}, \right. \right. \\
 & \quad \left. \left. \frac{2}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \Bigg) \\
 & \quad \left. \left( a \left( -1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) - b \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) \right) -
 \end{aligned}$$

$$\begin{aligned}
 & \left( 5 a^2 (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \quad \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)\right) / \\
 & \left( \left( 15 (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) + \right. \\
 & \quad 2 \left( 2 (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \right. \right. \\
 & \quad \quad \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \\
 & \quad \left. \left( a \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) - b \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \right) \right) + \\
 & \left( 5 a b (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \\
 & \quad \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \right) / \\
 & \left( \left( 15 (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) + \right. \\
 & \quad 2 \left( 2 (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \right. \right. \\
 & \quad \quad \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \\
 & \quad \left. \left( a \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) - b \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \right) \right) \right) + \\
 & \left( \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \left( \frac{1}{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \right)^{1/3} \left( \left(-a \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \right. \right.
 \end{aligned}$$



$$\begin{aligned}
 & b \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \Big/ \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) - \\
 & \left( \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \left( a + b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + \right. \right. \\
 & \quad \left. \left. b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \Big/ \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)^2 \right) \\
 & \left( a \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) - \left( 12 b^2 (a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \right. \right. \right. \\
 & \quad \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \right) \Big/ \right. \\
 & \left. \left( \left( a + b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right. \right. \\
 & \quad \left. \left. \left( -9 (a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] - \right. \right. \right. \\
 & \quad \left. \left. 2 \left( 2 (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Big/ + \\
 & \left( 9 a^2 (a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right. \\
 & \quad \left. \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Big/ \left( \left( 9 (a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + 2 \left( 2 (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \\
 & \left. \left( a \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) \Big/ +
 \end{aligned}$$

$$\begin{aligned}
 & \left( 3 a b (a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}\right] \right. \\
 & \left. \left(1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right)\right) / \left( \left( 9(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2, \right. \right. \right. \\
 & \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}\right] + 2\left( 2(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \right. \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}\right] + (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \right. \right. \right. \\
 & \left. \left. \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}\right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2 \right) \\
 & \left. \left( a\left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right) - b\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right) \right) \right) - \\
 & \left( 5 a^2 (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}\right] \right. \\
 & \left. \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right)\right) / \\
 & \left( \left( 15(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}\right] + \right. \right. \\
 & \left. \left. 2\left( 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}\right] + (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \right. \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}\right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2 \right) \\
 & \left. \left( a\left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right) - b\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right) \right) \right) + \\
 & \left( 5 a b (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}\right] \right. \\
 & \left. \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right)\right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( \left( 15 (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \right. \\
 & \quad 2 \left( 2 (a-b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
 & \quad \quad \left. \left. \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + (a+b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \right. \right. \\
 & \quad \quad \left. \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \\
 & \left. \left( a \left( -1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) - b \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) \right) \left/ \left( 2 (-a^2 b + b^3) \right. \right. \\
 & \quad \left. \left. \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right)^{2/3} \left( \frac{a+b - a \tan \left[ \frac{1}{2} (c+dx) \right]^2 + b \tan \left[ \frac{1}{2} (c+dx) \right]^2}{1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2} \right)^{2/3} \right) \right) + \\
 & \quad \frac{1}{2 (-a^2 b + b^3) \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right)^{2/3}} \\
 & \quad 3 \\
 & \quad \tan \left[ \frac{1}{2} (c+dx) \right] \\
 & \quad \left( \frac{1}{1 - \tan \left[ \frac{1}{2} (c+dx) \right]^2} \right)^{1/3} \\
 & \quad \left( \frac{a+b - a \tan \left[ \frac{1}{2} (c+dx) \right]^2 + b \tan \left[ \frac{1}{2} (c+dx) \right]^2}{1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2} \right)^{1/3} \\
 & \quad \left( a \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + \right. \\
 & \quad \left( 12 b^2 (a+b) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right. \\
 & \quad \left. \left( -a \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + b \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \right) \right. \\
 & \quad \left. \left. \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) \right/ \left( \left( a+b - a \tan \left[ \frac{1}{2} (c+dx) \right]^2 + b \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right)^2 \right. \right. \\
 & \quad \left. \left. \left( -9 (a+b) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] - \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
& 2 \left( 2 (a-b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right], \right. \\
& \quad \left. \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \right. \\
& \quad \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) - \\
& \left( 12 b^2 (a+b) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right. \\
& \quad \left. \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \right) / \\
& \left( \left( a+b - a \tan \left[ \frac{1}{2} (c+dx) \right]^2 + b \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \left( -9 (a+b) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \right. \right. \right. \\
& \quad \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] - 2 \left( 2 (a-b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \right. \right. \\
& \quad \left. \left. \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}, \right. \right. \\
& \quad \left. \left. \frac{2}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) - \\
& \left( 12 b^2 (a+b) \left( \frac{1}{9 (a+b)} 2 (a-b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \\
& \quad \left. \left. \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + \frac{1}{9} \right. \\
& \quad \left. \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right. \\
& \quad \left. \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \right) \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) / \\
& \left( \left( a+b - a \tan \left[ \frac{1}{2} (c+dx) \right]^2 + b \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \left( -9 (a+b) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \right. \right. \right. \\
& \quad \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] - 2 \left( 2 (a-b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
 & \left. \left. \left. \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + (a+b)\operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right]\right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) - \\
 & \left( 9a^2(a+b)\operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \quad \left. \left( a\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] - b\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \right. \\
 & \quad \left. \left. \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) / \\
 & \left( \left( 9(a+b)\operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) + \right. \\
 & \quad \left. 2 \left( 2(a-b)\operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + (a+b)\operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \right. \right. \right. \\
 & \quad \left. \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right]\right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \\
 & \quad \left. \left. \left( a \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) \right) - \\
 & \left( 3ab(a+b)\operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \quad \left. \left( a\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] - b\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \right. \\
 & \quad \left. \left. \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) / \\
 & \left( \left( 9(a+b)\operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) + \right. \\
 & \quad \left. 2 \left( 2(a-b)\operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + (a+b)\operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \right. \right. \right. \\
 & \quad \left. \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right]\right) \right) \right)
 \end{aligned}$$

$$\begin{aligned}
& \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) \\
& \left( a \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right)^2 \Bigg) + \\
& \left( 5a^2(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \right. \\
& \left. \tan\left[\frac{1}{2}(c+dx)\right]^2 \left( a \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] - b \right. \right. \\
& \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Bigg) / \\
& \left( \left( 15(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) + \right. \\
& \left. 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
& \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \right. \right. \\
& \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \Bigg) \\
& \left( a \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right)^2 \Bigg) - \\
& \left( 5ab(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
& \left. \tan\left[\frac{1}{2}(c+dx)\right]^2 \left( a \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] - b \right. \right. \\
& \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Bigg) / \\
& \left( \left( 15(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) + \right. \\
& \left. 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
 & \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} + (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) \\
 & \left( a \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right)^2 \Bigg) + \\
 & \left( 9a^2 (a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \Bigg) / \\
 & \left( \left( 9(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \right. \\
 & \left. \left. 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} + (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \right. \right. \right. \right. \\
 & \left. \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \\
 & \left. \left( a \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) \Bigg) + \\
 & \left( 3ab (a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \Bigg) / \\
 & \left( \left( 9(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \right. \\
 & \left. \left. 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} + (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \right. \right. \right. \right. \\
 & \left. \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \\
 & \left. \left( a \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) \Bigg) +
 \end{aligned}$$

$$\begin{aligned}
& \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) \\
& \left( a \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Bigg) + \\
& \left( 9a^2(a+b) \left( \frac{1}{9(a+b)} 2(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
& \quad \left. \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{9} \right. \right. \right. \\
& \quad \left. \left. \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \right. \right. \\
& \quad \left. \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Bigg) / \\
& \left( \left( 9(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) + \right. \\
& \quad \left. 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
& \quad \left. \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \right. \right. \right. \right. \\
& \quad \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \Bigg) \\
& \left( a \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Bigg) + \\
& \left( 3ab(a+b) \left( \frac{1}{9(a+b)} 2(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
& \quad \left. \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{9} \right. \right. \right. \\
& \quad \left. \left. \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \right. \right. \\
& \quad \left. \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Bigg) /
\end{aligned}$$



$$\begin{aligned}
 & \left( \left( 9 (a+b) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \right. \\
 & \quad 2 \left( 2 (a-b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
 & \quad \quad \left. \left. \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \right. \right. \\
 & \quad \quad \left. \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \\
 & \quad \left. \left( a \left( -1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) - b \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) \right) - \\
 & \left( 5 a^2 (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right. \\
 & \quad \left. \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right]^3 \right) / \\
 & \left( \left( 15 (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \right. \\
 & \quad 2 \left( 2 (a-b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
 & \quad \quad \left. \left. \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + (a+b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \right. \right. \\
 & \quad \quad \left. \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \\
 & \quad \left. \left( a \left( -1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) - b \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) \right) + \\
 & \left( 5 a b (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right. \\
 & \quad \left. \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right]^3 \right) / \\
 & \left( \left( 15 (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & 2 \left( 2 (a - b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right], \right. \\
 & \quad \left. \frac{(a - b) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] + (a + b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \right. \\
 & \quad \left. \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, \frac{(a - b) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right) \\
 & \left( a \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right) - b \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right) \right) - \\
 & \left( 5 a^2 (a + b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right], \frac{(a - b) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] \\
 & \quad \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right] \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right) \right) / \\
 & \left( \left( 15 (a + b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right], \frac{(a - b) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right) \right) + \\
 & 2 \left( 2 (a - b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right], \right. \\
 & \quad \left. \frac{(a - b) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] + (a + b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \right. \\
 & \quad \left. \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2, \frac{(a - b) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right) \\
 & \left( a \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right) - b \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right) \right) \right) + \\
 & \left( 5 a b (a + b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right], \frac{(a - b) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] \\
 & \quad \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right] \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right) \right) / \\
 & \left( \left( 15 (a + b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right], \frac{(a - b) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right) \right) + \\
 & 2 \left( 2 (a - b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right], \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} + (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) \\
 & \left( a \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Bigg) - \left( 5a^2(a+b) \right. \\
 & \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \left( \frac{1}{5(a+b)} - 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \frac{1}{5} \right. \\
 & \left. \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Bigg) / \\
 & \left( \left( 15(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) + \right. \\
 & \left. 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} + (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \right. \right. \right. \\
 & \left. \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \\
 & \left( a \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Bigg) + \left( 5ab(a+b) \right. \\
 & \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \left( \frac{1}{5(a+b)} - 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \frac{1}{5} \right. \\
 & \left. \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \Bigg)
 \end{aligned}$$

$$\begin{aligned}
& \left. \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] \right) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \Big/ \\
& \left( \left( 15 (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right)^2 + \right. \\
& 2 \left( 2 (a-b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
& \left. \left. \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + (a+b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \right. \right. \\
& \left. \left. \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \Big) \\
& \left( a \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) - b \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) \Big) + \\
& \left( 12 b^2 (a+b) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right)^2 \\
& \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \left( -2 \left( 2 (a-b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \\
& \left. \left. \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \right. \right. \\
& \left. \left. \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \\
& \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] - 9 (a+b) \left( \frac{1}{9 (a+b)} 2 (a-b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \right. \right. \\
& \left. \left. \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \right. \\
& \left. \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] + \frac{1}{9} \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
& \left. \left. \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] \right) \Big) - 2 \\
& \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \left( 2 (a-b) \left( \frac{1}{a+b} (a-b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, \frac{8}{3}, \frac{7}{2}, \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
 & \left. \left( \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \left. \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{5}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + \\
 & (a+b) \left( \frac{1}{5(a+b)} 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{5}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \left. \frac{4}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{7}{3}, \frac{2}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right. \\
 & \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \Big/ \\
 & \left( \left( a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( -9(a+b) \operatorname{AppellF1}\left[ \right. \right. \right. \\
 & \left. \left. \left. \frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] - \right. \right. \\
 & \left. \left. 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \right. \right. \right. \right. \\
 & \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) - \\
 & \left( 9a^2(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right. \\
 & \left. \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \right. \right. \right. \right. \\
 & \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \sec\left[\frac{1}{2}(c+dx)\right]^2 \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \tan\left[\frac{1}{2}(c+dx)\right] + 9(a+b) \left( \frac{1}{9(a+b)} 2(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \right. \right. \\
 & \quad \left. \left. \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \quad \left. \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{9} \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) + 2 \\
 & \tan\left[\frac{1}{2}(c+dx)\right]^2 \left( 2(a-b) \left( \frac{1}{a+b} (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{8}{3}, \frac{7}{2}, \right. \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{5}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) + \\
 & (a+b) \left( \frac{1}{5(a+b)} 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{5}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \quad \left. \frac{4}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{7}{3}, \frac{2}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \quad \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) \right) \Big/ \\
 & \left( \left( 9(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) + \right. \\
 & \quad \left. 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2
 \end{aligned}$$

$$\begin{aligned}
 & \left( a \left( -1 + \tan \left[ \frac{1}{2} (c + dx) \right]^2 \right) - b \left( 1 + \tan \left[ \frac{1}{2} (c + dx) \right]^2 \right) \right) - \\
 & \left( 3ab(a+b) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c + dx) \right]^2}{a+b} \right] \right. \\
 & \left. \left( 1 + \tan \left[ \frac{1}{2} (c + dx) \right]^2 \right) \left( 2 \left( 2(a-b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b) \tan \left[ \frac{1}{2} (c + dx) \right]^2}{a+b} \right] + (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \right. \right. \right. \right. \\
 & \left. \left. \left. \tan \left[ \frac{1}{2} (c + dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c + dx) \right]^2}{a+b} \right] \right) \sec \left[ \frac{1}{2} (c + dx) \right]^2 \right. \\
 & \left. \tan \left[ \frac{1}{2} (c + dx) \right] + 9(a+b) \left( \frac{1}{9(a+b)} 2(a-b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c + dx) \right]^2}{a+b} \right] \sec \left[ \frac{1}{2} (c + dx) \right]^2 \right. \right. \\
 & \left. \left. \tan \left[ \frac{1}{2} (c + dx) \right] + \frac{1}{9} \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b) \tan \left[ \frac{1}{2} (c + dx) \right]^2}{a+b} \right] \sec \left[ \frac{1}{2} (c + dx) \right]^2 \tan \left[ \frac{1}{2} (c + dx) \right] \right) \right) + 2 \\
 & \tan \left[ \frac{1}{2} (c + dx) \right]^2 \left( 2(a-b) \left( \frac{1}{a+b} (a-b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, \frac{8}{3}, \frac{7}{2}, \right. \right. \right. \right. \\
 & \left. \left. \left. \tan \left[ \frac{1}{2} (c + dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c + dx) \right]^2}{a+b} \right] \sec \left[ \frac{1}{2} (c + dx) \right]^2 \right. \right. \\
 & \left. \left. \tan \left[ \frac{1}{2} (c + dx) \right] + \frac{1}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}, \frac{5}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b) \tan \left[ \frac{1}{2} (c + dx) \right]^2}{a+b} \right] \sec \left[ \frac{1}{2} (c + dx) \right]^2 \tan \left[ \frac{1}{2} (c + dx) \right] \right) \right) + \\
 & (a+b) \left( \frac{1}{5(a+b)} 2(a-b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}, \frac{5}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b) \tan \left[ \frac{1}{2} (c + dx) \right]^2}{a+b} \right] \sec \left[ \frac{1}{2} (c + dx) \right]^2 \tan \left[ \frac{1}{2} (c + dx) \right] + \right. \\
 & \left. \frac{4}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{7}{3}, \frac{2}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c + dx) \right]^2}{a+b} \right] \right)
 \end{aligned}$$





$$\begin{aligned}
 & \left. \left( \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \left. \frac{5}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{4}{3}, \frac{5}{3}, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) + (a+b) \\
 & \left( \frac{1}{21(a+b)} 10(a-b) \operatorname{AppellF1}\left[\frac{7}{2}, \frac{4}{3}, \frac{5}{3}, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \left. \frac{20}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{7}{3}, \frac{2}{3}, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) \Big/ \\
 & \left( \left( 15(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \right. \\
 & \left. \left. 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right) + (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \right. \right. \right. \right. \\
 & \left. \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \\
 & \left. \left( a \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) - \\
 & \left( 5ab(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \\
 & \left( 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \right. \\
 & \left. \left. (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + 15 \\
 (a+b) & \left( \frac{1}{5(a+b)} 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right], \right. \\
 & \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \left. \frac{1}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right], \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) + 2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \left( 2(a-b) \left( \frac{1}{21(a+b)} 25(a-b) \operatorname{AppellF1}\left[\frac{7}{2}, \frac{1}{3}, \frac{8}{3}, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right], \right. \right. \\
 & \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \left. \frac{5}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{4}{3}, \frac{5}{3}, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right], \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) + (a+b) \\
 & \left( \frac{1}{21(a+b)} 10(a-b) \operatorname{AppellF1}\left[\frac{7}{2}, \frac{4}{3}, \frac{5}{3}, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right], \right. \\
 & \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \left. \frac{20}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{7}{3}, \frac{2}{3}, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right], \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \Bigg) \Bigg) \Bigg) \Bigg) \Bigg) / \\
 & \left( \left( 15(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right], \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + \right. \right. \\
 & \left. \left. 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right], \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \right. \right. \right. \right.
 \end{aligned}$$



$$\begin{aligned}
 & \left. (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right]\right) \\
 & \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^5 + 3 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \\
 & \left(2 \left(2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right]\right) + \right. \\
 & \left. (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right]\right) \\
 & \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + 15(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)\right) \Bigg) / \\
 & \left(2(a^2 - b^2) \left(\frac{1}{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}\right)^{2/3} \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \right. \\
 & \left(9(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & 2 \left(2(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) \\
 & \left(15(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & 2 \left(2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & \left. (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right]\right) \Bigg)
 \end{aligned}$$



$$\begin{aligned}
 & \left( 2 (a - b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, \frac{(a - b) \tan\left[\frac{1}{2}(c + dx)\right]^2}{a + b}\right] + \right. \\
 & \quad \left. (a + b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, \frac{(a - b) \tan\left[\frac{1}{2}(c + dx)\right]^2}{a + b}\right] \right) \\
 & \tan\left[\frac{1}{2}(c + dx)\right]^5 + 3 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, \right. \\
 & \quad \left. \frac{(a - b) \tan\left[\frac{1}{2}(c + dx)\right]^2}{a + b}\right] \tan\left[\frac{1}{2}(c + dx)\right] \\
 & \left( 2 \left( 2 (a - b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, \frac{(a - b) \tan\left[\frac{1}{2}(c + dx)\right]^2}{a + b}\right] + \right. \right. \\
 & \quad \left. \left. (a + b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, \frac{(a - b) \tan\left[\frac{1}{2}(c + dx)\right]^2}{a + b}\right] \right) \right) \\
 & \tan\left[\frac{1}{2}(c + dx)\right]^2 + 15 (a + b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, \right. \\
 & \quad \left. \frac{(a - b) \tan\left[\frac{1}{2}(c + dx)\right]^2}{a + b}\right] \left( 1 + \tan\left[\frac{1}{2}(c + dx)\right]^2 \right) \right) \Bigg) / \\
 & \left( 2 (a^2 - b^2) \left( \frac{1}{1 - \tan\left[\frac{1}{2}(c + dx)\right]^2} \right)^{2/3} \left( -1 + \tan\left[\frac{1}{2}(c + dx)\right]^2 \right) \right) \\
 & \left( 9 (a + b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, \frac{(a - b) \tan\left[\frac{1}{2}(c + dx)\right]^2}{a + b}\right] + \right. \\
 & \quad 2 \left( 2 (a - b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, \frac{(a - b) \tan\left[\frac{1}{2}(c + dx)\right]^2}{a + b}\right] + \right. \\
 & \quad \left. (a + b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a - b) \tan\left[\frac{1}{2}(c + dx)\right]^2}{a + b}\right] \tan\left[\frac{1}{2}(c + dx)\right]^2 \right) \right) \\
 & \left( 15 (a + b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, \frac{(a - b) \tan\left[\frac{1}{2}(c + dx)\right]^2}{a + b}\right] + \right. \\
 & \quad \left. 2 \left( 2 (a - b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, \frac{(a - b) \tan\left[\frac{1}{2}(c + dx)\right]^2}{a + b}\right] + \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left( (a+b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \right. \\
 & \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \left( a \left( -1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) - b \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right)^2 \Bigg) + \\
 & \left( (a-b) (a+b) \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \right. \\
 & \left. \left( \frac{a+b - a \tan \left[ \frac{1}{2} (c+dx) \right]^2 + b \tan \left[ \frac{1}{2} (c+dx) \right]^2}{1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2} \right)^{1/3} \right. \\
 & \left. \left( 10 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \right. \\
 & \left. \left( 2 (a-b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) + \right. \\
 & \left. \left. (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \right) \\
 & \tan \left[ \frac{1}{2} (c+dx) \right]^5 + 3 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \\
 & \left. \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \tan \left[ \frac{1}{2} (c+dx) \right] \\
 & \left( 2 \left( 2 (a-b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) + \right. \\
 & \left. (a+b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \\
 & \tan \left[ \frac{1}{2} (c+dx) \right]^2 + 15 (a+b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \\
 & \left. \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) \Bigg) \Bigg) / \\
 & \left( 2 (a^2 - b^2) \left( \frac{1}{1 - \tan \left[ \frac{1}{2} (c+dx) \right]^2} \right)^{2/3} \left( -1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \left( 1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right)^{2/3} \right. \\
 & \left. \left( 9 (a+b) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[ \frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & 2 \left( 2 (a - b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \frac{(a - b) \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right]^2 + \right. \\
 & \quad (a + b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \right. \\
 & \quad \quad \left. \left. \frac{(a - b) \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] \right) \tan \left[ \frac{1}{2} (c + d x) \right]^2 \Bigg) \\
 & \left( 15 (a + b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \frac{(a - b) \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right]^2 + \right. \\
 & \quad 2 \left( 2 (a - b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \frac{(a - b) \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right]^2 + \right. \\
 & \quad \quad \left. (a + b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \frac{(a - b) \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right]^2 \right) \Bigg) \\
 & \quad \tan \left[ \frac{1}{2} (c + d x) \right]^2 \Bigg) \left( a \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) - b \left( 1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) \right) \Bigg) - \\
 & \left( 3 (a - b) (a + b) \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right] \left( 1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right)^{1/3} \right. \\
 & \quad \left. \left( \frac{a + b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2}{1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2} \right)^{1/3} \right) \\
 & \left( 10 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \frac{(a - b) \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right]^2 \right. \\
 & \quad \left( 2 (a - b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \frac{(a - b) \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right]^2 + \right. \\
 & \quad \quad \left. (a + b) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \frac{(a - b) \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right]^2 \right) \Bigg) \\
 & \quad \tan \left[ \frac{1}{2} (c + d x) \right]^5 + 3 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \right. \\
 & \quad \quad \left. \frac{(a - b) \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right] \tan \left[ \frac{1}{2} (c + d x) \right] \\
 & \quad \left( 2 \left( 2 (a - b) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \frac{(a - b) \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b} \right]^2 + \right. \right.
 \end{aligned}$$



$$\begin{aligned}
 & \left. (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \\
 & \tan\left[\frac{1}{2}(c+dx)\right]^2 + 15(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \right] \Bigg) / \\
 & \left( 2(a^2 - b^2) \left( \frac{1}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^{2/3} \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \right. \\
 & \left. \left( 9(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \right. \\
 & \left. \left. 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \right. \right. \\
 & \left. \left. (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right. \\
 & \left. \left( 15(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \right. \\
 & \left. \left. 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \right. \right. \\
 & \left. \left. \left. (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \right) \right. \\
 & \left. \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( a \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right] - \\
 & \left( (a-b)(a+b) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \left( \frac{1}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^{1/3} \right. \\
 & \left. \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^{1/3} \left( \frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^{1/3} \right. \\
 & \left. \left( 10 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( 2 (a - b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2, \frac{(a - b) \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2}{a + b}\right] + \right. \\
 & \quad \left. (a + b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2, \frac{(a - b) \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2}{a + b}\right] \right) \\
 & \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^5 + 3 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2, \right. \\
 & \quad \left. \frac{(a - b) \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2}{a + b}\right] \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right] \\
 & \left( 2 \left( 2 (a - b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2, \frac{(a - b) \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2}{a + b}\right] + \right. \right. \\
 & \quad \left. \left. (a + b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2, \frac{(a - b) \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2}{a + b}\right] \right) \right) \\
 & \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2 + 15 (a + b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2, \right. \\
 & \quad \left. \frac{(a - b) \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2}{a + b}\right] \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2 \right) \right) \Bigg) / \\
 & \left( (a^2 - b^2) \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2 \right) \left( 9 (a + b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \right. \right. \right. \\
 & \quad \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2, \frac{(a - b) \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2}{a + b}\right] + 2 \left( 2 (a - b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \right. \right. \\
 & \quad \left. \left. \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2, \frac{(a - b) \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2}{a + b}\right] + (a + b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \right. \right. \\
 & \quad \left. \left. \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2, \frac{(a - b) \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2}{a + b}\right] \right) \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2 \right) \\
 & \left( 15 (a + b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2, \frac{(a - b) \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2}{a + b}\right] + \right. \\
 & \quad \left. 2 \left( 2 (a - b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2, \frac{(a - b) \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2}{a + b}\right] + \right. \right. \\
 & \quad \left. \left. (a + b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2, \frac{(a - b) \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2}{a + b}\right] \right) \right)
 \end{aligned}$$



$$\begin{aligned}
& \left( 9 (a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
& 2 \left( 2 (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
& (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
& \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \left. \right) \\
& \left( 15 (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
& 2 \left( 2 (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
& (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \left. \right) \\
& \tan\left[\frac{1}{2}(c+dx)\right]^2 \left( a \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \left. \right) - \\
& \left( 3 (a-b) (a+b) \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^{1/3} \right. \\
& \left. \left( \frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^{1/3} \right. \\
& \left( 2 \left( 2 (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \right. \\
& (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \left. \right) \left. \right) \\
& \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + 9 (a+b) \left( \frac{1}{9 (a+b)} \right. \\
& 2 (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \\
& \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{9} \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right.
\end{aligned}$$

$$\begin{aligned}
 & \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) + \\
 & 2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \left( 2(a-b) \left( \frac{1}{a+b} (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{8}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \right. \\
 & \quad \left. \frac{1}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) + (a+b) \left( \frac{1}{5(a+b)} 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \frac{4}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \quad \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \frac{4}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{7}{3}, \frac{2}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) \\
 & \left( 10 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right. \\
 & \quad \left( 2(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + \right. \\
 & \quad \left. (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \\
 & \quad \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^5 + 3 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \quad \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \\
 & \quad \left( 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + \right. \right. \\
 & \quad \left. \left. (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \right) \\
 & \quad \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + 15(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \right) \right) \right) / \\
 & \left( 2(a^2 - b^2) \left( \frac{1}{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \right)^{2/3} \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right. \right. \\
 & \left. \left( 9(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \right. \\
 & \left. \left. 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \right. \right. \\
 & \left. \left. \left. (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) \\
 & \left( 15(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & \left. 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \right. \\
 & \left. \left. (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \right) \\
 & \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( a \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) - \\
 & \left( 3(a-b)(a+b) \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right)^{1/3} \right. \\
 & \left. \left( \frac{a+b - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \right)^{1/3} \right. \\
 & \left. \left( 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \right. \right. \\
 & \left. \left. \left. (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \right) \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + 15(a+b) \left( \frac{1}{5(a+b)} \right. \\
 & \quad \left. 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \quad \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + \\
 & \quad 2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \left( 2(a-b) \left( \frac{1}{21(a+b)} 25(a-b) \operatorname{AppellF1}\left[\frac{7}{2}, \frac{1}{3}, \frac{8}{3}, \right. \right. \right. \\
 & \quad \left. \left. \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right] + \frac{5}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{4}{3}, \frac{5}{3}, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) + \\
 & \quad (a+b) \left( \frac{1}{21(a+b)} 10(a-b) \operatorname{AppellF1}\left[\frac{7}{2}, \frac{4}{3}, \frac{5}{3}, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \quad \left. \frac{20}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{7}{3}, \frac{2}{3}, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \quad \left. \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) \\
 & \quad \left( 10 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \quad \left. \left( 2(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \right. \\
 & \quad \left. \left. (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \right) \\
 & \quad \tan\left[\frac{1}{2}(c+dx)\right]^5 + 3 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right.
 \end{aligned}$$

$$\begin{aligned}
 & \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \\
 & \left( 2 \left( 2 (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right]^2 + \right. \right. \\
 & \quad \left. \left. (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right]^2 \right) \right. \\
 & \quad \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + 15 (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \right) \right) / \\
 & \left( 2 (a^2 - b^2) \left( \frac{1}{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \right)^{2/3} \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right. \\
 & \quad \left( 9 (a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right]^2 + \right. \\
 & \quad 2 \left( 2 (a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right]^2 + \right. \\
 & \quad \left. (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \\
 & \quad \left( 15 (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right]^2 + \right. \\
 & \quad 2 \left( 2 (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right]^2 + \right. \\
 & \quad \left. (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \\
 & \left. \left( a \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) + \left( 3 (a-b) \right. \\
 & \left. (a+b) \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right)^{1/3} \right)
 \end{aligned}$$



$$\begin{aligned}
 & \left( \frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^{1/3} \\
 & \left( 25 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \quad \left. \left( 2(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) + \right. \\
 & \quad \left. (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \right) \\
 & \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^4 + \\
 & 10 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) + \\
 & \quad \left. (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \right) \\
 & \tan\left[\frac{1}{2}(c+dx)\right]^5 \left( \frac{1}{5(a+b)} 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \quad \left. \frac{1}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \quad \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) + \\
 & 10 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \\
 & \tan\left[\frac{1}{2}(c+dx)\right]^5 \left( 2(a-b) \left( \frac{1}{a+b} (a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{8}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \quad \left. \frac{1}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{5}{3}, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \right) \\
 & \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + (a+b) \left( \frac{1}{5(a+b)} 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left. \left. \frac{4}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \frac{4}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{7}{3}, \frac{2}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right] \right) \right) + \\
 & \frac{3}{2} \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \\
 & \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \left( 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \right. \\
 & \left. \left. (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \right) \\
 & \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + 15(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \left. \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) + \\
 & 3 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \left( \frac{1}{9(a+b)} 2(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \left. \left. \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \left. \frac{1}{9} \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \right) \\
 & \left( 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \right. \\
 & \left. \left. (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \right) \\
 & \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + 15(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) + \\
 3 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \\
 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] & \left(15(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \\
 2 \left(2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \\
 15(a+b) & \left(\frac{1}{5(a+b)} 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \left. \frac{1}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) + \\
 2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 & \left(2(a-b) \left(\frac{1}{21(a+b)} 25(a-b) \operatorname{AppellF1}\left[\frac{7}{2}, \frac{1}{3}, \frac{8}{3}, \right. \right. \right. \\
 & \left. \left. \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \frac{5}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{4}{3}, \frac{5}{3}, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) + \\
 (a+b) & \left(\frac{1}{21(a+b)} 10(a-b) \operatorname{AppellF1}\left[\frac{7}{2}, \frac{4}{3}, \frac{5}{3}, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right.
 \end{aligned}$$

$$\begin{aligned}
& \left. \left. \left. \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \right. \right. \right. \right. \right. \\
& \left. \left. \left. \left. \frac{20}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{7}{3}, \frac{2}{3}, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right], \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \right. \right. \right. \\
& \left. \left. \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right] \right] \right] \right] \right] \right] / \\
& \left( 2(a^2 - b^2) \left( \frac{1}{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \right)^{2/3} \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right. \\
& \left. \left( 9(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, \frac{2}{3}, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right], \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \right. \\
& \left. \left. 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{5}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right], \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \right. \\
& \left. \left. (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right], \right. \right. \\
& \left. \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right. \\
& \left. \left( 15(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \frac{2}{3}, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right], \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
& \left. \left. 2 \left( 2(a-b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \frac{5}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right], \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \right. \\
& \left. \left. (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, \frac{2}{3}, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right], \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \right) \\
& \left. \left. \left. \left. \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( a \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) \right) \right) \right) \right)
\end{aligned}$$

**Problem 713: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Sec}[c+dx]^{2/3}}{a+b \operatorname{Sec}[c+dx]} dx$$

Optimal (type 6, 174 leaves, 6 steps):

$$\frac{a \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{6}, 1, \frac{3}{2}, \sin[c+dx]^2, \frac{a^2 \sin[c+dx]^2}{a^2-b^2}\right] \sin[c+dx]}{(a^2-b^2) d (\cos[c+dx]^2)^{1/6} \operatorname{Sec}[c+dx]^{1/3}} -$$

$$\frac{1}{(a^2-b^2) d} b \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \sin[c+dx]^2, \frac{a^2 \sin[c+dx]^2}{a^2-b^2}\right]$$

$$(\cos[c+dx]^2)^{1/3} \operatorname{Sec}[c+dx]^{2/3} \sin[c+dx]$$

Result (type 6, 4609 leaves):

$$\left( 9 (a^2 - b^2) \operatorname{Sec}[c+dx]^{5/3} \sin[c+dx] \right.$$

$$\left( \left( b \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{6}, 1, \frac{3}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2}\right] \sqrt{1+\tan[c+dx]^2} \right) / \right.$$

$$\left( 9 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{6}, 1, \frac{3}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2}\right] + \right.$$

$$\left( 6 b^2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{6}, 2, \frac{5}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2}\right] + \right.$$

$$\left. \left. (-a^2 + b^2) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{7}{6}, 1, \frac{5}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2}\right] \right) \tan[c+dx]^2 \right) +$$

$$\left( a \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2}\right] \right) /$$

$$\left( -9 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2}\right] - \right.$$

$$2 \left( 3 b^2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2}\right] + 2 (-a^2 + b^2) \right.$$

$$\left. \left. \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2}\right] \right) \tan[c+dx]^2 \right) \right) /$$

$$\left( d (a + b \operatorname{Sec}[c+dx]) (1 + \tan[c+dx]^2)^{2/3} (-a^2 + b^2 (1 + \tan[c+dx]^2)) \right.$$

$$\left( - \frac{1}{(1 + \tan[c+dx]^2)^{2/3} (-a^2 + b^2 (1 + \tan[c+dx]^2))^2} 18 b^2 (a^2 - b^2) \operatorname{Sec}[c+dx]^2 \tan[c+dx]^2 \right.$$

$$\left( \left( b \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{6}, 1, \frac{3}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2}\right] \sqrt{1+\tan[c+dx]^2} \right) / \right.$$

$$\left( 9 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{6}, 1, \frac{3}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2}\right] + \right.$$

$$\left( 6 b^2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{6}, 2, \frac{5}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2}\right] + (-a^2 + b^2) \right.$$

$$\left. \left. \operatorname{AppellF1}\left[\frac{3}{2}, \frac{7}{6}, 1, \frac{5}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2}\right] \right) \tan[c+dx]^2 \right) +$$

$$\left( a \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2}\right] \right) /$$

$$\left( -9 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2}\right] - \right.$$

$$\begin{aligned}
& 2 \left( 3 b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] + 2 \left( -a^2 + b^2 \right) \right. \\
& \quad \left. \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] \right) \tan [c+d x]^2 \Bigg) - \\
& \quad \frac{1}{(1+\tan [c+d x]^2)^{5/3} \left( -a^2 + b^2 (1+\tan [c+d x]^2) \right)} 12 \left( a^2 - b^2 \right) \operatorname{Sec} [c+d x]^2 \tan [c+d x]^2 \\
& \quad \left( \left( b \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{6}, 1, \frac{3}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] \sqrt{1+\tan [c+d x]^2} \right) / \right. \\
& \quad \left( 9 \left( a^2 - b^2 \right) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{6}, 1, \frac{3}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] + \right. \\
& \quad \left( 6 b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{6}, 2, \frac{5}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] + \left( -a^2 + b^2 \right) \right. \\
& \quad \left. \left. \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{7}{6}, 1, \frac{5}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] \right) \tan [c+d x]^2 \right) + \\
& \quad \left( a \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] \right) / \\
& \quad \left( -9 \left( a^2 - b^2 \right) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] - \right. \\
& \quad \left. 2 \left( 3 b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] + 2 \left( -a^2 + b^2 \right) \right. \right. \\
& \quad \left. \left. \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] \right) \tan [c+d x]^2 \right) \Bigg) + \\
& \quad \frac{1}{(1+\tan [c+d x]^2)^{2/3} \left( -a^2 + b^2 (1+\tan [c+d x]^2) \right)} 9 \left( a^2 - b^2 \right) \operatorname{Sec} [c+d x]^2 \\
& \quad \left( \left( b \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{6}, 1, \frac{3}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] \sqrt{1+\tan [c+d x]^2} \right) / \right. \\
& \quad \left( 9 \left( a^2 - b^2 \right) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{6}, 1, \frac{3}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] + \right. \\
& \quad \left( 6 b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{6}, 2, \frac{5}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] + \left( -a^2 + b^2 \right) \right. \\
& \quad \left. \left. \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{7}{6}, 1, \frac{5}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] \right) \tan [c+d x]^2 \right) + \\
& \quad \left( a \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] \right) / \\
& \quad \left( -9 \left( a^2 - b^2 \right) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] - \right. \\
& \quad \left. 2 \left( 3 b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] + 2 \left( -a^2 + b^2 \right) \right. \right. \\
& \quad \left. \left. \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] \right) \tan [c+d x]^2 \right) \Bigg) + \\
& \quad \frac{1}{(1+\tan [c+d x]^2)^{2/3} \left( -a^2 + b^2 (1+\tan [c+d x]^2) \right)} 9 \left( a^2 - b^2 \right) \tan [c+d x]
\end{aligned}$$

$$\begin{aligned}
 & \left( \left( b \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{6}, 1, \frac{3}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2} \right] \operatorname{Sec}[c+dx]^2 \tan[c+dx] \right) / \right. \\
 & \quad \left( \sqrt{1+\tan[c+dx]^2} \right. \\
 & \quad \left( 9(a^2-b^2) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{6}, 1, \frac{3}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2} \right] + \right. \\
 & \quad \left( 6b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{6}, 2, \frac{5}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2} \right] + (-a^2+b^2) \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{7}{6}, 1, \frac{5}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2} \right] \right) \tan[c+dx]^2 \right) \right) + \\
 & \left( b \left( \frac{1}{3(a^2-b^2)} 2b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{6}, 2, \frac{5}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2} \right] \right. \right. \\
 & \quad \left. \operatorname{Sec}[c+dx]^2 \tan[c+dx] - \frac{1}{9} \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{7}{6}, 1, \frac{5}{2}, -\tan[c+dx]^2, \right. \right. \\
 & \quad \left. \left. \frac{b^2 \tan[c+dx]^2}{a^2-b^2} \right] \operatorname{Sec}[c+dx]^2 \tan[c+dx] \right) \sqrt{1+\tan[c+dx]^2} \right) / \\
 & \left( 9(a^2-b^2) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{6}, 1, \frac{3}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2} \right] + \right. \\
 & \left( 6b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{6}, 2, \frac{5}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2} \right] + (-a^2+b^2) \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{7}{6}, 1, \frac{5}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2} \right] \right) \tan[c+dx]^2 \right) + \\
 & \left( a \left( \frac{1}{3(a^2-b^2)} 2b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2} \right] \right. \right. \\
 & \quad \left. \operatorname{Sec}[c+dx]^2 \tan[c+dx] - \frac{4}{9} \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \right. \right. \\
 & \quad \left. \left. -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2} \right] \operatorname{Sec}[c+dx]^2 \tan[c+dx] \right) \right) / \\
 & \left( -9(a^2-b^2) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2} \right] - \right. \\
 & \left. 2 \left( 3b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2} \right] + 2(-a^2+b^2) \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2} \right] \right) \tan[c+dx]^2 \right) - \\
 & \left( b \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{6}, 1, \frac{3}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2} \right] \sqrt{1+\tan[c+dx]^2} \right. \\
 & \quad \left( 2 \left( 6b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{6}, 2, \frac{5}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2} \right] + \right. \right. \\
 & \quad \left. \left. (-a^2+b^2) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{7}{6}, 1, \frac{5}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2} \right] \right) \right) \\
 & \quad \left. \operatorname{Sec}[c+dx]^2 \tan[c+dx] + 9(a^2-b^2) \left( \frac{1}{3(a^2-b^2)} 2b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{6}, 2, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left( \frac{5}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2} \right) \operatorname{Sec}[c+dx]^2 \tan[c+dx] - \frac{1}{9} \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{7}{6}, 1, \frac{5}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2} \right] \operatorname{Sec}[c+dx]^2 \tan[c+dx] \right) + \\
 & \tan[c+dx]^2 \left( 6b^2 \left( \frac{1}{5(a^2-b^2)} 12b^2 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{6}, 3, \frac{7}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2} \right] \operatorname{Sec}[c+dx]^2 \tan[c+dx] - \frac{1}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{7}{6}, 2, \frac{7}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2} \right] \operatorname{Sec}[c+dx]^2 \tan[c+dx] \right) + \right. \\
 & \left. (-a^2+b^2) \left( \frac{1}{5(a^2-b^2)} 6b^2 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{7}{6}, 2, \frac{7}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2} \right] \operatorname{Sec}[c+dx]^2 \tan[c+dx] - \frac{7}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{13}{6}, 1, \frac{7}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2} \right] \operatorname{Sec}[c+dx]^2 \tan[c+dx] \right) \right) \Big) \Big) \Big) / \\
 & \left( 9(a^2-b^2) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{6}, 1, \frac{3}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2} \right] + \right. \\
 & \left. \left( 6b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{6}, 2, \frac{5}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2} \right] + (-a^2+b^2) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{7}{6}, 1, \frac{5}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2} \right] \right) \tan[c+dx]^2 \right)^2 - \\
 & \left( a \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2} \right] \right. \\
 & \left. \left( -4 \left( 3b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2} \right] + \right. \right. \right. \\
 & \left. \left. 2(-a^2+b^2) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2} \right] \right) \right. \\
 & \left. \operatorname{Sec}[c+dx]^2 \tan[c+dx] - 9(a^2-b^2) \left( \frac{1}{3(a^2-b^2)} 2b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2} \right] \operatorname{Sec}[c+dx]^2 \tan[c+dx] - \frac{4}{9} \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2} \right] \operatorname{Sec}[c+dx]^2 \tan[c+dx] \right) \right) - \\
 & 2 \tan[c+dx]^2 \left( 3b^2 \left( \frac{1}{5(a^2-b^2)} 12b^2 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, 3, \frac{7}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2} \right] \operatorname{Sec}[c+dx]^2 \tan[c+dx] - \frac{4}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, 2, \frac{7}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2} \right] \operatorname{Sec}[c+dx]^2 \tan[c+dx] \right) + \right. \\
 & \left. \left. \left( \frac{1}{5(a^2-b^2)} 12b^2 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, 3, \frac{7}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2} \right] \operatorname{Sec}[c+dx]^2 \tan[c+dx] - \frac{4}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, 2, \frac{7}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2} \right] \operatorname{Sec}[c+dx]^2 \tan[c+dx] \right) \right) \right)
 \end{aligned}$$





$$\begin{aligned}
 & \left. \left. \left. \text{AppellF1}\left[\frac{3}{2}, \frac{11}{6}, 1, \frac{5}{2}, -\text{Tan}[c+dx]^2, \frac{b^2 \text{Tan}[c+dx]^2}{a^2-b^2}\right] \text{Tan}[c+dx]^2\right)\right)\right) / \\
 & \left( d (a+b \text{Sec}[c+dx]) (1+\text{Tan}[c+dx]^2)^{5/6} (-a^2+b^2 (1+\text{Tan}[c+dx]^2)) \right. \\
 & \left( -\frac{1}{(1+\text{Tan}[c+dx]^2)^{5/6} (-a^2+b^2 (1+\text{Tan}[c+dx]^2))^2} 18 b^2 (a^2-b^2) \text{Sec}[c+dx]^2 \text{Tan}[c+dx]^2 \right. \\
 & \left. \left( \left( b \text{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, -\text{Tan}[c+dx]^2, \frac{b^2 \text{Tan}[c+dx]^2}{a^2-b^2}\right] \sqrt{1+\text{Tan}[c+dx]^2}\right) / \right. \right. \\
 & \left. \left( 9 (a^2-b^2) \text{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, -\text{Tan}[c+dx]^2, \frac{b^2 \text{Tan}[c+dx]^2}{a^2-b^2}\right] + \right. \right. \\
 & \left. \left. 2 \left( 3 b^2 \text{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, -\text{Tan}[c+dx]^2, \frac{b^2 \text{Tan}[c+dx]^2}{a^2-b^2}\right] + (-a^2+b^2) \right. \right. \right. \\
 & \left. \left. \left. \text{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, -\text{Tan}[c+dx]^2, \frac{b^2 \text{Tan}[c+dx]^2}{a^2-b^2}\right] \right) \text{Tan}[c+dx]^2 \right) \right) + \\
 & \left( a \text{AppellF1}\left[\frac{1}{2}, \frac{5}{6}, 1, \frac{3}{2}, -\text{Tan}[c+dx]^2, \frac{b^2 \text{Tan}[c+dx]^2}{a^2-b^2}\right] \right) / \\
 & \left( -9 (a^2-b^2) \text{AppellF1}\left[\frac{1}{2}, \frac{5}{6}, 1, \frac{3}{2}, -\text{Tan}[c+dx]^2, \frac{b^2 \text{Tan}[c+dx]^2}{a^2-b^2}\right] + \right. \\
 & \left( -6 b^2 \text{AppellF1}\left[\frac{3}{2}, \frac{5}{6}, 2, \frac{5}{2}, -\text{Tan}[c+dx]^2, \frac{b^2 \text{Tan}[c+dx]^2}{a^2-b^2}\right] + 5 (a^2-b^2) \right. \\
 & \left. \left. \left. \left. \left. \left. \text{AppellF1}\left[\frac{3}{2}, \frac{11}{6}, 1, \frac{5}{2}, -\text{Tan}[c+dx]^2, \frac{b^2 \text{Tan}[c+dx]^2}{a^2-b^2}\right] \right) \text{Tan}[c+dx]^2 \right) \right) \right) \right) - \\
 & \frac{1}{(1+\text{Tan}[c+dx]^2)^{11/6} (-a^2+b^2 (1+\text{Tan}[c+dx]^2))} 15 (a^2-b^2) \text{Sec}[c+dx]^2 \text{Tan}[c+dx]^2 \\
 & \left( \left( b \text{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, -\text{Tan}[c+dx]^2, \frac{b^2 \text{Tan}[c+dx]^2}{a^2-b^2}\right] \sqrt{1+\text{Tan}[c+dx]^2}\right) / \right. \\
 & \left( 9 (a^2-b^2) \text{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, -\text{Tan}[c+dx]^2, \frac{b^2 \text{Tan}[c+dx]^2}{a^2-b^2}\right] + \right. \\
 & \left. 2 \left( 3 b^2 \text{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, -\text{Tan}[c+dx]^2, \frac{b^2 \text{Tan}[c+dx]^2}{a^2-b^2}\right] + (-a^2+b^2) \right. \right. \\
 & \left. \left. \left. \left. \left. \left. \text{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, -\text{Tan}[c+dx]^2, \frac{b^2 \text{Tan}[c+dx]^2}{a^2-b^2}\right] \right) \text{Tan}[c+dx]^2 \right) \right) \right) + \\
 & \left( a \text{AppellF1}\left[\frac{1}{2}, \frac{5}{6}, 1, \frac{3}{2}, -\text{Tan}[c+dx]^2, \frac{b^2 \text{Tan}[c+dx]^2}{a^2-b^2}\right] \right) / \\
 & \left( -9 (a^2-b^2) \text{AppellF1}\left[\frac{1}{2}, \frac{5}{6}, 1, \frac{3}{2}, -\text{Tan}[c+dx]^2, \frac{b^2 \text{Tan}[c+dx]^2}{a^2-b^2}\right] + \right. \\
 & \left( -6 b^2 \text{AppellF1}\left[\frac{3}{2}, \frac{5}{6}, 2, \frac{5}{2}, -\text{Tan}[c+dx]^2, \frac{b^2 \text{Tan}[c+dx]^2}{a^2-b^2}\right] + 5 (a^2-b^2) \right. \\
 & \left. \left. \left. \left. \left. \left. \text{AppellF1}\left[\frac{3}{2}, \frac{11}{6}, 1, \frac{5}{2}, -\text{Tan}[c+dx]^2, \frac{b^2 \text{Tan}[c+dx]^2}{a^2-b^2}\right] \right) \text{Tan}[c+dx]^2 \right) \right) \right) \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{(1 + \tan[c + dx])^{5/6} (-a^2 + b^2 (1 + \tan[c + dx]^2))} 9 (a^2 - b^2) \sec[c + dx]^2 \\
 & \left( \left( b \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, -\tan[c + dx]^2, \frac{b^2 \tan[c + dx]^2}{a^2 - b^2} \right] \sqrt{1 + \tan[c + dx]^2} \right) / \right. \\
 & \quad \left( 9 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, -\tan[c + dx]^2, \frac{b^2 \tan[c + dx]^2}{a^2 - b^2} \right] + \right. \\
 & \quad \left. 2 \left( 3 b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, -\tan[c + dx]^2, \frac{b^2 \tan[c + dx]^2}{a^2 - b^2} \right] + (-a^2 + b^2) \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, -\tan[c + dx]^2, \frac{b^2 \tan[c + dx]^2}{a^2 - b^2} \right] \right) \tan[c + dx]^2 \right) + \\
 & \quad \left( a \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{5}{6}, 1, \frac{3}{2}, -\tan[c + dx]^2, \frac{b^2 \tan[c + dx]^2}{a^2 - b^2} \right] \right) / \\
 & \quad \left( -9 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{5}{6}, 1, \frac{3}{2}, -\tan[c + dx]^2, \frac{b^2 \tan[c + dx]^2}{a^2 - b^2} \right] + \right. \\
 & \quad \left( -6 b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{6}, 2, \frac{5}{2}, -\tan[c + dx]^2, \frac{b^2 \tan[c + dx]^2}{a^2 - b^2} \right] + 5 (a^2 - b^2) \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{11}{6}, 1, \frac{5}{2}, -\tan[c + dx]^2, \frac{b^2 \tan[c + dx]^2}{a^2 - b^2} \right] \right) \tan[c + dx]^2 \right) \Big) + \\
 & \frac{1}{(1 + \tan[c + dx])^{5/6} (-a^2 + b^2 (1 + \tan[c + dx]^2))} 9 (a^2 - b^2) \tan[c + dx] \\
 & \left( \left( b \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, -\tan[c + dx]^2, \frac{b^2 \tan[c + dx]^2}{a^2 - b^2} \right] \sec[c + dx]^2 \tan[c + dx] \right) / \right. \\
 & \quad \left( \sqrt{1 + \tan[c + dx]^2} \right. \\
 & \quad \left( 9 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, -\tan[c + dx]^2, \frac{b^2 \tan[c + dx]^2}{a^2 - b^2} \right] + \right. \\
 & \quad \left. 2 \left( 3 b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, -\tan[c + dx]^2, \frac{b^2 \tan[c + dx]^2}{a^2 - b^2} \right] + (-a^2 + b^2) \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, -\tan[c + dx]^2, \frac{b^2 \tan[c + dx]^2}{a^2 - b^2} \right] \right) \tan[c + dx]^2 \right) \Big) + \\
 & \quad \left( b \left( \frac{1}{3 (a^2 - b^2)} 2 b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, -\tan[c + dx]^2, \frac{b^2 \tan[c + dx]^2}{a^2 - b^2} \right] \right. \right. \\
 & \quad \left. \left. \sec[c + dx]^2 \tan[c + dx] - \frac{2}{9} \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, -\tan[c + dx]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{b^2 \tan[c + dx]^2}{a^2 - b^2} \right] \sec[c + dx]^2 \tan[c + dx] \right) \sqrt{1 + \tan[c + dx]^2} \right) / \\
 & \quad \left( 9 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, -\tan[c + dx]^2, \frac{b^2 \tan[c + dx]^2}{a^2 - b^2} \right] + \right. \\
 & \quad \left. 2 \left( 3 b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, -\tan[c + dx]^2, \frac{b^2 \tan[c + dx]^2}{a^2 - b^2} \right] + (-a^2 + b^2) \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, -\tan[c + dx]^2, \frac{b^2 \tan[c + dx]^2}{a^2 - b^2} \right] \right) \tan[c + dx]^2 \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \left( a \left( \frac{1}{3(a^2 - b^2)} 2 b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{6}, 2, \frac{5}{2}, -\operatorname{Tan}[c + d x]^2, \frac{b^2 \operatorname{Tan}[c + d x]^2}{a^2 - b^2} \right] \right. \right. \\
 & \quad \left. \left. \operatorname{Sec}[c + d x]^2 \operatorname{Tan}[c + d x] - \frac{5}{9} \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{11}{6}, 1, \frac{5}{2}, \right. \right. \right. \\
 & \quad \left. \left. \left. -\operatorname{Tan}[c + d x]^2, \frac{b^2 \operatorname{Tan}[c + d x]^2}{a^2 - b^2} \right] \operatorname{Sec}[c + d x]^2 \operatorname{Tan}[c + d x] \right) \right) / \\
 & \left( -9(a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{5}{6}, 1, \frac{3}{2}, -\operatorname{Tan}[c + d x]^2, \frac{b^2 \operatorname{Tan}[c + d x]^2}{a^2 - b^2} \right] + \right. \\
 & \quad \left( -6 b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{6}, 2, \frac{5}{2}, -\operatorname{Tan}[c + d x]^2, \frac{b^2 \operatorname{Tan}[c + d x]^2}{a^2 - b^2} \right] + 5(a^2 - b^2) \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{11}{6}, 1, \frac{5}{2}, -\operatorname{Tan}[c + d x]^2, \frac{b^2 \operatorname{Tan}[c + d x]^2}{a^2 - b^2} \right] \right) \operatorname{Tan}[c + d x]^2 \right) - \\
 & \left( b \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, -\operatorname{Tan}[c + d x]^2, \frac{b^2 \operatorname{Tan}[c + d x]^2}{a^2 - b^2} \right] \sqrt{1 + \operatorname{Tan}[c + d x]^2} \right. \\
 & \quad \left( 4 \left( 3 b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, -\operatorname{Tan}[c + d x]^2, \frac{b^2 \operatorname{Tan}[c + d x]^2}{a^2 - b^2} \right] + \right. \right. \\
 & \quad \left. \left. (-a^2 + b^2) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, -\operatorname{Tan}[c + d x]^2, \frac{b^2 \operatorname{Tan}[c + d x]^2}{a^2 - b^2} \right] \right) \right. \\
 & \quad \left. \operatorname{Sec}[c + d x]^2 \operatorname{Tan}[c + d x] + 9(a^2 - b^2) \left( \frac{1}{3(a^2 - b^2)} 2 b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 2, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{5}{2}, -\operatorname{Tan}[c + d x]^2, \frac{b^2 \operatorname{Tan}[c + d x]^2}{a^2 - b^2} \right] \operatorname{Sec}[c + d x]^2 \operatorname{Tan}[c + d x] - \frac{2}{9} \operatorname{AppellF1} \left[ \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, -\operatorname{Tan}[c + d x]^2, \frac{b^2 \operatorname{Tan}[c + d x]^2}{a^2 - b^2} \right] \operatorname{Sec}[c + d x]^2 \operatorname{Tan}[c + d x] \right) \right) + \\
 & \quad 2 \operatorname{Tan}[c + d x]^2 \left( 3 b^2 \left( \frac{1}{5(a^2 - b^2)} 12 b^2 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, 3, \frac{7}{2}, -\operatorname{Tan}[c + d x]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{b^2 \operatorname{Tan}[c + d x]^2}{a^2 - b^2} \right] \operatorname{Sec}[c + d x]^2 \operatorname{Tan}[c + d x] - \frac{2}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}, 2, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{7}{2}, -\operatorname{Tan}[c + d x]^2, \frac{b^2 \operatorname{Tan}[c + d x]^2}{a^2 - b^2} \right] \operatorname{Sec}[c + d x]^2 \operatorname{Tan}[c + d x] \right) \right) + \\
 & \quad (-a^2 + b^2) \left( \frac{1}{5(a^2 - b^2)} 6 b^2 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}, 2, \frac{7}{2}, -\operatorname{Tan}[c + d x]^2, \right. \right. \\
 & \quad \left. \left. \frac{b^2 \operatorname{Tan}[c + d x]^2}{a^2 - b^2} \right] \operatorname{Sec}[c + d x]^2 \operatorname{Tan}[c + d x] - \frac{8}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{7}{3}, 1, \right. \right. \\
 & \quad \left. \left. \frac{7}{2}, -\operatorname{Tan}[c + d x]^2, \frac{b^2 \operatorname{Tan}[c + d x]^2}{a^2 - b^2} \right] \operatorname{Sec}[c + d x]^2 \operatorname{Tan}[c + d x] \right) \right) \right) / \\
 & \left( 9(a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, -\operatorname{Tan}[c + d x]^2, \frac{b^2 \operatorname{Tan}[c + d x]^2}{a^2 - b^2} \right] + \right. \\
 & \quad \left. 2 \left( 3 b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, -\operatorname{Tan}[c + d x]^2, \frac{b^2 \operatorname{Tan}[c + d x]^2}{a^2 - b^2} \right] + (-a^2 + b^2) \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \text{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2}\right] \tan[c+dx]^2 \Big)^2 - \\
 & \left( a \text{AppellF1}\left[\frac{1}{2}, \frac{5}{6}, 1, \frac{3}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2}\right] \right. \\
 & \left( 2 \left( -6 b^2 \text{AppellF1}\left[\frac{3}{2}, \frac{5}{6}, 2, \frac{5}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2}\right] + \right. \right. \\
 & \left. \left. 5 (a^2-b^2) \text{AppellF1}\left[\frac{3}{2}, \frac{11}{6}, 1, \frac{5}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2}\right] \right) \right. \\
 & \left. \sec[c+dx]^2 \tan[c+dx] - 9 (a^2-b^2) \left( \frac{1}{3 (a^2-b^2)} 2 b^2 \text{AppellF1}\left[\frac{3}{2}, \frac{5}{6}, 2, \right. \right. \right. \\
 & \left. \left. \frac{5}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2}\right] \sec[c+dx]^2 \tan[c+dx] - \frac{5}{9} \text{AppellF1}\left[ \right. \right. \\
 & \left. \left. \frac{3}{2}, \frac{11}{6}, 1, \frac{5}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2}\right] \sec[c+dx]^2 \tan[c+dx] \right) \Big) + \\
 & \tan[c+dx]^2 \left( -6 b^2 \left( \frac{1}{5 (a^2-b^2)} 12 b^2 \text{AppellF1}\left[\frac{5}{2}, \frac{5}{6}, 3, \frac{7}{2}, -\tan[c+dx]^2, \right. \right. \right. \\
 & \left. \left. \frac{b^2 \tan[c+dx]^2}{a^2-b^2}\right] \sec[c+dx]^2 \tan[c+dx] - \text{AppellF1}\left[\frac{5}{2}, \frac{11}{6}, 2, \right. \right. \\
 & \left. \left. \frac{7}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2}\right] \sec[c+dx]^2 \tan[c+dx] \right) + \\
 & 5 (a^2-b^2) \left( \frac{1}{5 (a^2-b^2)} 6 b^2 \text{AppellF1}\left[\frac{5}{2}, \frac{11}{6}, 2, \frac{7}{2}, -\tan[c+dx]^2, \right. \right. \\
 & \left. \left. \frac{b^2 \tan[c+dx]^2}{a^2-b^2}\right] \sec[c+dx]^2 \tan[c+dx] - \frac{11}{5} \text{AppellF1}\left[\frac{5}{2}, \frac{17}{6}, 1, \right. \right. \\
 & \left. \left. \frac{7}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2}\right] \sec[c+dx]^2 \tan[c+dx] \right) \Big) \Big) \Big) \Big) \Big) / \\
 & \left( -9 (a^2-b^2) \text{AppellF1}\left[\frac{1}{2}, \frac{5}{6}, 1, \frac{3}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2}\right] + \right. \\
 & \left( -6 b^2 \text{AppellF1}\left[\frac{3}{2}, \frac{5}{6}, 2, \frac{5}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2}\right] + 5 (a^2-b^2) \right. \\
 & \left. \left. \text{AppellF1}\left[\frac{3}{2}, \frac{11}{6}, 1, \frac{5}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2}\right] \tan[c+dx]^2 \right) \right) \Big) \Big) \Big) \Big) \Big)
 \end{aligned}$$

**Problem 715: Result more than twice size of optimal antiderivative.**

$$\int \frac{1}{\sec[c+dx]^{1/3} (a+b \sec[c+dx])} dx$$

Optimal (type 6, 174 leaves, 6 steps):

$$\begin{aligned}
& - \frac{b \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{6}, 1, \frac{3}{2}, \sin[c+dx]^2, \frac{a^2 \sin[c+dx]^2}{a^2-b^2}\right] \sin[c+dx]}{(a^2-b^2) d (\cos[c+dx]^2)^{1/6} \operatorname{Sec}[c+dx]^{1/3}} + \\
& \frac{1}{(a^2-b^2) d} a \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{2}{3}, 1, \frac{3}{2}, \sin[c+dx]^2, \frac{a^2 \sin[c+dx]^2}{a^2-b^2}\right] \\
& (\cos[c+dx]^2)^{1/3} \operatorname{Sec}[c+dx]^{2/3} \sin[c+dx]
\end{aligned}$$

Result (type 6, 9174 leaves):

$$\begin{aligned}
& \left( \left( \frac{\operatorname{Sec}[c+dx]^{2/3}}{2(b+a \cos[c+dx])} + \frac{\cos[2(c+dx)] \operatorname{Sec}[c+dx]^{2/3}}{2(b+a \cos[c+dx])} \right) \right. \\
& \operatorname{Tan}[c+dx] \left( \left( 9(2a^4 - 5a^2b^2 + 3b^4) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{6}, 1, \right. \right. \right. \\
& \left. \left. \left. \frac{3}{2}, -\operatorname{Tan}[c+dx]^2, \frac{b^2 \operatorname{Tan}[c+dx]^2}{a^2-b^2}\right] \sqrt{1+\operatorname{Tan}[c+dx]^2} \right) / \right. \\
& \left( a \left( -9(a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{6}, 1, \frac{3}{2}, -\operatorname{Tan}[c+dx]^2, \frac{b^2 \operatorname{Tan}[c+dx]^2}{a^2-b^2}\right] + \right. \right. \\
& \left( -6b^2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{6}, 2, \frac{5}{2}, -\operatorname{Tan}[c+dx]^2, \frac{b^2 \operatorname{Tan}[c+dx]^2}{a^2-b^2}\right] + \right. \\
& \left. \left. (a^2-b^2) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{7}{6}, 1, \frac{5}{2}, -\operatorname{Tan}[c+dx]^2, \frac{b^2 \operatorname{Tan}[c+dx]^2}{a^2-b^2}\right] \right) \right) \\
& \left. \operatorname{Tan}[c+dx]^2 \right) (a^2-b^2(1+\operatorname{Tan}[c+dx]^2)) \left. \right) - \\
& \left( 9b(-a^2+b^2) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, -\operatorname{Tan}[c+dx]^2, \frac{b^2 \operatorname{Tan}[c+dx]^2}{a^2-b^2}\right] \right) / \\
& \left( \left( 9(a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, -\operatorname{Tan}[c+dx]^2, \frac{b^2 \operatorname{Tan}[c+dx]^2}{a^2-b^2}\right] + \right. \right. \\
& \left. \left. 2 \left( 3b^2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, -\operatorname{Tan}[c+dx]^2, \frac{b^2 \operatorname{Tan}[c+dx]^2}{a^2-b^2}\right] + \right. \right. \right. \\
& \left. \left. \left. 2(-a^2+b^2) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, -\operatorname{Tan}[c+dx]^2, \frac{b^2 \operatorname{Tan}[c+dx]^2}{a^2-b^2}\right] \right) \right) \right) \\
& \left. \operatorname{Tan}[c+dx]^2 \right) (-a^2+b^2(1+\operatorname{Tan}[c+dx]^2)) \left. \right) - \\
& \left( \sqrt{1+\operatorname{Tan}[c+dx]^2} \left( 3 \left( -6b^2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{6}, 2, \frac{7}{2}, -\operatorname{Tan}[c+dx]^2, \frac{b^2 \operatorname{Tan}[c+dx]^2}{a^2-b^2}\right] + \right. \right. \right. \\
& \left. \left. \left. (a^2-b^2) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{7}{6}, 1, \frac{7}{2}, -\operatorname{Tan}[c+dx]^2, \frac{b^2 \operatorname{Tan}[c+dx]^2}{a^2-b^2}\right] \right) \right) \right) \\
& \operatorname{Tan}[c+dx]^2 (-a^2+b^2(1+\operatorname{Tan}[c+dx]^2)) + 5(a^2-b^2) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{6}, 1, \right. \\
& \left. \left. \frac{5}{2}, -\operatorname{Tan}[c+dx]^2, \frac{b^2 \operatorname{Tan}[c+dx]^2}{a^2-b^2}\right] (9a^2-b^2(9+7 \operatorname{Tan}[c+dx]^2)) \right) / \\
& \left( a \left( -15(a^2-b^2) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{6}, 1, \frac{5}{2}, -\operatorname{Tan}[c+dx]^2, \frac{b^2 \operatorname{Tan}[c+dx]^2}{a^2-b^2}\right] + \right. \right.
\end{aligned}$$

$$\begin{aligned}
 & \left( -6 b^2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{6}, 2, \frac{7}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2}\right] + \right. \\
 & \quad \left. (a^2-b^2) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{7}{6}, 1, \frac{7}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2}\right] \right) \tan[c+dx]^2 \\
 & \left. (a^2-b^2 (1+\tan[c+dx]^2)) \right) \Big/ \left( d (1+\tan[c+dx]^2)^{2/3} \right. \\
 & \left. \left( -\frac{1}{3 (1+\tan[c+dx]^2)^{5/3}} 4 \operatorname{Sec}[c+dx]^2 \tan[c+dx]^2 \left( \left( 9 (2 a^4 - 5 a^2 b^2 + 3 b^4) \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{6}, 1, \frac{3}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2}\right] \sqrt{1+\tan[c+dx]^2} \right) \right) \right) \Big/ \\
 & \left( a \left( -9 (a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{6}, 1, \frac{3}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2}\right] + \right. \right. \\
 & \quad \left( -6 b^2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{6}, 2, \frac{5}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2}\right] + \right. \\
 & \quad \left. \left. (a^2-b^2) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{7}{6}, 1, \frac{5}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2}\right] \right) \right) \tan[c+dx]^2 \\
 & \left. (a^2-b^2 (1+\tan[c+dx]^2)) \right) - \\
 & \left( 9 b (-a^2+b^2) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2}\right] \right) \Big/ \\
 & \left( \left( 9 (a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2}\right] + 2 \right. \right. \\
 & \quad \left( 3 b^2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2}\right] + \right. \\
 & \quad \left. \left. 2 (-a^2+b^2) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2}\right] \right) \right) \tan[c+dx]^2 \\
 & \left. (-a^2+b^2 (1+\tan[c+dx]^2)) \right) - \\
 & \left( \sqrt{1+\tan[c+dx]^2} \left( 3 \left( -6 b^2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{6}, 2, \frac{7}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2}\right] + \right. \right. \right. \\
 & \quad \left. \left. (a^2-b^2) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{7}{6}, 1, \frac{7}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2}\right] \right) \right) \tan[c+dx]^2 \\
 & \left. (-a^2+b^2 (1+\tan[c+dx]^2)) + 5 (a^2-b^2) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{6}, \right. \right. \\
 & \quad \left. \left. 1, \frac{5}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2}\right] (9 a^2 - b^2 (9 + 7 \tan[c+dx]^2)) \right) \Big/ \\
 & \left( a \left( -15 (a^2-b^2) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{6}, 1, \frac{5}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2}\right] + \right. \right. \\
 & \quad \left( -6 b^2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{6}, 2, \frac{7}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2}\right] + \right. \\
 & \quad \left. \left. (a^2-b^2) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{7}{6}, 1, \frac{7}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2}\right] \right) \right)
 \end{aligned}$$





$$\begin{aligned}
 & \left. \text{Sec}[c+dx]^2 \text{Tan}[c+dx] \sqrt{1+\text{Tan}[c+dx]^2} \right) / \\
 & \left( a \left( -9(a^2-b^2) \text{AppellF1}\left[\frac{1}{2}, \frac{1}{6}, 1, \frac{3}{2}, -\text{Tan}[c+dx]^2, \frac{b^2 \text{Tan}[c+dx]^2}{a^2-b^2}\right] + \right. \right. \\
 & \quad \left( -6b^2 \text{AppellF1}\left[\frac{3}{2}, \frac{1}{6}, 2, \frac{5}{2}, -\text{Tan}[c+dx]^2, \frac{b^2 \text{Tan}[c+dx]^2}{a^2-b^2}\right] + (a^2-b^2) \right. \\
 & \quad \quad \left. \left. \text{AppellF1}\left[\frac{3}{2}, \frac{7}{6}, 1, \frac{5}{2}, -\text{Tan}[c+dx]^2, \frac{b^2 \text{Tan}[c+dx]^2}{a^2-b^2}\right] \right) \text{Tan}[c+dx]^2 \right) \\
 & \quad \left. (a^2-b^2(1+\text{Tan}[c+dx]^2))^2 \right) + \left( 9(2a^4-5a^2b^2+3b^4) \text{AppellF1}\left[\frac{1}{2}, \frac{1}{6}, \right. \right. \\
 & \quad \left. \left. 1, \frac{3}{2}, -\text{Tan}[c+dx]^2, \frac{b^2 \text{Tan}[c+dx]^2}{a^2-b^2}\right] \text{Sec}[c+dx]^2 \text{Tan}[c+dx] \right) / \\
 & \left( a \sqrt{1+\text{Tan}[c+dx]^2} \left( -9(a^2-b^2) \text{AppellF1}\left[\frac{1}{2}, \frac{1}{6}, 1, \frac{3}{2}, -\text{Tan}[c+dx]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{b^2 \text{Tan}[c+dx]^2}{a^2-b^2}\right] + \left( -6b^2 \text{AppellF1}\left[\frac{3}{2}, \frac{1}{6}, 2, \frac{5}{2}, -\text{Tan}[c+dx]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{b^2 \text{Tan}[c+dx]^2}{a^2-b^2}\right] + (a^2-b^2) \text{AppellF1}\left[\frac{3}{2}, \frac{7}{6}, 1, \frac{5}{2}, -\text{Tan}[c+dx]^2, \right. \right. \\
 & \quad \left. \left. \frac{b^2 \text{Tan}[c+dx]^2}{a^2-b^2}\right] \right) \text{Tan}[c+dx]^2 \right) (a^2-b^2(1+\text{Tan}[c+dx]^2)) \Big) + \\
 & \left( 9(2a^4-5a^2b^2+3b^4) \left( \frac{1}{3(a^2-b^2)} 2b^2 \text{AppellF1}\left[\frac{3}{2}, \frac{1}{6}, 2, \frac{5}{2}, -\text{Tan}[c+dx]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{b^2 \text{Tan}[c+dx]^2}{a^2-b^2}\right] \text{Sec}[c+dx]^2 \text{Tan}[c+dx] - \frac{1}{9} \text{AppellF1}\left[\frac{3}{2}, \frac{7}{6}, 1, \frac{5}{2}, -\text{Tan}[c+dx]^2, \right. \right. \\
 & \quad \left. \left. \frac{b^2 \text{Tan}[c+dx]^2}{a^2-b^2}\right] \text{Sec}[c+dx]^2 \text{Tan}[c+dx] \right) \sqrt{1+\text{Tan}[c+dx]^2} \Big) / \\
 & \left( a \left( -9(a^2-b^2) \text{AppellF1}\left[\frac{1}{2}, \frac{1}{6}, 1, \frac{3}{2}, -\text{Tan}[c+dx]^2, \frac{b^2 \text{Tan}[c+dx]^2}{a^2-b^2}\right] + \right. \right. \\
 & \quad \left( -6b^2 \text{AppellF1}\left[\frac{3}{2}, \frac{1}{6}, 2, \frac{5}{2}, -\text{Tan}[c+dx]^2, \frac{b^2 \text{Tan}[c+dx]^2}{a^2-b^2}\right] + (a^2-b^2) \right. \\
 & \quad \quad \left. \left. \text{AppellF1}\left[\frac{3}{2}, \frac{7}{6}, 1, \frac{5}{2}, -\text{Tan}[c+dx]^2, \frac{b^2 \text{Tan}[c+dx]^2}{a^2-b^2}\right] \right) \text{Tan}[c+dx]^2 \right) \\
 & \quad \left. (a^2-b^2(1+\text{Tan}[c+dx]^2))^2 \right) + \left( 18b^3(-a^2+b^2) \text{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \right. \right. \\
 & \quad \left. \left. -\text{Tan}[c+dx]^2, \frac{b^2 \text{Tan}[c+dx]^2}{a^2-b^2}\right] \text{Sec}[c+dx]^2 \text{Tan}[c+dx] \right) / \\
 & \left( \left( 9(a^2-b^2) \text{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, -\text{Tan}[c+dx]^2, \frac{b^2 \text{Tan}[c+dx]^2}{a^2-b^2}\right] + \right. \right. \\
 & \quad 2 \left( 3b^2 \text{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, -\text{Tan}[c+dx]^2, \frac{b^2 \text{Tan}[c+dx]^2}{a^2-b^2}\right] + \right. \\
 & \quad \quad \left. \left. 2(-a^2+b^2) \text{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, -\text{Tan}[c+dx]^2, \frac{b^2 \text{Tan}[c+dx]^2}{a^2-b^2}\right] \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left( \tan [c+d x]^2 \right)^2 \left( -a^2+b^2 \left( 1+\tan [c+d x]^2 \right) \right)^2 \right) - \\
 & \left( 9 b \left( -a^2+b^2 \right) \left( \frac{1}{3 \left( a^2-b^2 \right)} 2 b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, -\tan [c+d x]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] \operatorname{Sec}[c+d x]^2 \tan [c+d x] - \frac{4}{9} \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, 1, \right. \right. \\
 & \quad \left. \left. \frac{5}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] \operatorname{Sec}[c+d x]^2 \tan [c+d x] \right) \right) / \\
 & \left( \left( 9 \left( a^2-b^2 \right) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] + \right. \right. \\
 & \quad \left. \left( 3 b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] + 2 \left( -a^2+b^2 \right) \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] \right) \tan [c+d x]^2 \right) \\
 & \left. \left( -a^2+b^2 \left( 1+\tan [c+d x]^2 \right) \right) \right) - \left( 9 \left( 2 a^4-5 a^2 b^2+3 b^4 \right) \operatorname{AppellF1} \left[ \frac{1}{2}, \right. \right. \\
 & \quad \left. \frac{1}{6}, 1, \frac{3}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] \sqrt{1+\tan [c+d x]^2} \\
 & \left( 2 \left( -6 b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{6}, 2, \frac{5}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] + \right. \right. \\
 & \quad \left. \left. \left( a^2-b^2 \right) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{7}{6}, 1, \frac{5}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] \right) \right) \\
 & \operatorname{Sec}[c+d x]^2 \tan [c+d x] - 9 \left( a^2-b^2 \right) \left( \frac{1}{3 \left( a^2-b^2 \right)} 2 b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{6}, 2, \right. \right. \\
 & \quad \left. \frac{5}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] \operatorname{Sec}[c+d x]^2 \tan [c+d x] - \frac{1}{9} \operatorname{AppellF1} \left[ \right. \\
 & \quad \left. \frac{3}{2}, \frac{7}{6}, 1, \frac{5}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] \operatorname{Sec}[c+d x]^2 \tan [c+d x] \right) + \\
 & \tan [c+d x]^2 \left( -6 b^2 \left( \frac{1}{5 \left( a^2-b^2 \right)} 12 b^2 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{6}, 3, \frac{7}{2}, -\tan [c+d x]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] \operatorname{Sec}[c+d x]^2 \tan [c+d x] - \frac{1}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{7}{6}, 2, \right. \right. \\
 & \quad \left. \frac{7}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] \operatorname{Sec}[c+d x]^2 \tan [c+d x] \right) + \\
 & \left( a^2-b^2 \right) \left( \frac{1}{5 \left( a^2-b^2 \right)} 6 b^2 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{7}{6}, 2, \frac{7}{2}, -\tan [c+d x]^2, \right. \right. \\
 & \quad \left. \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] \operatorname{Sec}[c+d x]^2 \tan [c+d x] - \frac{7}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{13}{6}, 1, \right. \\
 & \quad \left. \frac{7}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] \operatorname{Sec}[c+d x]^2 \tan [c+d x] \right) \right) \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( a \left( -9 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{6}, 1, \frac{3}{2}, -\tan [c + d x]^2, \frac{b^2 \tan [c + d x]^2}{a^2 - b^2} \right] + \right. \right. \\
 & \quad \left( -6 b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{6}, 2, \frac{5}{2}, -\tan [c + d x]^2, \frac{b^2 \tan [c + d x]^2}{a^2 - b^2} \right] + \right. \\
 & \quad \left. \left. (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{7}{6}, 1, \frac{5}{2}, -\tan [c + d x]^2, \frac{b^2 \tan [c + d x]^2}{a^2 - b^2} \right] \right) \right. \\
 & \quad \left. \left. \tan [c + d x]^2 \right)^2 (a^2 - b^2 (1 + \tan [c + d x]^2)) \right) + \\
 & \left( 9 b (-a^2 + b^2) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, -\tan [c + d x]^2, \frac{b^2 \tan [c + d x]^2}{a^2 - b^2} \right] \right. \\
 & \quad \left( 4 \left( 3 b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, -\tan [c + d x]^2, \frac{b^2 \tan [c + d x]^2}{a^2 - b^2} \right] + \right. \right. \\
 & \quad \left. \left. 2 (-a^2 + b^2) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, -\tan [c + d x]^2, \frac{b^2 \tan [c + d x]^2}{a^2 - b^2} \right] \right) \right. \\
 & \quad \left. \sec [c + d x]^2 \tan [c + d x] + 9 (a^2 - b^2) \left( \frac{1}{3 (a^2 - b^2)} 2 b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 2, \right. \right. \right. \\
 & \quad \left. \left. \frac{5}{2}, -\tan [c + d x]^2, \frac{b^2 \tan [c + d x]^2}{a^2 - b^2} \right] \sec [c + d x]^2 \tan [c + d x] - \frac{4}{9} \operatorname{AppellF1} \left[ \right. \right. \\
 & \quad \left. \left. \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, -\tan [c + d x]^2, \frac{b^2 \tan [c + d x]^2}{a^2 - b^2} \right] \sec [c + d x]^2 \tan [c + d x] \right) + \\
 & \quad 2 \tan [c + d x]^2 \left( 3 b^2 \left( \frac{1}{5 (a^2 - b^2)} 12 b^2 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, 3, \frac{7}{2}, -\tan [c + d x]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{b^2 \tan [c + d x]^2}{a^2 - b^2} \right] \sec [c + d x]^2 \tan [c + d x] - \frac{4}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, 2, \right. \right. \\
 & \quad \left. \left. \frac{7}{2}, -\tan [c + d x]^2, \frac{b^2 \tan [c + d x]^2}{a^2 - b^2} \right] \sec [c + d x]^2 \tan [c + d x] \right) + \\
 & \quad \left. 2 (-a^2 + b^2) \left( \frac{1}{5 (a^2 - b^2)} 6 b^2 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, 2, \frac{7}{2}, -\tan [c + d x]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{b^2 \tan [c + d x]^2}{a^2 - b^2} \right] \sec [c + d x]^2 \tan [c + d x] - 2 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{8}{3}, 1, \right. \right. \\
 & \quad \left. \left. \frac{7}{2}, -\tan [c + d x]^2, \frac{b^2 \tan [c + d x]^2}{a^2 - b^2} \right] \sec [c + d x]^2 \tan [c + d x] \right) \right) \right) \Big/ \\
 & \left( \left( 9 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, -\tan [c + d x]^2, \frac{b^2 \tan [c + d x]^2}{a^2 - b^2} \right] + \right. \right. \\
 & \quad \left. \left. 2 \left( 3 b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, -\tan [c + d x]^2, \frac{b^2 \tan [c + d x]^2}{a^2 - b^2} \right] + 2 (-a^2 + b^2) \right. \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, -\tan [c + d x]^2, \frac{b^2 \tan [c + d x]^2}{a^2 - b^2} \right] \right) \tan [c + d x]^2 \right)^2 \\
 & \quad \left. (-a^2 + b^2 (1 + \tan [c + d x]^2)) \right) - \left( 2 b^2 \sec [c + d x]^2 \tan [c + d x] \sqrt{1 + \tan [c + d x]^2} \right)
 \end{aligned}$$

$$\begin{aligned}
& \left( 3 \left( -6 b^2 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{6}, 2, \frac{7}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] + \right. \right. \\
& \quad \left. \left. (a^2-b^2) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{7}{6}, 1, \frac{7}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] \right) \right. \\
& \quad \left. \tan [c+d x]^2 \left( -a^2+b^2 \left( 1+\tan [c+d x]^2 \right) \right) + 5 \left( a^2-b^2 \right) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{6}, \right. \right. \\
& \quad \left. \left. 1, \frac{5}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] \left( 9 a^2-b^2 \left( 9+7 \tan [c+d x]^2 \right) \right) \right) \Bigg) / \\
& \left( a \left( -15 \left( a^2-b^2 \right) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{6}, 1, \frac{5}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] + \right. \right. \\
& \quad \left( -6 b^2 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{6}, 2, \frac{7}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] + \left( a^2-b^2 \right) \right. \\
& \quad \left. \left. \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{7}{6}, 1, \frac{7}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] \right) \tan [c+d x]^2 \right) \\
& \quad \left. \left( a^2-b^2 \left( 1+\tan [c+d x]^2 \right) \right)^2 \right) - \left( \operatorname{Sec} [c+d x]^2 \tan [c+d x] \right. \\
& \quad \left. \left( 3 \left( -6 b^2 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{6}, 2, \frac{7}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] + \right. \right. \right. \\
& \quad \left. \left. \left( a^2-b^2 \right) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{7}{6}, 1, \frac{7}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] \right) \right. \\
& \quad \left. \tan [c+d x]^2 \left( -a^2+b^2 \left( 1+\tan [c+d x]^2 \right) \right) + 5 \left( a^2-b^2 \right) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{6}, \right. \right. \\
& \quad \left. \left. 1, \frac{5}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] \left( 9 a^2-b^2 \left( 9+7 \tan [c+d x]^2 \right) \right) \right) \Bigg) / \\
& \left( a \sqrt{1+\tan [c+d x]^2} \left( -15 \left( a^2-b^2 \right) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{6}, 1, \frac{5}{2}, -\tan [c+d x]^2, \right. \right. \right. \\
& \quad \left. \left. \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] + \left( -6 b^2 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{6}, 2, \frac{7}{2}, -\tan [c+d x]^2, \right. \right. \right. \\
& \quad \left. \left. \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] + \left( a^2-b^2 \right) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{7}{6}, 1, \frac{7}{2}, -\tan [c+d x]^2, \right. \right. \\
& \quad \left. \left. \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] \right) \tan [c+d x]^2 \right) \left( a^2-b^2 \left( 1+\tan [c+d x]^2 \right) \right) \Bigg) + \\
& \left( \sqrt{1+\tan [c+d x]^2} \left( 2 \left( -6 b^2 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{6}, 2, \frac{7}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] + \right. \right. \right. \\
& \quad \left. \left. \left( a^2-b^2 \right) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{7}{6}, 1, \frac{7}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] \right) \right) \\
& \quad \left. \operatorname{Sec} [c+d x]^2 \tan [c+d x] - 15 \left( a^2-b^2 \right) \left( \frac{1}{5 \left( a^2-b^2 \right)} 6 b^2 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{6}, 2, \right. \right. \right. \\
& \quad \left. \left. \frac{7}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] \operatorname{Sec} [c+d x]^2 \tan [c+d x] - \frac{1}{5} \operatorname{AppellF1} \left[ \right. \right. \\
& \quad \left. \left. \frac{5}{2}, \frac{7}{6}, 1, \frac{7}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] \operatorname{Sec} [c+d x]^2 \tan [c+d x] \right) \Bigg) +
\end{aligned}$$

$$\begin{aligned}
 & \tan [c+d x]^2 \left( -6 b^2 \left( \frac{1}{7\left(a^2-b^2\right)} 20 b^2 \operatorname{AppellF1}\left[\frac{7}{2}, \frac{1}{6}, 3, \frac{9}{2}, -\tan [c+d x]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{b^2 \tan [c+d x]^2}{a^2-b^2}\right] \operatorname{Sec}[c+d x]^2 \tan [c+d x] - \frac{5}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{7}{6}, 2, \right. \right. \\
 & \quad \left. \left. \frac{9}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2}\right] \operatorname{Sec}[c+d x]^2 \tan [c+d x] \right) + \\
 & \quad \left( a^2-b^2 \right) \left( \frac{1}{7\left(a^2-b^2\right)} 10 b^2 \operatorname{AppellF1}\left[\frac{7}{2}, \frac{7}{6}, 2, \frac{9}{2}, -\tan [c+d x]^2, \right. \right. \\
 & \quad \left. \left. \frac{b^2 \tan [c+d x]^2}{a^2-b^2}\right] \operatorname{Sec}[c+d x]^2 \tan [c+d x] - \frac{5}{3} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{13}{6}, 1, \right. \right. \\
 & \quad \left. \left. \frac{9}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2}\right] \operatorname{Sec}[c+d x]^2 \tan [c+d x] \right) \Big) \Big) \\
 & \left( 3 \left( -6 b^2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{6}, 2, \frac{7}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2}\right] + \right. \right. \\
 & \quad \left. \left. \left( a^2-b^2 \right) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{7}{6}, 1, \frac{7}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2}\right] \right) \right) \\
 & \quad \tan [c+d x]^2 \left( -a^2+b^2\left(1+\tan [c+d x]^2\right) \right) + 5\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{6}, \right. \\
 & \quad \left. 1, \frac{5}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2}\right] \left( 9 a^2-b^2\left( 9+7 \tan [c+d x]^2 \right) \right) \Big) \Big) / \\
 & \left( a \left( -15\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{6}, 1, \frac{5}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2}\right] + \right. \right. \\
 & \quad \left( -6 b^2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{6}, 2, \frac{7}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2}\right] + \right. \\
 & \quad \left. \left. \left( a^2-b^2 \right) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{7}{6}, 1, \frac{7}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2}\right] \right) \right) \\
 & \quad \left. \tan [c+d x]^2 \right)^2 \left( a^2-b^2\left(1+\tan [c+d x]^2\right) \right) \Big) - \\
 & \left( \sqrt{1+\tan [c+d x]^2} \left( -70 b^2\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{6}, 1, \frac{5}{2}, -\tan [c+d x]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{b^2 \tan [c+d x]^2}{a^2-b^2}\right] \operatorname{Sec}[c+d x]^2 \tan [c+d x] + \right. \\
 & \quad \left. 6 b^2 \left( -6 b^2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{6}, 2, \frac{7}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2}\right] + \left(a^2-b^2\right) \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1}\left[\frac{5}{2}, \frac{7}{6}, 1, \frac{7}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2}\right] \right) \operatorname{Sec}[c+d x]^2 \right. \\
 & \quad \left. \tan [c+d x]^3 + 6 \left( -6 b^2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{6}, 2, \frac{7}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2}\right] + \right. \right. \\
 & \quad \left. \left. \left( a^2-b^2 \right) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{7}{6}, 1, \frac{7}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2}\right] \right) \right) \\
 & \quad \left. \operatorname{Sec}[c+d x]^2 \tan [c+d x] \left( -a^2+b^2\left(1+\tan [c+d x]^2\right) \right) \right) +
 \end{aligned}$$

$$\begin{aligned}
& 3 \operatorname{Tan}[c+dx]^2 \left( -6b^2 \left( \frac{1}{7(a^2-b^2)} 20b^2 \operatorname{AppellF1} \left[ \frac{7}{2}, \frac{1}{6}, 3, \frac{9}{2}, -\operatorname{Tan}[c+dx]^2, \right. \right. \right. \\
& \quad \left. \left. \frac{b^2 \operatorname{Tan}[c+dx]^2}{a^2-b^2} \right] \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx] - \frac{5}{21} \operatorname{AppellF1} \left[ \frac{7}{2}, \frac{7}{6}, 2, \right. \right. \\
& \quad \left. \left. \frac{9}{2}, -\operatorname{Tan}[c+dx]^2, \frac{b^2 \operatorname{Tan}[c+dx]^2}{a^2-b^2} \right] \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx] \right) + \\
& (a^2-b^2) \left( \frac{1}{7(a^2-b^2)} 10b^2 \operatorname{AppellF1} \left[ \frac{7}{2}, \frac{7}{6}, 2, \frac{9}{2}, -\operatorname{Tan}[c+dx]^2, \right. \right. \\
& \quad \left. \left. \frac{b^2 \operatorname{Tan}[c+dx]^2}{a^2-b^2} \right] \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx] - \frac{5}{3} \operatorname{AppellF1} \left[ \frac{7}{2}, \frac{13}{6}, 1, \right. \right. \\
& \quad \left. \left. \frac{9}{2}, -\operatorname{Tan}[c+dx]^2, \frac{b^2 \operatorname{Tan}[c+dx]^2}{a^2-b^2} \right] \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx] \right) \Bigg) \\
& (-a^2+b^2(1+\operatorname{Tan}[c+dx]^2)) + 5(a^2-b^2) \left( \frac{1}{5(a^2-b^2)} 6b^2 \operatorname{AppellF1} \left[ \right. \right. \\
& \quad \left. \left. \frac{5}{2}, \frac{1}{6}, 2, \frac{7}{2}, -\operatorname{Tan}[c+dx]^2, \frac{b^2 \operatorname{Tan}[c+dx]^2}{a^2-b^2} \right] \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx] - \right. \\
& \quad \left. \frac{1}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{7}{6}, 1, \frac{7}{2}, -\operatorname{Tan}[c+dx]^2, \frac{b^2 \operatorname{Tan}[c+dx]^2}{a^2-b^2} \right] \right. \\
& \quad \left. \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx] \right) (9a^2-b^2(9+7\operatorname{Tan}[c+dx]^2)) \Bigg) \Bigg) / \\
& \left( a \left( -15(a^2-b^2) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{6}, 1, \frac{5}{2}, -\operatorname{Tan}[c+dx]^2, \frac{b^2 \operatorname{Tan}[c+dx]^2}{a^2-b^2} \right] + \right. \right. \\
& \quad \left( -6b^2 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{6}, 2, \frac{7}{2}, -\operatorname{Tan}[c+dx]^2, \frac{b^2 \operatorname{Tan}[c+dx]^2}{a^2-b^2} \right] + \right. \\
& \quad \left. \left. (a^2-b^2) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{7}{6}, 1, \frac{7}{2}, -\operatorname{Tan}[c+dx]^2, \frac{b^2 \operatorname{Tan}[c+dx]^2}{a^2-b^2} \right] \right) \right. \\
& \quad \left. \left. \left. \left. \left. \left. \operatorname{Tan}[c+dx]^2 \right) (a^2-b^2(1+\operatorname{Tan}[c+dx]^2)) \right) \right) \right) \right) \right) \Bigg)
\end{aligned}$$

**Problem 716: Result more than twice size of optimal antiderivative.**

$$\int \frac{1}{\operatorname{Sec}[c+dx]^{2/3} (a+b \operatorname{Sec}[c+dx])} dx$$

Optimal (type 6, 174 leaves, 6 steps):

$$\begin{aligned}
& - \frac{b \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{1}{3}, 1, \frac{3}{2}, \operatorname{Sin}[c+dx]^2, \frac{a^2 \operatorname{Sin}[c+dx]^2}{a^2-b^2} \right] \operatorname{Sin}[c+dx]}{(a^2-b^2) d (\operatorname{Cos}[c+dx]^2)^{1/3} \operatorname{Sec}[c+dx]^{2/3}} + \\
& \frac{1}{(a^2-b^2) d} a \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{5}{6}, 1, \frac{3}{2}, \operatorname{Sin}[c+dx]^2, \frac{a^2 \operatorname{Sin}[c+dx]^2}{a^2-b^2} \right] \\
& (\operatorname{Cos}[c+dx]^2)^{1/6} \operatorname{Sec}[c+dx]^{1/3} \operatorname{Sin}[c+dx]
\end{aligned}$$

Result (type 6, 9178 leaves):

$$\begin{aligned}
 & \left( \left( \frac{\operatorname{Sec}[c+dx]^{1/3}}{2(b+a\cos[c+dx])} + \frac{\cos[2(c+dx)] \operatorname{Sec}[c+dx]^{1/3}}{2(b+a\cos[c+dx])} \right) \right. \\
 & \quad \operatorname{Tan}[c+dx] \left( \left( \left( 9(a^4 - 4a^2b^2 + 3b^4) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, -\operatorname{Tan}[c+dx]^2, \frac{b^2 \operatorname{Tan}[c+dx]^2}{a^2 - b^2}\right] \sqrt{1 + \operatorname{Tan}[c+dx]^2} \right) \right) / \right. \\
 & \quad \left( a \left( -9(a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, -\operatorname{Tan}[c+dx]^2, \frac{b^2 \operatorname{Tan}[c+dx]^2}{a^2 - b^2}\right] - \right. \right. \\
 & \quad \left. \left. 2 \left( 3b^2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, -\operatorname{Tan}[c+dx]^2, \frac{b^2 \operatorname{Tan}[c+dx]^2}{a^2 - b^2}\right] + \right. \right. \right. \\
 & \quad \left. \left. \left. (-a^2 + b^2) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, -\operatorname{Tan}[c+dx]^2, \frac{b^2 \operatorname{Tan}[c+dx]^2}{a^2 - b^2}\right] \right) \right) \right. \\
 & \quad \left. \left. \operatorname{Tan}[c+dx]^2 \right) (a^2 - b^2 (1 + \operatorname{Tan}[c+dx]^2)) \right) - \\
 & \quad \left( 18b(-a^2 + b^2) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{5}{6}, 1, \frac{3}{2}, -\operatorname{Tan}[c+dx]^2, \frac{b^2 \operatorname{Tan}[c+dx]^2}{a^2 - b^2}\right] \right) / \\
 & \quad \left( \left( 9(a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{5}{6}, 1, \frac{3}{2}, -\operatorname{Tan}[c+dx]^2, \frac{b^2 \operatorname{Tan}[c+dx]^2}{a^2 - b^2}\right] + \right. \right. \\
 & \quad \left( 6b^2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{6}, 2, \frac{5}{2}, -\operatorname{Tan}[c+dx]^2, \frac{b^2 \operatorname{Tan}[c+dx]^2}{a^2 - b^2}\right] + \right. \\
 & \quad \left. \left. 5(-a^2 + b^2) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{11}{6}, 1, \frac{5}{2}, -\operatorname{Tan}[c+dx]^2, \frac{b^2 \operatorname{Tan}[c+dx]^2}{a^2 - b^2}\right] \right) \right) \\
 & \quad \left. \operatorname{Tan}[c+dx]^2 \right) (-a^2 + b^2 (1 + \operatorname{Tan}[c+dx]^2)) \right) - \\
 & \quad \left( \sqrt{1 + \operatorname{Tan}[c+dx]^2} \left( 6 \left( -3b^2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, -\operatorname{Tan}[c+dx]^2, \frac{b^2 \operatorname{Tan}[c+dx]^2}{a^2 - b^2}\right] + \right. \right. \right. \\
 & \quad \left. \left. \left. (a^2 - b^2) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, -\operatorname{Tan}[c+dx]^2, \frac{b^2 \operatorname{Tan}[c+dx]^2}{a^2 - b^2}\right] \right) \right) \right. \\
 & \quad \left. \operatorname{Tan}[c+dx]^2 (-a^2 + b^2 (1 + \operatorname{Tan}[c+dx]^2)) + 5(a^2 - b^2) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, -\operatorname{Tan}[c+dx]^2, \frac{b^2 \operatorname{Tan}[c+dx]^2}{a^2 - b^2}\right] \right) \right) / \\
 & \quad \left( a \left( -15(a^2 - b^2) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, -\operatorname{Tan}[c+dx]^2, \frac{b^2 \operatorname{Tan}[c+dx]^2}{a^2 - b^2}\right] - \right. \right. \\
 & \quad \left. \left. 2 \left( 3b^2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, -\operatorname{Tan}[c+dx]^2, \frac{b^2 \operatorname{Tan}[c+dx]^2}{a^2 - b^2}\right] + \right. \right. \right. \\
 & \quad \left. \left. \left. (-a^2 + b^2) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, -\operatorname{Tan}[c+dx]^2, \frac{b^2 \operatorname{Tan}[c+dx]^2}{a^2 - b^2}\right] \right) \right) \operatorname{Tan}[c+dx]^2 \right) \\
 & \quad \left. \left. \left. (a^2 - b^2 (1 + \operatorname{Tan}[c+dx]^2)) \right) \right) \right) / \left( 2d(1 + \operatorname{Tan}[c+dx]^2)^{5/6} \right. \\
 & \quad \left. \left( -\frac{1}{6(1 + \operatorname{Tan}[c+dx]^2)^{11/6}} 5 \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx]^2 \left( \left( 9(a^4 - 4a^2b^2 + 3b^4) \right. \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
& \text{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2}\right] \sqrt{1+\tan[c+dx]^2} \Big/ \\
& \left( a \left( -9(a^2-b^2) \text{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2}\right] - 2 \right. \right. \\
& \quad \left( 3b^2 \text{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2}\right] + \right. \\
& \quad \left. \left. (-a^2+b^2) \text{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2}\right] \right) \right. \\
& \quad \left. \tan[c+dx]^2 \right) (a^2-b^2(1+\tan[c+dx]^2)) \Big) - \\
& \left( 18b(-a^2+b^2) \text{AppellF1}\left[\frac{1}{2}, \frac{5}{6}, 1, \frac{3}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2}\right] \right) \Big/ \\
& \left( \left( 9(a^2-b^2) \text{AppellF1}\left[\frac{1}{2}, \frac{5}{6}, 1, \frac{3}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2}\right] + \right. \right. \\
& \quad \left( 6b^2 \text{AppellF1}\left[\frac{3}{2}, \frac{5}{6}, 2, \frac{5}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2}\right] + \right. \\
& \quad \left. \left. 5(-a^2+b^2) \text{AppellF1}\left[\frac{3}{2}, \frac{11}{6}, 1, \frac{5}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2}\right] \right) \right. \\
& \quad \left. \tan[c+dx]^2 \right) (-a^2+b^2(1+\tan[c+dx]^2)) \Big) - \\
& \left( \sqrt{1+\tan[c+dx]^2} \left( 6 \left( -3b^2 \text{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2}\right] + \right. \right. \right. \\
& \quad \left. \left. (a^2-b^2) \text{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2}\right] \right) \right. \\
& \quad \left. \tan[c+dx]^2 (-a^2+b^2(1+\tan[c+dx]^2)) + 5(a^2-b^2) \text{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, \right. \right. \\
& \quad \left. \left. 1, \frac{5}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2}\right] (9a^2-b^2(9+8\tan[c+dx]^2)) \right) \Big) \Big/ \\
& \left( a \left( -15(a^2-b^2) \text{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2}\right] - \right. \right. \\
& \quad 2 \left( 3b^2 \text{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2}\right] + \right. \\
& \quad \left. \left. (-a^2+b^2) \text{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2}\right] \right) \right. \\
& \quad \left. \tan[c+dx]^2 \right) (a^2-b^2(1+\tan[c+dx]^2)) \Big) \Big) + \\
& \frac{1}{2(1+\tan[c+dx]^2)^{5/6}} \text{Sec}[c+dx]^2 \left( \left( 9(a^4-4a^2b^2+3b^4) \text{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, 1, \right. \right. \right. \\
& \quad \left. \left. \frac{3}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2}\right] \sqrt{1+\tan[c+dx]^2} \right) \Big/ \\
& \left( a \left( -9(a^2-b^2) \text{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, -\tan[c+dx]^2, \frac{b^2 \tan[c+dx]^2}{a^2-b^2}\right] - \right. \right.
\end{aligned}$$



$$\begin{aligned}
 & 2 \left( 3 b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] + \right. \\
 & \quad \left. (-a^2+b^2) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] \right) \\
 & \quad \left. \tan [c+d x]^2 \left( a^2-b^2 \left( 1+\tan [c+d x]^2 \right) \right) \right) - \\
 & \left( 18 b \left( -a^2+b^2 \right) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{5}{6}, 1, \frac{3}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] \right) / \\
 & \left( \left( 9 \left( a^2-b^2 \right) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{5}{6}, 1, \frac{3}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] + \right. \right. \\
 & \quad \left. \left( 6 b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{6}, 2, \frac{5}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] + \right. \right. \\
 & \quad \left. \left. 5 \left( -a^2+b^2 \right) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{11}{6}, 1, \frac{5}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] \right) \right) \\
 & \quad \left. \tan [c+d x]^2 \left( -a^2+b^2 \left( 1+\tan [c+d x]^2 \right) \right) \right) - \\
 & \left( \sqrt{1+\tan [c+d x]^2} \left( 6 \left( -3 b^2 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] + \right. \right. \right. \\
 & \quad \left. \left. \left( a^2-b^2 \right) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] \right) \right) \\
 & \quad \left. \tan [c+d x]^2 \left( -a^2+b^2 \left( 1+\tan [c+d x]^2 \right) \right) + 5 \left( a^2-b^2 \right) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \right. \right. \\
 & \quad \left. \left. 1, \frac{5}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] \left( 9 a^2-b^2 \left( 9+8 \tan [c+d x]^2 \right) \right) \right) \right) / \\
 & \left( a \left( -15 \left( a^2-b^2 \right) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] - \right. \right. \\
 & \quad \left. \left. 2 \left( 3 b^2 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] + \left( -a^2+b^2 \right) \right. \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] \right) \tan [c+d x]^2 \right) \\
 & \quad \left. \left. \left( a^2-b^2 \left( 1+\tan [c+d x]^2 \right) \right) \right) \right) + \frac{1}{2 \left( 1+\tan [c+d x]^2 \right)^{5/6}} \tan [c+d x] \\
 & \left( \left( 18 b^2 \left( a^4-4 a^2 b^2+3 b^4 \right) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] \right) \right. \\
 & \quad \left. \sec [c+d x]^2 \tan [c+d x] \sqrt{1+\tan [c+d x]^2} \right) / \\
 & \left( a \left( -9 \left( a^2-b^2 \right) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] - \right. \right. \\
 & \quad \left. \left. 2 \left( 3 b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] + \left( -a^2+b^2 \right) \right. \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] \right) \tan [c+d x]^2 \right) \right)
 \end{aligned}$$

$$\begin{aligned}
& \left. \left( a^2 - b^2 (1 + \tan[c + dx]^2) \right)^2 \right) + \left( 9 (a^4 - 4a^2b^2 + 3b^4) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, \right. \right. \\
& \left. \left. 1, \frac{3}{2}, -\tan[c + dx]^2, \frac{b^2 \tan[c + dx]^2}{a^2 - b^2} \right] \operatorname{Sec}[c + dx]^2 \tan[c + dx] \right) / \\
& \left( a \sqrt{1 + \tan[c + dx]^2} \left( -9 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, -\tan[c + dx]^2, \right. \right. \right. \\
& \left. \left. \frac{b^2 \tan[c + dx]^2}{a^2 - b^2} \right] - 2 \left( 3b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, -\tan[c + dx]^2, \right. \right. \right. \\
& \left. \left. \frac{b^2 \tan[c + dx]^2}{a^2 - b^2} \right] + (-a^2 + b^2) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, -\tan[c + dx]^2, \right. \right. \\
& \left. \left. \frac{b^2 \tan[c + dx]^2}{a^2 - b^2} \right] \right) \tan[c + dx]^2 \right) (a^2 - b^2 (1 + \tan[c + dx]^2)) \Big) + \\
& \left( 9 (a^4 - 4a^2b^2 + 3b^4) \left( \frac{1}{3(a^2 - b^2)} 2b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, -\tan[c + dx]^2, \right. \right. \right. \\
& \left. \left. \frac{b^2 \tan[c + dx]^2}{a^2 - b^2} \right] \operatorname{Sec}[c + dx]^2 \tan[c + dx] - \frac{2}{9} \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, -\tan[ \right. \right. \\
& \left. \left. c + dx]^2, \frac{b^2 \tan[c + dx]^2}{a^2 - b^2} \right] \operatorname{Sec}[c + dx]^2 \tan[c + dx] \right) \sqrt{1 + \tan[c + dx]^2} \Big) / \\
& \left( a \left( -9 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, -\tan[c + dx]^2, \frac{b^2 \tan[c + dx]^2}{a^2 - b^2} \right] - \right. \right. \\
& \left. \left. 2 \left( 3b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, -\tan[c + dx]^2, \frac{b^2 \tan[c + dx]^2}{a^2 - b^2} \right] + (-a^2 + b^2) \right. \right. \right. \\
& \left. \left. \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, -\tan[c + dx]^2, \frac{b^2 \tan[c + dx]^2}{a^2 - b^2} \right] \right) \tan[c + dx]^2 \right) \\
& (a^2 - b^2 (1 + \tan[c + dx]^2)) \Big) + \left( 36b^3 (-a^2 + b^2) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{5}{6}, 1, \frac{3}{2}, \right. \right. \\
& \left. \left. -\tan[c + dx]^2, \frac{b^2 \tan[c + dx]^2}{a^2 - b^2} \right] \operatorname{Sec}[c + dx]^2 \tan[c + dx] \right) / \\
& \left( \left( 9 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{5}{6}, 1, \frac{3}{2}, -\tan[c + dx]^2, \frac{b^2 \tan[c + dx]^2}{a^2 - b^2} \right] + \right. \right. \\
& \left( 6b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{6}, 2, \frac{5}{2}, -\tan[c + dx]^2, \frac{b^2 \tan[c + dx]^2}{a^2 - b^2} \right] + \right. \\
& \left. \left. 5 (-a^2 + b^2) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{11}{6}, 1, \frac{5}{2}, -\tan[c + dx]^2, \frac{b^2 \tan[c + dx]^2}{a^2 - b^2} \right] \right) \right) \\
& \tan[c + dx]^2 \Big) (-a^2 + b^2 (1 + \tan[c + dx]^2))^2 \Big) - \\
& \left( 18b (-a^2 + b^2) \left( \frac{1}{3(a^2 - b^2)} 2b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{6}, 2, \frac{5}{2}, -\tan[c + dx]^2, \right. \right. \right. \\
& \left. \left. \frac{b^2 \tan[c + dx]^2}{a^2 - b^2} \right] \operatorname{Sec}[c + dx]^2 \tan[c + dx] - \frac{5}{9} \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{11}{6}, 1, \right. \right. \\
& \left. \left. \frac{5}{2}, -\tan[c + dx]^2, \frac{b^2 \tan[c + dx]^2}{a^2 - b^2} \right] \operatorname{Sec}[c + dx]^2 \tan[c + dx] \right) \Big) /
\end{aligned}$$

$$\begin{aligned}
 & \left( \left( 9 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{5}{6}, 1, \frac{3}{2}, -\tan[c + dx]^2, \frac{b^2 \tan[c + dx]^2}{a^2 - b^2} \right] + \right. \right. \\
 & \quad \left( 6 b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{6}, 2, \frac{5}{2}, -\tan[c + dx]^2, \frac{b^2 \tan[c + dx]^2}{a^2 - b^2} \right] + 5 (-a^2 + b^2) \right. \\
 & \quad \quad \left. \left. \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{11}{6}, 1, \frac{5}{2}, -\tan[c + dx]^2, \frac{b^2 \tan[c + dx]^2}{a^2 - b^2} \right] \right) \tan[c + dx]^2 \right) \\
 & \quad \left. (-a^2 + b^2 (1 + \tan[c + dx]^2)) \right) - \left( 9 (a^4 - 4 a^2 b^2 + 3 b^4) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, \right. \right. \\
 & \quad \left. \left. 1, \frac{3}{2}, -\tan[c + dx]^2, \frac{b^2 \tan[c + dx]^2}{a^2 - b^2} \right] \sqrt{1 + \tan[c + dx]^2} \right. \\
 & \quad \left( -4 \left( 3 b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, -\tan[c + dx]^2, \frac{b^2 \tan[c + dx]^2}{a^2 - b^2} \right] + \right. \right. \\
 & \quad \quad \left. \left. (-a^2 + b^2) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, -\tan[c + dx]^2, \frac{b^2 \tan[c + dx]^2}{a^2 - b^2} \right] \right) \right) \\
 & \quad \operatorname{Sec}[c + dx]^2 \tan[c + dx] - 9 (a^2 - b^2) \left( \frac{1}{3 (a^2 - b^2)} 2 b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 2, \right. \right. \\
 & \quad \left. \left. \frac{5}{2}, -\tan[c + dx]^2, \frac{b^2 \tan[c + dx]^2}{a^2 - b^2} \right] \operatorname{Sec}[c + dx]^2 \tan[c + dx] - \frac{2}{9} \operatorname{AppellF1} \left[ \right. \right. \\
 & \quad \left. \left. \frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, -\tan[c + dx]^2, \frac{b^2 \tan[c + dx]^2}{a^2 - b^2} \right] \operatorname{Sec}[c + dx]^2 \tan[c + dx] \right) - \\
 & \quad 2 \tan[c + dx]^2 \left( 3 b^2 \left( \frac{1}{5 (a^2 - b^2)} 12 b^2 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, 3, \frac{7}{2}, -\tan[c + dx]^2, \right. \right. \right. \\
 & \quad \quad \left. \left. \frac{b^2 \tan[c + dx]^2}{a^2 - b^2} \right] \operatorname{Sec}[c + dx]^2 \tan[c + dx] - \frac{2}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}, 2, \right. \right. \\
 & \quad \quad \left. \left. \frac{7}{2}, -\tan[c + dx]^2, \frac{b^2 \tan[c + dx]^2}{a^2 - b^2} \right] \operatorname{Sec}[c + dx]^2 \tan[c + dx] \right) + \\
 & \quad \left. (-a^2 + b^2) \left( \frac{1}{5 (a^2 - b^2)} 6 b^2 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}, 2, \frac{7}{2}, -\tan[c + dx]^2, \right. \right. \right. \\
 & \quad \quad \left. \left. \frac{b^2 \tan[c + dx]^2}{a^2 - b^2} \right] \operatorname{Sec}[c + dx]^2 \tan[c + dx] - \frac{8}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{7}{3}, 1, \right. \right. \\
 & \quad \quad \left. \left. \frac{7}{2}, -\tan[c + dx]^2, \frac{b^2 \tan[c + dx]^2}{a^2 - b^2} \right] \operatorname{Sec}[c + dx]^2 \tan[c + dx] \right) \right) \right) / \\
 & \quad \left( a \left( -9 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, -\tan[c + dx]^2, \frac{b^2 \tan[c + dx]^2}{a^2 - b^2} \right] - \right. \right. \\
 & \quad \left. \left. 2 \left( 3 b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, -\tan[c + dx]^2, \frac{b^2 \tan[c + dx]^2}{a^2 - b^2} \right] + \right. \right. \right. \\
 & \quad \quad \left. \left. (-a^2 + b^2) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, -\tan[c + dx]^2, \frac{b^2 \tan[c + dx]^2}{a^2 - b^2} \right] \right) \right) \\
 & \quad \left. \tan[c + dx]^2 \right)^2 (a^2 - b^2 (1 + \tan[c + dx]^2)) \right) +
 \end{aligned}$$

$$\begin{aligned}
& \left( 18 b (-a^2 + b^2) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{5}{6}, 1, \frac{3}{2}, -\tan [c + d x]^2, \frac{b^2 \tan [c + d x]^2}{a^2 - b^2} \right] \right. \\
& \quad \left( 2 \left( 6 b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{6}, 2, \frac{5}{2}, -\tan [c + d x]^2, \frac{b^2 \tan [c + d x]^2}{a^2 - b^2} \right] + \right. \right. \\
& \quad \quad \left. \left. 5 (-a^2 + b^2) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{11}{6}, 1, \frac{5}{2}, -\tan [c + d x]^2, \frac{b^2 \tan [c + d x]^2}{a^2 - b^2} \right] \right) \right. \\
& \quad \left. \operatorname{Sec} [c + d x]^2 \tan [c + d x] + 9 (a^2 - b^2) \left( \frac{1}{3 (a^2 - b^2)} 2 b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{6}, 2, \right. \right. \right. \\
& \quad \quad \left. \left. \frac{5}{2}, -\tan [c + d x]^2, \frac{b^2 \tan [c + d x]^2}{a^2 - b^2} \right] \operatorname{Sec} [c + d x]^2 \tan [c + d x] - \frac{5}{9} \operatorname{AppellF1} \left[ \right. \right. \\
& \quad \quad \left. \left. \frac{3}{2}, \frac{11}{6}, 1, \frac{5}{2}, -\tan [c + d x]^2, \frac{b^2 \tan [c + d x]^2}{a^2 - b^2} \right] \operatorname{Sec} [c + d x]^2 \tan [c + d x] \right) \right) + \\
& \quad \tan [c + d x]^2 \left( 6 b^2 \left( \frac{1}{5 (a^2 - b^2)} 12 b^2 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{6}, 3, \frac{7}{2}, -\tan [c + d x]^2, \right. \right. \right. \\
& \quad \quad \left. \left. \frac{b^2 \tan [c + d x]^2}{a^2 - b^2} \right] \operatorname{Sec} [c + d x]^2 \tan [c + d x] - \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{11}{6}, 2, \right. \right. \\
& \quad \quad \left. \left. \frac{7}{2}, -\tan [c + d x]^2, \frac{b^2 \tan [c + d x]^2}{a^2 - b^2} \right] \operatorname{Sec} [c + d x]^2 \tan [c + d x] \right) + \\
& \quad \left. 5 (-a^2 + b^2) \left( \frac{1}{5 (a^2 - b^2)} 6 b^2 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{11}{6}, 2, \frac{7}{2}, -\tan [c + d x]^2, \right. \right. \right. \\
& \quad \quad \left. \left. \frac{b^2 \tan [c + d x]^2}{a^2 - b^2} \right] \operatorname{Sec} [c + d x]^2 \tan [c + d x] - \frac{11}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{17}{6}, 1, \right. \right. \\
& \quad \quad \left. \left. \frac{7}{2}, -\tan [c + d x]^2, \frac{b^2 \tan [c + d x]^2}{a^2 - b^2} \right] \operatorname{Sec} [c + d x]^2 \tan [c + d x] \right) \right) \right) \Big/ \\
& \left( \left( 9 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{5}{6}, 1, \frac{3}{2}, -\tan [c + d x]^2, \frac{b^2 \tan [c + d x]^2}{a^2 - b^2} \right] + \right. \right. \\
& \quad \left( 6 b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{6}, 2, \frac{5}{2}, -\tan [c + d x]^2, \frac{b^2 \tan [c + d x]^2}{a^2 - b^2} \right] + 5 (-a^2 + b^2) \right. \\
& \quad \quad \left. \left. \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{11}{6}, 1, \frac{5}{2}, -\tan [c + d x]^2, \frac{b^2 \tan [c + d x]^2}{a^2 - b^2} \right] \right) \tan [c + d x]^2 \right)^2 \\
& \quad \left. (-a^2 + b^2 (1 + \tan [c + d x]^2)) \right) - \left( 2 b^2 \operatorname{Sec} [c + d x]^2 \tan [c + d x] \sqrt{1 + \tan [c + d x]^2} \right. \\
& \quad \left( 6 \left( -3 b^2 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, -\tan [c + d x]^2, \frac{b^2 \tan [c + d x]^2}{a^2 - b^2} \right] + \right. \right. \\
& \quad \quad \left. \left. (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, -\tan [c + d x]^2, \frac{b^2 \tan [c + d x]^2}{a^2 - b^2} \right] \right) \right) \\
& \quad \tan [c + d x]^2 (-a^2 + b^2 (1 + \tan [c + d x]^2)) + 5 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \right. \\
& \quad \left. \left. 1, \frac{5}{2}, -\tan [c + d x]^2, \frac{b^2 \tan [c + d x]^2}{a^2 - b^2} \right] (9 a^2 - b^2 (9 + 8 \tan [c + d x]^2)) \right) \Big/
\end{aligned}$$

$$\begin{aligned}
 & \left( a \left( -15 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, -\tan [c + d x]^2, \frac{b^2 \tan [c + d x]^2}{a^2 - b^2} \right] - \right. \right. \\
 & \quad 2 \left( 3 b^2 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, -\tan [c + d x]^2, \frac{b^2 \tan [c + d x]^2}{a^2 - b^2} \right] + (-a^2 + b^2) \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, -\tan [c + d x]^2, \frac{b^2 \tan [c + d x]^2}{a^2 - b^2} \right] \right) \tan [c + d x]^2 \right) \\
 & \left. (a^2 - b^2 (1 + \tan [c + d x]^2))^2 \right) - \left( \operatorname{Sec} [c + d x]^2 \tan [c + d x] \right. \\
 & \left. \left( 6 \left( -3 b^2 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, -\tan [c + d x]^2, \frac{b^2 \tan [c + d x]^2}{a^2 - b^2} \right] + \right. \right. \right. \\
 & \quad \left. \left. (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, -\tan [c + d x]^2, \frac{b^2 \tan [c + d x]^2}{a^2 - b^2} \right] \right) \right. \\
 & \quad \left. \tan [c + d x]^2 (-a^2 + b^2 (1 + \tan [c + d x]^2)) + 5 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \right. \right. \\
 & \quad \left. \left. 1, \frac{5}{2}, -\tan [c + d x]^2, \frac{b^2 \tan [c + d x]^2}{a^2 - b^2} \right] (9 a^2 - b^2 (9 + 8 \tan [c + d x]^2)) \right) \right) / \\
 & \left( a \sqrt{1 + \tan [c + d x]^2} \left( -15 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, -\tan [c + d x]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{b^2 \tan [c + d x]^2}{a^2 - b^2} \right] - 2 \left( 3 b^2 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, -\tan [c + d x]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{b^2 \tan [c + d x]^2}{a^2 - b^2} \right] + (-a^2 + b^2) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, -\tan [c + d x]^2, \right. \right. \\
 & \quad \left. \left. \frac{b^2 \tan [c + d x]^2}{a^2 - b^2} \right] \right) \tan [c + d x]^2 \right) (a^2 - b^2 (1 + \tan [c + d x]^2)) \right) + \\
 & \left( \sqrt{1 + \tan [c + d x]^2} \left( -4 \left( 3 b^2 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, -\tan [c + d x]^2, \frac{b^2 \tan [c + d x]^2}{a^2 - b^2} \right] + \right. \right. \right. \\
 & \quad \left. \left. (-a^2 + b^2) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, -\tan [c + d x]^2, \frac{b^2 \tan [c + d x]^2}{a^2 - b^2} \right] \right) \right) \\
 & \quad \operatorname{Sec} [c + d x]^2 \tan [c + d x] - 15 (a^2 - b^2) \left( \frac{1}{5 (a^2 - b^2)} 6 b^2 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, 2, \right. \right. \\
 & \quad \left. \left. \frac{7}{2}, -\tan [c + d x]^2, \frac{b^2 \tan [c + d x]^2}{a^2 - b^2} \right] \operatorname{Sec} [c + d x]^2 \tan [c + d x] - \frac{2}{5} \operatorname{AppellF1} \left[ \right. \right. \\
 & \quad \left. \left. \frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, -\tan [c + d x]^2, \frac{b^2 \tan [c + d x]^2}{a^2 - b^2} \right] \operatorname{Sec} [c + d x]^2 \tan [c + d x] \right) - \\
 & \quad 2 \tan [c + d x]^2 \left( 3 b^2 \left( \frac{1}{7 (a^2 - b^2)} 20 b^2 \operatorname{AppellF1} \left[ \frac{7}{2}, \frac{1}{3}, 3, \frac{9}{2}, -\tan [c + d x]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{b^2 \tan [c + d x]^2}{a^2 - b^2} \right] \operatorname{Sec} [c + d x]^2 \tan [c + d x] - \frac{10}{21} \operatorname{AppellF1} \left[ \frac{7}{2}, \frac{4}{3}, 2, \right. \right. \\
 & \quad \left. \left. \frac{9}{2}, -\tan [c + d x]^2, \frac{b^2 \tan [c + d x]^2}{a^2 - b^2} \right] \operatorname{Sec} [c + d x]^2 \tan [c + d x] \right) \right) + \\
 & \quad \left. (-a^2 + b^2) \left( \frac{1}{7 (a^2 - b^2)} 10 b^2 \operatorname{AppellF1} \left[ \frac{7}{2}, \frac{4}{3}, 2, \frac{9}{2}, -\tan [c + d x]^2, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
& \left. \left. \left. \frac{b^2 \tan [c+d x]^2}{a^2-b^2} \right] \operatorname{Sec}[c+d x]^2 \tan [c+d x] - \frac{40}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{7}{3}, 1, \frac{9}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2}\right] \operatorname{Sec}[c+d x]^2 \tan [c+d x] \right) \right) \\
& \left( 6 \left( -3 b^2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2}\right] + \right. \right. \\
& \quad \left. \left. (a^2-b^2) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2}\right] \right) \right. \\
& \quad \left. \tan [c+d x]^2 \left(-a^2+b^2\left(1+\tan [c+d x]^2\right)\right) + 5\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2}\right] \left(9 a^2-b^2\left(9+8 \tan [c+d x]^2\right)\right) \right) \right) / \\
& \left( a \left( -15\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2}\right] - \right. \right. \\
& \quad \left. \left. 2\left( 3 b^2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2}\right] + \right. \right. \right. \\
& \quad \left. \left. \left. \left(-a^2+b^2\right) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2}\right] \right) \right) \right. \\
& \quad \left. \left. \tan [c+d x]^2 \right)^2 \left(a^2-b^2\left(1+\tan [c+d x]^2\right)\right) \right) - \\
& \left( \sqrt{1+\tan [c+d x]^2} \left( -80 b^2\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2}\right] \operatorname{Sec}[c+d x]^2 \tan [c+d x] + 12 b^2 \left( -3 b^2 \right. \right. \right. \\
& \quad \left. \left. \left. \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2}\right] + \left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2}\right] \right) \operatorname{Sec}[c+d x]^2 \tan [c+d x]^3 + \right. \right. \\
& \quad \left. \left. 12 \left( -3 b^2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2}\right] + \right. \right. \right. \\
& \quad \left. \left. \left. \left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2}\right] \right) \right) \right. \\
& \quad \left. \left. \operatorname{Sec}[c+d x]^2 \tan [c+d x] \left(-a^2+b^2\left(1+\tan [c+d x]^2\right)\right) + \right. \right. \\
& \quad \left. \left. 6 \tan [c+d x]^2 \left( -3 b^2 \left( \frac{1}{7\left(a^2-b^2\right)} 20 b^2 \operatorname{AppellF1}\left[\frac{7}{2}, \frac{1}{3}, 3, \frac{9}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2}\right] \operatorname{Sec}[c+d x]^2 \tan [c+d x] - \frac{10}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{4}{3}, 2, \frac{9}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2}\right] \operatorname{Sec}[c+d x]^2 \tan [c+d x] \right) + \right. \right. \right. \\
& \quad \left. \left. \left. \left(a^2-b^2\right) \left( \frac{1}{7\left(a^2-b^2\right)} 10 b^2 \operatorname{AppellF1}\left[\frac{7}{2}, \frac{4}{3}, 2, \frac{9}{2}, -\tan [c+d x]^2, \frac{b^2 \tan [c+d x]^2}{a^2-b^2}\right] \right) \right) \right) \right)
\end{aligned}$$

$$\begin{aligned}
 & \left. \left. \left. \left. \frac{b^2 \operatorname{Tan}[c+dx]^2}{a^2-b^2} \right] \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx] - \frac{40}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{7}{3}, 1, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{9}{2}, -\operatorname{Tan}[c+dx]^2, \frac{b^2 \operatorname{Tan}[c+dx]^2}{a^2-b^2} \right] \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx] \right) \right) \\
 & \left. \left. \left. \left. (-a^2+b^2(1+\operatorname{Tan}[c+dx]^2)) + 5(a^2-b^2) \left( \frac{1}{5(a^2-b^2)} 6b^2 \operatorname{AppellF1}\left[ \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, -\operatorname{Tan}[c+dx]^2, \frac{b^2 \operatorname{Tan}[c+dx]^2}{a^2-b^2} \right] \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx] - \right. \right. \\
 & \left. \left. \frac{2}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, -\operatorname{Tan}[c+dx]^2, \frac{b^2 \operatorname{Tan}[c+dx]^2}{a^2-b^2} \right] \right. \right. \\
 & \left. \left. \left. \left. \operatorname{Sec}[c+dx]^2 \operatorname{Tan}[c+dx] \right) (9a^2-b^2(9+8\operatorname{Tan}[c+dx]^2)) \right) \right) \right) / \\
 & \left( a \left( -15(a^2-b^2) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, -\operatorname{Tan}[c+dx]^2, \frac{b^2 \operatorname{Tan}[c+dx]^2}{a^2-b^2} \right] - \right. \right. \\
 & \left. \left. 2 \left( 3b^2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, -\operatorname{Tan}[c+dx]^2, \frac{b^2 \operatorname{Tan}[c+dx]^2}{a^2-b^2} \right] + \right. \right. \right. \\
 & \left. \left. \left. (-a^2+b^2) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, -\operatorname{Tan}[c+dx]^2, \frac{b^2 \operatorname{Tan}[c+dx]^2}{a^2-b^2} \right] \right) \right) \right) \\
 & \left. \left. \left. \left. \operatorname{Tan}[c+dx]^2 \right) (a^2-b^2(1+\operatorname{Tan}[c+dx]^2)) \right) \right) \right) \right)
 \end{aligned}$$

**Problem 718: Attempted integration timed out after 120 seconds.**

$$\int \operatorname{Sec}[c+dx]^{5/3} \sqrt{a+b \operatorname{Sec}[c+dx]} dx$$

Optimal (type 8, 28 leaves, 0 steps):

$$\operatorname{Int}\left[\operatorname{Sec}[c+dx]^{5/3} \sqrt{a+b \operatorname{Sec}[c+dx]}, x\right]$$

Result (type 1, 1 leaves):

???

**Problem 720: Attempted integration timed out after 120 seconds.**

$$\int \operatorname{Sec}[c+dx]^{2/3} \sqrt{a+b \operatorname{Sec}[c+dx]} dx$$

Optimal (type 8, 28 leaves, 0 steps):

$$\operatorname{Int}\left[\operatorname{Sec}[c+dx]^{2/3} \sqrt{a+b \operatorname{Sec}[c+dx]}, x\right]$$

Result (type 1, 1 leaves):

???

**Problem 726: Attempted integration timed out after 120 seconds.**

$$\int \frac{\sqrt{a + b \operatorname{Sec}[c + d x]}}{\operatorname{Sec}[c + d x]^{7/3}} dx$$

Optimal (type 8, 28 leaves, 0 steps):

$$\operatorname{Int}\left[\frac{\sqrt{a + b \operatorname{Sec}[c + d x]}}{\operatorname{Sec}[c + d x]^{7/3}}, x\right]$$

Result (type 1, 1 leaves):

???

**Problem 727: Attempted integration timed out after 120 seconds.**

$$\int \operatorname{Sec}[c + d x]^{7/3} (a + b \operatorname{Sec}[c + d x])^{3/2} dx$$

Optimal (type 8, 28 leaves, 0 steps):

$$\operatorname{Int}\left[\operatorname{Sec}[c + d x]^{7/3} (a + b \operatorname{Sec}[c + d x])^{3/2}, x\right]$$

Result (type 1, 1 leaves):

???

**Problem 728: Attempted integration timed out after 120 seconds.**

$$\int \operatorname{Sec}[c + d x]^{5/3} (a + b \operatorname{Sec}[c + d x])^{3/2} dx$$

Optimal (type 8, 28 leaves, 0 steps):

$$\operatorname{Int}\left[\operatorname{Sec}[c + d x]^{5/3} (a + b \operatorname{Sec}[c + d x])^{3/2}, x\right]$$

Result (type 1, 1 leaves):

???

**Problem 729: Attempted integration timed out after 120 seconds.**

$$\int \operatorname{Sec}[c + d x]^{4/3} (a + b \operatorname{Sec}[c + d x])^{3/2} dx$$

Optimal (type 8, 28 leaves, 0 steps):

$$\operatorname{Int}\left[\operatorname{Sec}[c + d x]^{4/3} (a + b \operatorname{Sec}[c + d x])^{3/2}, x\right]$$

Result (type 1, 1 leaves):

???



**Problem 730: Attempted integration timed out after 120 seconds.**

$$\int \text{Sec}[c + d x]^{2/3} (a + b \text{Sec}[c + d x])^{3/2} dx$$

Optimal (type 8, 28 leaves, 0 steps):

$$\text{Int}[\text{Sec}[c + d x]^{2/3} (a + b \text{Sec}[c + d x])^{3/2}, x]$$

Result (type 1, 1 leaves):

???

**Problem 732: Attempted integration timed out after 120 seconds.**

$$\int \frac{(a + b \text{Sec}[c + d x])^{3/2}}{\text{Sec}[c + d x]^{1/3}} dx$$

Optimal (type 8, 28 leaves, 0 steps):

$$\text{Int}\left[\frac{(a + b \text{Sec}[c + d x])^{3/2}}{\text{Sec}[c + d x]^{1/3}}, x\right]$$

Result (type 1, 1 leaves):

???

**Problem 736: Attempted integration timed out after 120 seconds.**

$$\int \frac{(a + b \text{Sec}[c + d x])^{3/2}}{\text{Sec}[c + d x]^{7/3}} dx$$

Optimal (type 8, 28 leaves, 0 steps):

$$\text{Int}\left[\frac{(a + b \text{Sec}[c + d x])^{3/2}}{\text{Sec}[c + d x]^{7/3}}, x\right]$$

Result (type 1, 1 leaves):

???

**Problem 737: Attempted integration timed out after 120 seconds.**

$$\int \text{Sec}[c + d x]^{7/3} (a + b \text{Sec}[c + d x])^{5/2} dx$$

Optimal (type 8, 28 leaves, 0 steps):

$$\text{Int}[\text{Sec}[c + d x]^{7/3} (a + b \text{Sec}[c + d x])^{5/2}, x]$$

Result (type 1, 1 leaves):

???

**Problem 738: Attempted integration timed out after 120 seconds.**

$$\int \text{Sec}[c + d x]^{5/3} (a + b \text{Sec}[c + d x])^{5/2} dx$$

Optimal (type 8, 28 leaves, 0 steps):

$$\text{Int}[\text{Sec}[c + d x]^{5/3} (a + b \text{Sec}[c + d x])^{5/2}, x]$$

Result (type 1, 1 leaves):

???

**Problem 739: Attempted integration timed out after 120 seconds.**

$$\int \text{Sec}[c + d x]^{4/3} (a + b \text{Sec}[c + d x])^{5/2} dx$$

Optimal (type 8, 28 leaves, 0 steps):

$$\text{Int}[\text{Sec}[c + d x]^{4/3} (a + b \text{Sec}[c + d x])^{5/2}, x]$$

Result (type 1, 1 leaves):

???

**Problem 740: Attempted integration timed out after 120 seconds.**

$$\int \text{Sec}[c + d x]^{2/3} (a + b \text{Sec}[c + d x])^{5/2} dx$$

Optimal (type 8, 28 leaves, 0 steps):

$$\text{Int}[\text{Sec}[c + d x]^{2/3} (a + b \text{Sec}[c + d x])^{5/2}, x]$$

Result (type 1, 1 leaves):

???

**Problem 742: Attempted integration timed out after 120 seconds.**

$$\int \frac{(a + b \text{Sec}[c + d x])^{5/2}}{\text{Sec}[c + d x]^{1/3}} dx$$

Optimal (type 8, 28 leaves, 0 steps):

$$\text{Int}\left[\frac{(a + b \text{Sec}[c + d x])^{5/2}}{\text{Sec}[c + d x]^{1/3}}, x\right]$$

Result (type 1, 1 leaves):

???

**Problem 744: Attempted integration timed out after 120 seconds.**

$$\int \frac{(a + b \operatorname{Sec}[c + d x])^{5/2}}{\operatorname{Sec}[c + d x]^{4/3}} dx$$

Optimal (type 8, 28 leaves, 0 steps):

$$\operatorname{Int}\left[\frac{(a + b \operatorname{Sec}[c + d x])^{5/2}}{\operatorname{Sec}[c + d x]^{4/3}}, x\right]$$

Result (type 1, 1 leaves):

???

**Problem 746: Attempted integration timed out after 120 seconds.**

$$\int \frac{(a + b \operatorname{Sec}[c + d x])^{5/2}}{\operatorname{Sec}[c + d x]^{7/3}} dx$$

Optimal (type 8, 28 leaves, 0 steps):

$$\operatorname{Int}\left[\frac{(a + b \operatorname{Sec}[c + d x])^{5/2}}{\operatorname{Sec}[c + d x]^{7/3}}, x\right]$$

Result (type 1, 1 leaves):

???

**Problem 756: Attempted integration timed out after 120 seconds.**

$$\int \frac{1}{\operatorname{Sec}[c + d x]^{7/3} \sqrt{a + b \operatorname{Sec}[c + d x]}} dx$$

Optimal (type 8, 28 leaves, 0 steps):

$$\operatorname{Int}\left[\frac{1}{\operatorname{Sec}[c + d x]^{7/3} \sqrt{a + b \operatorname{Sec}[c + d x]}}, x\right]$$

Result (type 1, 1 leaves):

???

**Problem 758: Attempted integration timed out after 120 seconds.**

$$\int \frac{\operatorname{Sec}[c + d x]^{5/3}}{(a + b \operatorname{Sec}[c + d x])^{3/2}} dx$$

Optimal (type 8, 28 leaves, 0 steps):

$$\operatorname{Int}\left[\frac{\operatorname{Sec}[c + d x]^{5/3}}{(a + b \operatorname{Sec}[c + d x])^{3/2}}, x\right]$$

Result (type 1, 1 leaves):

???

**Problem 760: Attempted integration timed out after 120 seconds.**

$$\int \frac{\sec [c + d x]^{2/3}}{(a + b \sec [c + d x])^{3/2}} dx$$

Optimal (type 8, 28 leaves, 0 steps):

$$\text{Int} \left[ \frac{\sec [c + d x]^{2/3}}{(a + b \sec [c + d x])^{3/2}}, x \right]$$

Result (type 1, 1 leaves):

???

**Problem 762: Attempted integration timed out after 120 seconds.**

$$\int \frac{1}{\sec [c + d x]^{1/3} (a + b \sec [c + d x])^{3/2}} dx$$

Optimal (type 8, 28 leaves, 0 steps):

$$\text{Int} \left[ \frac{1}{\sec [c + d x]^{1/3} (a + b \sec [c + d x])^{3/2}}, x \right]$$

Result (type 1, 1 leaves):

???

**Problem 764: Attempted integration timed out after 120 seconds.**

$$\int \frac{1}{\sec [c + d x]^{4/3} (a + b \sec [c + d x])^{3/2}} dx$$

Optimal (type 8, 28 leaves, 0 steps):

$$\text{Int} \left[ \frac{1}{\sec [c + d x]^{4/3} (a + b \sec [c + d x])^{3/2}}, x \right]$$

Result (type 1, 1 leaves):

???

**Problem 766: Attempted integration timed out after 120 seconds.**

$$\int \frac{1}{\sec [c + d x]^{7/3} (a + b \sec [c + d x])^{3/2}} dx$$

Optimal (type 8, 28 leaves, 0 steps):

$$\text{Int}\left[\frac{1}{\text{Sec}[c + d x]^{7/3} (a + b \text{Sec}[c + d x])^{3/2}}, x\right]$$

Result (type 1, 1 leaves):

???

**Problem 768: Attempted integration timed out after 120 seconds.**

$$\int \frac{\text{Sec}[c + d x]^{5/3}}{(a + b \text{Sec}[c + d x])^{5/2}} dx$$

Optimal (type 8, 28 leaves, 0 steps):

$$\text{Int}\left[\frac{\text{Sec}[c + d x]^{5/3}}{(a + b \text{Sec}[c + d x])^{5/2}}, x\right]$$

Result (type 1, 1 leaves):

???

**Problem 770: Attempted integration timed out after 120 seconds.**

$$\int \frac{\text{Sec}[c + d x]^{2/3}}{(a + b \text{Sec}[c + d x])^{5/2}} dx$$

Optimal (type 8, 28 leaves, 0 steps):

$$\text{Int}\left[\frac{\text{Sec}[c + d x]^{2/3}}{(a + b \text{Sec}[c + d x])^{5/2}}, x\right]$$

Result (type 1, 1 leaves):

???

**Problem 772: Attempted integration timed out after 120 seconds.**

$$\int \frac{1}{\text{Sec}[c + d x]^{1/3} (a + b \text{Sec}[c + d x])^{5/2}} dx$$

Optimal (type 8, 28 leaves, 0 steps):

$$\text{Int}\left[\frac{1}{\text{Sec}[c + d x]^{1/3} (a + b \text{Sec}[c + d x])^{5/2}}, x\right]$$

Result (type 1, 1 leaves):

???

### Problem 774: Attempted integration timed out after 120 seconds.

$$\int \frac{1}{\operatorname{Sec}[c + d x]^{4/3} (a + b \operatorname{Sec}[c + d x])^{5/2}} dx$$

Optimal (type 8, 28 leaves, 0 steps):

$$\operatorname{Int}\left[\frac{1}{\operatorname{Sec}[c + d x]^{4/3} (a + b \operatorname{Sec}[c + d x])^{5/2}}, x\right]$$

Result (type 1, 1 leaves):

???

### Problem 776: Attempted integration timed out after 120 seconds.

$$\int \frac{1}{\operatorname{Sec}[c + d x]^{7/3} (a + b \operatorname{Sec}[c + d x])^{5/2}} dx$$

Optimal (type 8, 28 leaves, 0 steps):

$$\operatorname{Int}\left[\frac{1}{\operatorname{Sec}[c + d x]^{7/3} (a + b \operatorname{Sec}[c + d x])^{5/2}}, x\right]$$

Result (type 1, 1 leaves):

???

### Problem 780: Result more than twice size of optimal antiderivative.

$$\int \frac{(d \operatorname{Sec}[e + f x])^n}{a + b \operatorname{Sec}[e + f x]} dx$$

Optimal (type 6, 192 leaves, 6 steps):

$$\begin{aligned} & \frac{1}{(a^2 - b^2) f} a \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}(-1+n), 1, \frac{3}{2}, \operatorname{Sin}[e + f x]^2, \frac{a^2 \operatorname{Sin}[e + f x]^2}{a^2 - b^2}\right] \\ & \operatorname{Cos}[e + f x] (\operatorname{Cos}[e + f x]^2)^{\frac{1}{2}(-1+n)} (d \operatorname{Sec}[e + f x])^n \operatorname{Sin}[e + f x] - \\ & \frac{1}{(a^2 - b^2) f} b \operatorname{AppellF1}\left[\frac{1}{2}, \frac{n}{2}, 1, \frac{3}{2}, \operatorname{Sin}[e + f x]^2, \frac{a^2 \operatorname{Sin}[e + f x]^2}{a^2 - b^2}\right] \\ & (\operatorname{Cos}[e + f x]^2)^{n/2} (d \operatorname{Sec}[e + f x])^n \operatorname{Sin}[e + f x] \end{aligned}$$

Result (type 6, 5280 leaves):

$$\begin{aligned} & \left( (d \operatorname{Sec}[e + f x])^n \operatorname{Tan}[e + f x] \left( -b \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1}{2} - \frac{n}{2}, \frac{3}{2}, -\operatorname{Tan}[e + f x]^2\right] + \right. \right. \\ & \quad \left. \left. a \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, 1 - \frac{n}{2}, \frac{3}{2}, -\operatorname{Tan}[e + f x]^2\right] + \left( 3 a b^2 (a^2 - b^2) \right. \right. \right. \\ & \quad \left. \left. \left. \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{n}{2}, 1, \frac{3}{2}, -\operatorname{Tan}[e + f x]^2, \frac{b^2 \operatorname{Tan}[e + f x]^2}{a^2 - b^2}\right] (1 + \operatorname{Tan}[e + f x]^2)^{n/2} \right) \right) \right) / \end{aligned}$$

$$\begin{aligned}
 & \left( \left( 3 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{n}{2}, 1, \frac{3}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2} \right] + \right. \right. \\
 & \quad \left( (a^2 - b^2) n \operatorname{AppellF1} \left[ \frac{3}{2}, 1 - \frac{n}{2}, 1, \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2} \right] + \right. \\
 & \quad \left. \left. 2 b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{n}{2}, 2, \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2} \right] \right) \tan[e + f x]^2 \right) \\
 & (a^2 - b^2 (1 + \tan[e + f x]^2)) - \left( 3 b^3 (-a^2 + b^2) \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{1}{2} - \frac{n}{2}, 1, \right. \right. \\
 & \quad \left. \left. \frac{3}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2} \right] (1 + \tan[e + f x]^2)^{\frac{1+n}{2}} \right) / \\
 & \left( \left( 3 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{1}{2} - \frac{n}{2}, 1, \frac{3}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2} \right] + \right. \right. \\
 & \quad \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{1}{2} - \frac{n}{2}, 2, \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2} \right] + (a^2 - b^2) (1 + n) \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{2} - \frac{n}{2}, 1, \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2} \right] \right) \tan[e + f x]^2 \right) \\
 & \left. \left. \left. (-a^2 + b^2 (1 + \tan[e + f x]^2)) \right) \right) \right) / \left( a^2 f (a + b \sec[e + f x]) \right) \\
 & \left( \frac{1}{a^2} \sec[e + f x]^2 \left( -b \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{1}{2} - \frac{n}{2}, \frac{3}{2}, -\tan[e + f x]^2 \right] + \right. \right. \\
 & \quad a \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, 1 - \frac{n}{2}, \frac{3}{2}, -\tan[e + f x]^2 \right] + \left( 3 a b^2 (a^2 - b^2) \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{n}{2}, 1, \frac{3}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2} \right] (1 + \tan[e + f x]^2)^{n/2} \right) \right) / \\
 & \left( \left( 3 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{n}{2}, 1, \frac{3}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2} \right] + \right. \right. \\
 & \quad \left( (a^2 - b^2) n \operatorname{AppellF1} \left[ \frac{3}{2}, 1 - \frac{n}{2}, 1, \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2} \right] + \right. \\
 & \quad \left. \left. 2 b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{n}{2}, 2, \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2} \right] \right) \tan[e + f x]^2 \right) \\
 & (a^2 - b^2 (1 + \tan[e + f x]^2)) - \left( 3 b^3 (-a^2 + b^2) \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{1}{2} - \frac{n}{2}, \right. \right. \\
 & \quad \left. \left. 1, \frac{3}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2} \right] (1 + \tan[e + f x]^2)^{\frac{1+n}{2}} \right) / \\
 & \left( \left( 3 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{1}{2} - \frac{n}{2}, 1, \frac{3}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2} \right] + \right. \right. \\
 & \quad \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{1}{2} - \frac{n}{2}, 2, \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2} \right] + \right. \\
 & \quad \left. \left. (a^2 - b^2) (1 + n) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{2} - \frac{n}{2}, 1, \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2} \right] \right) \right) \\
 & \left. \left. \left. \tan[e + f x]^2 \right) (-a^2 + b^2 (1 + \tan[e + f x]^2)) \right) \right) +
 \end{aligned}$$

$$\begin{aligned}
& \frac{1}{a^2} \tan[e+fx] \left( \left( 6 a b^4 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{n}{2}, 1, \frac{3}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2 - b^2}\right] \right. \right. \\
& \quad \left. \left. \operatorname{Sec}[e+fx]^2 \tan[e+fx] (1 + \tan[e+fx]^2)^{n/2} \right) / \right. \\
& \left( \left( 3 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{n}{2}, 1, \frac{3}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2 - b^2}\right] + \right. \right. \\
& \quad \left( (a^2 - b^2) n \operatorname{AppellF1}\left[\frac{3}{2}, 1 - \frac{n}{2}, 1, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2 - b^2}\right] + \right. \\
& \quad \left. \left. 2 b^2 \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{n}{2}, 2, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2 - b^2}\right] \right) \tan[e+fx]^2 \right) \\
& \left. (a^2 - b^2 (1 + \tan[e+fx]^2))^2 \right) + \left( 3 a b^2 (a^2 - b^2) n \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{n}{2}, 1, \frac{3}{2}, \right. \right. \\
& \quad \left. \left. -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2 - b^2}\right] \operatorname{Sec}[e+fx]^2 \tan[e+fx] (1 + \tan[e+fx]^2)^{-1+\frac{n}{2}} \right) / \\
& \left( \left( 3 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{n}{2}, 1, \frac{3}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2 - b^2}\right] + \right. \right. \\
& \quad \left( (a^2 - b^2) n \operatorname{AppellF1}\left[\frac{3}{2}, 1 - \frac{n}{2}, 1, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2 - b^2}\right] + \right. \\
& \quad \left. \left. 2 b^2 \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{n}{2}, 2, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2 - b^2}\right] \right) \tan[e+fx]^2 \right) \\
& \left. (a^2 - b^2 (1 + \tan[e+fx]^2)) \right) + \left( 3 a b^2 (a^2 - b^2) \left( \frac{1}{3} n \operatorname{AppellF1}\left[\frac{3}{2}, 1 - \frac{n}{2}, \right. \right. \right. \\
& \quad \left. \left. 1, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2 - b^2}\right] \operatorname{Sec}[e+fx]^2 \tan[e+fx] + \right. \\
& \quad \left. \frac{1}{3 (a^2 - b^2)} 2 b^2 \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{n}{2}, 2, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2 - b^2}\right] \right) \\
& \quad \left. \operatorname{Sec}[e+fx]^2 \tan[e+fx] \right) (1 + \tan[e+fx]^2)^{n/2} / \\
& \left( \left( 3 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{n}{2}, 1, \frac{3}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2 - b^2}\right] + \right. \right. \\
& \quad \left( (a^2 - b^2) n \operatorname{AppellF1}\left[\frac{3}{2}, 1 - \frac{n}{2}, 1, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2 - b^2}\right] + \right. \\
& \quad \left. \left. 2 b^2 \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{n}{2}, 2, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2 - b^2}\right] \right) \tan[e+fx]^2 \right) \\
& \left. (a^2 - b^2 (1 + \tan[e+fx]^2)) \right) + \left( 6 b^5 (-a^2 + b^2) \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2} - \frac{n}{2}, 1, \frac{3}{2}, \right. \right. \\
& \quad \left. \left. -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2 - b^2}\right] \operatorname{Sec}[e+fx]^2 \tan[e+fx] (1 + \tan[e+fx]^2)^{\frac{1-n}{2}} \right) / \\
& \left( \left( 3 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2} - \frac{n}{2}, 1, \frac{3}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2 - b^2}\right] + \right. \right. \\
& \quad \left( 2 b^2 \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2} - \frac{n}{2}, 2, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2 - b^2}\right] + \right.
\end{aligned}$$



$$\begin{aligned}
 & \left( (a^2 - b^2) (1+n) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{2} - \frac{n}{2}, 1, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2 - b^2} \right] \right) \\
 & \tan[e+fx]^2 \left( -a^2 + b^2 (1 + \tan[e+fx]^2) \right)^2 - \left( 3b^3 (-a^2 + b^2) \right. \\
 & \left. \left( \frac{1}{3(a^2 - b^2)} 2b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{1}{2} - \frac{n}{2}, 2, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2 - b^2} \right] \right. \right. \\
 & \left. \left. \sec[e+fx]^2 \tan[e+fx] - \frac{2}{3} \left( -\frac{1}{2} - \frac{n}{2} \right) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{2} - \frac{n}{2}, 1, \frac{5}{2}, -\tan[e+fx]^2, \right. \right. \right. \\
 & \left. \left. \left. \frac{b^2 \tan[e+fx]^2}{a^2 - b^2} \right] \sec[e+fx]^2 \tan[e+fx] \right) (1 + \tan[e+fx]^2)^{\frac{1+n}{2}} \right) / \\
 & \left( \left( 3(a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{1}{2} - \frac{n}{2}, 1, \frac{3}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2 - b^2} \right] + \right. \right. \\
 & \left. \left( 2b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{1}{2} - \frac{n}{2}, 2, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2 - b^2} \right] + \right. \right. \\
 & \left. \left. (a^2 - b^2) (1+n) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{2} - \frac{n}{2}, 1, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2 - b^2} \right] \right) \right) \\
 & \tan[e+fx]^2 \left( -a^2 + b^2 (1 + \tan[e+fx]^2) \right) - \\
 & \left( 3b^3 (-a^2 + b^2) (1+n) \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{1}{2} - \frac{n}{2}, 1, \frac{3}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2 - b^2} \right] \right. \\
 & \left. \sec[e+fx]^2 \tan[e+fx] (1 + \tan[e+fx]^2)^{-1+\frac{1+n}{2}} \right) / \\
 & \left( \left( 3(a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{1}{2} - \frac{n}{2}, 1, \frac{3}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2 - b^2} \right] + \right. \right. \\
 & \left. \left( 2b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{1}{2} - \frac{n}{2}, 2, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2 - b^2} \right] + \right. \right. \\
 & \left. \left. (a^2 - b^2) (1+n) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{2} - \frac{n}{2}, 1, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2 - b^2} \right] \right) \right) \\
 & \tan[e+fx]^2 \left( -a^2 + b^2 (1 + \tan[e+fx]^2) \right) + a \operatorname{Csc}[e+fx] \operatorname{Sec}[e+fx] \\
 & \left( -\operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, 1 - \frac{n}{2}, \frac{3}{2}, -\tan[e+fx]^2 \right] + (1 + \tan[e+fx]^2)^{-1+\frac{n}{2}} \right) - b \\
 & \operatorname{Csc}[e+fx] \operatorname{Sec}[e+fx] \\
 & \left( -\operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{1}{2} - \frac{n}{2}, \frac{3}{2}, -\tan[e+fx]^2 \right] + (1 + \tan[e+fx]^2)^{-\frac{1}{2}+\frac{n}{2}} \right) + \\
 & \left( 3b^3 (-a^2 + b^2) \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{1}{2} - \frac{n}{2}, 1, \frac{3}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2 - b^2} \right] \right. \\
 & \left. (1 + \tan[e+fx]^2)^{\frac{1+n}{2}} \right. \\
 & \left. \left( 2 \left( 2b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{1}{2} - \frac{n}{2}, 2, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2 - b^2} \right] + \right. \right. \right. \\
 & \left. \left. (a^2 - b^2) (1+n) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{2} - \frac{n}{2}, 1, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2 - b^2} \right] \right) \right)
 \end{aligned}$$

$$\begin{aligned}
& \text{Sec}[e + f x]^2 \text{Tan}[e + f x] + 3 (a^2 - b^2) \left( \frac{1}{3 (a^2 - b^2)} 2 b^2 \text{AppellF1}\left[\frac{3}{2}, \right. \right. \\
& \quad \left. \left. -\frac{1}{2} - \frac{n}{2}, 2, \frac{5}{2}, -\text{Tan}[e + f x]^2, \frac{b^2 \text{Tan}[e + f x]^2}{a^2 - b^2}\right] \text{Sec}[e + f x]^2 \text{Tan}[e + f x] - \right. \\
& \quad \left. \frac{2}{3} \left(-\frac{1}{2} - \frac{n}{2}\right) \text{AppellF1}\left[\frac{3}{2}, \frac{1}{2} - \frac{n}{2}, 1, \frac{5}{2}, -\text{Tan}[e + f x]^2, \frac{b^2 \text{Tan}[e + f x]^2}{a^2 - b^2}\right] \right. \\
& \quad \left. \text{Sec}[e + f x]^2 \text{Tan}[e + f x] \right) + \text{Tan}[e + f x]^2 \left( 2 b^2 \left( \frac{1}{5 (a^2 - b^2)} 12 b^2 \text{AppellF1}\left[ \right. \right. \right. \\
& \quad \left. \left. \frac{5}{2}, -\frac{1}{2} - \frac{n}{2}, 3, \frac{7}{2}, -\text{Tan}[e + f x]^2, \frac{b^2 \text{Tan}[e + f x]^2}{a^2 - b^2}\right] \text{Sec}[e + f x]^2 \right. \\
& \quad \left. \text{Tan}[e + f x] - \frac{6}{5} \left(-\frac{1}{2} - \frac{n}{2}\right) \text{AppellF1}\left[\frac{5}{2}, \frac{1}{2} - \frac{n}{2}, 2, \frac{7}{2}, -\text{Tan}[e + f x]^2, \right. \right. \\
& \quad \left. \left. \frac{b^2 \text{Tan}[e + f x]^2}{a^2 - b^2}\right] \text{Sec}[e + f x]^2 \text{Tan}[e + f x] \right) + (a^2 - b^2) (1 + n) \\
& \quad \left( \frac{1}{5 (a^2 - b^2)} 6 b^2 \text{AppellF1}\left[\frac{5}{2}, \frac{1}{2} - \frac{n}{2}, 2, \frac{7}{2}, -\text{Tan}[e + f x]^2, \frac{b^2 \text{Tan}[e + f x]^2}{a^2 - b^2}\right] \right. \\
& \quad \left. \text{Sec}[e + f x]^2 \text{Tan}[e + f x] - \frac{6}{5} \left(\frac{1}{2} - \frac{n}{2}\right) \text{AppellF1}\left[\frac{5}{2}, \frac{3}{2} - \frac{n}{2}, 1, \frac{7}{2}, \right. \right. \\
& \quad \left. \left. -\text{Tan}[e + f x]^2, \frac{b^2 \text{Tan}[e + f x]^2}{a^2 - b^2}\right] \text{Sec}[e + f x]^2 \text{Tan}[e + f x] \right) \Big) \Big) \Big) / \\
& \left( \left( 3 (a^2 - b^2) \text{AppellF1}\left[\frac{1}{2}, -\frac{1}{2} - \frac{n}{2}, 1, \frac{3}{2}, -\text{Tan}[e + f x]^2, \frac{b^2 \text{Tan}[e + f x]^2}{a^2 - b^2}\right] + \right. \right. \\
& \quad \left( 2 b^2 \text{AppellF1}\left[\frac{3}{2}, -\frac{1}{2} - \frac{n}{2}, 2, \frac{5}{2}, -\text{Tan}[e + f x]^2, \frac{b^2 \text{Tan}[e + f x]^2}{a^2 - b^2}\right] + (a^2 - b^2) \right. \\
& \quad \left. \left. (1 + n) \text{AppellF1}\left[\frac{3}{2}, \frac{1}{2} - \frac{n}{2}, 1, \frac{5}{2}, -\text{Tan}[e + f x]^2, \frac{b^2 \text{Tan}[e + f x]^2}{a^2 - b^2}\right] \right) \right) \\
& \quad \left. \text{Tan}[e + f x]^2 \right)^2 (-a^2 + b^2 (1 + \text{Tan}[e + f x]^2)) \Big) - \\
& \left( 3 a b^2 (a^2 - b^2) \text{AppellF1}\left[\frac{1}{2}, -\frac{n}{2}, 1, \frac{3}{2}, -\text{Tan}[e + f x]^2, \frac{b^2 \text{Tan}[e + f x]^2}{a^2 - b^2}\right] \right. \\
& \quad \left. (1 + \text{Tan}[e + f x]^2)^{n/2} \right. \\
& \quad \left( 2 \left( (a^2 - b^2) n \text{AppellF1}\left[\frac{3}{2}, 1 - \frac{n}{2}, 1, \frac{5}{2}, -\text{Tan}[e + f x]^2, \frac{b^2 \text{Tan}[e + f x]^2}{a^2 - b^2}\right] + \right. \right. \\
& \quad \left. \left. 2 b^2 \text{AppellF1}\left[\frac{3}{2}, -\frac{n}{2}, 2, \frac{5}{2}, -\text{Tan}[e + f x]^2, \frac{b^2 \text{Tan}[e + f x]^2}{a^2 - b^2}\right] \right) \text{Sec}[e + f x]^2 \right. \\
& \quad \left. \text{Tan}[e + f x] + 3 (a^2 - b^2) \left( \frac{1}{3} n \text{AppellF1}\left[\frac{3}{2}, 1 - \frac{n}{2}, 1, \frac{5}{2}, -\text{Tan}[e + f x]^2, \right. \right. \right. \\
& \quad \left. \left. \frac{b^2 \text{Tan}[e + f x]^2}{a^2 - b^2}\right] \text{Sec}[e + f x]^2 \text{Tan}[e + f x] + \frac{1}{3 (a^2 - b^2)} 2 b^2 \text{AppellF1}\left[\frac{3}{2}, \right. \right. \\
& \quad \left. \left. -\frac{n}{2}, 2, \frac{5}{2}, -\text{Tan}[e + f x]^2, \frac{b^2 \text{Tan}[e + f x]^2}{a^2 - b^2}\right] \text{Sec}[e + f x]^2 \text{Tan}[e + f x] \right) + \right.
\end{aligned}$$

$$\begin{aligned}
 & \tan[e+fx]^2 \left( (a^2-b^2)^n \left( \frac{1}{5(a^2-b^2)} 6b^2 \operatorname{AppellF1}\left[\frac{5}{2}, 1-\frac{n}{2}, 2, \frac{7}{2}, -\tan[e+fx]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{b^2 \tan[e+fx]^2}{a^2-b^2} \right] \sec[e+fx]^2 \tan[e+fx] - \frac{6}{5} \left(1-\frac{n}{2}\right) \operatorname{AppellF1}\left[\frac{5}{2}, 2-\frac{n}{2}, 1, \frac{7}{2}, -\tan[e+fx]^2, \right. \right. \\
 & \quad \left. \left. \frac{b^2 \tan[e+fx]^2}{a^2-b^2} \right] \sec[e+fx]^2 \tan[e+fx] \right) + \\
 & 2b^2 \left( \frac{3}{5} n \operatorname{AppellF1}\left[\frac{5}{2}, 1-\frac{n}{2}, 2, \frac{7}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2} \right] \right. \\
 & \quad \left. \sec[e+fx]^2 \tan[e+fx] + \frac{1}{5(a^2-b^2)} 12b^2 \operatorname{AppellF1}\left[\frac{5}{2}, -\frac{n}{2}, 3, \frac{7}{2}, -\tan[e+fx]^2, \right. \right. \\
 & \quad \left. \left. \frac{b^2 \tan[e+fx]^2}{a^2-b^2} \right] \sec[e+fx]^2 \tan[e+fx] \right) \Bigg) \Bigg) \Bigg) \Bigg) / \\
 & \left( \left( 3(a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{n}{2}, 1, \frac{3}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2} \right] + \right. \right. \\
 & \quad \left( (a^2-b^2)^n \operatorname{AppellF1}\left[\frac{3}{2}, 1-\frac{n}{2}, 1, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2} \right] + \right. \\
 & \quad \left. \left. 2b^2 \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{n}{2}, 2, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2} \right] \right) \right. \\
 & \quad \left. \left. \tan[e+fx]^2 \right)^2 (a^2-b^2 (1+\tan[e+fx]^2)) \right) \Bigg) \Bigg) \Bigg) \Bigg)
 \end{aligned}$$

### Problem 781: Result more than twice size of optimal antiderivative.

$$\int \frac{(d \sec[e+fx])^n}{(a+b \sec[e+fx])^2} dx$$

Optimal (type 6, 299 leaves, 9 steps):

$$\begin{aligned}
 & \frac{1}{(a^2-b^2)^2 f} a^2 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}(-3+n), 2, \frac{3}{2}, \sin[e+fx]^2, \frac{a^2 \sin[e+fx]^2}{a^2-b^2}\right] \\
 & \quad \cos[e+fx] (\cos[e+fx]^2)^{\frac{1}{2}(-1+n)} (d \sec[e+fx])^n \sin[e+fx] + \\
 & \frac{1}{(a^2-b^2)^2 f} b^2 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}(-1+n), 2, \frac{3}{2}, \sin[e+fx]^2, \frac{a^2 \sin[e+fx]^2}{a^2-b^2}\right] \\
 & \quad \cos[e+fx] (\cos[e+fx]^2)^{\frac{1}{2}(-1+n)} (d \sec[e+fx])^n \sin[e+fx] - \\
 & \frac{1}{(a^2-b^2)^2 f} 2ab \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}(-2+n), 2, \frac{3}{2}, \sin[e+fx]^2, \frac{a^2 \sin[e+fx]^2}{a^2-b^2}\right] \\
 & \quad (\cos[e+fx]^2)^{n/2} (d \sec[e+fx])^n \sin[e+fx]
 \end{aligned}$$

Result (type 6, 10428 leaves):

$$\left( (d \sec[e+fx])^n \left( -\frac{1}{a^3} 2b \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1}{2}-\frac{n}{2}, \frac{3}{2}, -\tan[e+fx]^2\right] \tan[e+fx] + \right. \right.$$

$$\begin{aligned}
& \frac{\text{Hypergeometric2F1}\left[\frac{1}{2}, 1 - \frac{n}{2}, \frac{3}{2}, -\text{Tan}[e + f x]^2\right] \text{Tan}[e + f x]}{a^2} - \\
& \left( 6 b^3 (a^2 - b^2) \text{AppellF1}\left[\frac{1}{2}, -\frac{1}{2} - \frac{n}{2}, \frac{3}{2}, -\text{Tan}[e + f x]^2, \frac{b^2 \text{Tan}[e + f x]^2}{a^2 - b^2}\right] \right. \\
& \quad \left. \text{Tan}[e + f x] (1 + \text{Tan}[e + f x]^2)^{\frac{1+n}{2}} \right) / \\
& \left( a \left( 3 (a^2 - b^2) \text{AppellF1}\left[\frac{1}{2}, -\frac{1}{2} - \frac{n}{2}, \frac{3}{2}, -\text{Tan}[e + f x]^2, \frac{b^2 \text{Tan}[e + f x]^2}{a^2 - b^2}\right] + \right. \right. \\
& \quad \left( 4 b^2 \text{AppellF1}\left[\frac{3}{2}, -\frac{1}{2} - \frac{n}{2}, 3, \frac{5}{2}, -\text{Tan}[e + f x]^2, \frac{b^2 \text{Tan}[e + f x]^2}{a^2 - b^2}\right] + (a^2 - b^2) (1 + n) \right. \\
& \quad \left. \left. \text{AppellF1}\left[\frac{3}{2}, \frac{1}{2} - \frac{n}{2}, 2, \frac{5}{2}, -\text{Tan}[e + f x]^2, \frac{b^2 \text{Tan}[e + f x]^2}{a^2 - b^2}\right] \right) \text{Tan}[e + f x]^2 \right) \\
& \quad \left( a^2 - b^2 (1 + \text{Tan}[e + f x]^2) \right)^2 \left. + \left( 6 b^2 (a^2 - b^2) \text{AppellF1}\left[\frac{1}{2}, -\frac{n}{2}, 2, \frac{3}{2}, \right. \right. \right. \\
& \quad \left. \left. -\text{Tan}[e + f x]^2, \frac{b^2 \text{Tan}[e + f x]^2}{a^2 - b^2}\right] \text{Tan}[e + f x] (1 + \text{Tan}[e + f x]^2)^{n/2} \right) / \\
& \left( \left( 3 (a^2 - b^2) \text{AppellF1}\left[\frac{1}{2}, -\frac{n}{2}, 2, \frac{3}{2}, -\text{Tan}[e + f x]^2, \frac{b^2 \text{Tan}[e + f x]^2}{a^2 - b^2}\right] + \right. \right. \\
& \quad \left( (a^2 - b^2) n \text{AppellF1}\left[\frac{3}{2}, 1 - \frac{n}{2}, 2, \frac{5}{2}, -\text{Tan}[e + f x]^2, \frac{b^2 \text{Tan}[e + f x]^2}{a^2 - b^2}\right] + \right. \\
& \quad \left. \left. 4 b^2 \text{AppellF1}\left[\frac{3}{2}, -\frac{n}{2}, 3, \frac{5}{2}, -\text{Tan}[e + f x]^2, \frac{b^2 \text{Tan}[e + f x]^2}{a^2 - b^2}\right] \right) \text{Tan}[e + f x]^2 \right) \\
& \quad \left( a^2 - b^2 (1 + \text{Tan}[e + f x]^2) \right)^2 \left. + \left( 6 b^3 (a^2 - b^2) \text{AppellF1}\left[\frac{1}{2}, -\frac{1}{2} - \frac{n}{2}, 1, \frac{3}{2}, \right. \right. \right. \\
& \quad \left. \left. -\text{Tan}[e + f x]^2, \frac{b^2 \text{Tan}[e + f x]^2}{a^2 - b^2}\right] \text{Tan}[e + f x] (1 + \text{Tan}[e + f x]^2)^{\frac{1+n}{2}} \right) / \\
& \left( a^3 \left( 3 (a^2 - b^2) \text{AppellF1}\left[\frac{1}{2}, -\frac{1}{2} - \frac{n}{2}, 1, \frac{3}{2}, -\text{Tan}[e + f x]^2, \frac{b^2 \text{Tan}[e + f x]^2}{a^2 - b^2}\right] + \right. \right. \\
& \quad \left( 2 b^2 \text{AppellF1}\left[\frac{3}{2}, -\frac{1}{2} - \frac{n}{2}, 2, \frac{5}{2}, -\text{Tan}[e + f x]^2, \frac{b^2 \text{Tan}[e + f x]^2}{a^2 - b^2}\right] + (a^2 - b^2) (1 + n) \right. \\
& \quad \left. \left. \text{AppellF1}\left[\frac{3}{2}, \frac{1}{2} - \frac{n}{2}, 1, \frac{5}{2}, -\text{Tan}[e + f x]^2, \frac{b^2 \text{Tan}[e + f x]^2}{a^2 - b^2}\right] \right) \text{Tan}[e + f x]^2 \right) \\
& \quad \left( -a^2 + b^2 (1 + \text{Tan}[e + f x]^2) \right) \left. - \left( 3 b^2 (a^2 - b^2) \text{AppellF1}\left[\frac{1}{2}, -\frac{n}{2}, 1, \frac{3}{2}, \right. \right. \right. \\
& \quad \left. \left. -\text{Tan}[e + f x]^2, \frac{b^2 \text{Tan}[e + f x]^2}{a^2 - b^2}\right] \text{Tan}[e + f x] (1 + \text{Tan}[e + f x]^2)^{n/2} \right) / \\
& \left( a^2 \left( 3 (a^2 - b^2) \text{AppellF1}\left[\frac{1}{2}, -\frac{n}{2}, 1, \frac{3}{2}, -\text{Tan}[e + f x]^2, \frac{b^2 \text{Tan}[e + f x]^2}{a^2 - b^2}\right] + \right. \right. \\
& \quad \left( (a^2 - b^2) n \text{AppellF1}\left[\frac{3}{2}, 1 - \frac{n}{2}, 1, \frac{5}{2}, -\text{Tan}[e + f x]^2, \frac{b^2 \text{Tan}[e + f x]^2}{a^2 - b^2}\right] + \right. \\
& \quad \left. \left. 2 b^2 \text{AppellF1}\left[\frac{3}{2}, -\frac{n}{2}, 2, \frac{5}{2}, -\text{Tan}[e + f x]^2, \frac{b^2 \text{Tan}[e + f x]^2}{a^2 - b^2}\right] \right) \text{Tan}[e + f x]^2 \right)
\end{aligned}$$

$$\begin{aligned}
 & \left. \left( -a^2 + b^2 (1 + \tan[e + f x]^2) \right) \right) \Bigg) \Bigg) \Bigg) / \left( f (a + b \operatorname{Sec}[e + f x])^2 \right. \\
 & \left. - \frac{1}{a^3} 2 b \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{1}{2} - \frac{n}{2}, \frac{3}{2}, -\tan[e + f x]^2 \right] \operatorname{Sec}[e + f x]^2 + \right. \\
 & \left. \frac{\operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, 1 - \frac{n}{2}, \frac{3}{2}, -\tan[e + f x]^2 \right] \operatorname{Sec}[e + f x]^2}{a^2} - \right. \\
 & \left. \left( 24 b^5 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{1}{2} - \frac{n}{2}, 2, \frac{3}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2} \right] \right. \right. \\
 & \left. \left. \operatorname{Sec}[e + f x]^2 \tan[e + f x]^2 (1 + \tan[e + f x]^2)^{\frac{1+n}{2}} \right) \Bigg) \Bigg) / \right. \\
 & \left. \left( a \left( 3 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{1}{2} - \frac{n}{2}, 2, \frac{3}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2} \right] + \right. \right. \right. \\
 & \left. \left( 4 b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{1}{2} - \frac{n}{2}, 3, \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2} \right] + \right. \right. \\
 & \left. \left. (a^2 - b^2) (1 + n) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{2} - \frac{n}{2}, 2, \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2} \right] \right) \right. \\
 & \left. \left. \tan[e + f x]^2 (a^2 - b^2 (1 + \tan[e + f x]^2))^3 \right) + \right. \\
 & \left. \left( 24 b^4 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{n}{2}, 2, \frac{3}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2} \right] \right. \right. \\
 & \left. \left. \operatorname{Sec}[e + f x]^2 \tan[e + f x]^2 (1 + \tan[e + f x]^2)^{n/2} \right) \Bigg) \Bigg) / \right. \\
 & \left. \left( \left( 3 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{n}{2}, 2, \frac{3}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2} \right] + \right. \right. \right. \\
 & \left. \left( (a^2 - b^2) n \operatorname{AppellF1} \left[ \frac{3}{2}, 1 - \frac{n}{2}, 2, \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2} \right] + \right. \right. \\
 & \left. \left. 4 b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{n}{2}, 3, \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2} \right] \right) \tan[e + f x]^2 \right) \\
 & \left. (a^2 - b^2 (1 + \tan[e + f x]^2))^3 - \left( 6 b^3 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{1}{2} - \frac{n}{2}, 2, \frac{3}{2}, \right. \right. \right. \\
 & \left. \left. -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2} \right] \operatorname{Sec}[e + f x]^2 (1 + \tan[e + f x]^2)^{\frac{1+n}{2}} \right) \Bigg) \Bigg) / \right. \\
 & \left. \left( a \left( 3 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{1}{2} - \frac{n}{2}, 2, \frac{3}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2} \right] + \right. \right. \right. \\
 & \left. \left( 4 b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{1}{2} - \frac{n}{2}, 3, \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2} \right] + (a^2 - b^2) (1 + n) \right. \right. \\
 & \left. \left. \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{2} - \frac{n}{2}, 2, \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2} \right] \right) \tan[e + f x]^2 \right) \\
 & \left. (a^2 - b^2 (1 + \tan[e + f x]^2))^2 - \left( 6 b^3 (a^2 - b^2) \tan[e + f x] \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( \frac{1}{3(a^2 - b^2)} 4b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{1}{2} - \frac{n}{2}, \frac{5}{2}, -\operatorname{Tan}[e + fx]^2, \frac{b^2 \operatorname{Tan}[e + fx]^2}{a^2 - b^2} \right] \right. \\
 & \quad \left. \operatorname{Sec}[e + fx]^2 \operatorname{Tan}[e + fx] - \frac{2}{3} \left( -\frac{1}{2} - \frac{n}{2} \right) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{2} - \frac{n}{2}, 2, \frac{5}{2}, -\operatorname{Tan}[e + fx]^2, \right. \right. \\
 & \quad \quad \left. \left. \frac{b^2 \operatorname{Tan}[e + fx]^2}{a^2 - b^2} \right] \operatorname{Sec}[e + fx]^2 \operatorname{Tan}[e + fx] \right) (1 + \operatorname{Tan}[e + fx]^2)^{\frac{1+n}{2}} \Big/ \\
 & \left( a \left( 3(a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{1}{2} - \frac{n}{2}, 2, \frac{3}{2}, -\operatorname{Tan}[e + fx]^2, \frac{b^2 \operatorname{Tan}[e + fx]^2}{a^2 - b^2} \right] + \right. \right. \\
 & \quad \left( 4b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{1}{2} - \frac{n}{2}, 3, \frac{5}{2}, -\operatorname{Tan}[e + fx]^2, \frac{b^2 \operatorname{Tan}[e + fx]^2}{a^2 - b^2} \right] + \right. \\
 & \quad \quad \left. \left. (a^2 - b^2) (1+n) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{2} - \frac{n}{2}, 2, \frac{5}{2}, -\operatorname{Tan}[e + fx]^2, \frac{b^2 \operatorname{Tan}[e + fx]^2}{a^2 - b^2} \right] \right) \right. \\
 & \quad \left. \left. \operatorname{Tan}[e + fx]^2 \right) (a^2 - b^2 (1 + \operatorname{Tan}[e + fx]^2))^2 \right) - \\
 & \left( 6b^3 (a^2 - b^2) (1+n) \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{1}{2} - \frac{n}{2}, 2, \frac{3}{2}, -\operatorname{Tan}[e + fx]^2, \frac{b^2 \operatorname{Tan}[e + fx]^2}{a^2 - b^2} \right] \right. \\
 & \quad \left. \operatorname{Sec}[e + fx]^2 \operatorname{Tan}[e + fx]^2 (1 + \operatorname{Tan}[e + fx]^2)^{-1 + \frac{1+n}{2}} \right) \Big/ \\
 & \left( a \left( 3(a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{1}{2} - \frac{n}{2}, 2, \frac{3}{2}, -\operatorname{Tan}[e + fx]^2, \frac{b^2 \operatorname{Tan}[e + fx]^2}{a^2 - b^2} \right] + \right. \right. \\
 & \quad \left( 4b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{1}{2} - \frac{n}{2}, 3, \frac{5}{2}, -\operatorname{Tan}[e + fx]^2, \frac{b^2 \operatorname{Tan}[e + fx]^2}{a^2 - b^2} \right] + \right. \\
 & \quad \quad \left. \left. (a^2 - b^2) (1+n) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{2} - \frac{n}{2}, 2, \frac{5}{2}, -\operatorname{Tan}[e + fx]^2, \frac{b^2 \operatorname{Tan}[e + fx]^2}{a^2 - b^2} \right] \right) \right. \\
 & \quad \left. \left. \operatorname{Tan}[e + fx]^2 \right) (a^2 - b^2 (1 + \operatorname{Tan}[e + fx]^2))^2 \right) + \\
 & \left( 6b^2 (a^2 - b^2) n \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{n}{2}, 2, \frac{3}{2}, -\operatorname{Tan}[e + fx]^2, \frac{b^2 \operatorname{Tan}[e + fx]^2}{a^2 - b^2} \right] \right. \\
 & \quad \left. \operatorname{Sec}[e + fx]^2 \operatorname{Tan}[e + fx]^2 (1 + \operatorname{Tan}[e + fx]^2)^{-1 + \frac{n}{2}} \right) \Big/ \\
 & \left( \left( 3(a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{n}{2}, 2, \frac{3}{2}, -\operatorname{Tan}[e + fx]^2, \frac{b^2 \operatorname{Tan}[e + fx]^2}{a^2 - b^2} \right] + \right. \right. \\
 & \quad \left( (a^2 - b^2) n \operatorname{AppellF1} \left[ \frac{3}{2}, 1 - \frac{n}{2}, 2, \frac{5}{2}, -\operatorname{Tan}[e + fx]^2, \frac{b^2 \operatorname{Tan}[e + fx]^2}{a^2 - b^2} \right] + \right. \\
 & \quad \quad \left. \left. 4b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{n}{2}, 3, \frac{5}{2}, -\operatorname{Tan}[e + fx]^2, \frac{b^2 \operatorname{Tan}[e + fx]^2}{a^2 - b^2} \right] \right) \operatorname{Tan}[e + fx]^2 \right) \\
 & \quad \left( a^2 - b^2 (1 + \operatorname{Tan}[e + fx]^2) \right)^2 + \left( 6b^2 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{n}{2}, 2, \frac{3}{2}, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}[e + fx]^2, \frac{b^2 \operatorname{Tan}[e + fx]^2}{a^2 - b^2} \right] \operatorname{Sec}[e + fx]^2 (1 + \operatorname{Tan}[e + fx]^2)^{n/2} \right) \Big/ \\
 & \left( \left( 3(a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{n}{2}, 2, \frac{3}{2}, -\operatorname{Tan}[e + fx]^2, \frac{b^2 \operatorname{Tan}[e + fx]^2}{a^2 - b^2} \right] + \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( (a^2 - b^2) n \operatorname{AppellF1}\left[\frac{3}{2}, 1 - \frac{n}{2}, 2, \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2}\right] + \right. \\
 & \quad \left. 4 b^2 \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{n}{2}, 3, \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2}\right] \right) \tan[e + f x]^2 \\
 & (a^2 - b^2 (1 + \tan[e + f x]^2))^2 + \left( 6 b^2 (a^2 - b^2) \tan[e + f x] \right. \\
 & \left. \left( \frac{1}{3} n \operatorname{AppellF1}\left[\frac{3}{2}, 1 - \frac{n}{2}, 2, \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2}\right] \operatorname{Sec}[e + f x]^2 \right. \right. \\
 & \quad \left. \left. \tan[e + f x] + \frac{1}{3 (a^2 - b^2)} 4 b^2 \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{n}{2}, 3, \frac{5}{2}, -\tan[e + f x]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{b^2 \tan[e + f x]^2}{a^2 - b^2} \right] \operatorname{Sec}[e + f x]^2 \tan[e + f x] \right) (1 + \tan[e + f x]^2)^{n/2} \right) / \\
 & \left( \left( 3 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{n}{2}, 2, \frac{3}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2}\right] + \right. \right. \\
 & \quad \left( (a^2 - b^2) n \operatorname{AppellF1}\left[\frac{3}{2}, 1 - \frac{n}{2}, 2, \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2}\right] + \right. \\
 & \quad \left. \left. 4 b^2 \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{n}{2}, 3, \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2}\right] \right) \tan[e + f x]^2 \right) \\
 & (a^2 - b^2 (1 + \tan[e + f x]^2))^2 - \left( 12 b^5 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2} - \frac{n}{2}, 1, \frac{3}{2}, \right. \right. \\
 & \quad \left. \left. -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2} \right] \operatorname{Sec}[e + f x]^2 \tan[e + f x]^2 (1 + \tan[e + f x]^2)^{\frac{1+n}{2}} \right) / \\
 & \left( a^3 \left( 3 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2} - \frac{n}{2}, 1, \frac{3}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2}\right] + \right. \right. \\
 & \quad \left( 2 b^2 \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2} - \frac{n}{2}, 2, \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2}\right] + \right. \\
 & \quad \left. \left. (a^2 - b^2) (1 + n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2} - \frac{n}{2}, 1, \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2}\right] \right) \right) \\
 & \quad \left. \tan[e + f x]^2 \right) (-a^2 + b^2 (1 + \tan[e + f x]^2))^2 + \\
 & \left( 6 b^4 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{n}{2}, 1, \frac{3}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2}\right] \right. \\
 & \quad \left. \operatorname{Sec}[e + f x]^2 \tan[e + f x]^2 (1 + \tan[e + f x]^2)^{n/2} \right) / \\
 & \left( a^2 \left( 3 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{n}{2}, 1, \frac{3}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2}\right] + \right. \right. \\
 & \quad \left( (a^2 - b^2) n \operatorname{AppellF1}\left[\frac{3}{2}, 1 - \frac{n}{2}, 1, \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2}\right] + \right. \\
 & \quad \left. \left. 2 b^2 \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{n}{2}, 2, \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2}\right] \right) \tan[e + f x]^2 \right) \\
 & \quad \left. (-a^2 + b^2 (1 + \tan[e + f x]^2))^2 \right) + \left( 6 b^3 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2} - \frac{n}{2}, 1, \frac{3}{2}, \right. \right.
 \end{aligned}$$

$$\begin{aligned}
& -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}] \operatorname{Sec}[e+fx]^2 (1+\tan[e+fx]^2)^{\frac{1+n}{2}} \Big/ \\
& \left( a^3 \left( 3(a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}-\frac{n}{2}, 1, \frac{3}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] + \right. \right. \\
& \quad \left( 2b^2 \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}-\frac{n}{2}, 2, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] + (a^2-b^2)(1+n) \right. \\
& \quad \left. \left. \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}-\frac{n}{2}, 1, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] \right) \tan[e+fx]^2 \right) \\
& \quad \left. (-a^2+b^2(1+\tan[e+fx]^2)) \right) + \left( 6b^3(a^2-b^2) \tan[e+fx] \right. \\
& \quad \left. \left( \frac{1}{3(a^2-b^2)} 2b^2 \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}-\frac{n}{2}, 2, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] \right. \right. \\
& \quad \left. \left. \operatorname{Sec}[e+fx]^2 \tan[e+fx] - \frac{2}{3} \left(-\frac{1}{2}-\frac{n}{2}\right) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}-\frac{n}{2}, 1, \frac{5}{2}, -\tan[e+fx]^2, \right. \right. \right. \\
& \quad \left. \left. \left. \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] \operatorname{Sec}[e+fx]^2 \tan[e+fx] \right) (1+\tan[e+fx]^2)^{\frac{1+n}{2}} \right) \Big/ \\
& \left( a^3 \left( 3(a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}-\frac{n}{2}, 1, \frac{3}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] + \right. \right. \\
& \quad \left( 2b^2 \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}-\frac{n}{2}, 2, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] + \right. \\
& \quad \left. \left. (a^2-b^2)(1+n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}-\frac{n}{2}, 1, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] \right) \right) \\
& \quad \left. \tan[e+fx]^2 (-a^2+b^2(1+\tan[e+fx]^2)) \right) + \\
& \quad \left( 6b^3(a^2-b^2)(1+n) \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}-\frac{n}{2}, 1, \frac{3}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] \right. \\
& \quad \left. \operatorname{Sec}[e+fx]^2 \tan[e+fx]^2 (1+\tan[e+fx]^2)^{-1+\frac{1+n}{2}} \right) \Big/ \\
& \left( a^3 \left( 3(a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}-\frac{n}{2}, 1, \frac{3}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] + \right. \right. \\
& \quad \left( 2b^2 \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}-\frac{n}{2}, 2, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] + \right. \\
& \quad \left. \left. (a^2-b^2)(1+n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}-\frac{n}{2}, 1, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] \right) \right) \\
& \quad \left. \tan[e+fx]^2 (-a^2+b^2(1+\tan[e+fx]^2)) \right) - \\
& \quad \left( 3b^2(a^2-b^2)n \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{n}{2}, 1, \frac{3}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] \right. \\
& \quad \left. \operatorname{Sec}[e+fx]^2 \tan[e+fx]^2 (1+\tan[e+fx]^2)^{-1+\frac{n}{2}} \right) \Big/ \\
& \left( a^2 \left( 3(a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{n}{2}, 1, \frac{3}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] + \right. \right.
\end{aligned}$$



$$\begin{aligned}
 & \left( (a^2 - b^2) n \operatorname{AppellF1}\left[\frac{3}{2}, 1 - \frac{n}{2}, 1, \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2}\right] + \right. \\
 & \quad \left. 2 b^2 \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{n}{2}, 2, \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2}\right] \right) \tan[e + f x]^2 \\
 & \left( -a^2 + b^2 (1 + \tan[e + f x]^2) \right) - \left( 3 b^2 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{n}{2}, 1, \frac{3}{2}, \right. \right. \\
 & \quad \left. \left. -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2}\right] \operatorname{Sec}[e + f x]^2 (1 + \tan[e + f x]^2)^{n/2} \right) / \\
 & \left( a^2 \left( 3 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{n}{2}, 1, \frac{3}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2}\right] + \right. \right. \\
 & \quad \left( (a^2 - b^2) n \operatorname{AppellF1}\left[\frac{3}{2}, 1 - \frac{n}{2}, 1, \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2}\right] + \right. \\
 & \quad \left. \left. 2 b^2 \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{n}{2}, 2, \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2}\right] \right) \tan[e + f x]^2 \right) \\
 & \left. \left. (-a^2 + b^2 (1 + \tan[e + f x]^2)) \right) - \left( 3 b^2 (a^2 - b^2) \tan[e + f x] \right. \right. \\
 & \quad \left. \left. \left( \frac{1}{3} n \operatorname{AppellF1}\left[\frac{3}{2}, 1 - \frac{n}{2}, 1, \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2}\right] \operatorname{Sec}[e + f x]^2 \right. \right. \right. \\
 & \quad \left. \left. \tan[e + f x] + \frac{1}{3 (a^2 - b^2)} 2 b^2 \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{n}{2}, 2, \frac{5}{2}, -\tan[e + f x]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{b^2 \tan[e + f x]^2}{a^2 - b^2} \right] \operatorname{Sec}[e + f x]^2 \tan[e + f x] \right) (1 + \tan[e + f x]^2)^{n/2} \right) / \\
 & \left( a^2 \left( 3 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{n}{2}, 1, \frac{3}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2}\right] + \right. \right. \\
 & \quad \left( (a^2 - b^2) n \operatorname{AppellF1}\left[\frac{3}{2}, 1 - \frac{n}{2}, 1, \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2}\right] + \right. \\
 & \quad \left. \left. 2 b^2 \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{n}{2}, 2, \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2}\right] \right) \tan[e + f x]^2 \right) \\
 & \left. \left. (-a^2 + b^2 (1 + \tan[e + f x]^2)) \right) + \frac{1}{a^2} \operatorname{Sec}[e + f x]^2 \right. \\
 & \quad \left. \left( -\operatorname{Hypergeometric2F1}\left[\frac{1}{2}, 1 - \frac{n}{2}, \frac{3}{2}, -\tan[e + f x]^2\right] + (1 + \tan[e + f x]^2)^{-1 + \frac{n}{2}} \right) - \frac{1}{a^3} 2 \right. \\
 & \quad \left. b \operatorname{Sec}[e + f x]^2 \right. \\
 & \quad \left. \left( -\operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1}{2} - \frac{n}{2}, \frac{3}{2}, -\tan[e + f x]^2\right] + (1 + \tan[e + f x]^2)^{-\frac{1}{2} + \frac{n}{2}} \right) - \right. \\
 & \quad \left( 6 b^3 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2} - \frac{n}{2}, 1, \frac{3}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2}\right] \right. \\
 & \quad \left. \tan[e + f x] (1 + \tan[e + f x]^2)^{\frac{1+n}{2}} \right. \\
 & \quad \left. \left( 2 \left( 2 b^2 \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2} - \frac{n}{2}, 2, \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2}\right] + (a^2 - b^2) (1 + n) \right. \right. \right. \\
 & \quad \left. \left. \left. \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2} - \frac{n}{2}, 1, \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2}\right] \right) \operatorname{Sec}[e + f x]^2 \right) \right)
 \end{aligned}$$



$$\begin{aligned}
 & \left. \frac{b^2 \tan[e+fx]^2}{a^2-b^2} \right] \sec[e+fx]^2 \tan[e+fx] - \frac{6}{5} \left( -\frac{1}{2} - \frac{n}{2} \right) \text{AppellF1} \left[ \frac{5}{2}, \right. \\
 & \left. \frac{1}{2} - \frac{n}{2}, 3, \frac{7}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2} \right] \sec[e+fx]^2 \tan[e+fx] \Bigg) + \\
 & (a^2-b^2) (1+n) \left( \frac{1}{5(a^2-b^2)} 12 b^2 \text{AppellF1} \left[ \frac{5}{2}, \frac{1}{2} - \frac{n}{2}, 3, \frac{7}{2}, -\tan[e+fx]^2, \right. \right. \\
 & \left. \left. \frac{b^2 \tan[e+fx]^2}{a^2-b^2} \right] \sec[e+fx]^2 \tan[e+fx] - \frac{6}{5} \left( \frac{1}{2} - \frac{n}{2} \right) \text{AppellF1} \left[ \frac{5}{2}, \frac{3}{2} - \frac{n}{2}, \right. \right. \\
 & \left. \left. 2, \frac{7}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2} \right] \sec[e+fx]^2 \tan[e+fx] \right) \Bigg) \Bigg) \Bigg) \Bigg) / \\
 & \left( a \left( 3(a^2-b^2) \text{AppellF1} \left[ \frac{1}{2}, -\frac{1}{2} - \frac{n}{2}, 2, \frac{3}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2} \right] + \right. \right. \\
 & \left. \left( 4 b^2 \text{AppellF1} \left[ \frac{3}{2}, -\frac{1}{2} - \frac{n}{2}, 3, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2} \right] + (a^2-b^2) (1+n) \right. \right. \\
 & \left. \left. \text{AppellF1} \left[ \frac{3}{2}, \frac{1}{2} - \frac{n}{2}, 2, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2} \right] \right) \tan[e+fx]^2 \right)^2 \\
 & \left. (a^2-b^2 (1+\tan[e+fx]^2))^2 \right) + \left( 3 b^2 (a^2-b^2) \text{AppellF1} \left[ \frac{1}{2}, -\frac{n}{2}, 1, \frac{3}{2}, \right. \right. \\
 & \left. \left. -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2} \right] \tan[e+fx] (1+\tan[e+fx]^2)^{n/2} \right. \\
 & \left. \left( 2 \left( (a^2-b^2) n \text{AppellF1} \left[ \frac{3}{2}, 1 - \frac{n}{2}, 1, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2} \right] + \right. \right. \right. \\
 & \left. \left. 2 b^2 \text{AppellF1} \left[ \frac{3}{2}, -\frac{n}{2}, 2, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2} \right] \right) \sec[e+fx]^2 \right. \\
 & \left. \tan[e+fx] + 3(a^2-b^2) \left( \frac{1}{3} n \text{AppellF1} \left[ \frac{3}{2}, 1 - \frac{n}{2}, 1, \frac{5}{2}, -\tan[e+fx]^2, \right. \right. \right. \\
 & \left. \left. \frac{b^2 \tan[e+fx]^2}{a^2-b^2} \right] \sec[e+fx]^2 \tan[e+fx] + \frac{1}{3(a^2-b^2)} 2 b^2 \text{AppellF1} \left[ \frac{3}{2}, \right. \right. \\
 & \left. \left. -\frac{n}{2}, 2, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2} \right] \sec[e+fx]^2 \tan[e+fx] \right) + \\
 & \tan[e+fx]^2 \left( (a^2-b^2) n \left( \frac{1}{5(a^2-b^2)} 6 b^2 \text{AppellF1} \left[ \frac{5}{2}, 1 - \frac{n}{2}, 2, \frac{7}{2}, -\tan[e+fx]^2, \right. \right. \right. \\
 & \left. \left. \frac{b^2 \tan[e+fx]^2}{a^2-b^2} \right] \sec[e+fx]^2 \tan[e+fx] - \frac{6}{5} \left( 1 - \frac{n}{2} \right) \text{AppellF1} \left[ \frac{5}{2}, \right. \right. \\
 & \left. \left. 2 - \frac{n}{2}, 1, \frac{7}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2} \right] \sec[e+fx]^2 \tan[e+fx] \right) + \\
 & 2 b^2 \left( \frac{3}{5} n \text{AppellF1} \left[ \frac{5}{2}, 1 - \frac{n}{2}, 2, \frac{7}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2} \right] \right. \\
 & \left. \sec[e+fx]^2 \tan[e+fx] + \frac{1}{5(a^2-b^2)} 12 b^2 \text{AppellF1} \left[ \frac{5}{2}, -\frac{n}{2}, 3, \frac{7}{2}, \right. \right.
 \end{aligned}$$





$$\begin{aligned}
 & \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b} \right] \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 + \\
 & \left( 4 \operatorname{AppellF1}\left[\frac{1}{2}, 2+m, -m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] \right. \\
 & \left. \left( 1 - \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right) \right) / \\
 & \left( -3(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, 2+m, -m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] \right. + \\
 & 2 \left( (a-b) m \operatorname{AppellF1}\left[\frac{3}{2}, 2+m, 1-m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] \right. - \\
 & \left. (a+b)(2+m) \operatorname{AppellF1}\left[\frac{3}{2}, 3+m, -m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b} \right] \right) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 + \\
 & \left( 4 \operatorname{AppellF1}\left[\frac{1}{2}, 3+m, -m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] \right) / \\
 & \left( 3(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, 3+m, -m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] \right. - \\
 & 2 \left( (a-b) m \operatorname{AppellF1}\left[\frac{3}{2}, 3+m, 1-m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] \right. - \\
 & \left. (a+b)(3+m) \operatorname{AppellF1}\left[\frac{3}{2}, 4+m, -m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b} \right] \right) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right) / \\
 & \left( f \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right)^3 \left( -\frac{1}{\left( -1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right)^3} 6(a+b) m \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \right. \right. \\
 & \left. \left. \frac{\left( 1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right)^m}{\left( 1 - \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right)} \left( -\frac{a \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2} - \right. \right. \right. \\
 & \left. \left. \left. \left( \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \left( a - a \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right) \right) \right) \right) / \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left(1 + \tan\left[\frac{1}{2}(e+fx)\right]^2\right)^2 \left(b + \frac{a - a \tan\left[\frac{1}{2}(e+fx)\right]^2}{1 + \tan\left[\frac{1}{2}(e+fx)\right]^2}\right)^{-1+m} \\
 & \left( \operatorname{AppellF1}\left[\frac{1}{2}, 1+m, -m, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] \right. \\
 & \left. \left(-1 + \tan\left[\frac{1}{2}(e+fx)\right]^2\right)^2\right) / \left( 3(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, 1+m, -m, \frac{3}{2}, \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] - 2 \left( (a-b) m \operatorname{AppellF1}\left[\frac{3}{2}, 1+m, \right. \right. \right. \\
 & \left. \left. \left. 1-m, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] - (a+b)(1+m) \right. \right. \right. \\
 & \left. \left. \left. \operatorname{AppellF1}\left[\frac{3}{2}, 2+m, -m, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] \right) \right) \right) \\
 & \tan\left[\frac{1}{2}(e+fx)\right]^2 + \left( 4 \operatorname{AppellF1}\left[\frac{1}{2}, 2+m, -m, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] \left(1 - \tan\left[\frac{1}{2}(e+fx)\right]^2\right) \right) / \left( -3(a+b) \right. \\
 & \left. \operatorname{AppellF1}\left[\frac{1}{2}, 2+m, -m, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] + 2 \right. \\
 & \left. \left( (a-b) m \operatorname{AppellF1}\left[\frac{3}{2}, 2+m, 1-m, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] - (a+b)(2+m) \operatorname{AppellF1}\left[\frac{3}{2}, 3+m, -m, \frac{5}{2}, \right. \right. \right. \\
 & \left. \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) + \\
 & \left( 4 \operatorname{AppellF1}\left[\frac{1}{2}, 3+m, -m, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] \right) / \\
 & \left( 3(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, 3+m, -m, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] - 2 \left( (a-b) m \operatorname{AppellF1}\left[\frac{3}{2}, 3+m, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
& \left. 1 - m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2, \frac{(a - b) \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2}{a + b} \right] - \\
& \left. (a + b) \operatorname{AppellF1}\left[\frac{3}{2}, 4 + m, -m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2, \right. \right. \\
& \left. \left. \frac{(a - b) \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2}{a + b}\right] \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right) \right) + \\
& \frac{1}{\left(-1 + \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right)^4} 18 (a + b) \operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2 \\
& \left(\frac{1 + \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2}{1 - \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2}\right)^m \left(b + \frac{a - a \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2}\right)^m \\
& \left(\left(\operatorname{AppellF1}\left[\frac{1}{2}, 1 + m, -m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2, \frac{(a - b) \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2}{a + b}\right] \right. \right. \\
& \left. \left. \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right)^2\right) \right) / \\
& \left(3 (a + b) \operatorname{AppellF1}\left[\frac{1}{2}, 1 + m, -m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2, \frac{(a - b) \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2}{a + b}\right] - \right. \\
& 2 \left(\left(a - b\right) m \operatorname{AppellF1}\left[\frac{3}{2}, 1 + m, 1 - m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2, \right. \right. \\
& \left. \left. \frac{(a - b) \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2}{a + b}\right] - (a + b) (1 + m) \operatorname{AppellF1}\left[\frac{3}{2}, 2 + m, -m, \frac{5}{2}, \right. \right. \\
& \left. \left. \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2, \frac{(a - b) \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2}{a + b}\right] \right) \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2 \right) + \\
& \left(4 \operatorname{AppellF1}\left[\frac{1}{2}, 2 + m, -m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2, \frac{(a - b) \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2}{a + b}\right] \right. \\
& \left. \left(1 - \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2\right) \right) / \left(-3 (a + b) \operatorname{AppellF1}\left[\frac{1}{2}, 2 + m, \right. \right. \\
& \left. \left. -m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2, \frac{(a - b) \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2}{a + b}\right] + \right. \\
& \left. 2 \left(\left(a - b\right) m \operatorname{AppellF1}\left[\frac{3}{2}, 2 + m, 1 - m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2, \right. \right. \right.
\end{aligned}$$



$$\begin{aligned}
 & \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b} \right] - (a+b) (2+m) \operatorname{AppellF1}\left[\frac{3}{2}, 3+m, -m, \frac{5}{2}, \right. \\
 & \left. \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b} \right] \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \Bigg) + \\
 & \left( 4 \operatorname{AppellF1}\left[\frac{1}{2}, 3+m, -m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b} \right] \right) / \\
 & \left( 3 (a+b) \operatorname{AppellF1}\left[\frac{1}{2}, 3+m, -m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b} \right] - \right. \\
 & \left. 2 \left( (a-b) m \operatorname{AppellF1}\left[\frac{3}{2}, 3+m, 1-m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \\
 & \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b} \right] - (a+b) (3+m) \operatorname{AppellF1}\left[\frac{3}{2}, 4+m, -m, \frac{5}{2}, \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b} \right] \right) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \Bigg) - \\
 & \frac{1}{(-1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2)^3} 3 (a+b) \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \left( \frac{1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{1 - \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2} \right)^m \\
 & \left( b + \frac{a - a \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2} \right)^m \\
 & \left( \left( \operatorname{AppellF1}\left[\frac{1}{2}, 1+m, -m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b} \right] \right) \right. \\
 & \left. \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right)^2 \right) / \\
 & \left( 3 (a+b) \operatorname{AppellF1}\left[\frac{1}{2}, 1+m, -m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b} \right] - \right. \\
 & \left. 2 \left( (a-b) m \operatorname{AppellF1}\left[\frac{3}{2}, 1+m, 1-m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \\
 & \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b} \right] - (a+b) (1+m) \operatorname{AppellF1}\left[\frac{3}{2}, 2+m, -m, \frac{5}{2}, \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b} \right] \right) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \Bigg) +
 \end{aligned}$$

$$\begin{aligned}
& \left( 4 \operatorname{AppellF1} \left[ \frac{1}{2}, 2+m, -m, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2}{a+b} \right] \right. \\
& \left. \left( 1 - \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right) \right) / \left( -3 (a+b) \operatorname{AppellF1} \left[ \frac{1}{2}, 2+m, \right. \right. \\
& \left. \left. -m, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2}{a+b} \right] + \right. \\
& 2 \left( (a-b) m \operatorname{AppellF1} \left[ \frac{3}{2}, 2+m, 1-m, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, \right. \right. \\
& \left. \left. \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2}{a+b} \right] - (a+b) (2+m) \operatorname{AppellF1} \left[ \frac{3}{2}, 3+m, -m, \frac{5}{2}, \right. \right. \\
& \left. \left. \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2}{a+b} \right] \right) \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right) + \\
& \left( 4 \operatorname{AppellF1} \left[ \frac{1}{2}, 3+m, -m, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2}{a+b} \right] \right) / \\
& \left( 3 (a+b) \operatorname{AppellF1} \left[ \frac{1}{2}, 3+m, -m, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2}{a+b} \right] - \right. \\
& 2 \left( (a-b) m \operatorname{AppellF1} \left[ \frac{3}{2}, 3+m, 1-m, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, \right. \right. \\
& \left. \left. \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2}{a+b} \right] - (a+b) (3+m) \operatorname{AppellF1} \left[ \frac{3}{2}, 4+m, -m, \frac{5}{2}, \right. \right. \\
& \left. \left. \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2}{a+b} \right] \right) \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right) \Bigg) - \\
& \frac{1}{(-1 + \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2)^3} 6 (a+b) m \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right] \left( \frac{1 + \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2}{1 - \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2} \right)^{-1+m} \\
& \left( \frac{\operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]}{1 - \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2} + \right. \\
& \left. \left( \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right] \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right) \right) \right) / \\
& \left( 1 - \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right)^2 \left( b + \frac{a - a \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2}{1 + \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2} \right)^m
\end{aligned}$$

$$\begin{aligned}
 & \left( \left( \text{AppellF1} \left[ \frac{1}{2}, 1+m, -m, \frac{3}{2}, \text{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, \frac{(a-b) \text{Tan} \left[ \frac{1}{2} (e+fx) \right]^2}{a+b} \right] \right. \right. \\
 & \quad \left. \left. \left( -1 + \text{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right)^2 \right) \right) / \\
 & \left( 3 (a+b) \text{AppellF1} \left[ \frac{1}{2}, 1+m, -m, \frac{3}{2}, \text{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, \frac{(a-b) \text{Tan} \left[ \frac{1}{2} (e+fx) \right]^2}{a+b} \right] - \right. \\
 & \quad 2 \left( (a-b) m \text{AppellF1} \left[ \frac{3}{2}, 1+m, 1-m, \frac{5}{2}, \text{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, \right. \right. \\
 & \quad \quad \left. \left. \frac{(a-b) \text{Tan} \left[ \frac{1}{2} (e+fx) \right]^2}{a+b} \right] - (a+b) (1+m) \text{AppellF1} \left[ \frac{3}{2}, 2+m, -m, \frac{5}{2}, \right. \right. \\
 & \quad \quad \left. \left. \text{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, \frac{(a-b) \text{Tan} \left[ \frac{1}{2} (e+fx) \right]^2}{a+b} \right] \right) \text{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right) + \\
 & \left( 4 \text{AppellF1} \left[ \frac{1}{2}, 2+m, -m, \frac{3}{2}, \text{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, \frac{(a-b) \text{Tan} \left[ \frac{1}{2} (e+fx) \right]^2}{a+b} \right] \right. \\
 & \quad \left. \left( 1 - \text{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right) \right) / \left( -3 (a+b) \text{AppellF1} \left[ \frac{1}{2}, 2+m, \right. \right. \\
 & \quad \left. \left. -m, \frac{3}{2}, \text{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, \frac{(a-b) \text{Tan} \left[ \frac{1}{2} (e+fx) \right]^2}{a+b} \right] + \right. \\
 & \quad 2 \left( (a-b) m \text{AppellF1} \left[ \frac{3}{2}, 2+m, 1-m, \frac{5}{2}, \text{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, \right. \right. \\
 & \quad \quad \left. \left. \frac{(a-b) \text{Tan} \left[ \frac{1}{2} (e+fx) \right]^2}{a+b} \right] - (a+b) (2+m) \text{AppellF1} \left[ \frac{3}{2}, 3+m, -m, \frac{5}{2}, \right. \right. \\
 & \quad \quad \left. \left. \text{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, \frac{(a-b) \text{Tan} \left[ \frac{1}{2} (e+fx) \right]^2}{a+b} \right] \right) \text{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right) + \\
 & \left( 4 \text{AppellF1} \left[ \frac{1}{2}, 3+m, -m, \frac{3}{2}, \text{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, \frac{(a-b) \text{Tan} \left[ \frac{1}{2} (e+fx) \right]^2}{a+b} \right] \right) / \\
 & \left( 3 (a+b) \text{AppellF1} \left[ \frac{1}{2}, 3+m, -m, \frac{3}{2}, \text{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, \frac{(a-b) \text{Tan} \left[ \frac{1}{2} (e+fx) \right]^2}{a+b} \right] - \right. \\
 & \quad \left. 2 \left( (a-b) m \text{AppellF1} \left[ \frac{3}{2}, 3+m, 1-m, \frac{5}{2}, \text{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
& \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] - (a+b)(3+m) \operatorname{AppellF1}\left[\frac{3}{2}, 4+m, -m, \frac{5}{2}, \right. \right. \right. \\
& \left. \left. \left. \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right]\right) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right) - \\
& \frac{1}{\left(-1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right)^3} 6(a+b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \left(\frac{1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{1 - \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}\right)^m \\
& \left(b + \frac{a - a \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}\right)^m \\
& \left(\left(2 \operatorname{AppellF1}\left[\frac{1}{2}, 1+m, -m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right]\right) \right. \\
& \left. \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right)\right) / \\
& \left(3(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, 1+m, -m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right]\right) - \\
& 2 \left( (a-b) m \operatorname{AppellF1}\left[\frac{3}{2}, 1+m, 1-m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
& \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] - (a+b)(1+m) \operatorname{AppellF1}\left[\frac{3}{2}, 2+m, -m, \frac{5}{2}, \right. \right. \\
& \left. \left. \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right]\right) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 + \\
& \left(\left(-\frac{1}{3(a+b)}(a-b) m \operatorname{AppellF1}\left[\frac{3}{2}, 1+m, 1-m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \\
& \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] + \frac{1}{3}(1+m) \right. \right. \\
& \left. \left. \operatorname{AppellF1}\left[\frac{3}{2}, 2+m, -m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right]\right) \right. \\
& \left. \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right)^2\right) / \\
& \left(3(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, 1+m, -m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right]\right) -
\end{aligned}$$

$$\begin{aligned}
 & 2 \left( (a-b) m \operatorname{AppellF1} \left[ \frac{3}{2}, 1+m, 1-m, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2}{a+b} \right] - (a+b) (1+m) \operatorname{AppellF1} \left[ \frac{3}{2}, 2+m, -m, \frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2}{a+b} \right] \right) \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \Bigg) - \\
 & \left( 4 \operatorname{AppellF1} \left[ \frac{1}{2}, 2+m, -m, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2}{a+b} \right] \right. \\
 & \quad \left. \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right] \right) / \left( -3 (a+b) \operatorname{AppellF1} \left[ \frac{1}{2}, \right. \right. \\
 & \quad \left. \left. 2+m, -m, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2}{a+b} \right] + \right. \\
 & 2 \left( (a-b) m \operatorname{AppellF1} \left[ \frac{3}{2}, 2+m, 1-m, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2}{a+b} \right] - (a+b) (2+m) \operatorname{AppellF1} \left[ \frac{3}{2}, 3+m, -m, \frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2}{a+b} \right] \right) \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \Bigg) + \\
 & \left( 4 \left( -\frac{1}{3(a+b)} (a-b) m \operatorname{AppellF1} \left[ \frac{3}{2}, 2+m, 1-m, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right. \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2}{a+b} \right] \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right] + \frac{1}{3} (2+m) \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[ \frac{3}{2}, 3+m, -m, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2}{a+b} \right] \right. \right. \\
 & \quad \left. \left. \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right] \right) \left( 1 - \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right) \right) / \left( -3 (a+b) \right. \\
 & \quad \left. \operatorname{AppellF1} \left[ \frac{1}{2}, 2+m, -m, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2}{a+b} \right] + \right. \\
 & 2 \left( (a-b) m \operatorname{AppellF1} \left[ \frac{3}{2}, 2+m, 1-m, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2}{a+b} \right] - (a+b) (2+m) \operatorname{AppellF1} \left[ \frac{3}{2}, 3+m, -m, \frac{5}{2}, \right. \right.
 \end{aligned}$$

$$\begin{aligned}
& \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] \tan\left[\frac{1}{2}(e+fx)\right]^2 \Bigg) + \\
& \left( 4 \left( -\frac{1}{3(a+b)}(a-b) m \operatorname{AppellF1}\left[\frac{3}{2}, 3+m, 1-m, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \\
& \quad \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \right. \right. \\
& \quad \left. \frac{1}{3}(3+m) \operatorname{AppellF1}\left[\frac{3}{2}, 4+m, -m, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
& \quad \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) \right) \Bigg) / \\
& \left( 3(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, 3+m, -m, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] - \right. \\
& \quad 2 \left( (a-b) m \operatorname{AppellF1}\left[\frac{3}{2}, 3+m, 1-m, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
& \quad \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] - (a+b)(3+m) \operatorname{AppellF1}\left[\frac{3}{2}, 4+m, -m, \frac{5}{2}, \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) - \\
& \left( \operatorname{AppellF1}\left[\frac{1}{2}, 1+m, -m, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] \right) \\
& \left( -1 + \tan\left[\frac{1}{2}(e+fx)\right]^2 \right)^2 \left( -2 \left( (a-b) m \operatorname{AppellF1}\left[\frac{3}{2}, 1+m, \right. \right. \right. \\
& \quad \left. \left. 1-m, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] - \right. \right. \\
& \quad \left. (a+b)(1+m) \operatorname{AppellF1}\left[\frac{3}{2}, 2+m, -m, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
& \quad \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] \right) \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \right. \\
& \quad \left. 3(a+b) \left( -\frac{1}{3(a+b)}(a-b) m \operatorname{AppellF1}\left[\frac{3}{2}, 1+m, 1-m, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \\
& \quad \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \frac{1}{3}(1+m) \right) \right)
\end{aligned}$$

$$\begin{aligned}
 & \text{AppellF1}\left[\frac{3}{2}, 2+m, -m, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] \\
 & \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \Bigg) - 2 \tan\left[\frac{1}{2}(e+fx)\right]^2 \\
 & \left( (a-b)m \left( \frac{1}{5(a+b)} {}_3F_2\left(\frac{5}{2}, 1+m, 2-m, \frac{7}{2}, \right. \right. \right. \\
 & \left. \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right. \right. \\
 & \left. \left. + \frac{3}{5}(1+m) \text{AppellF1}\left[\frac{5}{2}, 2+m, 1-m, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) \right) - \\
 & (a+b)(1+m) \left( -\frac{1}{5(a+b)} {}_3F_2\left(\frac{5}{2}, 2+m, 1-m, \frac{7}{2}, \right. \right. \right. \\
 & \left. \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right. \right. \\
 & \left. \left. + \frac{3}{5}(2+m) \text{AppellF1}\left[\frac{5}{2}, 3+m, -m, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] \text{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) \right) \Bigg) \Bigg) / \\
 & \left( 3(a+b) \text{AppellF1}\left[\frac{1}{2}, 1+m, -m, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] - \right. \\
 & 2 \left( (a-b)m \text{AppellF1}\left[\frac{3}{2}, 1+m, 1-m, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] - (a+b)(1+m) \text{AppellF1}\left[\frac{3}{2}, 2+m, -m, \frac{5}{2}, \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \right)^2 - \\
 & \left( 4 \text{AppellF1}\left[\frac{1}{2}, 2+m, -m, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] \right. \\
 & \left. \left( 1 - \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \right) \left( 2 \left( (a-b)m \text{AppellF1}\left[\frac{3}{2}, 2+m, 1-m, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b} \Big] - \\
 & (a+b)(2+m) \operatorname{AppellF1}\left[\frac{3}{2}, 3+m, -m, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \\
 & \left. \frac{(a-b)\tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] - \\
 & 3(a+b) \left( -\frac{1}{3(a+b)}(a-b)m \operatorname{AppellF1}\left[\frac{3}{2}, 2+m, 1-m, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \frac{1}{3}(2+m) \right. \\
 & \left. \operatorname{AppellF1}\left[\frac{3}{2}, 3+m, -m, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) + 2 \tan\left[\frac{1}{2}(e+fx)\right]^2 \\
 & \left( (a-b)m \left( \frac{1}{5(a+b)} 3(a-b)(1-m) \operatorname{AppellF1}\left[\frac{5}{2}, 2+m, 2-m, \frac{7}{2}, \right. \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right. \right. \\
 & \left. \left. + \frac{3}{5}(2+m) \operatorname{AppellF1}\left[\frac{5}{2}, 3+m, 1-m, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \\
 & \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) \right) - \\
 & (a+b)(2+m) \left( -\frac{1}{5(a+b)} 3(a-b)m \operatorname{AppellF1}\left[\frac{5}{2}, 3+m, 1-m, \frac{7}{2}, \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right. \right. \\
 & \left. \left. + \frac{3}{5}(3+m) \operatorname{AppellF1}\left[\frac{5}{2}, 4+m, -m, \frac{7}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \\
 & \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) \right) \Big/ \\
 & \left( -3(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, 2+m, -m, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] \right) +
 \end{aligned}$$



$$\begin{aligned}
 & 2 \left( (a-b) m \operatorname{AppellF1} \left[ \frac{3}{2}, 2+m, 1-m, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2}{a+b} \right] - (a+b) (2+m) \operatorname{AppellF1} \left[ \frac{3}{2}, 3+m, -m, \frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2}{a+b} \right] \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \right)^2 - \\
 & \left( 4 \operatorname{AppellF1} \left[ \frac{1}{2}, 3+m, -m, \frac{3}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2}{a+b} \right] \right. \\
 & \left. - 2 \left( (a-b) m \operatorname{AppellF1} \left[ \frac{3}{2}, 3+m, 1-m, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2}{a+b} \right] - (a+b) (3+m) \operatorname{AppellF1} \left[ \frac{3}{2}, 4+m, -m, \right. \right. \\
 & \quad \left. \left. \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2}{a+b} \right] \right) \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \\
 & \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right] + 3 (a+b) \left( -\frac{1}{3(a+b)} (a-b) m \operatorname{AppellF1} \left[ \frac{3}{2}, 3+m, \right. \right. \\
 & \quad \left. \left. 1-m, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2}{a+b} \right] \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \right. \\
 & \quad \left. \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right] + \frac{1}{3} (3+m) \operatorname{AppellF1} \left[ \frac{3}{2}, 4+m, -m, \frac{5}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2}{a+b} \right] \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right] \right) \right) - \\
 & 2 \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2 \left( (a-b) m \left( \frac{1}{5(a+b)} 3(a-b) (1-m) \operatorname{AppellF1} \left[ \right. \right. \right. \\
 & \quad \left. \left. \frac{5}{2}, 3+m, 2-m, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2}{a+b} \right] \right. \\
 & \quad \left. \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right] + \frac{3}{5} (3+m) \operatorname{AppellF1} \left[ \frac{5}{2}, \right. \right. \\
 & \quad \left. \left. 4+m, 1-m, \frac{7}{2}, \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right]^2}{a+b} \right] \right. \\
 & \quad \left. \left. \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \operatorname{Tan} \left[ \frac{1}{2} (e+fx) \right] \right) \right) - (a+b) (3+m)
 \end{aligned}$$





$$\begin{aligned}
& \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b} \right] + (a+b) (1+m) \operatorname{AppellF1}\left[\frac{3}{2}, 2+m, -m, \frac{5}{2}, \right. \\
& \left. \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b} \right] \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right) - \\
& \left( 2 \operatorname{AppellF1}\left[\frac{1}{2}, 2+m, -m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b} \right] \right) / \\
& \left( -3 (a+b) \operatorname{AppellF1}\left[\frac{1}{2}, 2+m, -m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b} \right] \right) + \\
& 2 \left( (a-b) m \operatorname{AppellF1}\left[\frac{3}{2}, 2+m, 1-m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
& \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b} \right] - (a+b) (2+m) \operatorname{AppellF1}\left[\frac{3}{2}, 3+m, -m, \frac{5}{2}, \right. \right. \\
& \left. \left. \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b} \right] \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right) \right) + \\
& \frac{1}{(-1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2)^2} 3 (a+b) (b+a \operatorname{Cos}[e+fx])^m \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \\
& \operatorname{Sec}[e+fx]^m \left( \left( \operatorname{AppellF1}\left[\frac{1}{2}, 1+m, -m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \\
& \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b} \right] \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right) \right) \right) / \\
& \left( 3 (a+b) \operatorname{AppellF1}\left[\frac{1}{2}, 1+m, -m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b} \right] \right) + \\
& 2 \left( (-a+b) m \operatorname{AppellF1}\left[\frac{3}{2}, 1+m, 1-m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
& \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b} \right] + (a+b) (1+m) \operatorname{AppellF1}\left[\frac{3}{2}, 2+m, -m, \frac{5}{2}, \right. \right. \\
& \left. \left. \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b} \right] \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right) - \\
& \left( 2 \operatorname{AppellF1}\left[\frac{1}{2}, 2+m, -m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b} \right] \right) /
\end{aligned}$$

$$\begin{aligned}
 & \left( -3 (a+b) \operatorname{AppellF1}\left[\frac{1}{2}, 2+m, -m, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] + \right. \\
 & 2 \left( (a-b) m \operatorname{AppellF1}\left[\frac{3}{2}, 2+m, 1-m, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] - (a+b)(2+m) \operatorname{AppellF1}\left[\frac{3}{2}, 3+m, -m, \frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) - \\
 & \frac{1}{\left(-1 + \tan\left[\frac{1}{2}(e+fx)\right]^2\right)^2} 6 a (a+b) m (b+a \cos[e+fx])^{-1+m} \operatorname{Sec}[e+fx]^m \\
 & \sin[e+fx] \tan\left[\frac{1}{2}(e+fx)\right] \\
 & \left( \left( \operatorname{AppellF1}\left[\frac{1}{2}, 1+m, -m, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] \right) \right. \\
 & \quad \left. \left(-1 + \tan\left[\frac{1}{2}(e+fx)\right]^2\right) \right) / \\
 & \left( 3 (a+b) \operatorname{AppellF1}\left[\frac{1}{2}, 1+m, -m, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] + \right. \\
 & 2 \left( (-a+b) m \operatorname{AppellF1}\left[\frac{3}{2}, 1+m, 1-m, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] + (a+b)(1+m) \operatorname{AppellF1}\left[\frac{3}{2}, 2+m, -m, \frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) - \\
 & \left( 2 \operatorname{AppellF1}\left[\frac{1}{2}, 2+m, -m, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] \right) / \\
 & \left( -3 (a+b) \operatorname{AppellF1}\left[\frac{1}{2}, 2+m, -m, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] + \right. \\
 & 2 \left( (a-b) m \operatorname{AppellF1}\left[\frac{3}{2}, 2+m, 1-m, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right.
 \end{aligned}$$

$$\begin{aligned}
& \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b} \right] - (a+b)(2+m) \operatorname{AppellF1}\left[\frac{3}{2}, 3+m, -m, \frac{5}{2}, \right. \right. \\
& \left. \left. \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b} \right] \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right) \right) + \\
& \frac{1}{\left(-1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right)^2} 6(a+b)m(b+a \operatorname{Cos}[e+fx])^m \operatorname{Sec}[e+fx]^{1+m} \\
& \operatorname{Sin}[e+fx] \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \\
& \left( \left( \operatorname{AppellF1}\left[\frac{1}{2}, 1+m, -m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b} \right] \right) \right. \\
& \left. \left. \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right) \right) \right) / \\
& \left( 3(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, 1+m, -m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b} \right] \right) + \\
& 2 \left( (-a+b)m \operatorname{AppellF1}\left[\frac{3}{2}, 1+m, 1-m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
& \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b} \right] + (a+b)(1+m) \operatorname{AppellF1}\left[\frac{3}{2}, 2+m, -m, \frac{5}{2}, \right. \right. \\
& \left. \left. \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b} \right] \right) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 - \\
& \left( 2 \operatorname{AppellF1}\left[\frac{1}{2}, 2+m, -m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b} \right] \right) / \\
& \left( -3(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, 2+m, -m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b} \right] \right) + \\
& 2 \left( (a-b)m \operatorname{AppellF1}\left[\frac{3}{2}, 2+m, 1-m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
& \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b} \right] - (a+b)(2+m) \operatorname{AppellF1}\left[\frac{3}{2}, 3+m, -m, \frac{5}{2}, \right. \right. \\
& \left. \left. \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b} \right] \right) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right) \right) +
\end{aligned}$$

$$\begin{aligned}
 & \frac{1}{(-1 + \tan[\frac{1}{2}(e+fx)])^2} 6(a+b)(b+a \cos[e+fx])^m \sec[e+fx]^m \\
 & \tan[\frac{1}{2}(e+fx)] \\
 & \left( \left( \text{AppellF1}\left[\frac{1}{2}, 1+m, -m, \frac{3}{2}, \tan[\frac{1}{2}(e+fx)]^2, \frac{(a-b)\tan[\frac{1}{2}(e+fx)]^2}{a+b}\right] \right. \right. \\
 & \quad \left. \left. \sec[\frac{1}{2}(e+fx)]^2 \tan[\frac{1}{2}(e+fx)] \right) / \right. \\
 & \left( 3(a+b) \text{AppellF1}\left[\frac{1}{2}, 1+m, -m, \frac{3}{2}, \tan[\frac{1}{2}(e+fx)]^2, \frac{(a-b)\tan[\frac{1}{2}(e+fx)]^2}{a+b}\right] + \right. \\
 & \quad 2 \left( (-a+b) m \text{AppellF1}\left[\frac{3}{2}, 1+m, 1-m, \frac{5}{2}, \tan[\frac{1}{2}(e+fx)]^2, \right. \right. \\
 & \quad \quad \left. \left. \frac{(a-b)\tan[\frac{1}{2}(e+fx)]^2}{a+b}\right] + (a+b)(1+m) \text{AppellF1}\left[\frac{3}{2}, 2+m, -m, \frac{5}{2}, \right. \right. \\
 & \quad \quad \left. \left. \tan[\frac{1}{2}(e+fx)]^2, \frac{(a-b)\tan[\frac{1}{2}(e+fx)]^2}{a+b}\right] \right) \tan[\frac{1}{2}(e+fx)]^2 \left. \right) + \\
 & \left( \left( -\frac{1}{3(a+b)} (a-b) m \text{AppellF1}\left[\frac{3}{2}, 1+m, 1-m, \frac{5}{2}, \tan[\frac{1}{2}(e+fx)]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{(a-b)\tan[\frac{1}{2}(e+fx)]^2}{a+b}\right] \sec[\frac{1}{2}(e+fx)]^2 \tan[\frac{1}{2}(e+fx)] + \right. \\
 & \quad \left. \frac{1}{3}(1+m) \text{AppellF1}\left[\frac{3}{2}, 2+m, -m, \frac{5}{2}, \tan[\frac{1}{2}(e+fx)]^2, \frac{(a-b)\tan[\frac{1}{2}(e+fx)]^2}{a+b}\right] \right. \\
 & \quad \left. \sec[\frac{1}{2}(e+fx)]^2 \tan[\frac{1}{2}(e+fx)] \right) \left( -1 + \tan[\frac{1}{2}(e+fx)]^2 \right) \left. \right) / \\
 & \left( 3(a+b) \text{AppellF1}\left[\frac{1}{2}, 1+m, -m, \frac{3}{2}, \tan[\frac{1}{2}(e+fx)]^2, \frac{(a-b)\tan[\frac{1}{2}(e+fx)]^2}{a+b}\right] + \right. \\
 & \quad 2 \left( (-a+b) m \text{AppellF1}\left[\frac{3}{2}, 1+m, 1-m, \frac{5}{2}, \tan[\frac{1}{2}(e+fx)]^2, \right. \right. \\
 & \quad \quad \left. \left. \frac{(a-b)\tan[\frac{1}{2}(e+fx)]^2}{a+b}\right] + (a+b)(1+m) \text{AppellF1}\left[\frac{3}{2}, 2+m, -m, \frac{5}{2}, \right. \right. \\
 & \quad \quad \left. \left. \tan[\frac{1}{2}(e+fx)]^2, \frac{(a-b)\tan[\frac{1}{2}(e+fx)]^2}{a+b}\right] \right) \tan[\frac{1}{2}(e+fx)]^2 \left. \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] \tan\left[\frac{1}{2}(e+fx)\right]^2 \Bigg) - \\
 & \left( 2 \left( -\frac{1}{3(a+b)}(a-b) m \operatorname{AppellF1}\left[\frac{3}{2}, 2+m, 1-m, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \right. \right. \\
 & \quad \left. \frac{1}{3}(2+m) \operatorname{AppellF1}\left[\frac{3}{2}, 3+m, -m, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] \right) \right) \Bigg) / \\
 & \left( -3(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, 2+m, -m, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] + \right. \\
 & \quad \left. 2 \left( (a-b) m \operatorname{AppellF1}\left[\frac{3}{2}, 2+m, 1-m, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] - (a+b)(2+m) \operatorname{AppellF1}\left[\frac{3}{2}, 3+m, -m, \frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \Bigg) - \\
 & \left( \operatorname{AppellF1}\left[\frac{1}{2}, 1+m, -m, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] \right) \left( -1 + \right. \\
 & \quad \left. \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \left( 2 \left( (-a+b) m \operatorname{AppellF1}\left[\frac{3}{2}, 1+m, 1-m, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] + (a+b)(1+m) \operatorname{AppellF1}\left[\frac{3}{2}, 2+m, -m, \frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] \right) \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \right. \\
 & \quad \left. 3(a+b) \left( -\frac{1}{3(a+b)}(a-b) m \operatorname{AppellF1}\left[\frac{3}{2}, 1+m, 1-m, \right. \right. \right. \\
 & \quad \left. \left. \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(e+fx)\right] + \frac{1}{3}(1+m) \operatorname{AppellF1}\left[\frac{3}{2}, 2+m, -m, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right.
 \end{aligned}$$



$$\begin{aligned}
 & \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b} \right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \right] + \\
 & 2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \left( (-a+b) m \left( \frac{1}{5(a+b)} - 3(a-b)(1-m) \operatorname{AppellF1}\left[\frac{5}{2}, 1+m, 2-m, \right. \right. \right. \\
 & \left. \left. \left. \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b} \right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \right. \right. \right. \\
 & \left. \left. \left. + \frac{3}{5}(1+m) \operatorname{AppellF1}\left[\frac{5}{2}, 2+m, 1-m, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b} \right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \right) \right) + \\
 & (a+b)(1+m) \left( -\frac{1}{5(a+b)} - 3(a-b) m \operatorname{AppellF1}\left[\frac{5}{2}, 2+m, 1-m, \frac{7}{2}, \right. \right. \right. \\
 & \left. \left. \left. \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b} \right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \right. \right. \right. \\
 & \left. \left. \left. + \frac{3}{5}(2+m) \operatorname{AppellF1}\left[\frac{5}{2}, 3+m, -m, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b} \right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \right) \right) \right) \right) \Big/ \\
 & \left( 3(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, 1+m, -m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b} \right] \right) + \\
 & 2 \left( (-a+b) m \operatorname{AppellF1}\left[\frac{3}{2}, 1+m, 1-m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b} \right] + (a+b)(1+m) \operatorname{AppellF1}\left[\frac{3}{2}, 2+m, -m, \frac{5}{2}, \right. \right. \right. \\
 & \left. \left. \left. \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b} \right] \right) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right)^2 + \\
 & \left( 2 \operatorname{AppellF1}\left[\frac{1}{2}, 2+m, -m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b} \right] \right) \\
 & \left( 2 \left( (a-b) m \operatorname{AppellF1}\left[\frac{3}{2}, 2+m, 1-m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b} \right] - (a+b)(2+m) \operatorname{AppellF1}\left[\frac{3}{2}, 3+m, -m, \frac{5}{2}, \right. \right. \right. \right.
 \end{aligned}$$





$$\begin{aligned}
& \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b} \right] + 2 \left( - (a-b) m \operatorname{AppellF1}\left[\frac{3}{2}, 1+m, 1-m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] + (a+b)(1+m) \operatorname{AppellF1}\left[\frac{3}{2}, 2+m, -m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] \right) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right) - \\
& \left( 3(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, 1+m, -m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] \right. \\
& \left. (b+a \operatorname{Cos}[e+fx])^m \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Sec}[e+fx]^m \right) / \left( \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right) \right. \\
& \left. \left( 3(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, 1+m, -m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] + \right. \right. \\
& \left. \left. 2 \left( - (a-b) m \operatorname{AppellF1}\left[\frac{3}{2}, 1+m, 1-m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] + (a+b)(1+m) \operatorname{AppellF1}\left[\frac{3}{2}, 2+m, -m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] \right) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right) \right) + \\
& \left( 6a(a+b) m \operatorname{AppellF1}\left[\frac{1}{2}, 1+m, -m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] \right. \\
& \left. (b+a \operatorname{Cos}[e+fx])^{-1+m} \operatorname{Sec}[e+fx]^m \operatorname{Sin}[e+fx] \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] \right) / \left( \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right) \right. \\
& \left. \left( 3(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, 1+m, -m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] + \right. \right. \\
& \left. \left. 2 \left( - (a-b) m \operatorname{AppellF1}\left[\frac{3}{2}, 1+m, 1-m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] + (a+b)(1+m) \operatorname{AppellF1}\left[\frac{3}{2}, 2+m, -m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b}\right] \right) \right) \right) +
\end{aligned}$$







### Problem 823: Result more than twice size of optimal antiderivative.

$$\int \frac{1}{\cos [c+d x]^{7 / 2} (a+b \operatorname{Sec}[c+d x])} d x$$

Optimal (type 4, 128 leaves, 11 steps):

$$\frac{2 a \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{b^2 d} + \frac{2 \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{3 b d} +$$

$$\frac{2 a^2 \operatorname{EllipticPi}\left[\frac{2 a}{a+b}, \frac{1}{2}(c+d x), 2\right]}{b^2(a+b) d} + \frac{2 \operatorname{Sin}[c+d x]}{3 b d \cos [c+d x]^{3 / 2}} - \frac{2 a \operatorname{Sin}[c+d x]}{b^2 d \sqrt{\cos [c+d x]}}$$

Result (type 4, 257 leaves):

$$\frac{1}{6 b^2 d} \left( \frac{2(9 a^2 + 2 b^2) \operatorname{EllipticPi}\left[\frac{2 a}{a+b}, \frac{1}{2}(c+d x), 2\right]}{a+b} + \right.$$

$$8 b \left( 2 \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right] - \frac{2 b \operatorname{EllipticPi}\left[\frac{2 a}{a+b}, \frac{1}{2}(c+d x), 2\right]}{a+b} \right) +$$

$$\left( 3 \cos [2(c+d x)] \left( -4 a b \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\sqrt{\cos [c+d x]}\right], -1\right] + \right. \right.$$

$$4 b(a+b) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{\cos [c+d x]}\right], -1\right] -$$

$$\left. \left. 2\left(a^2 - 2 b^2\right) \operatorname{EllipticPi}\left[-\frac{a}{b}, -\operatorname{ArcSin}\left[\sqrt{\cos [c+d x]}\right], -1\right] \right) \operatorname{Sin}[c+d x] \right) /$$

$$\left( b \sqrt{1 - \cos [c+d x]^2} \left( -1 + 2 \cos [c+d x]^2 \right) \right) +$$

$$\frac{\sqrt{\cos [c+d x]} \left( -\frac{2 a \operatorname{Tan}[c+d x]}{b^2} + \frac{2 \operatorname{Sec}[c+d x] \operatorname{Tan}[c+d x]}{3 b} \right)}{d}$$

### Problem 837: Unable to integrate problem.

$$\int \cos [c+d x]^{5 / 2} \sqrt{a+b \operatorname{Sec}[c+d x]} d x$$

Optimal (type 4, 244 leaves, 10 steps):



$$\begin{aligned}
 & - \frac{4 b (a^2 - b^2) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{15 a^2 d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} + \\
 & \left( 2 (9 a^2 - 2 b^2) \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \sec [c+d x]} \right) / \\
 & \left( 15 a^2 d \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \right) + \frac{2 b \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{15 a d} + \\
 & \frac{2 \cos [c+d x]^{3/2} \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{5 d}
 \end{aligned}$$

Result (type 8, 27 leaves):

$$\int \cos [c+d x]^{5/2} \sqrt{a+b \sec [c+d x]} dx$$

**Problem 838: Unable to integrate problem.**

$$\int \cos [c+d x]^{3/2} \sqrt{a+b \sec [c+d x]} dx$$

Optimal (type 4, 192 leaves, 9 steps):

$$\begin{aligned}
 & \frac{2 (a^2 - b^2) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{3 a d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} + \\
 & \frac{2 b \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \sec [c+d x]}}{3 a d \sqrt{\frac{b+a \cos [c+d x]}{a+b}}} + \\
 & \frac{2 \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{3 d}
 \end{aligned}$$

Result (type 8, 27 leaves):

$$\int \cos [c+d x]^{3/2} \sqrt{a+b \sec [c+d x]} dx$$

**Problem 839: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]} dx$$

Optimal (type 4, 67 leaves, 4 steps):

$$\frac{2 \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \sec [c+d x]}}{d \sqrt{\frac{b+a \cos [c+d x]}{a+b}}}$$

Result (type 4, 198 leaves):

$$\left( \sqrt{\cos [c+d x]} \sec \left[ \frac{1}{2}(c+d x) \right]^2 \right. \\ \left. \sqrt{a+b \sec [c+d x]} \left( \operatorname{EllipticE}\left[ \operatorname{ArcSinh}\left[ \tan \left[ \frac{1}{2}(c+d x) \right] \right], \frac{-a+b}{a+b} \right] - \right. \right. \\ \left. \operatorname{EllipticF}\left[ \operatorname{ArcSinh}\left[ \tan \left[ \frac{1}{2}(c+d x) \right] \right], \frac{-a+b}{a+b} \right] + \right. \right. \\ \left. \left. \sqrt{\frac{1}{1+\cos [c+d x]}} \sqrt{\frac{b+a \cos [c+d x]}{(a+b)(1+\cos [c+d x])}} \sin [c+d x] \right) \right) / \\ \left( d \sqrt{\frac{1}{1+\cos [c+d x]}} \sqrt{\frac{b+a \cos [c+d x]}{(a+b)(1+\cos [c+d x])}} \right)$$

Problem 840: Unable to integrate problem.

$$\int \frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{\cos [c+d x]}} dx$$

Optimal (type 4, 138 leaves, 8 steps):

$$\frac{2 a \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} + \frac{2 b \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}}$$

Result (type 8, 27 leaves):

$$\int \frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{\cos [c+d x]}} dx$$

Problem 841: Attempted integration timed out after 120 seconds.

$$\int \frac{\sqrt{a+b \sec [c+d x]}}{\cos [c+d x]^{3/2}} dx$$

Optimal (type 4, 237 leaves, 13 steps):

$$\begin{aligned}
 & \frac{b \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} + \frac{a \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} - \\
 & \frac{\sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \sec [c+d x]}}{d \sqrt{\frac{b+a \cos [c+d x]}{a+b}}} + \frac{\sqrt{a+b \sec [c+d x]} \sin [c+d x]}{d \sqrt{\cos [c+d x]}}
 \end{aligned}$$

Result (type 1, 1 leaves):

???

### Problem 842: Unable to integrate problem.

$$\int \cos [c+d x]^{7 / 2}(a+b \sec [c+d x])^{3 / 2} d x$$

Optimal (type 4, 303 leaves, 11 steps):

$$\begin{aligned}
 & \frac{2\left(25 a^4-31 a^2 b^2+6 b^4\right) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{105 a^2 d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} + \\
 & \left(4 b\left(41 a^2-3 b^2\right) \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \sec [c+d x]}\right) / \\
 & \left(105 a^2 d \sqrt{\frac{b+a \cos [c+d x]}{a+b}}\right) + \frac{2\left(25 a^2+3 b^2\right) \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{105 a d} + \\
 & \frac{16 b \cos [c+d x]^{3 / 2} \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{35 d} + \\
 & \frac{2 a \cos [c+d x]^{5 / 2} \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{7 d}
 \end{aligned}$$

Result (type 8, 27 leaves):

$$\int \cos [c+d x]^{7 / 2}(a+b \sec [c+d x])^{3 / 2} d x$$

### Problem 843: Unable to integrate problem.

$$\int \cos [c+d x]^{5 / 2}(a+b \sec [c+d x])^{3 / 2} d x$$

Optimal (type 4, 240 leaves, 10 steps):

$$\frac{2 b (a^2 - b^2) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{5 a d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} +$$

$$\left(2\left(3 a^2+b^2\right) \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \sec [c+d x]}\right) /$$

$$\left(5 a d \sqrt{\frac{b+a \cos [c+d x]}{a+b}}\right) + \frac{4 b \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{5 d} +$$

$$\frac{2 a \cos [c+d x]^{3 / 2} \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{5 d}$$

Result (type 8, 27 leaves):

$$\int \cos [c+d x]^{5 / 2} (a+b \sec [c+d x])^{3 / 2} d x$$

**Problem 844: Unable to integrate problem.**

$$\int \cos [c+d x]^{3 / 2} (a+b \sec [c+d x])^{3 / 2} d x$$

Optimal (type 4, 187 leaves, 9 steps):

$$\frac{2\left(a^2-b^2\right) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{3 d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} +$$

$$\frac{8 b \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \sec [c+d x]}}{3 d \sqrt{\frac{b+a \cos [c+d x]}{a+b}}} +$$

$$\frac{2 a \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{3 d}$$

Result (type 8, 27 leaves):

$$\int \cos [c+d x]^{3 / 2} (a+b \sec [c+d x])^{3 / 2} d x$$

**Problem 845: Unable to integrate problem.**

$$\int \sqrt{\cos [c+d x]} (a+b \sec [c+d x])^{3 / 2} d x$$

Optimal (type 4, 209 leaves, 12 steps):

$$\begin{aligned}
 & \frac{2 a b \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} + \\
 & \frac{2 b^2 \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} + \\
 & \frac{2 a \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \sec [c+d x]}}{d \sqrt{\frac{b+a \cos [c+d x]}{a+b}}}
 \end{aligned}$$

Result (type 8, 27 leaves):

$$\int \sqrt{\cos [c+d x]} (a+b \sec [c+d x])^{3/2} dx$$

**Problem 846: Unable to integrate problem.**

$$\int \frac{(a+b \sec [c+d x])^{3/2}}{\sqrt{\cos [c+d x]}} dx$$

Optimal (type 4, 249 leaves, 13 steps):

$$\begin{aligned}
 & \frac{(2 a^2+b^2) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} + \\
 & \frac{3 a b \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} - \\
 & \frac{b \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \sec [c+d x]}}{d \sqrt{\frac{b+a \cos [c+d x]}{a+b}}} + \\
 & \frac{b \sqrt{a+b \sec [c+d x]} \operatorname{Sin}[c+d x]}{d \sqrt{\cos [c+d x]}}
 \end{aligned}$$

Result (type 8, 27 leaves):

$$\int \frac{(a+b \sec [c+d x])^{3/2}}{\sqrt{\cos [c+d x]}} dx$$

### Problem 847: Unable to integrate problem.

$$\int \frac{(a + b \operatorname{Sec}[c + d x])^{3/2}}{\operatorname{Cos}[c + d x]^{3/2}} dx$$

Optimal (type 4, 299 leaves, 14 steps):

$$\frac{7 a b \sqrt{\frac{b+a \operatorname{Cos}[c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{4 d \sqrt{\operatorname{Cos}[c+d x]} \sqrt{a+b \operatorname{Sec}[c+d x]}} +$$

$$\frac{(3 a^2 + 4 b^2) \sqrt{\frac{b+a \operatorname{Cos}[c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{4 d \sqrt{\operatorname{Cos}[c+d x]} \sqrt{a+b \operatorname{Sec}[c+d x]}} -$$

$$\frac{5 a \sqrt{\operatorname{Cos}[c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \operatorname{Sec}[c+d x]}}{4 d \sqrt{\frac{b+a \operatorname{Cos}[c+d x]}{a+b}}} +$$

$$\frac{b \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{2 d \operatorname{Cos}[c+d x]^{3/2}} + \frac{5 a \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{4 d \sqrt{\operatorname{Cos}[c+d x]}}$$

Result (type 8, 27 leaves):

$$\int \frac{(a + b \operatorname{Sec}[c + d x])^{3/2}}{\operatorname{Cos}[c + d x]^{3/2}} dx$$

### Problem 848: Unable to integrate problem.

$$\int \operatorname{Cos}[c + d x]^{9/2} (a + b \operatorname{Sec}[c + d x])^{5/2} dx$$

Optimal (type 4, 363 leaves, 12 steps):

$$\begin{aligned}
 & \frac{4 b (57 a^4 - 62 a^2 b^2 + 5 b^4) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{315 a^2 d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} + \\
 & \left(2 (147 a^4 + 279 a^2 b^2 - 10 b^4) \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \sec [c+d x]}\right) / \\
 & \left(315 a^2 d \sqrt{\frac{b+a \cos [c+d x]}{a+b}}\right) + \\
 & \frac{2 b (163 a^2 + 5 b^2) \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{315 a d} + \\
 & \frac{2 (49 a^2 + 75 b^2) \cos [c+d x]^{3/2} \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{315 d} + \\
 & \frac{38 a b \cos [c+d x]^{5/2} \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{63 d} + \\
 & \frac{2 a^2 \cos [c+d x]^{7/2} \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{9 d}
 \end{aligned}$$

Result (type 8, 27 leaves):

$$\int \cos [c+d x]^{9/2} (a+b \sec [c+d x])^{5/2} dx$$

**Problem 849: Unable to integrate problem.**

$$\int \cos [c+d x]^{7/2} (a+b \sec [c+d x])^{5/2} dx$$

Optimal (type 4, 303 leaves, 11 steps):

$$\begin{aligned}
 & \frac{2 (5 a^4 - 2 a^2 b^2 - 3 b^4) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{21 a d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} + \\
 & \left(2 b (29 a^2 + 3 b^2) \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \sec [c+d x]}\right) / \\
 & \left(21 a d \sqrt{\frac{b+a \cos [c+d x]}{a+b}}\right) + \frac{2 (5 a^2 + 9 b^2) \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{21 d} + \\
 & \frac{6 a b \cos [c+d x]^{3/2} \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{7 d} + \\
 & \frac{2 a^2 \cos [c+d x]^{5/2} \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{7 d}
 \end{aligned}$$

Result (type 8, 27 leaves):

$$\int \cos [c+d x]^{7/2} (a+b \sec [c+d x])^{5/2} dx$$

### Problem 850: Unable to integrate problem.

$$\int \cos [c + d x]^{5/2} (a + b \operatorname{Sec} [c + d x])^{5/2} dx$$

Optimal (type 4, 239 leaves, 10 steps):

$$\frac{16 b (a^2 - b^2) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), \frac{2 a}{a+b}\right]}{15 d \sqrt{\cos [c + d x]} \sqrt{a + b \operatorname{Sec} [c + d x]}} +$$

$$\left( 2 (9 a^2 + 23 b^2) \sqrt{\cos [c + d x]} \operatorname{EllipticE}\left[\frac{1}{2} (c + d x), \frac{2 a}{a+b}\right] \sqrt{a + b \operatorname{Sec} [c + d x]} \right) /$$

$$\left( 15 d \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \right) + \frac{22 a b \sqrt{\cos [c + d x]} \sqrt{a + b \operatorname{Sec} [c + d x]} \sin [c + d x]}{15 d} +$$

$$\frac{2 a^2 \cos [c + d x]^{3/2} \sqrt{a + b \operatorname{Sec} [c + d x]} \sin [c + d x]}{5 d}$$

Result (type 8, 27 leaves):

$$\int \cos [c + d x]^{5/2} (a + b \operatorname{Sec} [c + d x])^{5/2} dx$$

### Problem 851: Unable to integrate problem.

$$\int \cos [c + d x]^{3/2} (a + b \operatorname{Sec} [c + d x])^{5/2} dx$$

Optimal (type 4, 262 leaves, 13 steps):

$$\frac{2 a (a^2 + 2 b^2) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), \frac{2 a}{a+b}\right]}{3 d \sqrt{\cos [c + d x]} \sqrt{a + b \operatorname{Sec} [c + d x]}} +$$

$$\frac{2 b^3 \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2} (c + d x), \frac{2 a}{a+b}\right]}{d \sqrt{\cos [c + d x]} \sqrt{a + b \operatorname{Sec} [c + d x]}} +$$

$$\frac{14 a b \sqrt{\cos [c + d x]} \operatorname{EllipticE}\left[\frac{1}{2} (c + d x), \frac{2 a}{a+b}\right] \sqrt{a + b \operatorname{Sec} [c + d x]}}{3 d \sqrt{\frac{b+a \cos [c+d x]}{a+b}}} +$$

$$\frac{2 a^2 \sqrt{\cos [c + d x]} \sqrt{a + b \operatorname{Sec} [c + d x]} \sin [c + d x]}{3 d}$$

Result (type 8, 27 leaves):

$$\int \cos [c + d x]^{3/2} (a + b \operatorname{Sec} [c + d x])^{5/2} dx$$



### Problem 852: Unable to integrate problem.

$$\int \sqrt{\cos [c+d x]} (a+b \operatorname{Sec}[c+d x])^{5 / 2} d x$$

Optimal (type 4, 263 leaves, 13 steps):

$$\frac{b\left(4 a^2+b^2\right) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{d \sqrt{\cos [c+d x]} \sqrt{a+b \operatorname{Sec}[c+d x]}} +$$

$$\frac{5 a b^2 \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{d \sqrt{\cos [c+d x]} \sqrt{a+b \operatorname{Sec}[c+d x]}} + \frac{1}{d \sqrt{\frac{b+a \cos [c+d x]}{a+b}}}$$

$$\frac{\left(2 a^2-b^2\right) \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \operatorname{Sec}[c+d x]}}{d \sqrt{\cos [c+d x]}} +$$

$$\frac{b^2 \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{d \sqrt{\cos [c+d x]}}$$

Result (type 8, 27 leaves):

$$\int \sqrt{\cos [c+d x]} (a+b \operatorname{Sec}[c+d x])^{5 / 2} d x$$

### Problem 853: Unable to integrate problem.

$$\int \frac{(a+b \operatorname{Sec}[c+d x])^{5 / 2}}{\sqrt{\cos [c+d x]}} d x$$

Optimal (type 4, 314 leaves, 14 steps):

$$\frac{a\left(8 a^2+11 b^2\right) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{4 d \sqrt{\cos [c+d x]} \sqrt{a+b \operatorname{Sec}[c+d x]}} +$$

$$\frac{b\left(15 a^2+4 b^2\right) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{4 d \sqrt{\cos [c+d x]} \sqrt{a+b \operatorname{Sec}[c+d x]}} -$$

$$\frac{9 a b \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \operatorname{Sec}[c+d x]}}{4 d \sqrt{\frac{b+a \cos [c+d x]}{a+b}}} +$$

$$\frac{b^2 \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{2 d \cos [c+d x]^{3 / 2}} + \frac{9 a b \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{4 d \sqrt{\cos [c+d x]}}$$

Result (type 8, 27 leaves):

$$\int \frac{(a + b \operatorname{Sec}[c + d x])^{5/2}}{\sqrt{\operatorname{Cos}[c + d x]}} dx$$

Problem 854: Unable to integrate problem.

$$\int \frac{(a + b \operatorname{Sec}[c + d x])^{5/2}}{\operatorname{Cos}[c + d x]^{3/2}} dx$$

Optimal (type 4, 369 leaves, 15 steps):

$$\begin{aligned} & \frac{b (59 a^2 + 16 b^2) \sqrt{\frac{b+a \operatorname{Cos}[c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{24 d \sqrt{\operatorname{Cos}[c+d x]} \sqrt{a+b \operatorname{Sec}[c+d x]}} + \\ & \frac{5 a (a^2 + 4 b^2) \sqrt{\frac{b+a \operatorname{Cos}[c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{8 d \sqrt{\operatorname{Cos}[c+d x]} \sqrt{a+b \operatorname{Sec}[c+d x]}} - \\ & \left( (33 a^2 + 16 b^2) \sqrt{\operatorname{Cos}[c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \operatorname{Sec}[c+d x]} \right) / \\ & \left( 24 d \sqrt{\frac{b+a \operatorname{Cos}[c+d x]}{a+b}} \right) + \frac{b^2 \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{3 d \operatorname{Cos}[c+d x]^{5/2}} + \\ & \frac{13 a b \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{12 d \operatorname{Cos}[c+d x]^{3/2}} + \frac{(33 a^2 + 16 b^2) \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{24 d \sqrt{\operatorname{Cos}[c+d x]}} \end{aligned}$$

Result (type 8, 27 leaves):

$$\int \frac{(a + b \operatorname{Sec}[c + d x])^{5/2}}{\operatorname{Cos}[c + d x]^{3/2}} dx$$

Problem 855: Unable to integrate problem.

$$\int \frac{\operatorname{Cos}[c + d x]^{5/2}}{\sqrt{a + b \operatorname{Sec}[c + d x]}} dx$$

Optimal (type 4, 249 leaves, 10 steps):

$$\begin{aligned}
 & - \frac{2 b (7 a^2 + 8 b^2) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{15 a^3 d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} + \\
 & \left( \frac{2 (9 a^2 + 8 b^2) \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \sec [c+d x]}}{15 a^3 d \sqrt{\frac{b+a \cos [c+d x]}{a+b}}} - \frac{8 b \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{15 a^2 d} \right) + \\
 & \frac{2 \cos [c+d x]^{3/2} \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{5 a d}
 \end{aligned}$$

Result (type 8, 27 leaves):

$$\int \frac{\cos [c+d x]^{5/2}}{\sqrt{a+b \sec [c+d x]}} dx$$

Problem 856: Unable to integrate problem.

$$\int \frac{\cos [c+d x]^{3/2}}{\sqrt{a+b \sec [c+d x]}} dx$$

Optimal (type 4, 195 leaves, 9 steps):

$$\begin{aligned}
 & \frac{2 (a^2 + 2 b^2) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{3 a^2 d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} - \\
 & \frac{4 b \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \sec [c+d x]}}{3 a^2 d \sqrt{\frac{b+a \cos [c+d x]}{a+b}}} + \\
 & \frac{2 \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{3 a d}
 \end{aligned}$$

Result (type 8, 27 leaves):

$$\int \frac{\cos [c+d x]^{3/2}}{\sqrt{a+b \sec [c+d x]}} dx$$

Problem 857: Attempted integration timed out after 120 seconds.

$$\int \frac{\sqrt{\cos [c+d x]}}{\sqrt{a+b \sec [c+d x]}} dx$$

Optimal (type 4, 142 leaves, 8 steps):

$$\frac{2 b \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{a d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} + \frac{2 \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \sec [c+d x]}}{a d \sqrt{\frac{b+a \cos [c+d x]}{a+b}}}$$

Result (type 1, 1 leaves):

???

**Problem 858: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{1}{\sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} dx$$

Optimal (type 4, 67 leaves, 4 steps):

$$\frac{2 \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}}$$

Result (type 4, 102 leaves):

$$\frac{2 i \sqrt{\frac{b+a \cos [c+d x]}{(a+b)(1+\cos [c+d x])}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{-a+b}{a+b}\right]}{d \sqrt{\cos [c+d x]} \sqrt{\frac{1}{1+\cos [c+d x]} \sqrt{a+b \sec [c+d x]}}}$$

**Problem 859: Unable to integrate problem.**

$$\int \frac{1}{\cos [c+d x]^{3/2} \sqrt{a+b \sec [c+d x]}} dx$$

Optimal (type 4, 68 leaves, 4 steps):

$$\frac{2 \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}}$$

Result (type 8, 27 leaves):

$$\int \frac{1}{\cos [c+d x]^{3/2} \sqrt{a+b \sec [c+d x]}} dx$$

### Problem 860: Unable to integrate problem.

$$\int \frac{1}{\cos [c+d x]^{5 / 2} \sqrt{a+b \operatorname{Sec}[c+d x]}} d x$$

Optimal (type 4, 246 leaves, 13 steps):

$$\frac{\sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] - a \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{d \sqrt{\cos [c+d x]} \sqrt{a+b \operatorname{Sec}[c+d x]} - b d \sqrt{\cos [c+d x]} \sqrt{a+b \operatorname{Sec}[c+d x]}} + \frac{\sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \operatorname{Sec}[c+d x]} + \sqrt{a+b \operatorname{Sec}[c+d x]} \sin [c+d x]}{b d \sqrt{\frac{b+a \cos [c+d x]}{a+b}} + b d \sqrt{\cos [c+d x]}}$$

Result (type 8, 27 leaves):

$$\int \frac{1}{\cos [c+d x]^{5 / 2} \sqrt{a+b \operatorname{Sec}[c+d x]}} d x$$

### Problem 861: Unable to integrate problem.

$$\int \frac{1}{\cos [c+d x]^{7 / 2} \sqrt{a+b \operatorname{Sec}[c+d x]}} d x$$

Optimal (type 4, 312 leaves, 14 steps):

$$\frac{a \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{4 b d \sqrt{\cos [c+d x]} \sqrt{a+b \operatorname{Sec}[c+d x]}} + \frac{(3 a^2+4 b^2) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{4 b^2 d \sqrt{\cos [c+d x]} \sqrt{a+b \operatorname{Sec}[c+d x]}} + \frac{3 a \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \operatorname{Sec}[c+d x]}}{4 b^2 d \sqrt{\frac{b+a \cos [c+d x]}{a+b}}} + \frac{\sqrt{a+b \operatorname{Sec}[c+d x]} \sin [c+d x]}{2 b d \cos [c+d x]^{3 / 2}} - \frac{3 a \sqrt{a+b \operatorname{Sec}[c+d x]} \sin [c+d x]}{4 b^2 d \sqrt{\cos [c+d x]}}$$

Result (type 8, 27 leaves):

$$\int \frac{1}{\cos [c+d x]^{7 / 2} \sqrt{a+b \operatorname{Sec}[c+d x]}} d x$$

### Problem 862: Unable to integrate problem.

$$\int \frac{\cos[c + dx]^{5/2}}{(a + b \sec[c + dx])^{3/2}} dx$$

Optimal (type 4, 360 leaves, 11 steps):

$$\frac{8 b (a^2 + 4 b^2) \sqrt{\frac{b+a \cos[c+dx]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), \frac{2a}{a+b}\right] - \left(2(3a^4 + 8a^2b^2 - 16b^4) \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), \frac{2a}{a+b}\right] \sqrt{a+b \sec[c+dx]}\right) / \left(5a^4 d \sqrt{\cos[c+dx]} \sqrt{a+b \sec[c+dx]}\right) + \left(5a^4(a^2 - b^2) d \sqrt{\frac{b+a \cos[c+dx]}{a+b}}\right) + \frac{2b^2 \cos[c+dx]^{3/2} \sin[c+dx]}{a(a^2 - b^2) d \sqrt{a+b \sec[c+dx]}} - \frac{2b(3a^2 - 8b^2) \sqrt{\cos[c+dx]} \sqrt{a+b \sec[c+dx]} \sin[c+dx]}{5a^3(a^2 - b^2) d} + \frac{2(a^2 - 6b^2) \cos[c+dx]^{3/2} \sqrt{a+b \sec[c+dx]} \sin[c+dx]}{5a^2(a^2 - b^2) d}$$

Result (type 8, 27 leaves):

$$\int \frac{\cos[c + dx]^{5/2}}{(a + b \sec[c + dx])^{3/2}} dx$$

### Problem 863: Unable to integrate problem.

$$\int \frac{\cos[c + dx]^{3/2}}{(a + b \sec[c + dx])^{3/2}} dx$$

Optimal (type 4, 289 leaves, 10 steps):

$$\frac{2(a^2 + 8b^2) \sqrt{\frac{b+a \cos[c+dx]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), \frac{2a}{a+b}\right] - \left(2b(5a^2 - 8b^2) \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), \frac{2a}{a+b}\right] \sqrt{a+b \sec[c+dx]}\right) / \left(3a^3 d \sqrt{\cos[c+dx]} \sqrt{a+b \sec[c+dx]}\right) + \left(3a^3(a^2 - b^2) d \sqrt{\frac{b+a \cos[c+dx]}{a+b}}\right) + \frac{2b^2 \sqrt{\cos[c+dx]} \sin[c+dx]}{a(a^2 - b^2) d \sqrt{a+b \sec[c+dx]}} + \frac{2(a^2 - 4b^2) \sqrt{\cos[c+dx]} \sqrt{a+b \sec[c+dx]} \sin[c+dx]}{3a^2(a^2 - b^2) d}$$

Result (type 8, 27 leaves):

$$\int \frac{\cos [c+d x]^{3 / 2}}{(a+b \sec [c+d x])^{3 / 2}} d x$$

Problem 864: Unable to integrate problem.

$$\int \frac{\sqrt{\cos [c+d x]}}{(a+b \sec [c+d x])^{3 / 2}} d x$$

Optimal (type 4, 214 leaves, 9 steps):

$$\begin{aligned} & \frac{4 b \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{a^2 d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} + \\ & \left(2\left(a^2-2 b^2\right) \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \sec [c+d x]}\right) / \\ & \left(a^2\left(a^2-b^2\right) d \sqrt{\frac{b+a \cos [c+d x]}{a+b}}\right) + \frac{2 b^2 \sin [c+d x]}{a\left(a^2-b^2\right) d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} \end{aligned}$$

Result (type 8, 27 leaves):

$$\int \frac{\sqrt{\cos [c+d x]}}{(a+b \sec [c+d x])^{3 / 2}} d x$$

Problem 865: Unable to integrate problem.

$$\int \frac{1}{\sqrt{\cos [c+d x]}(a+b \sec [c+d x])^{3 / 2}} d x$$

Optimal (type 4, 200 leaves, 9 steps):

$$\begin{aligned} & \frac{2 \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{a d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} + \\ & \frac{2 b \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \sec [c+d x]}}{a\left(a^2-b^2\right) d \sqrt{\frac{b+a \cos [c+d x]}{a+b}}} - \\ & \frac{2 b \sin [c+d x]}{\left(a^2-b^2\right) d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} \end{aligned}$$

Result (type 8, 27 leaves):

$$\int \frac{1}{\sqrt{\cos [c+d x]}(a+b \sec [c+d x])^{3 / 2}} d x$$

**Problem 866: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{1}{\cos [c+d x]^{3 / 2}(a+b \operatorname{Sec}[c+d x])^{3 / 2}} d x$$

Optimal (type 4, 126 leaves, 6 steps):

$$\frac{2 \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \operatorname{Sec}[c+d x]} - (a^2-b^2) d \sqrt{\frac{b+a \cos [c+d x]}{a+b}}}{2 a \sin [c+d x] (a^2-b^2) d \sqrt{\cos [c+d x]} \sqrt{a+b \operatorname{Sec}[c+d x]}}$$

Result (type 4, 1845 leaves):

$$\frac{2 a (b+a \cos [c+d x]) \sin [c+d x]}{(a^2-b^2) d \cos [c+d x]^{3 / 2}(a+b \operatorname{Sec}[c+d x])^{3 / 2}} - \left( (b+a \cos [c+d x])^{5 / 2} \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \operatorname{Sec}[c+d x] \sqrt{1+\operatorname{Sec}[c+d x]} \left( i \operatorname{EllipticE}\left[ i \operatorname{ArcSinh}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right]\right], \frac{-a+b}{a+b}\right] - i \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right]\right], \frac{-a+b}{a+b}\right) + \sqrt{\frac{1}{1+\cos [c+d x]}} \sqrt{\frac{b+a \cos [c+d x]}{(a+b)(1+\cos [c+d x])}} \sin [c+d x] \right) / \left( (a^2-b^2)(-a^2+b^2) d \sqrt{\frac{b+a \cos [c+d x]}{(a+b)(1+\cos [c+d x])}} (a+b \operatorname{Sec}[c+d x])^{3 / 2} - \left( \left( \sqrt{b+a \cos [c+d x]} \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \sin [c+d x] \left( i \operatorname{EllipticE}\left[ i \operatorname{ArcSinh}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right]\right], \frac{-a+b}{a+b}\right] - i \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right]\right], \frac{-a+b}{a+b}\right) + \right.$$



$$\begin{aligned}
 & \left. \left. \left. \sqrt{\frac{1}{1 + \cos [c + d x]}} \sqrt{\frac{b + a \cos [c + d x]}{(a + b) (1 + \cos [c + d x])}} \sin [c + d x] \right) \right) / \right. \\
 & \left. \left( 2 (a^2 - b^2) \cos [c + d x]^{3/2} \sqrt{\frac{b + a \cos [c + d x]}{(a + b) (1 + \cos [c + d x])}} \sqrt{1 + \sec [c + d x]} \right) \right) + \\
 & \left( a \sqrt{\cos [c + d x]} \sec \left[ \frac{1}{2} (c + d x) \right]^2 \sqrt{1 + \sec [c + d x]} \sin [c + d x] \right. \\
 & \left( \text{EllipticE} \left[ \text{ArcSinh} \left[ \tan \left[ \frac{1}{2} (c + d x) \right] \right] \right], \frac{-a + b}{a + b} \right) - \\
 & \text{EllipticF} \left[ \text{ArcSinh} \left[ \tan \left[ \frac{1}{2} (c + d x) \right] \right] \right], \frac{-a + b}{a + b} \right) + \\
 & \left. \left. \left. \sqrt{\frac{1}{1 + \cos [c + d x]}} \sqrt{\frac{b + a \cos [c + d x]}{(a + b) (1 + \cos [c + d x])}} \sin [c + d x] \right) \right) / \right. \\
 & \left. \left( 2 (a^2 - b^2) \sqrt{b + a \cos [c + d x]} \sqrt{\frac{b + a \cos [c + d x]}{(a + b) (1 + \cos [c + d x])}} \right) \right) + \\
 & \left( \sqrt{b + a \cos [c + d x]} \sec \left[ \frac{1}{2} (c + d x) \right]^2 \sqrt{1 + \sec [c + d x]} \sin [c + d x] \right. \\
 & \left( \text{EllipticE} \left[ \text{ArcSinh} \left[ \tan \left[ \frac{1}{2} (c + d x) \right] \right] \right], \frac{-a + b}{a + b} \right) - \\
 & \text{EllipticF} \left[ \text{ArcSinh} \left[ \tan \left[ \frac{1}{2} (c + d x) \right] \right] \right], \frac{-a + b}{a + b} \right) + \\
 & \left. \left. \left. \sqrt{\frac{1}{1 + \cos [c + d x]}} \sqrt{\frac{b + a \cos [c + d x]}{(a + b) (1 + \cos [c + d x])}} \sin [c + d x] \right) \right) / \right. \\
 & \left. \left( 2 (a^2 - b^2) \sqrt{\cos [c + d x]} \sqrt{\frac{b + a \cos [c + d x]}{(a + b) (1 + \cos [c + d x])}} \right) \right) + \\
 & \left( \sqrt{\cos [c + d x]} \sqrt{b + a \cos [c + d x]} \sec \left[ \frac{1}{2} (c + d x) \right]^2 \sqrt{1 + \sec [c + d x]} \right. \\
 & \left( -\frac{a \sin [c + d x]}{(a + b) (1 + \cos [c + d x])} + \frac{(b + a \cos [c + d x]) \sin [c + d x]}{(a + b) (1 + \cos [c + d x])^2} \right) \\
 & \left( \text{EllipticE} \left[ \text{ArcSinh} \left[ \tan \left[ \frac{1}{2} (c + d x) \right] \right] \right], \frac{-a + b}{a + b} \right) -
 \end{aligned}$$

$$\begin{aligned}
& \left( \operatorname{EllipticF}\left[\operatorname{ArcSinh}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{-a+b}{a+b}\right] + \right. \\
& \left. \sqrt{\frac{1}{1+\cos[c+dx]}} \sqrt{\frac{b+a\cos[c+dx]}{(a+b)(1+\cos[c+dx])}} \sin[c+dx] \right) / \\
& \left( 2(a^2-b^2) \left( \frac{b+a\cos[c+dx]}{(a+b)(1+\cos[c+dx])} \right)^{3/2} - \right. \\
& \left. \sqrt{\cos[c+dx]} \sqrt{b+a\cos[c+dx]} \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \sqrt{1+\operatorname{Sec}[c+dx]} \right. \\
& \left. \left( \operatorname{EllipticE}\left[\operatorname{ArcSinh}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{-a+b}{a+b}\right] - \right. \right. \\
& \left. \left. \operatorname{EllipticF}\left[\operatorname{ArcSinh}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{-a+b}{a+b}\right] + \right. \right. \\
& \left. \left. \sqrt{\frac{1}{1+\cos[c+dx]}} \sqrt{\frac{b+a\cos[c+dx]}{(a+b)(1+\cos[c+dx])}} \sin[c+dx] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) / \\
& \left( (a^2-b^2) \sqrt{\frac{b+a\cos[c+dx]}{(a+b)(1+\cos[c+dx])}} \right) - \frac{1}{(a^2-b^2) \sqrt{\frac{b+a\cos[c+dx]}{(a+b)(1+\cos[c+dx])}}} \\
& \sqrt{\cos[c+dx]} \sqrt{b+a\cos[c+dx]} \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \sqrt{1+\operatorname{Sec}[c+dx]} \\
& \left( \cos[c+dx] \sqrt{\frac{1}{1+\cos[c+dx]}} \sqrt{\frac{b+a\cos[c+dx]}{(a+b)(1+\cos[c+dx])}} + \right. \\
& \left. \frac{1}{2} \left( \frac{1}{1+\cos[c+dx]} \right)^{3/2} \sqrt{\frac{b+a\cos[c+dx]}{(a+b)(1+\cos[c+dx])}} \sin[c+dx]^2 + \left( \sqrt{\frac{1}{1+\cos[c+dx]}} \right. \right. \\
& \left. \left. \sin[c+dx] \left( -\frac{a\sin[c+dx]}{(a+b)(1+\cos[c+dx])} + \frac{(b+a\cos[c+dx])\sin[c+dx]}{(a+b)(1+\cos[c+dx])^2} \right) \right) / \\
& \left( 2 \sqrt{\frac{b+a\cos[c+dx]}{(a+b)(1+\cos[c+dx])}} \right) + \frac{\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{2 \sqrt{1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{1+\frac{(-a+b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}}} -
\end{aligned}$$

$$\left( \frac{\sec\left[\frac{1}{2}(c+dx)\right]^2 \sqrt{1 + \frac{(-a+b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}}}{2\sqrt{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}} \right)$$

Problem 867: Unable to integrate problem.

$$\int \frac{1}{\cos[c+dx]^{5/2} (a+b\sec[c+dx])^{3/2}} dx$$

Optimal (type 4, 206 leaves, 10 steps):

$$\frac{2\sqrt{\frac{b+a\cos[c+dx]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+dx), \frac{2a}{a+b}\right] + 2a\sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), \frac{2a}{a+b}\right] \sqrt{a+b\sec[c+dx]}}{b(a^2-b^2)d\sqrt{\frac{b+a\cos[c+dx]}{a+b}}} - \frac{2a^2\sin[c+dx]}{b(a^2-b^2)d\sqrt{\cos[c+dx]} \sqrt{a+b\sec[c+dx]}}$$

Result (type 8, 27 leaves):

$$\int \frac{1}{\cos[c+dx]^{5/2} (a+b\sec[c+dx])^{3/2}} dx$$

Problem 868: Unable to integrate problem.

$$\int \frac{1}{\cos[c+dx]^{7/2} (a+b\sec[c+dx])^{3/2}} dx$$

Optimal (type 4, 345 leaves, 14 steps):

$$\frac{\sqrt{\frac{b+a\cos[c+dx]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), \frac{2a}{a+b}\right] - 3a\sqrt{\frac{b+a\cos[c+dx]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+dx), \frac{2a}{a+b}\right]}{b^2 d \sqrt{\cos[c+dx]} \sqrt{a+b\sec[c+dx]}} - \frac{\left( (3a^2-b^2)\sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), \frac{2a}{a+b}\right] \sqrt{a+b\sec[c+dx]} \right) / \left( b^2(a^2-b^2)d\sqrt{\frac{b+a\cos[c+dx]}{a+b}} \right) - \frac{2a^2\sin[c+dx]}{b(a^2-b^2)d\cos[c+dx]^{3/2}\sqrt{a+b\sec[c+dx]}} + \frac{(3a^2-b^2)\sqrt{a+b\sec[c+dx]}\sin[c+dx]}{b^2(a^2-b^2)d\sqrt{\cos[c+dx]}}$$

Result (type 8, 27 leaves):

$$\int \frac{1}{\cos [c+d x]^{7 / 2}(a+b \operatorname{Sec}[c+d x])^{3 / 2}} d x$$

Problem 869: Unable to integrate problem.

$$\int \frac{\cos [c+d x]^{3 / 2}}{(a+b \operatorname{Sec}[c+d x])^{5 / 2}} d x$$

Optimal (type 4, 391 leaves, 11 steps):

$$\frac{2\left(a^4+16 a^2 b^2-16 b^4\right) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]-\left(8 b\left(2 a^4-7 a^2 b^2+4 b^4\right) \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \operatorname{Sec}[c+d x]}\right) / \left(3 a^4\left(a^2-b^2\right)^2 d \sqrt{\frac{b+a \cos [c+d x]}{a+b}}\right)+\frac{2 b^2 \sqrt{\cos [c+d x]} \sin [c+d x]}{3 a\left(a^2-b^2\right) d(a+b \operatorname{Sec}[c+d x])^{3 / 2}}+\frac{4 b^2\left(5 a^2-3 b^2\right) \sqrt{\cos [c+d x]} \sin [c+d x]}{3 a^2\left(a^2-b^2\right)^2 d \sqrt{a+b \operatorname{Sec}[c+d x]}}+\frac{2\left(a^4-13 a^2 b^2+8 b^4\right) \sqrt{\cos [c+d x]} \sqrt{a+b \operatorname{Sec}[c+d x]} \sin [c+d x]}{3 a^3\left(a^2-b^2\right)^2 d}$$

Result (type 8, 27 leaves):

$$\int \frac{\cos [c+d x]^{3 / 2}}{(a+b \operatorname{Sec}[c+d x])^{5 / 2}} d x$$

Problem 870: Unable to integrate problem.

$$\int \frac{\sqrt{\cos [c+d x]}}{(a+b \operatorname{Sec}[c+d x])^{5 / 2}} d x$$

Optimal (type 4, 317 leaves, 10 steps):

$$\begin{aligned}
 & - \frac{2 b (9 a^2 - 8 b^2) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{3 a^3 (a^2 - b^2) d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} + \\
 & \left( 2 (3 a^4 - 15 a^2 b^2 + 8 b^4) \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \sec [c+d x]} \right) / \\
 & \left( 3 a^3 (a^2 - b^2)^2 d \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \right) + \frac{2 b^2 \sin [c+d x]}{3 a (a^2 - b^2) d \sqrt{\cos [c+d x]} (a+b \sec [c+d x])^{3/2}} + \\
 & \frac{8 b^2 (2 a^2 - b^2) \sin [c+d x]}{3 a^2 (a^2 - b^2)^2 d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}}
 \end{aligned}$$

Result (type 8, 27 leaves):

$$\int \frac{\sqrt{\cos [c+d x]}}{(a+b \sec [c+d x])^{5/2}} dx$$

**Problem 871: Unable to integrate problem.**

$$\int \frac{1}{\sqrt{\cos [c+d x]} (a+b \sec [c+d x])^{5/2}} dx$$

Optimal (type 4, 302 leaves, 10 steps):

$$\begin{aligned}
 & \frac{2 (3 a^2 - 2 b^2) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{3 a^2 (a^2 - b^2) d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} + \\
 & \left( 4 b (3 a^2 - b^2) \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \sec [c+d x]} \right) / \\
 & \left( 3 a^2 (a^2 - b^2)^2 d \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \right) - \frac{2 b \sin [c+d x]}{3 (a^2 - b^2) d \sqrt{\cos [c+d x]} (a+b \sec [c+d x])^{3/2}} - \\
 & \frac{2 b (5 a^2 - b^2) \sin [c+d x]}{3 a (a^2 - b^2)^2 d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}}
 \end{aligned}$$

Result (type 8, 27 leaves):

$$\int \frac{1}{\sqrt{\cos [c+d x]} (a+b \sec [c+d x])^{5/2}} dx$$

**Problem 872: Unable to integrate problem.**

$$\int \frac{1}{\cos [c+d x]^{3/2} (a+b \sec [c+d x])^{5/2}} dx$$

Optimal (type 4, 281 leaves, 10 steps):

$$\begin{aligned}
& \frac{2 b \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{3 a\left(a^2-b^2\right) d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} - \\
& \left(2\left(3 a^2+b^2\right) \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \sec [c+d x]}\right) / \\
& \left(3 a\left(a^2-b^2\right)^2 d \sqrt{\frac{b+a \cos [c+d x]}{a+b}}\right) + \frac{2 a \sin [c+d x]}{3\left(a^2-b^2\right) d \sqrt{\cos [c+d x]}(a+b \sec [c+d x])^{3 / 2}} + \\
& \frac{4\left(a^2+b^2\right) \sin [c+d x]}{3\left(a^2-b^2\right)^2 d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}}
\end{aligned}$$

Result (type 8, 27 leaves):

$$\int \frac{1}{\cos [c+d x]^{3 / 2}(a+b \sec [c+d x])^{5 / 2}} d x$$

**Problem 873: Unable to integrate problem.**

$$\int \frac{1}{\cos [c+d x]^{5 / 2}(a+b \sec [c+d x])^{5 / 2}} d x$$

Optimal (type 4, 277 leaves, 10 steps):

$$\begin{aligned}
& \frac{2 \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{3\left(a^2-b^2\right) d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} + \\
& \frac{8 b \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \sec [c+d x]}}{3\left(a^2-b^2\right)^2 d \sqrt{\frac{b+a \cos [c+d x]}{a+b}}} - \\
& \frac{2 a^2 \sin [c+d x]}{3 b\left(a^2-b^2\right) d \sqrt{\cos [c+d x]}(a+b \sec [c+d x])^{3 / 2}} + \\
& \frac{2 a\left(a^2-5 b^2\right) \sin [c+d x]}{3 b\left(a^2-b^2\right)^2 d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}}
\end{aligned}$$

Result (type 8, 27 leaves):

$$\int \frac{1}{\cos [c+d x]^{5 / 2}(a+b \sec [c+d x])^{5 / 2}} d x$$

**Problem 874: Unable to integrate problem.**

$$\int \frac{1}{\cos [c+d x]^{7 / 2}(a+b \sec [c+d x])^{5 / 2}} d x$$

Optimal (type 4, 370 leaves, 14 steps):

$$\frac{2 a \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{3 b\left(a^2-b^2\right) d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} +$$

$$\frac{2 \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{b^2 d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} +$$

$$\left(2 a\left(3 a^2-7 b^2\right) \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \sec [c+d x]}\right) /$$

$$\left(3 b^2\left(a^2-b^2\right)^2 d \sqrt{\frac{b+a \cos [c+d x]}{a+b}}\right) - \frac{2 a^2 \sin [c+d x]}{3 b\left(a^2-b^2\right) d \cos [c+d x]^{3 / 2}\left(a+b \sec [c+d x]\right)^{3 / 2}} -$$

$$\frac{2 a^2\left(3 a^2-7 b^2\right) \sin [c+d x]}{3 b^2\left(a^2-b^2\right)^2 d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}}$$

Result (type 8, 27 leaves):

$$\int \frac{1}{\cos [c+d x]^{7 / 2}\left(a+b \sec [c+d x]\right)^{5 / 2}} d x$$

**Problem 878: Result more than twice size of optimal antiderivative.**

$$\int \frac{(d \cos [e+f x])^n}{a+b \sec [e+f x]} d x$$

Optimal (type 6, 196 leaves, 7 steps):

$$\frac{1}{\left(a^2-b^2\right) f} a \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}(-1-n), 1, \frac{3}{2}, \sin [e+f x]^2, \frac{a^2 \sin [e+f x]^2}{a^2-b^2}\right]$$

$$\cos [e+f x]\left(d \cos [e+f x]\right)^n\left(\cos [e+f x]^2\right)^{\frac{1}{2}(-1-n)} \sin [e+f x] -$$

$$\frac{1}{\left(a^2-b^2\right) f} b \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{n}{2}, 1, \frac{3}{2}, \sin [e+f x]^2, \frac{a^2 \sin [e+f x]^2}{a^2-b^2}\right]$$

$$\left(d \cos [e+f x]\right)^n\left(\cos [e+f x]^2\right)^{-n / 2} \sin [e+f x]$$

Result (type 6, 5216 leaves):

$$\left(\left(d \cos [e+f x]\right)^n \tan [e+f x]\left(a \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, 1+\frac{n}{2}, \frac{3}{2}, -\tan [e+f x]^2\right] -\right.\right.$$

$$b \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1+n}{2}, \frac{3}{2}, -\tan [e+f x]^2\right] -\left(3 a b^2\left(a^2-b^2\right)\right.$$

$$\left.\left.\operatorname{AppellF1}\left[\frac{1}{2}, \frac{n}{2}, 1, \frac{3}{2}, -\tan [e+f x]^2, \frac{b^2 \tan [e+f x]^2}{a^2-b^2}\right]\left(1+\tan [e+f x]^2\right)^{-n / 2}\right)\right) /$$

$$\left(\left(-3\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{n}{2}, 1, \frac{3}{2}, -\tan [e+f x]^2, \frac{b^2 \tan [e+f x]^2}{a^2-b^2}\right] +\right.\right.$$

$$\begin{aligned}
& \left( (a^2 - b^2) n \operatorname{AppellF1}\left[\frac{3}{2}, 1 + \frac{n}{2}, 1, \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2}\right] - \right. \\
& \quad \left. 2 b^2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{n}{2}, 2, \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2}\right] \right) \tan[e + f x]^2 \\
& (a^2 - b^2 (1 + \tan[e + f x]^2)) - \left( 3 b^3 (-a^2 + b^2) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}(-1 + n), 1, \right. \right. \\
& \quad \left. \left. \frac{3}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2}\right] (1 + \tan[e + f x]^2)^{\frac{1-n}{2}} \right) / \\
& \left( \left( 3 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}(-1 + n), 1, \frac{3}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2}\right] + \right. \right. \\
& \quad \left( 2 b^2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}(-1 + n), 2, \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2}\right] - \right. \\
& \quad \left. (a^2 - b^2) (-1 + n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1+n}{2}, 1, \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2}\right] \right) \\
& \quad \left. \left. \tan[e + f x]^2 \right) (-a^2 + b^2 (1 + \tan[e + f x]^2)) \right) / \\
& \left( a^2 f (a + b \operatorname{Sec}[e + f x]) \left( \frac{1}{a^2} \operatorname{Sec}[e + f x]^2 \left( a \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, 1 + \frac{n}{2}, \frac{3}{2}, -\tan[e + f x]^2\right] - \right. \right. \right. \\
& \quad \left. \left. b \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1+n}{2}, \frac{3}{2}, -\tan[e + f x]^2\right] - \left( 3 a b^2 (a^2 - b^2) \right. \right. \right. \\
& \quad \left. \left. \left. \operatorname{AppellF1}\left[\frac{1}{2}, \frac{n}{2}, 1, \frac{3}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2}\right] (1 + \tan[e + f x]^2)^{-n/2} \right) \right) / \right. \\
& \quad \left( -3 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{n}{2}, 1, \frac{3}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2}\right] + \right. \\
& \quad \left( (a^2 - b^2) n \operatorname{AppellF1}\left[\frac{3}{2}, 1 + \frac{n}{2}, 1, \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2}\right] - \right. \\
& \quad \left. \left. 2 b^2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{n}{2}, 2, \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2}\right] \right) \tan[e + f x]^2 \right) \\
& (a^2 - b^2 (1 + \tan[e + f x]^2)) - \left( 3 b^3 (-a^2 + b^2) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}(-1 + n), \right. \right. \\
& \quad \left. \left. 1, \frac{3}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2}\right] (1 + \tan[e + f x]^2)^{\frac{1-n}{2}} \right) / \\
& \left( \left( 3 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}(-1 + n), 1, \frac{3}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2}\right] + \right. \right. \\
& \quad \left( 2 b^2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}(-1 + n), 2, \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2}\right] - \right. \\
& \quad \left. (a^2 - b^2) (-1 + n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1+n}{2}, 1, \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2}\right] \right) \\
& \quad \left. \left. \tan[e + f x]^2 \right) (-a^2 + b^2 (1 + \tan[e + f x]^2)) \right) + \\
& \frac{1}{a^2} \tan[e + f x] \left( - \left( \left( 6 a b^4 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{n}{2}, 1, \frac{3}{2}, -\tan[e + f x]^2, \right. \right. \right. \right.
\end{aligned}$$



$$\begin{aligned}
 & \left. \frac{b^2 \tan[e + f x]^2}{a^2 - b^2} \right] \sec[e + f x]^2 \tan[e + f x] (1 + \tan[e + f x]^2)^{-n/2} \Big/ \\
 & \left( \left( -3 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{n}{2}, 1, \frac{3}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2} \right] + \right. \right. \\
 & \quad \left( (a^2 - b^2) n \operatorname{AppellF1} \left[ \frac{3}{2}, 1 + \frac{n}{2}, 1, \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2} \right] - \right. \\
 & \quad \left. \left. 2 b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{n}{2}, 2, \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2} \right] \right) \right. \\
 & \quad \left. \left. \tan[e + f x]^2 \right) (a^2 - b^2 (1 + \tan[e + f x]^2)^2) \right) \Big) + \\
 & \left( 3 a b^2 (a^2 - b^2) n \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{n}{2}, 1, \frac{3}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2} \right] \right. \\
 & \quad \left. \sec[e + f x]^2 \tan[e + f x] (1 + \tan[e + f x]^2)^{-1 - \frac{n}{2}} \right) \Big/ \\
 & \left( \left( -3 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{n}{2}, 1, \frac{3}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2} \right] + \right. \right. \\
 & \quad \left( (a^2 - b^2) n \operatorname{AppellF1} \left[ \frac{3}{2}, 1 + \frac{n}{2}, 1, \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2} \right] - \right. \\
 & \quad \left. \left. 2 b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{n}{2}, 2, \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2} \right] \right) \right. \\
 & \quad \left. \left. \tan[e + f x]^2 \right) (a^2 - b^2 (1 + \tan[e + f x]^2)) \right) \Big) - \\
 & \left( 3 a b^2 (a^2 - b^2) \left( -\frac{1}{3} n \operatorname{AppellF1} \left[ \frac{3}{2}, 1 + \frac{n}{2}, 1, \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2} \right] \right. \right. \\
 & \quad \left. \sec[e + f x]^2 \tan[e + f x] + \frac{1}{3 (a^2 - b^2)} 2 b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{n}{2}, 2, \frac{5}{2}, -\tan[e + f x]^2, \right. \right. \\
 & \quad \left. \left. \frac{b^2 \tan[e + f x]^2}{a^2 - b^2} \right] \sec[e + f x]^2 \tan[e + f x] \right) (1 + \tan[e + f x]^2)^{-n/2} \Big/ \\
 & \left( \left( -3 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{n}{2}, 1, \frac{3}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2} \right] + \right. \right. \\
 & \quad \left( (a^2 - b^2) n \operatorname{AppellF1} \left[ \frac{3}{2}, 1 + \frac{n}{2}, 1, \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2} \right] - \right. \\
 & \quad \left. \left. 2 b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{n}{2}, 2, \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2} \right] \right) \tan[e + f x]^2 \right) \\
 & \quad (a^2 - b^2 (1 + \tan[e + f x]^2)) \Big) + \left( 6 b^5 (-a^2 + b^2) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2} (-1 + n), 1, \frac{3}{2}, \right. \right. \\
 & \quad \left. \left. -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2} \right] \sec[e + f x]^2 \tan[e + f x] (1 + \tan[e + f x]^2)^{\frac{1-n}{2}} \right) \Big/ \\
 & \left( \left( 3 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2} (-1 + n), 1, \frac{3}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2} \right] + \right. \right. \\
 & \quad \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{2} (-1 + n), 2, \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2} \right] - \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( (a^2 - b^2) (-1 + n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1+n}{2}, 1, \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2}\right] \right) \\
 & \left. \tan[e + f x]^2 \right) (-a^2 + b^2 (1 + \tan[e + f x]^2))^2) - \\
 & \left( 6 b^3 (-a^2 + b^2) \left(\frac{1}{2} - \frac{n}{2}\right) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2} (-1 + n), 1, \frac{3}{2}, -\tan[e + f x]^2, \right. \right. \\
 & \left. \left. \frac{b^2 \tan[e + f x]^2}{a^2 - b^2}\right] \operatorname{Sec}[e + f x]^2 \tan[e + f x] (1 + \tan[e + f x]^2)^{\frac{1}{2} - \frac{n}{2}} \right) / \\
 & \left( \left( 3 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2} (-1 + n), 1, \frac{3}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2}\right] + \right. \right. \\
 & \left. \left( 2 b^2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2} (-1 + n), 2, \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2}\right] - \right. \right. \\
 & \left. \left. (a^2 - b^2) (-1 + n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1+n}{2}, 1, \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2}\right] \right) \right) \\
 & \left. \tan[e + f x]^2 \right) (-a^2 + b^2 (1 + \tan[e + f x]^2))) - \\
 & \left( 3 b^3 (-a^2 + b^2) \left(-\frac{1}{3} (-1 + n) \operatorname{AppellF1}\left[\frac{3}{2}, 1 + \frac{1}{2} (-1 + n), 1, \frac{5}{2}, -\tan[e + f x]^2, \right. \right. \right. \\
 & \left. \left. \frac{b^2 \tan[e + f x]^2}{a^2 - b^2}\right] \operatorname{Sec}[e + f x]^2 \tan[e + f x] + \frac{1}{3 (a^2 - b^2)} \right. \\
 & \left. 2 b^2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2} (-1 + n), 2, \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2}\right] \right. \\
 & \left. \left. \operatorname{Sec}[e + f x]^2 \tan[e + f x] \right) (1 + \tan[e + f x]^2)^{\frac{1}{2} - \frac{n}{2}} \right) / \\
 & \left( \left( 3 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2} (-1 + n), 1, \frac{3}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2}\right] + \right. \right. \\
 & \left. \left( 2 b^2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2} (-1 + n), 2, \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2}\right] - \right. \right. \\
 & \left. \left. (a^2 - b^2) (-1 + n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1+n}{2}, 1, \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2}\right] \right) \right) \\
 & \left. \tan[e + f x]^2 \right) (-a^2 + b^2 (1 + \tan[e + f x]^2))) - b \operatorname{Csc}[e + f x] \operatorname{Sec}[e + f x] \\
 & \left( -\operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1+n}{2}, \frac{3}{2}, -\tan[e + f x]^2\right] + (1 + \tan[e + f x]^2)^{\frac{1}{2} (-1-n)} \right) + a \\
 & \operatorname{Csc}[e + f x] \operatorname{Sec}[e + f x] \\
 & \left( -\operatorname{Hypergeometric2F1}\left[\frac{1}{2}, 1 + \frac{n}{2}, \frac{3}{2}, -\tan[e + f x]^2\right] + (1 + \tan[e + f x]^2)^{-1 - \frac{n}{2}} \right) + \\
 & \left( 3 a b^2 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{n}{2}, 1, \frac{3}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2}\right] \right. \\
 & \left. (1 + \tan[e + f x]^2)^{-n/2} \right. \\
 & \left. \left( 2 \left( (a^2 - b^2) n \operatorname{AppellF1}\left[\frac{3}{2}, 1 + \frac{n}{2}, 1, \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2}\right] - \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & 2 b^2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{n}{2}, 2, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] \sec[e+fx]^2 \\
 & \tan[e+fx] - 3(a^2-b^2) \left( -\frac{1}{3} n \operatorname{AppellF1}\left[\frac{3}{2}, 1+\frac{n}{2}, 1, \frac{5}{2}, -\tan[e+fx]^2, \right. \right. \\
 & \quad \left. \left. \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] \sec[e+fx]^2 \tan[e+fx] + \frac{1}{3(a^2-b^2)} 2 b^2 \operatorname{AppellF1}\left[\frac{3}{2}, \right. \right. \\
 & \quad \left. \left. \frac{n}{2}, 2, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] \sec[e+fx]^2 \tan[e+fx] \right) + \\
 & \tan[e+fx]^2 \left( (a^2-b^2) n \left( \frac{1}{5(a^2-b^2)} 6 b^2 \operatorname{AppellF1}\left[\frac{5}{2}, 1+\frac{n}{2}, 2, \frac{7}{2}, -\tan[e+fx]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] \sec[e+fx]^2 \tan[e+fx] - \frac{6}{5} \left(1+\frac{n}{2}\right) \operatorname{AppellF1}\left[\frac{5}{2}, 2+\right. \right. \\
 & \quad \left. \left. \frac{n}{2}, 1, \frac{7}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] \sec[e+fx]^2 \tan[e+fx] \right) - \\
 & 2 b^2 \left( -\frac{3}{5} n \operatorname{AppellF1}\left[\frac{5}{2}, 1+\frac{n}{2}, 2, \frac{7}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] \right. \\
 & \quad \left. \sec[e+fx]^2 \tan[e+fx] + \frac{1}{5(a^2-b^2)} 12 b^2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{n}{2}, 3, \frac{7}{2}, \right. \right. \\
 & \quad \left. \left. -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] \sec[e+fx]^2 \tan[e+fx] \right) \right) \Big/ \\
 & \left( \left( -3(a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{n}{2}, 1, \frac{3}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] + \right. \right. \\
 & \quad \left( (a^2-b^2) n \operatorname{AppellF1}\left[\frac{3}{2}, 1+\frac{n}{2}, 1, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] - 2 b^2 \right. \\
 & \quad \left. \left. \operatorname{AppellF1}\left[\frac{3}{2}, \frac{n}{2}, 2, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] \right) \tan[e+fx]^2 \right)^2 \\
 & (a^2-b^2(1+\tan[e+fx]^2)) \Big) + \left( 3 b^3 (-a^2+b^2) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}(-1+n), \right. \right. \\
 & \quad \left. \left. 1, \frac{3}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] (1+\tan[e+fx]^2)^{\frac{1}{2}-\frac{n}{2}} \right. \\
 & \left. \left( 2 \left( 2 b^2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}(-1+n), 2, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] - \right. \right. \right. \\
 & \quad \left. \left. (a^2-b^2)(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1+n}{2}, 1, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] \right) \right. \\
 & \quad \left. \sec[e+fx]^2 \tan[e+fx] + 3(a^2-b^2) \left( -\frac{1}{3}(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, \right. \right. \right. \\
 & \quad \left. \left. 1+\frac{1}{2}(-1+n), 1, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] \sec[e+fx]^2 \right. \\
 & \quad \left. \tan[e+fx] + \frac{1}{3(a^2-b^2)} 2 b^2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}(-1+n), 2, \frac{5}{2}, \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2} \sec[e+fx]^2 \tan[e+fx] \Big) + \\
 & \tan[e+fx]^2 \left( 2b^2 \left( -\frac{3}{5}(-1+n) \operatorname{AppellF1}\left[\frac{5}{2}, 1+\frac{1}{2}(-1+n), 2, \frac{7}{2}, \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2} \right] \sec[e+fx]^2 \tan[e+fx] + \right. \right. \\
 & \quad \left. \frac{1}{5(a^2-b^2)} 12b^2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{2}(-1+n), 3, \frac{7}{2}, -\tan[e+fx]^2, \right. \right. \\
 & \quad \left. \left. \frac{b^2 \tan[e+fx]^2}{a^2-b^2} \right] \sec[e+fx]^2 \tan[e+fx] \right) - (a^2-b^2)(-1+n) \\
 & \left( \frac{1}{5(a^2-b^2)} 6b^2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1+n}{2}, 2, \frac{7}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2} \right] \right. \\
 & \quad \left. \sec[e+fx]^2 \tan[e+fx] - \frac{3}{5}(1+n) \operatorname{AppellF1}\left[\frac{5}{2}, 1+\frac{1+n}{2}, 1, \frac{7}{2}, \right. \right. \\
 & \quad \left. \left. -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2} \right] \sec[e+fx]^2 \tan[e+fx] \right) \Big) \Big) \Big) / \\
 & \left( \left( 3(a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}(-1+n), 1, \frac{3}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2} \right] + \right. \right. \\
 & \quad \left( 2b^2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}(-1+n), 2, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2} \right] - \right. \\
 & \quad \left. (a^2-b^2)(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1+n}{2}, 1, \frac{5}{2}, -\tan[e+fx]^2, \right. \right. \\
 & \quad \left. \left. \frac{b^2 \tan[e+fx]^2}{a^2-b^2} \right] \right) \tan[e+fx]^2 \Big)^2 (-a^2+b^2(1+\tan[e+fx]^2)) \Big) \Big) \Big) \Big)
 \end{aligned}$$

**Problem 879: Result more than twice size of optimal antiderivative.**

$$\int \frac{(d \cos[e+fx])^n}{(a+b \sec[e+fx])^2} dx$$

Optimal (type 6, 309 leaves, 10 steps):

$$\begin{aligned}
 & \frac{1}{(a^2-b^2)^2 f} a^2 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}(-3-n), 2, \frac{3}{2}, \sin[e+fx]^2, \frac{a^2 \sin[e+fx]^2}{a^2-b^2} \right] \\
 & \cos[e+fx] (d \cos[e+fx])^n (\cos[e+fx]^2)^{\frac{1}{2}(-1-n)} \sin[e+fx] + \\
 & \frac{1}{(a^2-b^2)^2 f} b^2 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}(-1-n), 2, \frac{3}{2}, \sin[e+fx]^2, \frac{a^2 \sin[e+fx]^2}{a^2-b^2} \right] \\
 & \cos[e+fx] (d \cos[e+fx])^n (\cos[e+fx]^2)^{\frac{1}{2}(-1-n)} \sin[e+fx] - \\
 & \frac{1}{(a^2-b^2)^2 f} 2ab \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}(-2-n), 2, \frac{3}{2}, \sin[e+fx]^2, \frac{a^2 \sin[e+fx]^2}{a^2-b^2} \right] \\
 & (d \cos[e+fx])^n (\cos[e+fx]^2)^{-n/2} \sin[e+fx]
 \end{aligned}$$

Result (type 6, 10296 leaves):

$$\begin{aligned}
 & \left( (d \cos [e + f x])^n \left( -\frac{1}{a^3} {}_2F_1\left[\frac{1}{2}, \frac{1}{2} + \frac{n}{2}, \frac{3}{2}, -\tan [e + f x]^2\right] \tan [e + f x] + \right. \right. \\
 & \quad \frac{1}{a^2} {}_2F_1\left[\frac{1}{2}, 1 + \frac{n}{2}, \frac{3}{2}, -\tan [e + f x]^2\right] \tan [e + f x] - \\
 & \quad \left. \left( 6 b^2 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{n}{2}, 2, \frac{3}{2}, -\tan [e + f x]^2, \frac{b^2 \tan [e + f x]^2}{a^2 - b^2}\right] \right. \right. \\
 & \quad \left. \left. \tan [e + f x] (1 + \tan [e + f x]^2)^{-n/2} \right) \right) / \\
 & \left( \left( -3 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{n}{2}, 2, \frac{3}{2}, -\tan [e + f x]^2, \frac{b^2 \tan [e + f x]^2}{a^2 - b^2}\right] + \right. \right. \\
 & \quad \left( (a^2 - b^2) n \operatorname{AppellF1}\left[\frac{3}{2}, 1 + \frac{n}{2}, 2, \frac{5}{2}, -\tan [e + f x]^2, \frac{b^2 \tan [e + f x]^2}{a^2 - b^2}\right] - \right. \\
 & \quad \left. \left. 4 b^2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{n}{2}, 3, \frac{5}{2}, -\tan [e + f x]^2, \frac{b^2 \tan [e + f x]^2}{a^2 - b^2}\right] \right) \tan [e + f x]^2 \right) \\
 & \left( a^2 - b^2 (1 + \tan [e + f x]^2) \right)^2 \left. + \left( 6 b^3 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2} (-1 + n), 2, \right. \right. \right. \\
 & \quad \left. \left. \frac{3}{2}, -\tan [e + f x]^2, \frac{b^2 \tan [e + f x]^2}{a^2 - b^2}\right] \tan [e + f x] (1 + \tan [e + f x]^2)^{\frac{1-n}{2}} \right) / \\
 & \left( a \left( -3 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2} (-1 + n), 2, \frac{3}{2}, -\tan [e + f x]^2, \frac{b^2 \tan [e + f x]^2}{a^2 - b^2}\right] + \right. \right. \\
 & \quad \left( -4 b^2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2} (-1 + n), 3, \frac{5}{2}, -\tan [e + f x]^2, \frac{b^2 \tan [e + f x]^2}{a^2 - b^2}\right] + \right. \\
 & \quad \left. \left. (a^2 - b^2) (-1 + n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1+n}{2}, 2, \frac{5}{2}, -\tan [e + f x]^2, \frac{b^2 \tan [e + f x]^2}{a^2 - b^2}\right] \right) \right) \\
 & \quad \left. \tan [e + f x]^2 (a^2 - b^2 (1 + \tan [e + f x]^2))^2 \right) + \\
 & \left( 3 b^2 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{n}{2}, 1, \frac{3}{2}, -\tan [e + f x]^2, \frac{b^2 \tan [e + f x]^2}{a^2 - b^2}\right] \right. \\
 & \quad \left. \tan [e + f x] (1 + \tan [e + f x]^2)^{-n/2} \right) / \\
 & \left( a^2 \left( -3 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{n}{2}, 1, \frac{3}{2}, -\tan [e + f x]^2, \frac{b^2 \tan [e + f x]^2}{a^2 - b^2}\right] + \right. \right. \\
 & \quad \left( (a^2 - b^2) n \operatorname{AppellF1}\left[\frac{3}{2}, 1 + \frac{n}{2}, 1, \frac{5}{2}, -\tan [e + f x]^2, \frac{b^2 \tan [e + f x]^2}{a^2 - b^2}\right] - \right. \\
 & \quad \left. \left. 2 b^2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{n}{2}, 2, \frac{5}{2}, -\tan [e + f x]^2, \frac{b^2 \tan [e + f x]^2}{a^2 - b^2}\right] \right) \tan [e + f x]^2 \right) \\
 & \left( -a^2 + b^2 (1 + \tan [e + f x]^2) \right) \left. - \left( 6 b^3 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2} (-1 + n), 1, \right. \right. \right. \\
 & \quad \left. \left. \frac{3}{2}, -\tan [e + f x]^2, \frac{b^2 \tan [e + f x]^2}{a^2 - b^2}\right] \tan [e + f x] (1 + \tan [e + f x]^2)^{\frac{1-n}{2}} \right) / \\
 & \left( a^3 \left( -3 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2} (-1 + n), 1, \frac{3}{2}, -\tan [e + f x]^2, \frac{b^2 \tan [e + f x]^2}{a^2 - b^2}\right] + \right. \right.
 \end{aligned}$$

$$\begin{aligned}
& \left( -2 b^2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}(-1+n), 2, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] + \right. \\
& \quad \left. (a^2-b^2)(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1+n}{2}, 1, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] \right) \\
& \quad \left. \tan[e+fx]^2 \left( -a^2+b^2(1+\tan[e+fx]^2) \right) \right) \Big/ \\
& \left( f(a+b \operatorname{Sec}[e+fx])^2 \left( -\frac{1}{a^3} 2 b \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1}{2}+\frac{n}{2}, \frac{3}{2}, -\tan[e+fx]^2\right] \operatorname{Sec}[e+fx]^2 + \right. \right. \\
& \quad \frac{1}{a^2} \\
& \quad \left. \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, 1+\frac{n}{2}, \frac{3}{2}, -\tan[e+fx]^2\right] \operatorname{Sec}[e+fx]^2 - \right. \\
& \quad \left. \left( 24 b^4 (a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{n}{2}, 2, \frac{3}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] \right. \right. \\
& \quad \left. \left. \operatorname{Sec}[e+fx]^2 \tan[e+fx]^2 (1+\tan[e+fx]^2)^{-n/2} \right) \Big/ \right. \\
& \quad \left( \left( -3 (a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{n}{2}, 2, \frac{3}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] + \right. \right. \\
& \quad \left( (a^2-b^2) n \operatorname{AppellF1}\left[\frac{3}{2}, 1+\frac{n}{2}, 2, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] - \right. \\
& \quad \left. \left. 4 b^2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{n}{2}, 3, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] \right) \tan[e+fx]^2 \right) \\
& \quad \left. (a^2-b^2(1+\tan[e+fx]^2))^3 \right) + \left( 24 b^5 (a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}(-1+n), 2, \frac{3}{2}, \right. \right. \\
& \quad \left. \left. -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] \operatorname{Sec}[e+fx]^2 \tan[e+fx]^2 (1+\tan[e+fx]^2)^{\frac{1}{2}-\frac{n}{2}} \right) \Big/ \\
& \left( a \left( -3 (a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}(-1+n), 2, \frac{3}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] + \right. \right. \\
& \quad \left( -4 b^2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}(-1+n), 3, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] + \right. \\
& \quad \left. \left. (a^2-b^2)(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1+n}{2}, 2, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] \right) \right) \\
& \quad \left. \tan[e+fx]^2 \left( a^2-b^2(1+\tan[e+fx]^2) \right)^3 \right) + \\
& \left( 6 b^2 (a^2-b^2) n \operatorname{AppellF1}\left[\frac{1}{2}, \frac{n}{2}, 2, \frac{3}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] \right. \\
& \quad \left. \operatorname{Sec}[e+fx]^2 \tan[e+fx]^2 (1+\tan[e+fx]^2)^{-1-\frac{n}{2}} \right) \Big/ \\
& \left( \left( -3 (a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{n}{2}, 2, \frac{3}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] + \right. \right. \\
& \quad \left. \left. (a^2-b^2) n \operatorname{AppellF1}\left[\frac{3}{2}, 1+\frac{n}{2}, 2, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] - \right. \right.
\end{aligned}$$

$$\begin{aligned}
 & 4 b^2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{n}{2}, 3, \frac{5}{2}, -\tan[e+f x]^2, \frac{b^2 \tan[e+f x]^2}{a^2-b^2}\right] \tan[e+f x]^2 \\
 & \left(a^2-b^2\left(1+\tan[e+f x]^2\right)\right)^2 - \left(6 b^2\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{n}{2}, 2, \frac{3}{2},\right.\right. \\
 & \left.\left.-\tan[e+f x]^2, \frac{b^2 \tan[e+f x]^2}{a^2-b^2}\right] \sec[e+f x]^2\left(1+\tan[e+f x]^2\right)^{-n/2}\right) / \\
 & \left(\left(-3\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{n}{2}, 2, \frac{3}{2}, -\tan[e+f x]^2, \frac{b^2 \tan[e+f x]^2}{a^2-b^2}\right] +\right.\right. \\
 & \left.\left.\left(\left(a^2-b^2\right) n \operatorname{AppellF1}\left[\frac{3}{2}, 1+\frac{n}{2}, 2, \frac{5}{2}, -\tan[e+f x]^2, \frac{b^2 \tan[e+f x]^2}{a^2-b^2}\right] -\right.\right.\right. \\
 & \left.\left.\left.4 b^2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{n}{2}, 3, \frac{5}{2}, -\tan[e+f x]^2, \frac{b^2 \tan[e+f x]^2}{a^2-b^2}\right]\right) \tan[e+f x]^2\right) \\
 & \left(a^2-b^2\left(1+\tan[e+f x]^2\right)\right)^2 - \left(6 b^2\left(a^2-b^2\right) \tan[e+f x]\right. \\
 & \left.\left(-\frac{1}{3} n \operatorname{AppellF1}\left[\frac{3}{2}, 1+\frac{n}{2}, 2, \frac{5}{2}, -\tan[e+f x]^2, \frac{b^2 \tan[e+f x]^2}{a^2-b^2}\right] \sec[e+f x]^2\right.\right. \\
 & \left.\left.\tan[e+f x] + \frac{1}{3\left(a^2-b^2\right)} 4 b^2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{n}{2}, 3, \frac{5}{2}, -\tan[e+f x]^2, \frac{b^2 \tan[e+f x]^2}{a^2-b^2}\right]\right.\right. \\
 & \left.\left.\sec[e+f x]^2 \tan[e+f x]\right)\left(1+\tan[e+f x]^2\right)^{-n/2}\right) / \\
 & \left(\left(-3\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{n}{2}, 2, \frac{3}{2}, -\tan[e+f x]^2, \frac{b^2 \tan[e+f x]^2}{a^2-b^2}\right] +\right.\right. \\
 & \left.\left.\left(\left(a^2-b^2\right) n \operatorname{AppellF1}\left[\frac{3}{2}, 1+\frac{n}{2}, 2, \frac{5}{2}, -\tan[e+f x]^2, \frac{b^2 \tan[e+f x]^2}{a^2-b^2}\right] -\right.\right.\right. \\
 & \left.\left.\left.4 b^2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{n}{2}, 3, \frac{5}{2}, -\tan[e+f x]^2, \frac{b^2 \tan[e+f x]^2}{a^2-b^2}\right]\right) \tan[e+f x]^2\right) \\
 & \left(a^2-b^2\left(1+\tan[e+f x]^2\right)\right)^2 + \left(12 b^3\left(a^2-b^2\right)\left(\frac{1}{2}-\frac{n}{2}\right) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}(-1+n), 2,\right.\right. \\
 & \left.\left.\frac{3}{2}, -\tan[e+f x]^2, \frac{b^2 \tan[e+f x]^2}{a^2-b^2}\right] \sec[e+f x]^2 \tan[e+f x]^2\left(1+\tan[e+f x]^2\right)^{-\frac{1}{2}-\frac{n}{2}}\right) / \\
 & \left(a\left(-3\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}(-1+n), 2, \frac{3}{2}, -\tan[e+f x]^2, \frac{b^2 \tan[e+f x]^2}{a^2-b^2}\right] +\right.\right. \\
 & \left.\left.\left(-4 b^2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}(-1+n), 3, \frac{5}{2}, -\tan[e+f x]^2, \frac{b^2 \tan[e+f x]^2}{a^2-b^2}\right] +\right.\right.\right. \\
 & \left.\left.\left.\left(a^2-b^2\right)(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1+n}{2}, 2, \frac{5}{2}, -\tan[e+f x]^2, \frac{b^2 \tan[e+f x]^2}{a^2-b^2}\right]\right)\right) \\
 & \left.\tan[e+f x]^2\right)\left(a^2-b^2\left(1+\tan[e+f x]^2\right)\right)^2 + \\
 & \left(6 b^3\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}(-1+n), 2, \frac{3}{2}, -\tan[e+f x]^2, \frac{b^2 \tan[e+f x]^2}{a^2-b^2}\right]\right. \\
 & \left.\sec[e+f x]^2\left(1+\tan[e+f x]^2\right)^{\frac{1}{2}-\frac{n}{2}}\right) /
 \end{aligned}$$

$$\begin{aligned}
& \left( a \left( -3 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2} (-1+n), 2, \frac{3}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2 - b^2} \right] + \right. \right. \\
& \quad \left( -4 b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{2} (-1+n), 3, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2 - b^2} \right] + \right. \\
& \quad \quad \left. (a^2 - b^2) (-1+n) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1+n}{2}, 2, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2 - b^2} \right] \right) \\
& \quad \left. \tan[e+fx]^2 \right) (a^2 - b^2 (1 + \tan[e+fx]^2))^2 \Big) + \\
& \left( 6 b^3 (a^2 - b^2) \tan[e+fx] \left( -\frac{1}{3} (-1+n) \operatorname{AppellF1} \left[ \frac{3}{2}, 1 + \frac{1}{2} (-1+n), 2, \frac{5}{2}, \right. \right. \right. \\
& \quad \left. \left. -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2 - b^2} \right] \sec[e+fx]^2 \tan[e+fx] + \frac{1}{3 (a^2 - b^2)} \right. \\
& \quad \left. 4 b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{2} (-1+n), 3, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2 - b^2} \right] \right. \\
& \quad \left. \sec[e+fx]^2 \tan[e+fx] \right) (1 + \tan[e+fx]^2)^{\frac{1}{2} - \frac{n}{2}} \Big) / \\
& \left( a \left( -3 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2} (-1+n), 2, \frac{3}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2 - b^2} \right] + \right. \right. \\
& \quad \left( -4 b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{2} (-1+n), 3, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2 - b^2} \right] + \right. \\
& \quad \quad \left. (a^2 - b^2) (-1+n) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1+n}{2}, 2, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2 - b^2} \right] \right) \\
& \quad \left. \tan[e+fx]^2 \right) (a^2 - b^2 (1 + \tan[e+fx]^2))^2 \Big) - \\
& \left( 6 b^4 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{n}{2}, 1, \frac{3}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2 - b^2} \right] \right. \\
& \quad \left. \sec[e+fx]^2 \tan[e+fx]^2 (1 + \tan[e+fx]^2)^{-n/2} \right) / \\
& \left( a^2 \left( -3 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{n}{2}, 1, \frac{3}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2 - b^2} \right] + \right. \right. \\
& \quad \left( (a^2 - b^2) n \operatorname{AppellF1} \left[ \frac{3}{2}, 1 + \frac{n}{2}, 1, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2 - b^2} \right] - \right. \\
& \quad \quad \left. 2 b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{n}{2}, 2, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2 - b^2} \right] \right) \\
& \quad \left. \tan[e+fx]^2 \right) (-a^2 + b^2 (1 + \tan[e+fx]^2))^2 \Big) + \\
& \left( 12 b^5 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2} (-1+n), 1, \frac{3}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2 - b^2} \right] \right. \\
& \quad \left. \sec[e+fx]^2 \tan[e+fx]^2 (1 + \tan[e+fx]^2)^{\frac{1}{2} - \frac{n}{2}} \right) / \\
& \left( a^3 \left( -3 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2} (-1+n), 1, \frac{3}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2 - b^2} \right] + \right. \right.
\end{aligned}$$



$$\begin{aligned}
 & \left( -2 b^2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}(-1+n), 2, \frac{5}{2}, -\operatorname{Tan}[e+f x]^2, \frac{b^2 \operatorname{Tan}[e+f x]^2}{a^2-b^2}\right] + \right. \\
 & \quad \left. (a^2-b^2)(-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1+n}{2}, 1, \frac{5}{2}, -\operatorname{Tan}[e+f x]^2, \frac{b^2 \operatorname{Tan}[e+f x]^2}{a^2-b^2}\right] \right) \\
 & \quad \operatorname{Tan}[e+f x]^2 \left( -a^2+b^2(1+\operatorname{Tan}[e+f x]^2) \right)^2 \Big) - \\
 & \left( 3 b^2 (a^2-b^2) n \operatorname{AppellF1}\left[\frac{1}{2}, \frac{n}{2}, 1, \frac{3}{2}, -\operatorname{Tan}[e+f x]^2, \frac{b^2 \operatorname{Tan}[e+f x]^2}{a^2-b^2}\right] \right. \\
 & \quad \left. \operatorname{Sec}[e+f x]^2 \operatorname{Tan}[e+f x]^2 (1+\operatorname{Tan}[e+f x]^2)^{-1-\frac{n}{2}} \right) / \\
 & \left( a^2 \left( -3 (a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{n}{2}, 1, \frac{3}{2}, -\operatorname{Tan}[e+f x]^2, \frac{b^2 \operatorname{Tan}[e+f x]^2}{a^2-b^2}\right] + \right. \right. \\
 & \quad \left( (a^2-b^2) n \operatorname{AppellF1}\left[\frac{3}{2}, 1+\frac{n}{2}, 1, \frac{5}{2}, -\operatorname{Tan}[e+f x]^2, \frac{b^2 \operatorname{Tan}[e+f x]^2}{a^2-b^2}\right] - \right. \\
 & \quad \left. \left. 2 b^2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{n}{2}, 2, \frac{5}{2}, -\operatorname{Tan}[e+f x]^2, \frac{b^2 \operatorname{Tan}[e+f x]^2}{a^2-b^2}\right] \right) \operatorname{Tan}[e+f x]^2 \right) \\
 & \quad \left. \left( -a^2+b^2(1+\operatorname{Tan}[e+f x]^2) \right) \right) + \left( 3 b^2 (a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{n}{2}, 1, \frac{3}{2}, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}[e+f x]^2, \frac{b^2 \operatorname{Tan}[e+f x]^2}{a^2-b^2}\right] \operatorname{Sec}[e+f x]^2 (1+\operatorname{Tan}[e+f x]^2)^{-n/2} \right) / \\
 & \left( a^2 \left( -3 (a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{n}{2}, 1, \frac{3}{2}, -\operatorname{Tan}[e+f x]^2, \frac{b^2 \operatorname{Tan}[e+f x]^2}{a^2-b^2}\right] + \right. \right. \\
 & \quad \left( (a^2-b^2) n \operatorname{AppellF1}\left[\frac{3}{2}, 1+\frac{n}{2}, 1, \frac{5}{2}, -\operatorname{Tan}[e+f x]^2, \frac{b^2 \operatorname{Tan}[e+f x]^2}{a^2-b^2}\right] - \right. \\
 & \quad \left. \left. 2 b^2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{n}{2}, 2, \frac{5}{2}, -\operatorname{Tan}[e+f x]^2, \frac{b^2 \operatorname{Tan}[e+f x]^2}{a^2-b^2}\right] \right) \operatorname{Tan}[e+f x]^2 \right) \\
 & \quad \left. \left( -a^2+b^2(1+\operatorname{Tan}[e+f x]^2) \right) \right) + \left( 3 b^2 (a^2-b^2) \operatorname{Tan}[e+f x] \right. \\
 & \quad \left. \left( -\frac{1}{3} n \operatorname{AppellF1}\left[\frac{3}{2}, 1+\frac{n}{2}, 1, \frac{5}{2}, -\operatorname{Tan}[e+f x]^2, \frac{b^2 \operatorname{Tan}[e+f x]^2}{a^2-b^2}\right] \operatorname{Sec}[e+f x]^2 \right. \right. \\
 & \quad \left. \left. \operatorname{Tan}[e+f x] + \frac{1}{3(a^2-b^2)} 2 b^2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{n}{2}, 2, \frac{5}{2}, -\operatorname{Tan}[e+f x]^2, \frac{b^2 \operatorname{Tan}[e+f x]^2}{a^2-b^2}\right] \right. \right. \\
 & \quad \left. \left. \operatorname{Sec}[e+f x]^2 \operatorname{Tan}[e+f x] \right) \right) (1+\operatorname{Tan}[e+f x]^2)^{-n/2} \Big) / \\
 & \left( a^2 \left( -3 (a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{n}{2}, 1, \frac{3}{2}, -\operatorname{Tan}[e+f x]^2, \frac{b^2 \operatorname{Tan}[e+f x]^2}{a^2-b^2}\right] + \right. \right. \\
 & \quad \left( (a^2-b^2) n \operatorname{AppellF1}\left[\frac{3}{2}, 1+\frac{n}{2}, 1, \frac{5}{2}, -\operatorname{Tan}[e+f x]^2, \frac{b^2 \operatorname{Tan}[e+f x]^2}{a^2-b^2}\right] - \right. \\
 & \quad \left. \left. 2 b^2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{n}{2}, 2, \frac{5}{2}, -\operatorname{Tan}[e+f x]^2, \frac{b^2 \operatorname{Tan}[e+f x]^2}{a^2-b^2}\right] \right) \operatorname{Tan}[e+f x]^2 \right) \\
 & \quad \left. \left( -a^2+b^2(1+\operatorname{Tan}[e+f x]^2) \right) \right) - \left( 12 b^3 (a^2-b^2) \left( \frac{1}{2} - \frac{n}{2} \right) \right)
 \end{aligned}$$

$$\begin{aligned}
& \text{AppellF1}\left[\frac{1}{2}, \frac{1}{2}(-1+n), 1, \frac{3}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] \\
& \text{Sec}[e+fx]^2 \tan[e+fx]^2 (1+\tan[e+fx]^2)^{\frac{1-n}{2}} \Big/ \\
& \left( a^3 \left( -3(a^2-b^2) \text{AppellF1}\left[\frac{1}{2}, \frac{1}{2}(-1+n), 1, \frac{3}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] + \right. \right. \\
& \quad \left( -2b^2 \text{AppellF1}\left[\frac{3}{2}, \frac{1}{2}(-1+n), 2, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] + \right. \\
& \quad \left. \left. (a^2-b^2)(-1+n) \text{AppellF1}\left[\frac{3}{2}, \frac{1+n}{2}, 1, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] \right) \right) \\
& \quad \left. \tan[e+fx]^2 \right) (-a^2+b^2(1+\tan[e+fx]^2)) \Big) - \\
& \left( 6b^3(a^2-b^2) \text{AppellF1}\left[\frac{1}{2}, \frac{1}{2}(-1+n), 1, \frac{3}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] \right. \\
& \quad \left. \text{Sec}[e+fx]^2 (1+\tan[e+fx]^2)^{\frac{1-n}{2}} \Big/ \right. \\
& \quad \left( a^3 \left( -3(a^2-b^2) \text{AppellF1}\left[\frac{1}{2}, \frac{1}{2}(-1+n), 1, \frac{3}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] + \right. \right. \\
& \quad \left( -2b^2 \text{AppellF1}\left[\frac{3}{2}, \frac{1}{2}(-1+n), 2, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] + \right. \\
& \quad \left. \left. (a^2-b^2)(-1+n) \text{AppellF1}\left[\frac{3}{2}, \frac{1+n}{2}, 1, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] \right) \right) \\
& \quad \left. \tan[e+fx]^2 \right) (-a^2+b^2(1+\tan[e+fx]^2)) \Big) - \\
& \left( 6b^3(a^2-b^2) \tan[e+fx] \left( -\frac{1}{3}(-1+n) \text{AppellF1}\left[\frac{3}{2}, 1+\frac{1}{2}(-1+n), 1, \frac{5}{2}, \right. \right. \right. \\
& \quad \left. \left. -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] \text{Sec}[e+fx]^2 \tan[e+fx] + \frac{1}{3(a^2-b^2)} \right. \\
& \quad \left. 2b^2 \text{AppellF1}\left[\frac{3}{2}, \frac{1}{2}(-1+n), 2, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] \right. \\
& \quad \left. \left. \text{Sec}[e+fx]^2 \tan[e+fx] \right) (1+\tan[e+fx]^2)^{\frac{1-n}{2}} \Big/ \right. \\
& \quad \left( a^3 \left( -3(a^2-b^2) \text{AppellF1}\left[\frac{1}{2}, \frac{1}{2}(-1+n), 1, \frac{3}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] + \right. \right. \\
& \quad \left( -2b^2 \text{AppellF1}\left[\frac{3}{2}, \frac{1}{2}(-1+n), 2, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] + \right. \\
& \quad \left. \left. (a^2-b^2)(-1+n) \text{AppellF1}\left[\frac{3}{2}, \frac{1+n}{2}, 1, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] \right) \right) \\
& \quad \left. \tan[e+fx]^2 \right) (-a^2+b^2(1+\tan[e+fx]^2)) \Big) + \frac{1}{a^2} \text{Sec}[e+fx]^2 \\
& \left( -\text{Hypergeometric2F1}\left[\frac{1}{2}, 1+\frac{n}{2}, \frac{3}{2}, -\tan[e+fx]^2\right] + (1+\tan[e+fx]^2)^{-1-\frac{n}{2}} \right) - \frac{1}{a^3} 2 \\
& b \text{Sec}[e+fx]^2
\end{aligned}$$

$$\begin{aligned}
 & \left( -\text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1}{2} + \frac{n}{2}, \frac{3}{2}, -\text{Tan}[e + f x]^2\right] + (1 + \text{Tan}[e + f x]^2)^{-\frac{1-n}{2}} \right) - \\
 & \left( 3 b^2 (a^2 - b^2) \text{AppellF1}\left[\frac{1}{2}, \frac{n}{2}, 1, \frac{3}{2}, -\text{Tan}[e + f x]^2, \frac{b^2 \text{Tan}[e + f x]^2}{a^2 - b^2}\right] \right. \\
 & \quad \left. \text{Tan}[e + f x] (1 + \text{Tan}[e + f x]^2)^{-n/2} \right. \\
 & \quad \left( 2 \left( (a^2 - b^2) n \text{AppellF1}\left[\frac{3}{2}, 1 + \frac{n}{2}, 1, \frac{5}{2}, -\text{Tan}[e + f x]^2, \frac{b^2 \text{Tan}[e + f x]^2}{a^2 - b^2}\right] - \right. \right. \\
 & \quad \left. \left. 2 b^2 \text{AppellF1}\left[\frac{3}{2}, \frac{n}{2}, 2, \frac{5}{2}, -\text{Tan}[e + f x]^2, \frac{b^2 \text{Tan}[e + f x]^2}{a^2 - b^2}\right] \right) \text{Sec}[e + f x]^2 \right. \\
 & \quad \left. \text{Tan}[e + f x] - 3 (a^2 - b^2) \left( -\frac{1}{3} n \text{AppellF1}\left[\frac{3}{2}, 1 + \frac{n}{2}, 1, \frac{5}{2}, -\text{Tan}[e + f x]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{b^2 \text{Tan}[e + f x]^2}{a^2 - b^2} \right] \text{Sec}[e + f x]^2 \text{Tan}[e + f x] + \frac{1}{3 (a^2 - b^2)} 2 b^2 \text{AppellF1}\left[\frac{3}{2}, \right. \right. \\
 & \quad \left. \left. \frac{n}{2}, 2, \frac{5}{2}, -\text{Tan}[e + f x]^2, \frac{b^2 \text{Tan}[e + f x]^2}{a^2 - b^2} \right] \text{Sec}[e + f x]^2 \text{Tan}[e + f x] \right) + \\
 & \quad \text{Tan}[e + f x]^2 \left( (a^2 - b^2) n \left( \frac{1}{5 (a^2 - b^2)} 6 b^2 \text{AppellF1}\left[\frac{5}{2}, 1 + \frac{n}{2}, 2, \frac{7}{2}, -\text{Tan}[e + f x]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{b^2 \text{Tan}[e + f x]^2}{a^2 - b^2} \right] \text{Sec}[e + f x]^2 \text{Tan}[e + f x] - \frac{6}{5} \left( 1 + \frac{n}{2} \right) \text{AppellF1}\left[\frac{5}{2}, \right. \right. \\
 & \quad \left. \left. 2 + \frac{n}{2}, 1, \frac{7}{2}, -\text{Tan}[e + f x]^2, \frac{b^2 \text{Tan}[e + f x]^2}{a^2 - b^2} \right] \text{Sec}[e + f x]^2 \text{Tan}[e + f x] \right) - \\
 & \quad 2 b^2 \left( -\frac{3}{5} n \text{AppellF1}\left[\frac{5}{2}, 1 + \frac{n}{2}, 2, \frac{7}{2}, -\text{Tan}[e + f x]^2, \frac{b^2 \text{Tan}[e + f x]^2}{a^2 - b^2} \right] \right. \\
 & \quad \left. \text{Sec}[e + f x]^2 \text{Tan}[e + f x] + \frac{1}{5 (a^2 - b^2)} 12 b^2 \text{AppellF1}\left[\frac{5}{2}, \frac{n}{2}, 3, \frac{7}{2}, \right. \right. \\
 & \quad \left. \left. -\text{Tan}[e + f x]^2, \frac{b^2 \text{Tan}[e + f x]^2}{a^2 - b^2} \right] \text{Sec}[e + f x]^2 \text{Tan}[e + f x] \right) \Big) / \\
 & \left( a^2 \left( -3 (a^2 - b^2) \text{AppellF1}\left[\frac{1}{2}, \frac{n}{2}, 1, \frac{3}{2}, -\text{Tan}[e + f x]^2, \frac{b^2 \text{Tan}[e + f x]^2}{a^2 - b^2}\right] + \right. \right. \\
 & \quad \left( (a^2 - b^2) n \text{AppellF1}\left[\frac{3}{2}, 1 + \frac{n}{2}, 1, \frac{5}{2}, -\text{Tan}[e + f x]^2, \frac{b^2 \text{Tan}[e + f x]^2}{a^2 - b^2}\right] - 2 b^2 \right. \\
 & \quad \left. \left. \text{AppellF1}\left[\frac{3}{2}, \frac{n}{2}, 2, \frac{5}{2}, -\text{Tan}[e + f x]^2, \frac{b^2 \text{Tan}[e + f x]^2}{a^2 - b^2}\right] \right) \text{Tan}[e + f x]^2 \right)^2 \\
 & \quad \left. (-a^2 + b^2 (1 + \text{Tan}[e + f x]^2)) \right) + \left( 6 b^2 (a^2 - b^2) \text{AppellF1}\left[\frac{1}{2}, \frac{n}{2}, 2, \frac{3}{2}, \right. \right. \\
 & \quad \left. \left. -\text{Tan}[e + f x]^2, \frac{b^2 \text{Tan}[e + f x]^2}{a^2 - b^2} \right] \text{Tan}[e + f x] (1 + \text{Tan}[e + f x]^2)^{-n/2} \right. \\
 & \quad \left( 2 \left( (a^2 - b^2) n \text{AppellF1}\left[\frac{3}{2}, 1 + \frac{n}{2}, 2, \frac{5}{2}, -\text{Tan}[e + f x]^2, \frac{b^2 \text{Tan}[e + f x]^2}{a^2 - b^2}\right] - \right. \right. \\
 & \quad \left. \left. 4 b^2 \text{AppellF1}\left[\frac{3}{2}, \frac{n}{2}, 3, \frac{5}{2}, -\text{Tan}[e + f x]^2, \frac{b^2 \text{Tan}[e + f x]^2}{a^2 - b^2}\right] \right) \text{Sec}[e + f x]^2 \right.
 \end{aligned}$$

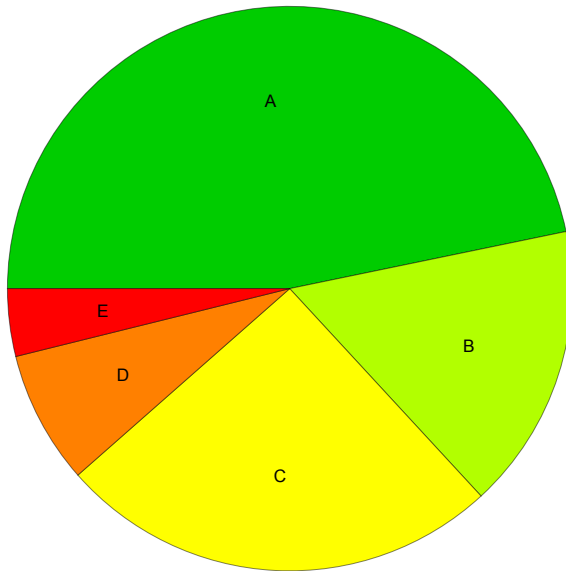
$$\begin{aligned}
& \tan[e + f x] - 3 (a^2 - b^2) \left( -\frac{1}{3} n \operatorname{AppellF1}\left[\frac{3}{2}, 1 + \frac{n}{2}, 2, \frac{5}{2}, -\tan[e + f x]^2, \right. \right. \\
& \quad \left. \left. \frac{b^2 \tan[e + f x]^2}{a^2 - b^2} \right] \operatorname{Sec}[e + f x]^2 \tan[e + f x] + \frac{1}{3 (a^2 - b^2)} 4 b^2 \operatorname{AppellF1}\left[\frac{3}{2}, \right. \right. \\
& \quad \left. \left. \frac{n}{2}, 3, \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2} \right] \operatorname{Sec}[e + f x]^2 \tan[e + f x] \right) + \\
& \tan[e + f x]^2 \left( (a^2 - b^2) n \left( \frac{1}{5 (a^2 - b^2)} 12 b^2 \operatorname{AppellF1}\left[\frac{5}{2}, 1 + \frac{n}{2}, 3, \frac{7}{2}, -\tan[e + f x]^2, \right. \right. \right. \\
& \quad \left. \left. \frac{b^2 \tan[e + f x]^2}{a^2 - b^2} \right] \operatorname{Sec}[e + f x]^2 \tan[e + f x] - \frac{6}{5} \left(1 + \frac{n}{2}\right) \operatorname{AppellF1}\left[\frac{5}{2}, \right. \right. \\
& \quad \left. \left. 2 + \frac{n}{2}, 2, \frac{7}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2} \right] \operatorname{Sec}[e + f x]^2 \tan[e + f x] \right) - \\
& 4 b^2 \left( -\frac{3}{5} n \operatorname{AppellF1}\left[\frac{5}{2}, 1 + \frac{n}{2}, 3, \frac{7}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2} \right] \right. \\
& \quad \left. \operatorname{Sec}[e + f x]^2 \tan[e + f x] + \frac{1}{5 (a^2 - b^2)} 18 b^2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{n}{2}, 4, \frac{7}{2}, \right. \right. \\
& \quad \left. \left. -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2} \right] \operatorname{Sec}[e + f x]^2 \tan[e + f x] \right) \Big) \Big) \Big) \Big) \Big) / \\
& \left( \left( -3 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{n}{2}, 2, \frac{3}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2} \right] + \right. \right. \\
& \quad \left( (a^2 - b^2) n \operatorname{AppellF1}\left[\frac{3}{2}, 1 + \frac{n}{2}, 2, \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2} \right] - 4 b^2 \right. \\
& \quad \left. \left. \operatorname{AppellF1}\left[\frac{3}{2}, \frac{n}{2}, 3, \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2} \right] \right) \tan[e + f x]^2 \right)^2 \\
& \left. (a^2 - b^2 (1 + \tan[e + f x]^2))^2 \right) + \left( 6 b^3 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2} (-1 + n), 1, \right. \right. \\
& \quad \left. \left. \frac{3}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2} \right] \tan[e + f x] (1 + \tan[e + f x]^2)^{\frac{1-n}{2}} \right. \\
& \left. \left( 2 \left( -2 b^2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2} (-1 + n), 2, \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2} \right] + \right. \right. \right. \\
& \quad \left. \left. (a^2 - b^2) (-1 + n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1+n}{2}, 1, \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2} \right] \right) \right. \\
& \quad \left. \operatorname{Sec}[e + f x]^2 \tan[e + f x] - 3 (a^2 - b^2) \left( -\frac{1}{3} (-1 + n) \operatorname{AppellF1}\left[\frac{3}{2}, 1 + \frac{1}{2} (-1 + n), \right. \right. \right. \\
& \quad \left. \left. \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2} \right] \operatorname{Sec}[e + f x]^2 \tan[e + f x] + \frac{1}{3 (a^2 - b^2)} \right. \\
& \quad \left. 2 b^2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2} (-1 + n), 2, \frac{5}{2}, -\tan[e + f x]^2, \frac{b^2 \tan[e + f x]^2}{a^2 - b^2} \right] \right. \\
& \quad \left. \left. \operatorname{Sec}[e + f x]^2 \tan[e + f x] \right) + \tan[e + f x]^2 \left( -2 b^2 \right. \right.
\end{aligned}$$

$$\begin{aligned}
 & \left( -\frac{3}{5} (-1+n) \operatorname{AppellF1}\left[\frac{5}{2}, 1+\frac{1}{2}(-1+n), 2, \frac{7}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] \right. \\
 & \quad \left. \operatorname{Sec}[e+fx]^2 \tan[e+fx] + \frac{1}{5(a^2-b^2)} 12 b^2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{2}(-1+n), \right. \right. \\
 & \quad \left. \left. 3, \frac{7}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] \operatorname{Sec}[e+fx]^2 \tan[e+fx] \right) + \\
 & (a^2-b^2) (-1+n) \left( \frac{1}{5(a^2-b^2)} 6 b^2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1+n}{2}, 2, \frac{7}{2}, -\tan[e+fx]^2, \right. \right. \\
 & \quad \left. \left. \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] \operatorname{Sec}[e+fx]^2 \tan[e+fx] - \frac{3}{5} (1+n) \operatorname{AppellF1}\left[\frac{5}{2}, 1+\frac{1+n}{2}, \right. \right. \\
 & \quad \left. \left. 1, \frac{7}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] \operatorname{Sec}[e+fx]^2 \tan[e+fx] \right) \Bigg) \Bigg) \Bigg) / \\
 & \left( a^3 \left( -3(a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}(-1+n), 1, \frac{3}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] + \right. \right. \\
 & \quad \left( -2 b^2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}(-1+n), 2, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] + (a^2-b^2) \right. \\
 & \quad \left. \left. (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1+n}{2}, 1, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] \right) \right. \\
 & \quad \left. \left. \tan[e+fx]^2 \right)^2 (-a^2+b^2(1+\tan[e+fx]^2)) \right) - \\
 & \left( 6 b^3 (a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}(-1+n), 2, \frac{3}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] \right. \\
 & \quad \left. \tan[e+fx] (1+\tan[e+fx]^2)^{\frac{1-n}{2}} \right. \\
 & \quad \left( 2 \left( -4 b^2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}(-1+n), 3, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] + \right. \right. \\
 & \quad \left. \left. (a^2-b^2) (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1+n}{2}, 2, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] \right) \right. \\
 & \quad \left. \operatorname{Sec}[e+fx]^2 \tan[e+fx] - 3(a^2-b^2) \left( -\frac{1}{3} (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, 1+\frac{1}{2}(-1+n), \right. \right. \right. \\
 & \quad \left. \left. 2, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] \operatorname{Sec}[e+fx]^2 \tan[e+fx] + \frac{1}{3(a^2-b^2)} \right. \\
 & \quad \left. \left. 4 b^2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}(-1+n), 3, \frac{5}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] \right. \right. \\
 & \quad \left. \left. \operatorname{Sec}[e+fx]^2 \tan[e+fx] \right) + \tan[e+fx]^2 \left( -4 b^2 \right. \right. \\
 & \quad \left( -\frac{3}{5} (-1+n) \operatorname{AppellF1}\left[\frac{5}{2}, 1+\frac{1}{2}(-1+n), 3, \frac{7}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] \right. \\
 & \quad \left. \operatorname{Sec}[e+fx]^2 \tan[e+fx] + \frac{1}{5(a^2-b^2)} 18 b^2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{2}(-1+n), \right. \right. \\
 & \quad \left. \left. 4, \frac{7}{2}, -\tan[e+fx]^2, \frac{b^2 \tan[e+fx]^2}{a^2-b^2}\right] \operatorname{Sec}[e+fx]^2 \tan[e+fx] \right) +
 \end{aligned}$$

$$\begin{aligned}
 & (a^2 - b^2) (-1 + n) \left( \frac{1}{5(a^2 - b^2)} 12 b^2 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1+n}{2}, 3, \frac{7}{2}, -\operatorname{Tan}[e + f x]^2, \right. \right. \\
 & \quad \left. \left. \frac{b^2 \operatorname{Tan}[e + f x]^2}{a^2 - b^2} \right] \operatorname{Sec}[e + f x]^2 \operatorname{Tan}[e + f x] - \frac{3}{5} (1 + n) \operatorname{AppellF1} \left[ \frac{5}{2}, 1 + \frac{1+n}{2}, \right. \right. \\
 & \quad \left. \left. 2, \frac{7}{2}, -\operatorname{Tan}[e + f x]^2, \frac{b^2 \operatorname{Tan}[e + f x]^2}{a^2 - b^2} \right] \operatorname{Sec}[e + f x]^2 \operatorname{Tan}[e + f x] \right) \Bigg) \Bigg) \Bigg) / \\
 & \left( a \left( -3 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{2} (-1 + n), 2, \frac{3}{2}, -\operatorname{Tan}[e + f x]^2, \frac{b^2 \operatorname{Tan}[e + f x]^2}{a^2 - b^2} \right] + \right. \right. \\
 & \quad \left. \left( -4 b^2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{2} (-1 + n), 3, \frac{5}{2}, -\operatorname{Tan}[e + f x]^2, \frac{b^2 \operatorname{Tan}[e + f x]^2}{a^2 - b^2} \right] + (a^2 - b^2) \right. \right. \\
 & \quad \left. \left. (-1 + n) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1+n}{2}, 2, \frac{5}{2}, -\operatorname{Tan}[e + f x]^2, \frac{b^2 \operatorname{Tan}[e + f x]^2}{a^2 - b^2} \right] \right) \right. \\
 & \quad \left. \left. \left. \left. \left. \operatorname{Tan}[e + f x]^2 \right)^2 (a^2 - b^2 (1 + \operatorname{Tan}[e + f x]^2))^2 \right) \right) \right) \right) \Bigg) \Bigg) \Bigg)
 \end{aligned}$$

## Summary of Integration Test Results

879 integration problems



A - 411 optimal antiderivatives

B - 144 more than twice size of optimal antiderivatives

C - 223 unnecessarily complex antiderivatives

D - 67 unable to integrate problems

E - 34 integration timeouts